

Exercise 1

| r  | Suffixes in lexicographical order |
|----|-----------------------------------|
| 0  | \$                                |
| 1  | A B A C C B A C \$                |
| 2  | A C \$                            |
| 3  | A C C A B A C C B A C \$          |
| 4  | A C C B A C \$                    |
| 5  | B A C \$                          |
| 6  | B A C C A B A C C B A C \$        |
| 7  | B A C C B A C \$                  |
| 8  | C \$                              |
| 9  | C A B A C C B A C \$              |
| 10 | C B A C \$                        |
| 11 | C C A B A C C B A C \$            |
| 12 | C C B A C \$                      |

$r = [0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12]$

1.  $\text{pos} = [12, 4, 10, 1, 6, 9, 0, 5, 11, 3, 8, 2, 7]$
2.  $\text{lcp} = [-1, 0, 1, 2, 3, 0, 3, 4, 0, 1, 1, 1, 2, -1]$

3. RMQ:

Sparse table:  $\text{ST}[k][i] = \min(\text{ST}[k-1][i], \text{ST}[k-1][i + 2^{k-1}])$

|            |    |   |   |   |   |   |   |   |    |   |   |    |    |    |
|------------|----|---|---|---|---|---|---|---|----|---|---|----|----|----|
| Lcp, k = 0 | -1 | 0 | 1 | 2 | 3 | 0 | 3 | 4 | 0  | 1 | 1 | 1  | 2  | -1 |
| k = 1      | -1 | 0 | 1 | 2 | 0 | 0 | 3 | 0 | 0  | 1 | 1 | 1  | -1 |    |
| k = 2      | -1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0  | 1 | 1 | -1 |    |    |
| k = 3      | -1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | -1 |   |   |    |    |    |
| k = 4      | -1 |   |   |   |   |   |   |   |    |   |   |    |    |    |

Exercise 2

1.  $S = \text{summer}\$$

F            L  
\$ summe r  
e r\$sum m  
m er\$su m  
m mer\$ s u  
r \$summ e  
s ummer \$  
u mmer\$ s

BWT = rmmue\$s

LF = [4, 2, 3, 6, 1, 0, 5]

C-array:

| C[\$] | C[e] | C[m] | C[r] | C[s] | C[u] |
|-------|------|------|------|------|------|
| 0     | 1    | 2    | 4    | 5    | 6    |

Occurrences table:

|          | r | m | m | u | e | \$ | s |
|----------|---|---|---|---|---|----|---|
|          | 0 | 1 | 2 | 3 | 4 | 5  | 6 |
| Occ (\$) | 0 | 0 | 0 | 0 | 0 | 1  | 1 |
| Occ (e)  | 0 | 0 | 0 | 0 | 1 | 1  | 1 |
| Occ (m)  | 0 | 1 | 2 | 2 | 2 | 2  | 2 |
| Occ (r)  | 1 | 1 | 1 | 1 | 1 | 1  | 1 |
| Occ (s)  | 0 | 0 | 0 | 0 | 0 | 0  | 1 |
| Occ (u)  | 0 | 0 | 0 | 1 | 1 | 1  | 1 |

2.

| F    | L    |
|------|------|
| 0 \$ | B 0  |
| 0 A  | D 0  |
| 1 A  | C 0  |
| 2 A  | \$ 0 |
| 3 A  | B 1  |
| 4 A  | B 2  |
| 0 B  | A 0  |
| 1 B  | A 1  |
| 2 B  | A 2  |
| 3 B  | A 3  |
| 0 C  | D 1  |
| 0 D  | B 3  |
| 1 D  | A 4  |

The ranking (idea similar to occurrences, just in one row)

- 1) Look at B 0. We know, that we need to have 1\$+5A before that. So it should be on 6<sup>th</sup> position in F.
- 2) Same to other characters  
We just sort them and get F

3) From the first row we know, that B will come before \$. So our string will end with B\$.

4) This B is the first B we meet in F (skipping \$ and A). And we see it on the 6<sup>th</sup> position, and we look at the A, which should be before this B. So now we have AB\$ as the end of our string.

We proceed

And get

This!!!

**ABABADCABABDAB\$**

### 3. Importance of \$!!! Example: strings AB and BA

Without \$:

String one: AB

String 2: BA

For both strings:

| Permutation | BWT |
|-------------|-----|
|-------------|-----|

|           |           |
|-----------|-----------|
| <b>AB</b> | <b>BA</b> |
|-----------|-----------|

|           |  |
|-----------|--|
| <b>BA</b> |  |
|-----------|--|

With \$:

String one: BA\$

String 2: AB\$

1:

| Permutation | BWT |
|-------------|-----|
|-------------|-----|

|             |             |
|-------------|-------------|
| <b>\$BA</b> | <b>AB\$</b> |
|-------------|-------------|

|             |  |
|-------------|--|
| <b>A\$B</b> |  |
|-------------|--|

|             |  |
|-------------|--|
| <b>BA\$</b> |  |
|-------------|--|

2:

| Permutation | BWT |
|-------------|-----|
|-------------|-----|

|             |             |
|-------------|-------------|
| <b>\$AB</b> | <b>B\$A</b> |
|-------------|-------------|

|             |  |
|-------------|--|
| <b>AB\$</b> |  |
|-------------|--|

|             |  |
|-------------|--|
| <b>B\$A</b> |  |
|-------------|--|