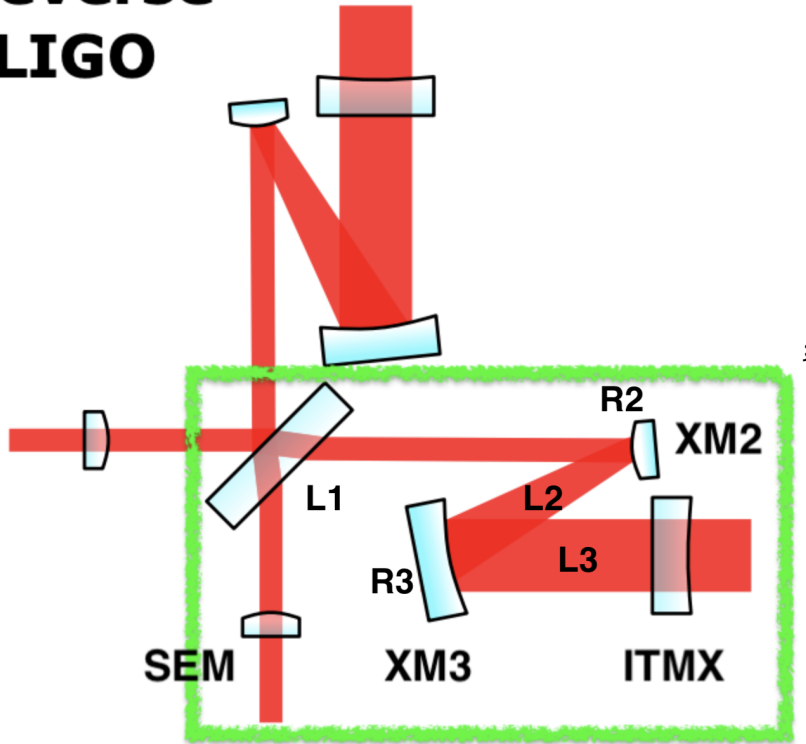


Reverse aLIGO

In[]:=



```

In[ ]:= ClearAll["Global'*"];
ITMXXM3 = {{1, L3}, {0, 1}};
XM3XM2 = {{1, L2}, {0, 1}};
XM2SEM = {{1, L1}, {0, 1}};
XM3 = {{1, 0}, {-2 / (R3 * Cos[α]), 1}};
XM2 = {{1, 0}, {-2 / (R2 * Cos[α]), 1}};
Mtot = XM2SEM.XM2.XM3XM2.XM3.ITMXXM3;
q0 = z + I * Pi * w0^2 / λ;
ABCD = Mtot.{q0, 1};
qout = ABCD[[1]] / ABCD[[2]];
positive = L1 > 0 && L2 > 0 && L3 > 0 && R2 < 0 && R3 > 0 && z > 0 && w0 > 0 && λ > 0 && α > 0;
cons = {L1 ∈ Reals, L2 ∈ Reals, L3 ∈ Reals,
        R2 ∈ Reals, R3 ∈ Reals, α ∈ Reals, z ∈ Reals, w0 ∈ Reals, λ ∈ Reals};
zout = Simplify[ComplexExpand[Re[qout]], positive];
zR = Simplify[ComplexExpand[Im[qout]], positive];
Rc = zout + zR^2 / zout;
Rc

```

$$\begin{aligned}
 \text{Out[]} = & \left(16 \pi^2 R2^4 R3^4 w0^4 \lambda^2 \cos[\alpha]^8 \right. \\
 & (128 L2^2 \pi^2 w0^4 + 16 \pi^2 R2^2 w0^4 + 32 \pi^2 R2 R3 w0^4 + 16 \pi^2 R3^2 w0^4 + 128 L2^2 L3^2 \lambda^2 + 16 L3^2 R2^2 \lambda^2 + \\
 & 64 L2 L3 R2 R3 \lambda^2 + 32 L3^2 R2 R3 \lambda^2 + 16 L2^2 R3^2 \lambda^2 + 32 L2 L3 R3^2 \lambda^2 + 16 L3^2 R3^2 \lambda^2 + \\
 & 3 R2^2 R3^2 \lambda^2 + 256 L2^2 L3 z \lambda^2 + 32 L3 R2^2 z \lambda^2 + 64 L2 R2 R3 z \lambda^2 + 64 L3 R2 R3 z \lambda^2 + \\
 & 32 L2 R3^2 z \lambda^2 + 32 L3 R3^2 z \lambda^2 + 128 L2^2 z^2 \lambda^2 + 16 R2^2 z^2 \lambda^2 + 32 R2 R3 z^2 \lambda^2 + 16 R3^2 z^2 \lambda^2 - \\
 & \left. 8 \times (16 L2 \pi^2 (R2 + R3) w0^4 + 16 L2^2 R3 (L3 + z) \lambda^2 + 3 R2 R3 (R2 + R3) (L3 + z) \lambda^2 + \right.
