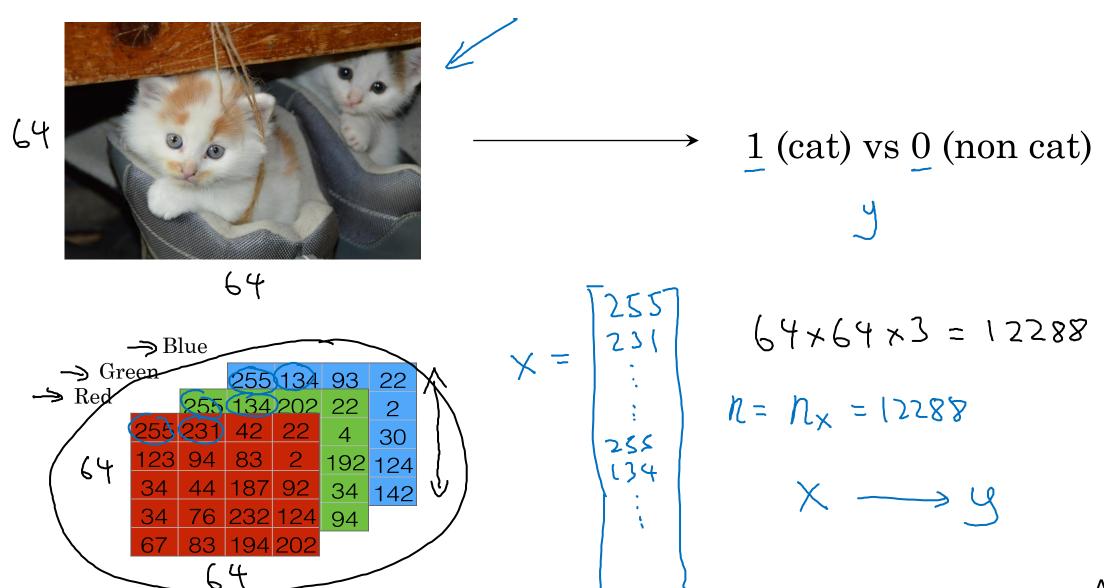


Basics of Neural Network Programming

Binary Classification

Binary Classification



Andrew Ng

Notation

$$(x,y)$$
 $\times \in \mathbb{R}^{n_x}$, $y \in \{0,1\}$
 $m + rainiy examples: \{(x^{(i)}, y^{(i)}), (x^{(i)}, y^{(2i)}), ..., (x^{(m)}, y^{(m)})\}$

$$M = M + rain \qquad M + est = \# + test examples.$$

$$X = \begin{bmatrix} x^{(i)} & x^{(2i)} & ... & x^{(m)} \end{bmatrix}$$

$$X = \begin{bmatrix} x^{(i)} & x^{(2i)} & ... & x^{(m)} \end{bmatrix}$$

$$X = \begin{bmatrix} x^{(i)} & x^{(2i)} & ... & x^{(m)} \end{bmatrix}$$

$$X \in \mathbb{R}^{n_x \times m}$$



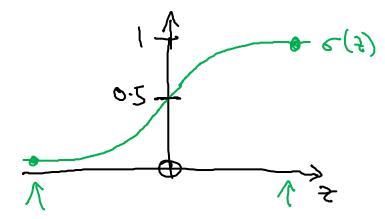
Basics of Neural Network Programming

Logistic Regression

Logistic Regression

Given X, wort
$$\hat{y} = P(y=1|X)$$
 $x \in \mathbb{R}^{n_X}$

Output
$$\hat{y} = 5(\omega^T \times + b)$$



$$X_0 = 1, \quad x \in \mathbb{R}^{n_x + 1}$$

$$Y = 6 (0^{T}x)$$

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Basics of Neural Network Programming

Logistic Regression cost function

Given
$$\{(x^{(1)}, y^{(1)}), \dots, (x^{(m)}, y^{(m)})\}$$
, want $\hat{y}^{(i)} \approx y^{(i)}$.

