

Mini-batch gradient descent

Batch vs. mini-batch gradient descent X { 4 } \ \ { 5 t }.

Vectorization allows you to efficiently compute on m examples.

Andrew Ng

stop of grabit dect Mini-batch gradient descent veg Xiti. (as ifmel soo) Formal peop on X Sts. I [] = M [[] X { t } + P [[]] ALD = BCO (500) | lectoisel implementation (1000 examples) A TW = 9 TW (3 TW) Compute cost $J^{\{t\}} = \frac{1}{1000} \stackrel{\text{Red}}{=} J(y^{(i)}, y^{(i)}) + \frac{\lambda}{2.1000} \stackrel{\text{E}}{=} ||W^{(t)}||_F^2$ Bookprop to compart grobates cort Jeez (vsy (x8t2) Y8t2)) W:= W - ddw (2), btl) = btl) - albter "I epoch" poss through training set.



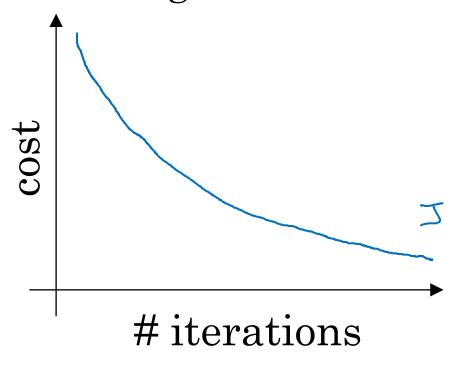
deeplearning.ai

Optimization Algorithms

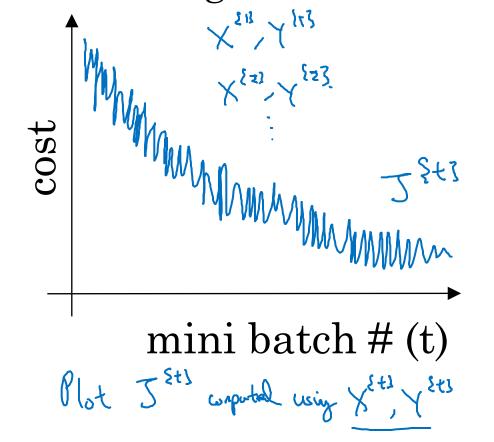
Understanding mini-batch gradient descent

Training with mini batch gradient descent

Batch gradient descent



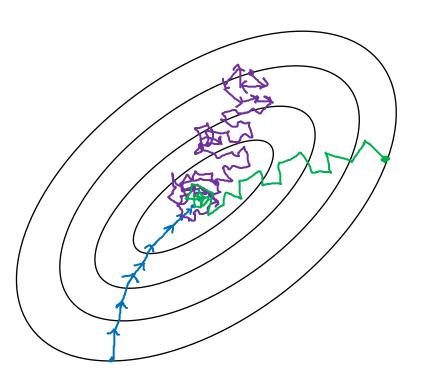
Mini-batch gradient descent



Choosing your mini-batch size

> If mini-both Size = m : Borth godul desch. (X [1]) = (X, Y) > If mini-both Size = 1 : Stochasta graph desch. Every example is it our (X [18] Y [1]) = (x (1), y (1)) ... (x (2) (1)) mini-both.

In practice: Someth in-bother I all m



Stochostic

gredent

legant

Lose speakup

from vortinitation

In-bother (min-hoth size not too by/small) Furlest learnly. Vectorantian. (N 1 000)

· Vectorian.

(N 2 000)

Pe

Make procon without

processy entire truly set.

Bootch

gradient desent

(min; horter size = m)

Two long

Too long per iteration

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Choosing your mini-batch size