 \end{aligned}$$

$$\begin{aligned}
& L2 \left(3 R2 R3^2 + 16 L3^2 (R2 + R3) + 32 L3 (R2 + R3) z + 16 R2 z^2 + 16 R3 z^2 \right) \lambda^2 \Big) \cos[\alpha] + \\
& 4 \times \left(4 \pi^2 (R2 + R3)^2 w0^4 + \left(4 L2^2 R3^2 + R2^2 R3^2 + 4 L3^2 (R2 + R3)^2 + 8 L2 R3 (2 R2 + R3) z + \right. \right. \\
& \quad \left. \left. 4 R2^2 z^2 + 8 R2 R3 z^2 + 4 R3^2 z^2 + 8 L3 (L2 R3 (2 R2 + R3) + (R2 + R3)^2 z) \right) \lambda^2 \right) \cos[2\alpha] - \\
& 8 L3 R2^2 R3 \lambda^2 \cos[3\alpha] - 8 L2 R2 R3^2 \lambda^2 \cos[3\alpha] - 8 L3 R2 R3^2 \lambda^2 \cos[3\alpha] - \\
& 8 R2^2 R3 z \lambda^2 \cos[3\alpha] - 8 R2 R3^2 z \lambda^2 \cos[3\alpha] + R2^2 R3^2 \lambda^2 \cos[4\alpha] \Big) \Big) / \\
& \left(\left(16 \pi^2 w0^4 (-2 L2 + (R2 + R3) \cos[\alpha])^2 + \lambda^2 \right. \right. \\
& \quad \left. \left(8 L2 L3 + R2 R3 + 8 L2 z - 4 (L2 R3 + L3 (R2 + R3) + (R2 + R3) z) \cos[\alpha] + R2 R3 \cos[2\alpha] \right)^2 \right) \\
& (128 L1 L2^2 \pi^2 w0^4 + 16 L1 \pi^2 R2^2 w0^4 + 16 L2 \pi^2 R2^2 w0^4 + 32 L1 \pi^2 R2 R3 w0^4 + \\
& 32 L2 \pi^2 R2 R3 w0^4 + 16 L1 \pi^2 R3^2 w0^4 + 128 L1 L2^2 L3^2 \lambda^2 + 16 L1 L3^2 R2^2 \lambda^2 + \\
& 16 L2 L3^2 R2^2 \lambda^2 + 64 L1 L2 L3 R2 R3 \lambda^2 + 32 L2^2 L3 R2 R3 \lambda^2 + 32 L1 L3^2 R2 R3 \lambda^2 + \\
& 32 L2 L3^2 R2 R3 \lambda^2 + 16 L1 L2^2 R3^2 \lambda^2 + 32 L1 L2 L3 R3^2 \lambda^2 + 16 L1 L3^2 R3^2 \lambda^2 + \\
& 3 L1 R2^2 R3^2 \lambda^2 + 3 L2 R2^2 R3^2 \lambda^2 + 3 L3 R2^2 R3^2 \lambda^2 + 256 L1 L2^2 L3 z \lambda^2 + 32 L1 L3 R2^2 z \lambda^2 + \\
& 32 L2 L3 R2^2 z \lambda^2 + 64 L1 L2 R2 R3 z \lambda^2 + 32 L2^2 R2 R3 z \lambda^2 + 64 L1 L3 R2 R3 z \lambda^2 + \\
& 64 L2 L3 R2 R3 z \lambda^2 + 32 L1 L2 R3^2 z \lambda^2 + 32 L1 L3 R3^2 z \lambda^2 + 3 R2^2 R3^2 z \lambda^2 + 128 L1 L2^2 z^2 \lambda^2 + \\