Loss (error) function: $\int (\hat{y}, y) = \frac{1}{2} (\hat{y} - y)^2$

The entropy of the contraction of the c

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Basics of Neural Network Programming

Gradient Descent

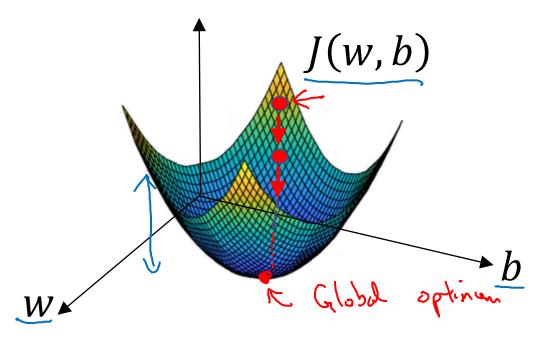
deeplearning.ai

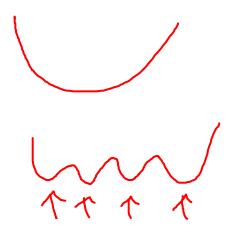
Gradient Descent

Recap:
$$\hat{y} = \sigma(w^T x + b)$$
, $\sigma(z) = \frac{1}{1 + e^{-z}}$

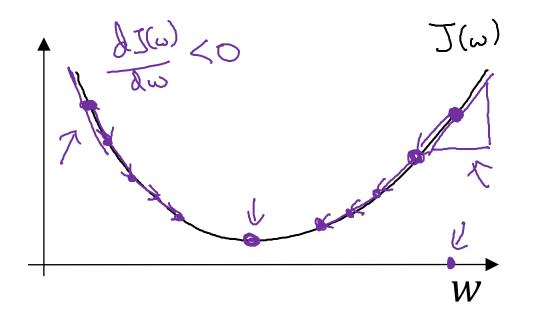
$$J(w,b) = \frac{1}{m} \sum_{i=1}^{m} \mathcal{L}(\hat{y}^{(i)}, y^{(i)}) = -\frac{1}{m} \sum_{i=1}^{m} (y^{(i)} \log \hat{y}^{(i)} + (1 - y^{(i)}) \log(1 - \hat{y}^{(i)}))$$

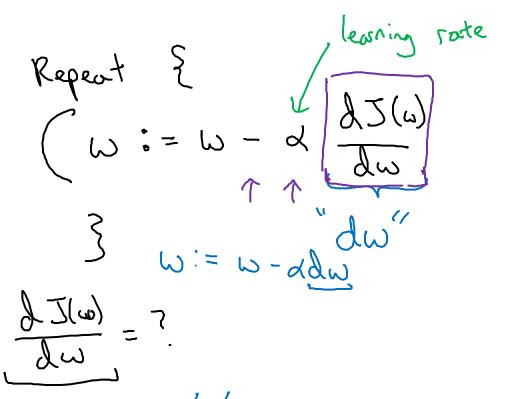
Want to find w, b that minimize J(w, b)