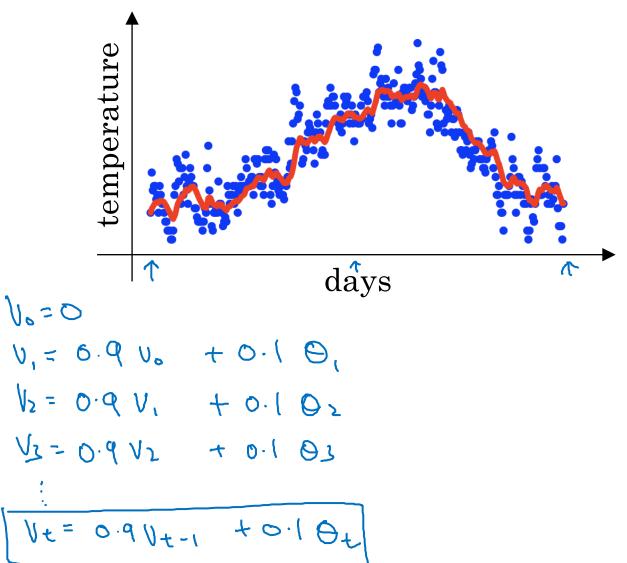
If small tray set: Use both graher descent.
(m < 2000) Typical minz-borth sizes! -> 64 , 128, 256, 512 2^{2} 2^{8} 2^{3} Make sure ministrate fit in CPU/GPU memory. X Ex Y Ex 3



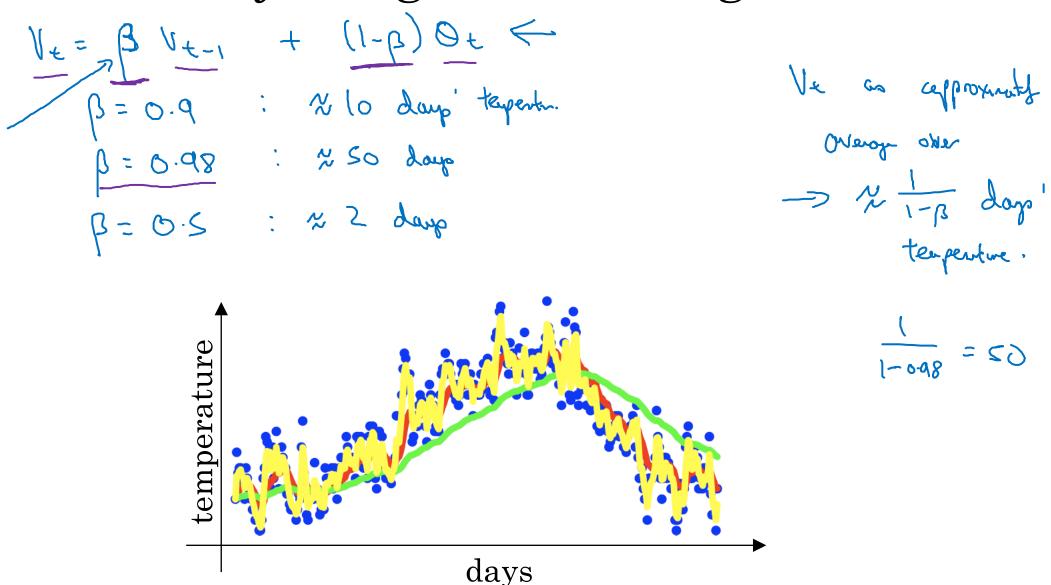
Exponentially weighted averages

Temperature in London

```
\theta_{1} = 40^{\circ}F 4^{\circ}C \leftarrow
\theta_{2} = 49^{\circ}F 4^{\circ}C
\theta_{3} = 45^{\circ}F
\vdots
\theta_{180} = 60^{\circ}F C
\vdots
\theta_{181} = 56^{\circ}F
\vdots
```