& 16 L1 R2^2 z^2 \lambda^2 + 16 L2 R2^2 z^2 \lambda^2 + 32 L1 R2 R3 z^2 \lambda^2 + 32 L2 R2 R3 z^2 \lambda^2 + 16 L1 R3^2 z^2 \lambda^2 - \\
& 4 (L1 (32 L2 \pi^2 (R2 + R3) w0^4 + 32 L2^2 R3 (L3 + z) \lambda^2 + 6 R2 R3 (R2 + R3) (L3 + z) \lambda^2 + \\
& \quad 2 L2 (3 R2 R3^2 + 16 L3^2 (R2 + R3) + 32 L3 (R2 + R3) z + 16 R2 z^2 + 16 R3 z^2) \lambda^2) + \\
& \quad R2 (6 L2 R3 (R2 + R3) (L3 + z) \lambda^2 + 3 R3 (R2 + R3) (\pi^2 w0^4 + (L3 + z)^2 \lambda^2) + \\
& \quad L2^2 (16 \pi^2 w0^4 + (16 L3^2 + 3 R3^2 + 32 L3 z + 16 z^2) \lambda^2)) \Big) \cos[\alpha] + \\
& 4 (L1 (4 \pi^2 (R2 + R3)^2 w0^4 + (4 L2^2 R3^2 + R2^2 R3^2 + 4 L3^2 (R2 + R3)^2 + 8 L2 R3 (2 R2 + R3) \\
& \quad z + 4 R2^2 z^2 + 8 R2 R3 z^2 + 4 R3^2 z^2 + 8 L3 (L2 R3 (2 R2 + R3) + (R2 + R3)^2 z) \Big) \lambda^2) + \\
& \quad R2 (4 L2 \pi^2 (R2 + 2 R3) w0^4 + 8 L2^2 R3 (L3 + z) \lambda^2 + R2 R3^2 (L3 + z) \lambda^2 + \\
& \quad L2 (4 L3^2 (R2 + 2 R3) + 8 L3 (R2 + 2 R3) z + 8 R3 z^2 + R2 (R3^2 + 4 z^2) \Big) \lambda^2) \Big) \cos[2\alpha] - \\
& 4 \pi^2 R2^2 R3 w0^4 \cos[3\alpha] - 4 \pi^2 R2 R3^2 w0^4 \cos[3\alpha] - 8 L1 L3 R2^2 R3 \lambda^2 \cos[3\alpha] - \\
& 8 L2 L3 R2^2 R3 \lambda^2 \cos[3\alpha] - 4 L3^2 R2^2 R3 \lambda^2 \cos[3\alpha] - \\
& 8 L1 L2 R2 R3^2 \lambda^2 \cos[3\alpha] - 4 L2^2 R2 R3^2 \lambda^2 \cos[3\alpha] - \\
& 8 L1 L3 R2 R3^2 \lambda^2 \cos[3\alpha] - 8 L2 L3 R2 R3^2 \lambda^2 \cos[3\alpha] - 4 L3^2 R2 R3^2 \lambda^2 \cos[3\alpha] - \\
& 8 L1 R2^2 R3 z \lambda^2 \cos[3\alpha] - 8 L2 R2^2 R3 z \lambda^2 \cos[3\alpha] - 8 L3 R2^2 R3 z \lambda^2 \cos[3\alpha] - \\
& 8 L1 R2 R3^2 z \lambda^2 \cos[3\alpha] - 8 L2 R2 R3^2 z \lambda^2 \cos[3\alpha] - 8 L3 R2 R3^2 z \lambda^2 \cos[3\alpha] - \\
& 4 R2^2 R3 z^2 \lambda^2 \cos[3\alpha] - 4 R2 R3^2 z^2 \lambda^2 \cos[3\alpha] + L1 R2^2 R3^2 \lambda^2 \cos[4\alpha] + \\
& L2 R2^2 R3^2 \lambda^2 \cos[4\alpha] + L3 R2^2 R3^2 \lambda^2 \cos[4\alpha] + R2^2 R3^2 z \lambda^2 \cos[4\alpha] \Big) \Big) + \\