Gradient Descent





$$J(\omega,b)$$

$$b:=b-\lambda \frac{\partial J(\omega,b)}{\partial \omega}$$

$$\frac{\partial J(\omega,b)}{\partial \omega}$$

$$\frac{\partial J(\omega,b)}{\partial \omega}$$

$$\frac{\partial J(\omega,b)}{\partial \omega}$$

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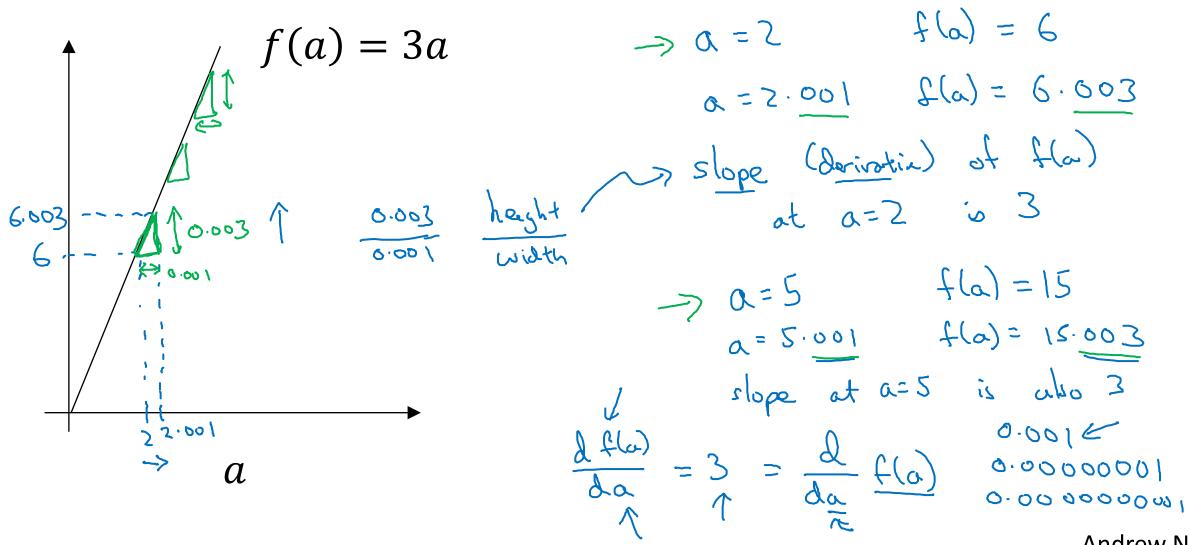


Basics of Neural Network Programming

Derivatives

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Intuition about derivatives



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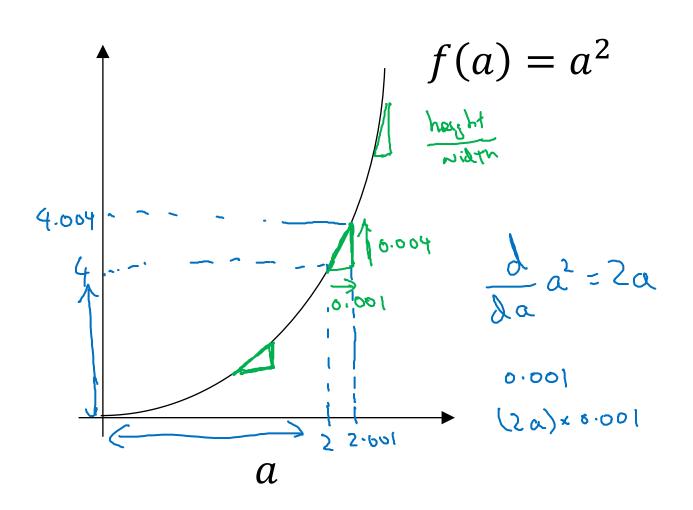