Exponentially weighted averages

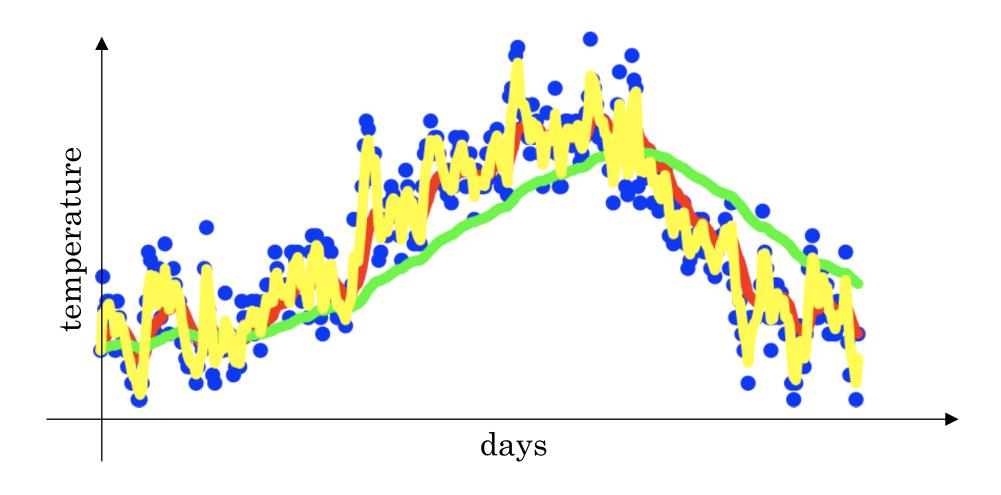




Understanding exponentially weighted averages

Exponentially weighted averages

$$v_t = \beta v_{t-1} + (1 - \beta)\theta_t$$



Exponentially weighted averages

$$v_t = \beta v_{t-1} + (1-\beta)\theta_t$$

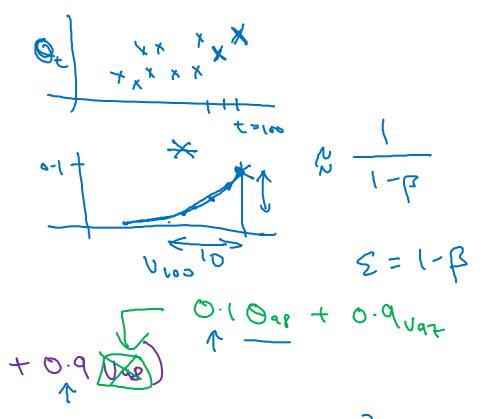
$$v_{100} = 0.9v_{99} + 0.1\theta_{100}$$

$$v_{99} = 0.9v_{98} + 0.1\theta_{99}$$

$$v_{98} = 0.9v_{97} + 0.1\theta_{98}$$
...

$$\frac{1}{100} = 0.10 \cos + 0.9 \log (0.10 \cos + 0.9 \log)$$

$$= 0.10 \cos + 0.1 \times 0.9 \cdot 0.9 + 0.1 (0.9)^2 \log + 0.1 (0.9)^2 \log_{10} +$$



$$\frac{100}{100} = \frac{1}{100} = \frac{$$

Implementing exponentially weighted averages

$$v_0 = 0$$

 $v_1 = \beta v_0 + (1 - \beta) \theta_1$
 $v_2 = \beta v_1 + (1 - \beta) \theta_2$
 $v_3 = \beta v_2 + (1 - \beta) \theta_3$

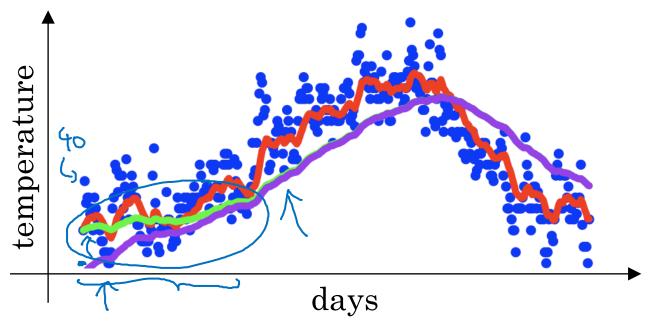
$$V_{0} := 0$$
 $V_{0} := \beta V + (1-\beta) O_{1}$
 $V_{0} := \beta V + (1-\beta) O_{2}$
 $V_{0} := \beta V + (1-\beta) O_{2}$

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Bias correction in exponentially weighted average