& (128 L1 L2^2 \pi^2 w0^4 + 16 L1 \pi^2 R2^2 w0^4 + 16 L2 \pi^2 R2^2 w0^4 + 32 L1 \pi^2 R2 R3 w0^4 + \\
& 32 L2 \pi^2 R2 R3 w0^4 + \\
& 16 L1 \pi^2 R3^2 w0^4 + \\
& 128 L1 L2^2 L3^2 \lambda^2 + 16 L1 L3^2 R2^2 \lambda^2 + \\
& 16 L2 L3^2 R2^2 \lambda^2 + 64 L1 L2 L3 R2 R3 \lambda^2 + \\
& 32 L2^2 L3 R2 R3 \lambda^2 + 32 L1 L3^2 R2 R3 \lambda^2 + \\
& 32 L2 L3^2 R2 R3 \lambda^2 + 16 L1 L2^2 R3^2 \lambda^2 + \\
& 32 L1 L2 L3 R3^2 \lambda^2 + 16 L1 L3^2 R3^2 \lambda^2 + \\
& 3 L1 R2^2 R3^2 \lambda^2 + 3 L2 R2^2 R3^2 \lambda^2 + 3 L3 R2^2 R3^2 \lambda^2 + \\
& 256 L1 L2^2 L3 z \lambda^2 + 32 L1 L3 R2^2 z \lambda^2 + \\
& 32 L2 L3 R2^2 z \lambda^2 + 64 L1 L2 R2 R3 z \lambda^2 +
\end{aligned}$$

$$\begin{aligned}
& 32 L2^2 R2 R3 z \lambda^2 + 64 L1 L3 R2 R3 z \lambda^2 + \\
& 64 L2 L3 R2 R3 z \lambda^2 + 32 L1 L2 R3^2 z \lambda^2 + \\
& 32 L1 L3 R3^2 z \lambda^2 + 3 R2^2 R3^2 z \lambda^2 + 128 L1 L2^2 z^2 \lambda^2 + \\
& 16 L1 R2^2 z^2 \lambda^2 + 16 L2 R2^2 z^2 \lambda^2 + 32 L1 R2 R3 z^2 \lambda^2 + \\
& 32 L2 R2 R3 z^2 \lambda^2 + 16 L1 R3^2 z^2 \lambda^2 - \\
& 4 \left(L1 \left(32 L2 \pi^2 (R2 + R3) w0^4 + 32 L2^2 R3 (L3 + z) \lambda^2 + 6 R2 R3 (R2 + R3) (L3 + z) \lambda^2 + \right. \right. \\
& \quad \left. \left. 2 L2 \left(3 R2 R3^2 + 16 L3^2 (R2 + R3) + 32 L3 (R2 + R3) z + 16 R2 z^2 + 16 R3 z^2 \right) \lambda^2 \right) + \right. \\
& \quad \left. R2 \left(6 L2 R3 (R2 + R3) (L3 + z) \lambda^2 + 3 R3 (R2 + R3) \left(\pi^2 w0^4 + (L3 + z)^2 \lambda^2 \right) + \right. \right. \\
& \quad \left. \left. L2^2 \left(16 \pi^2 w0^4 + \left(16 L3^2 + 3 R3^2 + 32 L3 z + 16 z^2 \right) \lambda^2 \right) \right) \right) \cos[\alpha] + \\
& 4 \left(L1 \left(4 \pi^2 (R2 + R3)^2 w0^4 + \left(4 L2^2 R3^2 + R2^2 R3^2 + 4 L3^2 (R2 + R3)^2 + 8 L2 R3 (2 R2 + R3) z + \right. \right. \right. \\