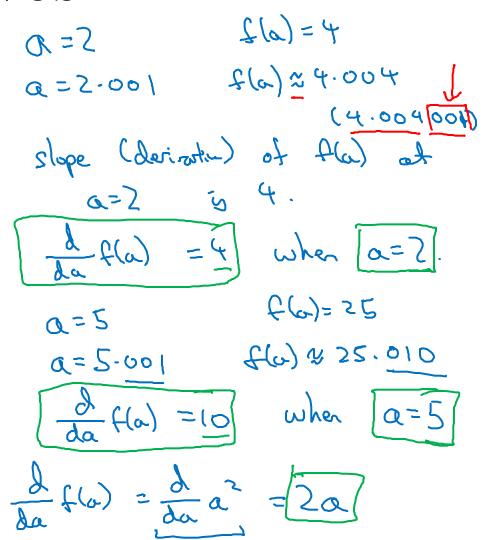
Basics of Neural Network Programming

More derivatives examples

Intuition about derivatives









Basics of Neural Network Programming

Computation Graph

Computation Graph

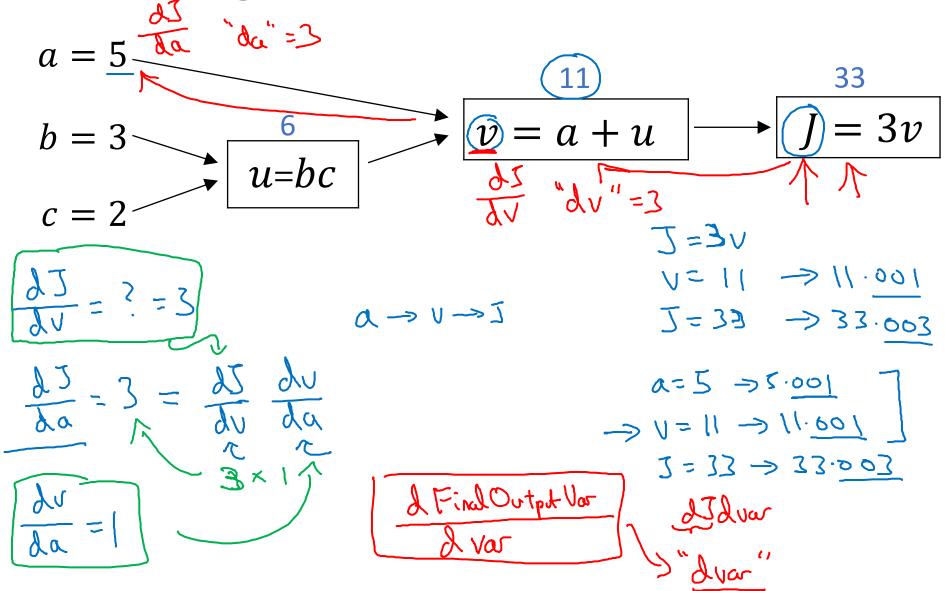
$$J(a,b,c) = 3(a+bc) = 3(5+3*2) = 33$$
 $U = bc$
 $V = atu$
 $J = 3v$
 $V = a+u$
 $J = 3v$
 $V = a+u$
 $J = 3v$

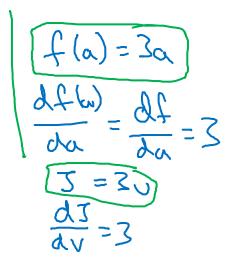


Basics of Neural Network Programming

Derivatives with a Computation Graph

Computing derivatives







Basics of Neural Network Programming

Logistic Regression Gradient descent

Logistic regression recap

$$\Rightarrow z = w^{T}x + b$$

$$\Rightarrow \hat{y} = a = \sigma(z)$$

$$\Rightarrow \mathcal{L}(a, y) = -(y \log(a) + (1 - y) \log(1 - a))$$

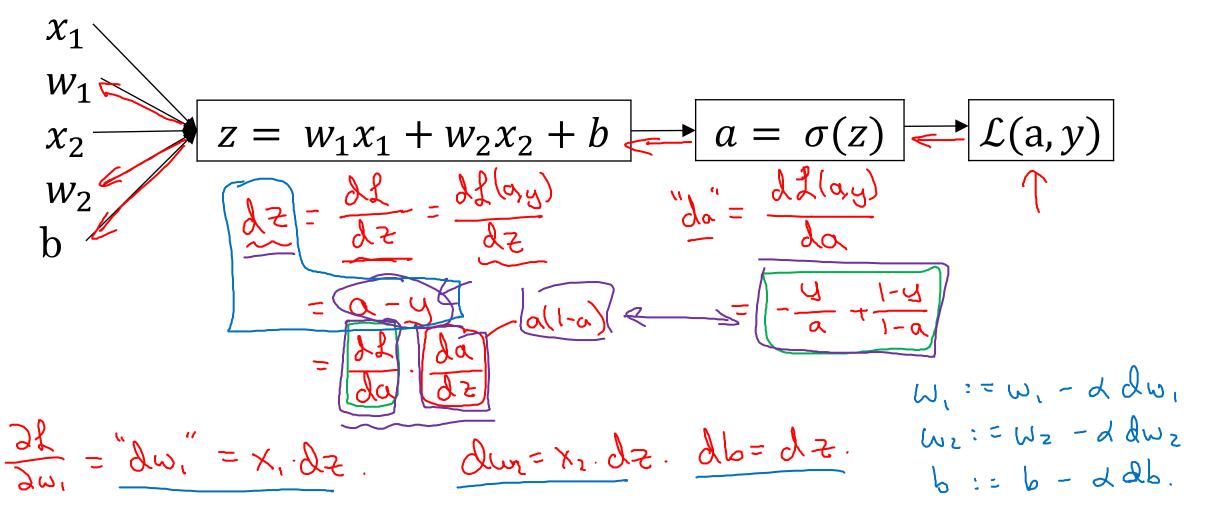
$$\begin{cases} \lambda_{1} \\ \lambda_{2} \\ \lambda_{3} \\ \lambda_{4} \end{cases}$$