Bias correction



$$v_t = \beta v_{t-1} + (1 - \beta)\theta_t$$

$$v_0 = 0$$

$$v_1 = 0.98 v_0 + 0.02 \Theta_1$$

$$v_2 = 0.98 v_1 + 0.02 \Theta_2$$

$$= 0.98 \times 0.02 \times \Theta_1 + 0.02 \Theta_2$$

$$= 0.98 \times 0.02 \times \Theta_1 + 0.02 \Theta_2$$

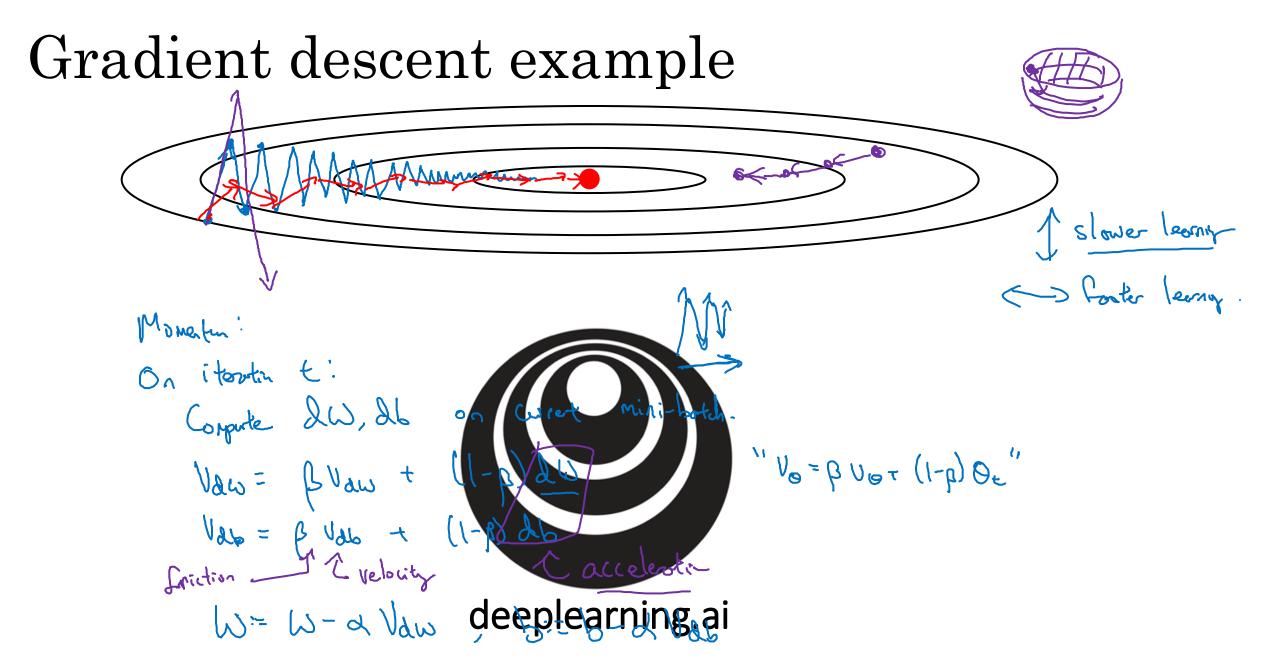
$$\frac{1-\beta^{t}}{t=2:} \quad 1-\beta^{t} = 1-(0.98)^{2} = 0.0396$$

$$\frac{1-\beta^{t}}{0.0396} = 0.0396$$

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Gradient descent with momentum



Implementation details

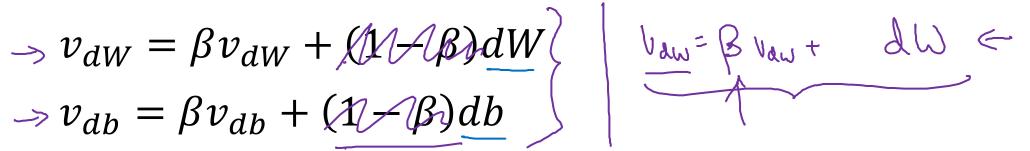
On iteration t:

Compute dW, db on the current mini-batch

$$v_{dW} = \beta v_{dW} + M \beta dW$$

$$v_{db} = \beta v_{db} + (1 - \beta) db$$

$$W = W - \alpha v_{dW}, \ b = b - \alpha v_{db}$$

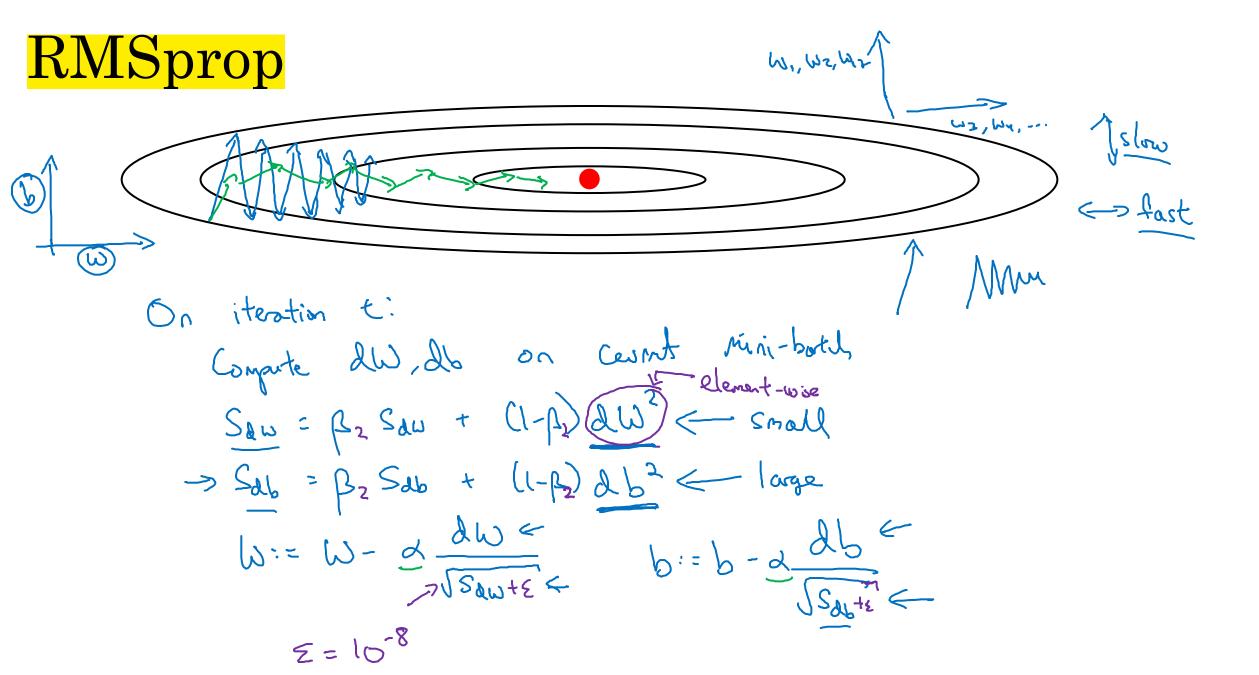


Hyperparameters:
$$\alpha, \beta$$

$$\beta = 0.9$$
Overlage on last 100 graduits



RMSprop





Adam optimization algorithm

Adam optimization algorithm

Hyperparameters choice:

$$\rightarrow$$
 d: needs to be tune
 \rightarrow β_i : 0.9 \rightarrow (dw)
 \rightarrow β_2 : 0.999 \rightarrow (dw²)
 \rightarrow Σ : 10-8