& \quad \left. \left. \left. 4 R2^2 z^2 + 8 R2 R3 z^2 + 4 R3^2 z^2 + 8 L3 \left(L2 R3 (2 R2 + R3) + (R2 + R3)^2 z \right) \right) \lambda^2 \right) + \right. \\
& \quad \left. R2 \left(4 L2 \pi^2 (R2 + 2 R3) w0^4 + 8 L2^2 R3 (L3 + z) \lambda^2 + R2 R3^2 (L3 + z) \lambda^2 + \right. \right. \\
& \quad \left. \left. L2 \left(4 L3^2 (R2 + 2 R3) + 8 L3 (R2 + 2 R3) z + 8 R3 z^2 + R2 (R3^2 + 4 z^2) \right) \lambda^2 \right) \right) \cos[2\alpha] - \\
& 4 \pi^2 R2^2 R3 w0^4 \cos[3\alpha] - 4 \pi^2 R2 R3^2 w0^4 \cos[3\alpha] - 8 L1 L3 R2^2 R3 \lambda^2 \cos[3\alpha] - \\
& 8 L2 L3 R2^2 R3 \lambda^2 \cos[3\alpha] - \\
& 4 L3^2 R2^2 R3 \lambda^2 \cos[3\alpha] - 8 L1 L2 R2 R3^2 \lambda^2 \cos[3\alpha] - \\
& 4 L2^2 R2 R3^2 \lambda^2 \cos[3\alpha] - 8 L1 L3 R2 R3^2 \lambda^2 \cos[3\alpha] - \\
& 8 L2 L3 R2 R3^2 \lambda^2 \cos[3\alpha] - 4 L3^2 R2 R3^2 \lambda^2 \cos[3\alpha] - \\
& 8 L1 R2^2 R3 z \lambda^2 \cos[3\alpha] - 8 L2 R2^2 R3 z \lambda^2 \cos[3\alpha] - \\
& 8 L3 R2^2 R3 z \lambda^2 \cos[3\alpha] - 8 L1 R2 R3^2 z \lambda^2 \cos[3\alpha] - \\
& 8 L2 R2 R3^2 z \lambda^2 \cos[3\alpha] - 8 L3 R2 R3^2 z \lambda^2 \cos[3\alpha] - \\
& 4 R2^2 R3 z^2 \lambda^2 \cos[3\alpha] - 4 R2 R3^2 z^2 \lambda^2 \cos[3\alpha] + \\
& L1 R2^2 R3^2 \lambda^2 \cos[4\alpha] + L2 R2^2 R3^2 \lambda^2 \cos[4\alpha] + \\
& L3 R2^2 R3^2 \lambda^2 \cos[4\alpha] + R2^2 R3^2 z \lambda^2 \cos[4\alpha] \Big) / \\
& (128 L2^2 \pi^2 w0^4 + 16 \pi^2 R2^2 w0^4 + 32 \pi^2 R2 R3 w0^4 + 16 \pi^2 R3^2 w0^4 + \\
& 128 L2^2 L3^2 \lambda^2 + 16 L3^2 R2^2 \lambda^2 + 64 L2 L3 R2 R3 \lambda^2 + \\
& 32 L3^2 R2 R3 \lambda^2 + 16 L2^2 R3^2 \lambda^2 + 32 L2 L3 R3^2 \lambda^2 + \\
& 16 L3^2 R3^2 \lambda^2 + 3 R2^2 R3^2 \lambda^2 + 256 L2^2 L3 z \lambda^2 + \\
& 32 L3 R2^2 z \lambda^2 + 64 L2 R2 R3 z \lambda^2 + 64 L3 R2 R3 z \lambda^2 + \\
& 32 L2 R3^2 z \lambda^2 + 32 L3 R3^2 z \lambda^2 + 128 L2^2 z^2 \lambda^2 + \\