$$\begin{cases} \lambda_{1} \\ \lambda_{2} \\ \lambda_{3} \end{cases}$$

$$\begin{cases} \lambda_{1} \\ \lambda_{2} \\ \lambda_{3} \end{cases}$$

$$\begin{cases} \lambda_{2} \\ \lambda_{3} \\ \lambda_{4} \end{cases}$$

Logistic regression derivatives





Basics of Neural Network Programming

Gradient descent on m examples



Basics of Neural Network Programming

Vectorization

deeplearning.ai

for i in rage
$$(n-x)$$
:
 $2+=\omega T:]+x \times T:$



Basics of Neural Network Programming

More vectorization examples

Neural network programming guideline

Whenever possible, avoid explicit for-loops.



Basics of Neural Network Programming

Vectorizing Logistic Regression

Vectorizing Logistic Regression

$$Z^{(1)} = w^{T}x^{(1)} + b$$

$$Z^{(2)} = w^{T}x^{(2)} + b$$

$$Z^{(3)} = w^{T}x^{(3)} + b$$

$$Z^{(3)} = \sigma(z^{(3)})$$

$$Z^$$



Basics of Neural Network Programming

Vectorizing Logistic Regression's Gradient Computation

Vectorizing Logistic Regression

$$\frac{dz^{(1)} = a^{(1)} - y^{(1)}}{dz^{(2)}} = \frac{dz^{(2)} - y^{(2)}}{dz^{(2)}} - \frac{dz^{(2)}}{dz^{(2)}} - \frac{dz^{(2)}}{dz^{(2)}} = \frac{dz^{(2)} - y^{(2)}}{dz^{(2)}} - \frac{dz^{(2)}}{dz^{(2)}} = \frac{dz^{(2)} - y^{(2)}}{dz^{(2)}} - \frac{dz^{(2)}}{dz^{(2)}} - \frac$$

$$db = \frac{1}{m} \sum_{i=1}^{m} dz^{(i)}$$

$$= \frac{1}{m} \left[x^{(i)} + \dots + x^{(i)} dz^{(m)} \right]$$

$$= \frac{1}{m} \left[x^{(i)} + \dots + x^{(i)} dz^{(m)} \right]$$

$$= \frac{1}{m} \left[x^{(i)} + \dots + x^{(i)} dz^{(m)} \right]$$

$$= \frac{1}{m} \left[x^{(i)} + \dots + x^{(i)} dz^{(m)} \right]$$



Basics of Neural Network Programming

Broadcasting in Python

Broadcasting example

Calories from Carbs, Proteins, Fats in 100g of different foods:

Apples Beef Eggs Potatoes

Carb
$$56.0$$
 0.0 4.4 68.0 104.0 52.0 8.0 104.0 52.0 99.0 0.9 13.4 135.0 99.0 0.9 13.4 135.0 $135.$

Broadcasting example

$$\begin{bmatrix} 1 \\ 2 \\ 3 \\ 4 \end{bmatrix} + \begin{bmatrix} 100 \\ 100 \\ 100 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix} + \begin{bmatrix} 100 & 200 & 300 \\ 100 & 200 & 300 \end{bmatrix}$$

$$(m,n) (2)3)$$

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix} + \begin{bmatrix} 100 \\ 200 \end{bmatrix}$$

$$(m,n)$$

General Principle

$$(M, 1) \qquad + \qquad (I, n) \qquad \sim (M, n)$$

$$(M, 1) \qquad + \qquad R$$

$$\begin{bmatrix} 1 \\ 2 \\ 1 \end{bmatrix} \qquad + \qquad 100 \qquad = \qquad \begin{bmatrix} 101 \\ 102 \\ 103 \end{bmatrix}$$

$$[1 \ 23] \qquad + \qquad 100 \qquad = \qquad \begin{bmatrix} 101 \\ 102 \\ 103 \end{bmatrix}$$

Matlab/Octave: bsxfun

Implementing Logistic Regression.