Adam: Adaptiv moment estimation

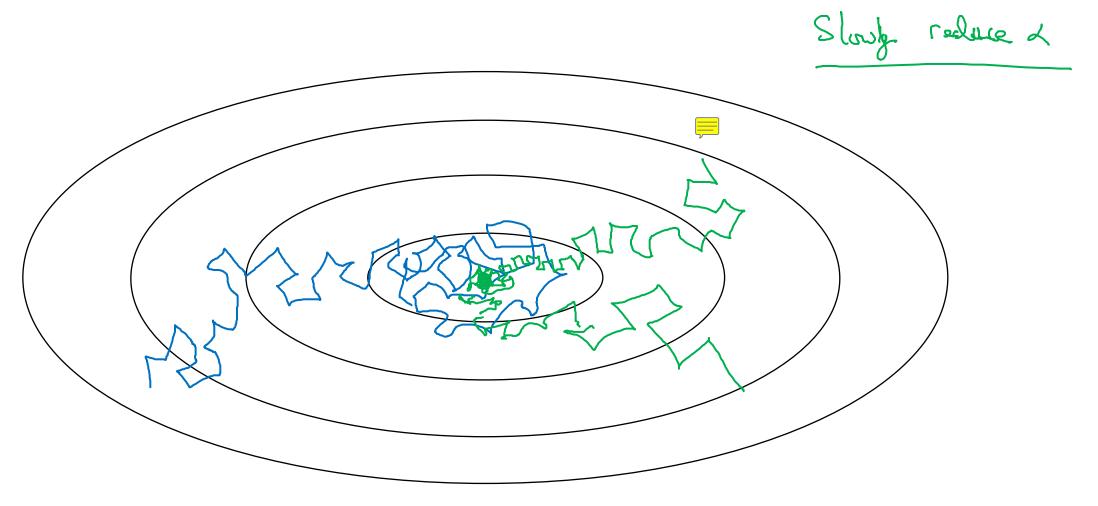


Adam Coates

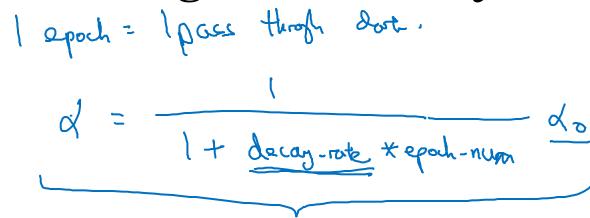


Learning rate decay

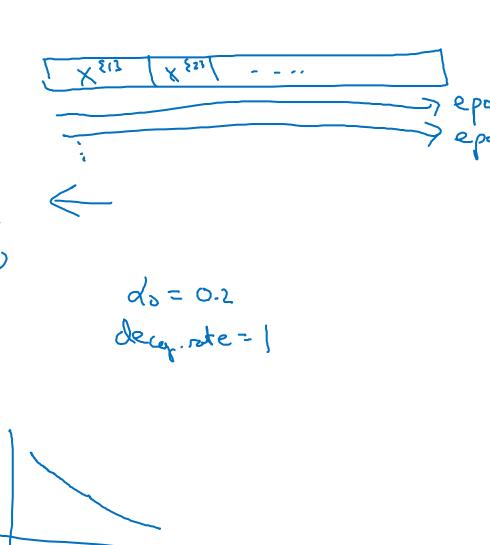
Learning rate decay



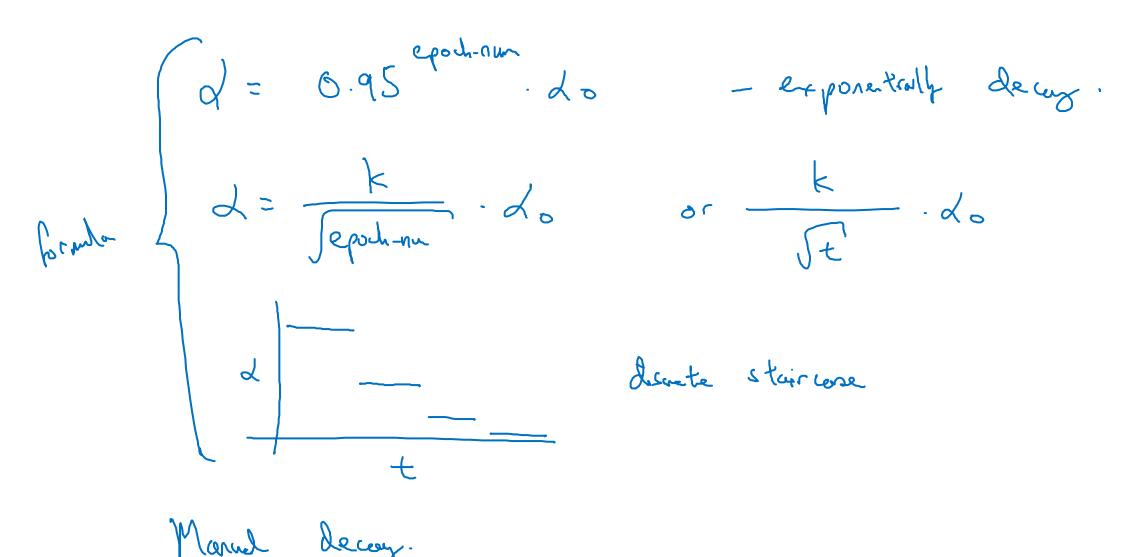
Learning rate decay



Epoch	2
	0.1
2	0.067
3	G · V S