& 16 R2^2 z^2 \lambda^2 + 32 R2 R3 z^2 \lambda^2 + 16 R3^2 z^2 \lambda^2 - \\
& 8 \times \left(16 L2 \pi^2 (R2 + R3) w0^4 + 16 L2^2 R3 (L3 + z) \lambda^2 + 3 R2 R3 (R2 + R3) (L3 + z) \lambda^2 + \right. \\
& \quad \left. L2 \left(3 R2 R3^2 + 16 L3^2 (R2 + R3) + 32 L3 (R2 + R3) z + 16 R2 z^2 + 16 R3 z^2 \right) \lambda^2 \right) \cos[\alpha] + \\
& 4 \times \left(4 \pi^2 (R2 + R3)^2 w0^4 + \left(4 L2^2 R3^2 + R2^2 R3^2 + 4 L3^2 (R2 + R3)^2 + 8 L2 R3 (2 R2 + R3) z + \right. \right. \\
& \quad \left. \left. 4 R2^2 z^2 + 8 R2 R3 z^2 + 4 R3^2 z^2 + 8 L3 \left(L2 R3 (2 R2 + R3) + (R2 + R3)^2 z \right) \right) \lambda^2 \right) \cos[2\alpha] - \\
& 8 L3 R2^2 R3 \lambda^2 \cos[3\alpha] - 8 L2 R2 R3^2 \lambda^2 \cos[3\alpha] - 8 L3 R2 R3^2 \lambda^2 \cos[3\alpha] - \\
& 8 R2^2 R3 z \lambda^2 \cos[3\alpha] - 8 R2 R3^2 z \lambda^2 \cos[3\alpha] + R2^2 R3^2 \lambda^2 \cos[4\alpha] \Big)
\end{aligned}$$

```

In[ ]:= w0val = 0.042941172520941984;
zval = 15471.415708812849;
alphaval = 1 / 180 * Pi;
lambda val = 1064 * 10^(-9);
L3val = 100;
L1val = 80;
R2val = -9.6;
subs = {w0 -> w0val, z -> zval, alpha -> alphaval, lambda -> lambda val, L3 -> L3val, L1 -> L1val, R2 -> R2val};
Rceval = Rc /. subs;
Rcevalsim = Simplify[Rceval]

Out[ ]:= { (5.96454 * 10^43 - 5.04636 * 10^43 R3 + 1.86774 * 10^43 R3^2 - 3.94982 * 10^42 R3^3 + 5.22009 * 10^41 R3^4 -
4.41489 * 10^40 R3^5 + 2.33347 * 10^39 R3^6 - 7.04704 * 10^37 R3^7 + 9.31005 * 10^35 R3^8 +
L2^8 (2.38112 * 10^38 - 5.44949 * 10^34 R3 + 5.55174 * 10^30 R3^2 - 3.28551 * 10^26 R3^3 +
1.23482 * 10^22 R3^4 - 3.01762 * 10^17 R3^5 + 4.68329 * 10^12 R3^6 - 4.22221 * 10^7 R3^7 + 169.444 R3^8) +
L2^7 (9.01274 * 10^39 - 9.54364 * 10^38 R3 + 1.90913 * 10^35 R3^2 - 1.66651 * 10^31 R3^3 + 8.2172 * 10^26
R3^4 - 2.4704 * 10^22 R3^5 + 4.52751 * 10^17 R3^6 - 4.68417 * 10^12 R3^7 + 2.11142 * 10^7 R3^8) +