J = 0,
$$dw_1 = 0$$
, $dw_2 = 0$, $db = 0$

for $i = 1$ to m :

 $z^{(i)} = w^T x^{(i)} + b$
 $a^{(i)} = \sigma(z^{(i)}) \leftarrow$
 $J += -[y^{(i)} \log a^{(i)} + (1-y^{(i)}) \log(1-a^{(i)})]$
 $dz^{(i)} = a^{(i)} - y^{(i)} \leftarrow$

$$dw_1 += x_1^{(i)} dz^{(i)} d$$

$$Z = \omega^{T} X + b$$

$$= n p \cdot dot (\omega \cdot T \cdot X) + b$$

$$A = \sigma(Z)$$

$$dZ = A - Y$$

$$dw = m \times dZ^{T}$$

$$db = m n p \cdot sun(dZ)$$

$$\omega := \omega - d d\omega$$

$$b := b - d d\omega$$

Neural network programming guideline

Whenever possible, avoid explicit for-loops.

$$U = AV$$

$$U_{i} = \sum_{j} \sum_{i} A_{i,j} V_{j}$$

$$U = np.zeros((n, i))$$

$$for i \dots \leftarrow C$$

$$for j \dots \leftarrow C$$

$$u \in AUIT_{i}I * vC_{j}I$$

Vectors and matrix valued functions

Say you need to apply the exponential operation on every element of a matrix/vector.

$$v = \begin{bmatrix} v_1 \\ \vdots \\ v_n \end{bmatrix} \rightarrow u = \begin{bmatrix} e^{v_1} \\ e^{v_2} \end{bmatrix}$$

$$v = \begin{bmatrix} v_1 \\ \vdots \\ v_n \end{bmatrix} \rightarrow u = \begin{bmatrix} e^{v_1} \\ e^{v_n} \end{bmatrix}$$

$$u = \text{np. exp}(v) \leftarrow \text{np. log}(v)$$

$$\text{np. log}(v)$$

$$\text{np. abs}(v)$$

$$\text{np. haximun}(v, o)$$

$$\text{np. haximun}(v, o)$$

$$\text{np. haximun}(v, o)$$

Logistic regression derivatives

$$J = 0, \quad dw1 = 0, \quad dw2 = 0, \quad db = 0$$

$$\int for \ i = 1 \ to \ n:$$

$$Z^{(i)} = w^T x^{(i)} + b$$

$$a^{(i)} = \sigma(z^{(i)})$$

$$J + = -[y^{(i)} \log \hat{y}^{(i)} + (1 - y^{(i)}) \log(1 - \hat{y}^{(i)})]$$

$$dz^{(i)} = a^{(i)}(1 - a^{(i)})$$

$$dw_1 + x_1^{(i)} dz^{(i)}$$

$$dw_2 + x_2^{(i)} dz^{(i)}$$

$$db + dz^{(i)}$$

$$J = J/m, \quad dw_1 = dw_1/m, \quad dw_2 = dw_2/m, \quad db = db/m$$

$$\int dw / = m.$$

Logistic regression on m examples

$$\frac{J(\omega,b)}{J(\omega,b)} = \frac{1}{m} \sum_{i=1}^{m} f(\alpha^{(i)}, y^{(i)})$$

$$\frac{J(\omega,b)}{J(\omega,b)} = \frac{1}{m} \sum_{i=1}^{m} f(\alpha^{(i)}, y^{(i)})$$

$$\frac{J(\omega,b)}{J(\omega,b)} = \frac{1}{m} \sum_{i=1}^{m} \frac{J(\alpha^{(i)}, y^{(i)})}{J(\alpha^{(i)}, y^{(i)})}$$