4	0. <u>a</u> ct
·	- - -



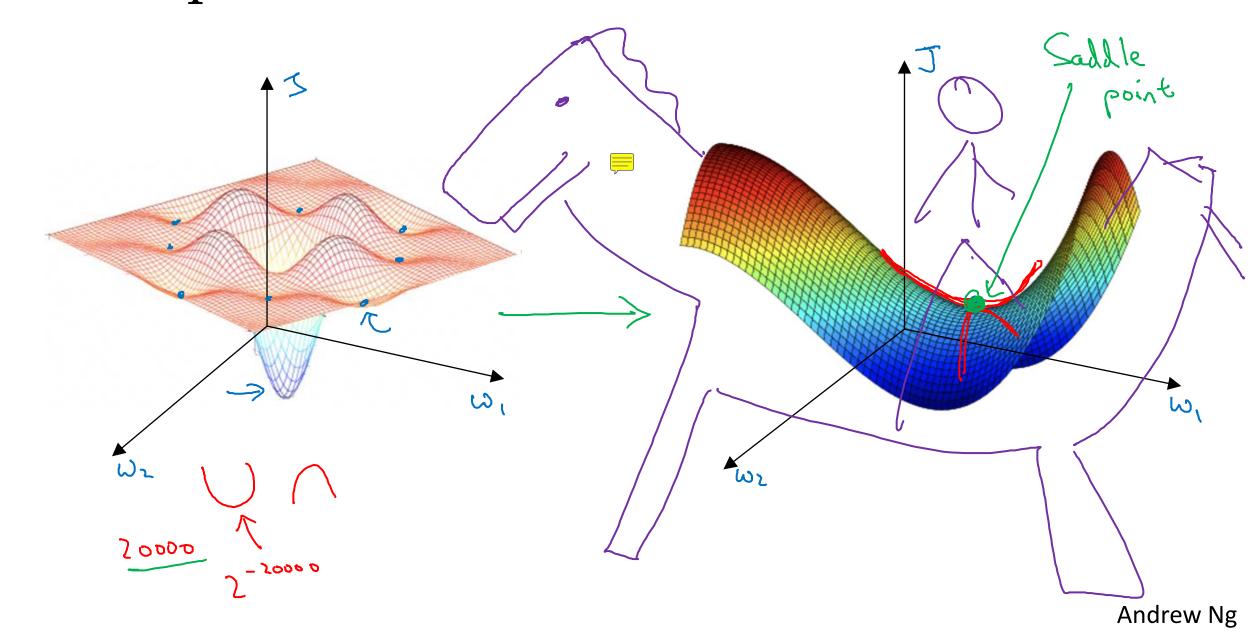
Other learning rate decay methods



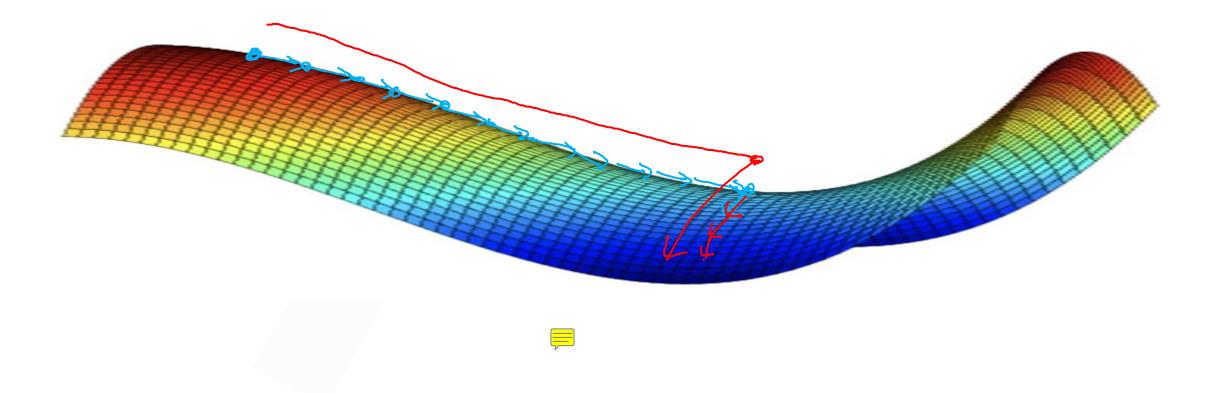


The problem of local optima

Local optima in neural networks



Problem of plateaus



- Unlikely to get stuck in a bad local optima
- Plateaus can make learning slow