L2^6 (1.49236 * 10^41 - 3.1574 * 10^40 R3 + 1.67259 * 10^39 R3^2 - 2.86563 * 10^35 R3^3 + 2.08399 * 10^31
R3^4 - 8.21946 * 10^26 R3^5 + 1.85316 * 10^22 R3^6 - 2.26407 * 10^17 R3^7 + 1.17116 * 10^12 R3^8) +
L2^5 (1.41193 * 10^42 - 4.47963 * 10^41 R3 + 4.73922 * 10^40 R3^2 - 1.67415 * 10^39 R3^3 + 2.38898 * 10^35
R3^4 - 1.38963 * 10^31 R3^5 + 4.11027 * 10^26 R3^6 - 6.17768 * 10^21 R3^7 + 3.77362 * 10^16 R3^8) +
L2^4 (8.3482 * 10^42 - 3.53119 * 10^42 R3 + 5.60171 * 10^41 R3^2 - 3.95088 * 10^40 R3^3 + 1.04675 * 10^39
R3^4 - 1.19464 * 10^35 R3^5 + 5.2113 * 10^30 R3^6 - 1.02756 * 10^26 R3^7 + 7.72182 * 10^20 R3^8) +
L2^3 (3.15874 * 10^43 - 1.67011 * 10^43 R3 + 3.53209 * 10^42 R3^2 - 3.73525 * 10^41 R3^3 + 1.97568 * 10^40
R3^4 - 4.18636 * 10^38 R3^5 + 3.58336 * 10^34 R3^6 - 1.0421 * 10^30 R3^7 + 1.0274 * 10^25 R3^8) +
L2^2 (7.46921 * 10^43 - 4.73909 * 10^43 R3 + 1.2528 * 10^43 R3^2 - 1.76625 * 10^42 R3^3 + 1.40076 * 10^41
R3^4 - 5.92613 * 10^39 R3^5 + 1.04587 * 10^38 R3^6 - 5.96972 * 10^33 R3^7 + 8.68124 * 10^28 R3^8) +
L2 (1.00915 * 10^44 - 7.47038 * 10^43 R3 + 2.36983 * 10^43 R3^2 - 4.17626 * 10^42 R3^3 + 4.41556 * 10^41
R3^4 - 2.80109 * 10^40 R3^5 + 9.8727 * 10^38 R3^6 - 1.49225 * 10^37 R3^7 + 4.26109 * 10^32 R3^8) ) /
( (2.50701 * 10^10 - 5.22438 * 10^9 R3 + 2.72178 * 10^8 R3^2 + L2^2 (1.08845 * 10^9 - 62276.2 R3 +
0.999695 R3^2) + L2 (1.04475 * 10^10 - 1.08888 * 10^9 R3 + 31142.9 R3^2) )^2
(2.36585 * 10^10 - 5.07805 * 10^9 R3 + 2.72257 * 10^8 R3^2 + L2^2 (1.08878 * 10^9 - 62295.2 R3 + 1. R3^2) +
L2 (1.01549 * 10^10 - 1.08919 * 10^9 R3 + 31152.2 R3^2) ) *
(5.01403 * 10^10 - 1.04488 * 10^10 R3 + 5.44356 * 10^8 R3^2 +
L2^2 (2.17689 * 10^9 - 124552. R3 + 1.99939 R3^2) +
L2 (2.0895 * 10^10 - 2.17775 * 10^9 R3 + 62285.9 R3^2) ) ) }

In[ ]:=

In[ ]:= Rceval /. {L2 -> 45.5, R3 -> 100}

Out[ ]:= {-79.5919}

```