Logistic regression on m examples

$$J=0; dw_{1}=0; dw_{2}=0; db=0$$

$$For i=1 to m$$

$$Z^{(i)}=\omega^{T}x^{(i)}+b$$

$$Q^{(i)}=6(Z^{(i)})$$

$$J+=-[y^{(i)}(\log Q^{(i)}+(1-y^{(i)})\log(1-Q^{(i)})]$$

$$dz^{(i)}=Q^{(i)}-y^{(i)}$$

$$dw_{1}+=x^{(i)}dz^{(i)}$$

$$dw_{2}+=x^{(i)}dz^{(i)}$$

$$J=0; dw_{2}(1-Q^{(i)})$$

$$dz^{(i)}=Q^{(i)}+(1-y^{(i)})\log(1-Q^{(i)})$$

$$dz^{(i)}=Q^{(i)}-y^{(i)}$$

$$dw_{1}+=x^{(i)}dz^{(i)}$$

$$dw_{2}+=x^{(i)}dz^{(i)}$$

$$dw_{2}+=dz^{(i)}$$

$$dw_{3}+=dz^{(i)}$$

$$dw_{4}+=dz^{(i)}$$

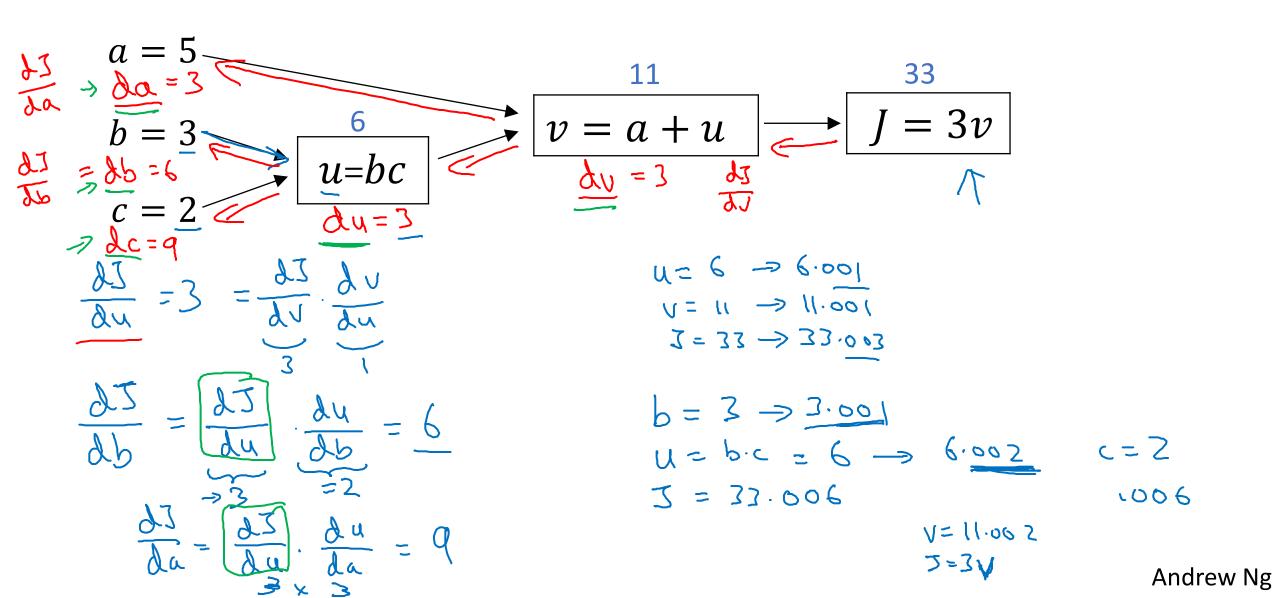
$$dw_{5}+=dz^{(i)}$$

$$dw_{7}+=m; dw_{7}+=m; db/=m.$$

$$d\omega_1 = \frac{\partial J}{\partial \omega_1}$$
 $\omega_1 := \omega_1 - d d\omega_1$
 $\omega_2 := \omega_2 - d d\omega_2$
 $b := b - d db$

Vectorization

Computing derivatives



More derivative examples

$$f(a) = a^2$$

$$f(\omega) = \alpha^3$$

$$\frac{\lambda}{\lambda a} (\omega) = 3a^{2}$$

$$3x2^{3} = 12$$

$$a = 2$$
 $f(a) = 4$
 $a = 2-001$ $f(a) = 4-004$

$$a = 5.001$$
 $f(a) = 8$
 $a = 5.001$ $f(a) = 8$

$$0.0002 \qquad 0.0002 \qquad 0$$



Basics of Neural Network Programming

A note on python/ numpy vectors

Python Demo

Python / numpy vectors

```
import numpy as np
a = np.random.randn(5)
a = np.random.randn((5,1))
a = np.random.randn((1,5))
assert (a.shape = (5,1))
```