

# Data Mining Homework Set 2

Course: BETA-INFOMDM Data Mining (INFOMDM)

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**Number of questions:** 5

# Data Mining Homework Set 2

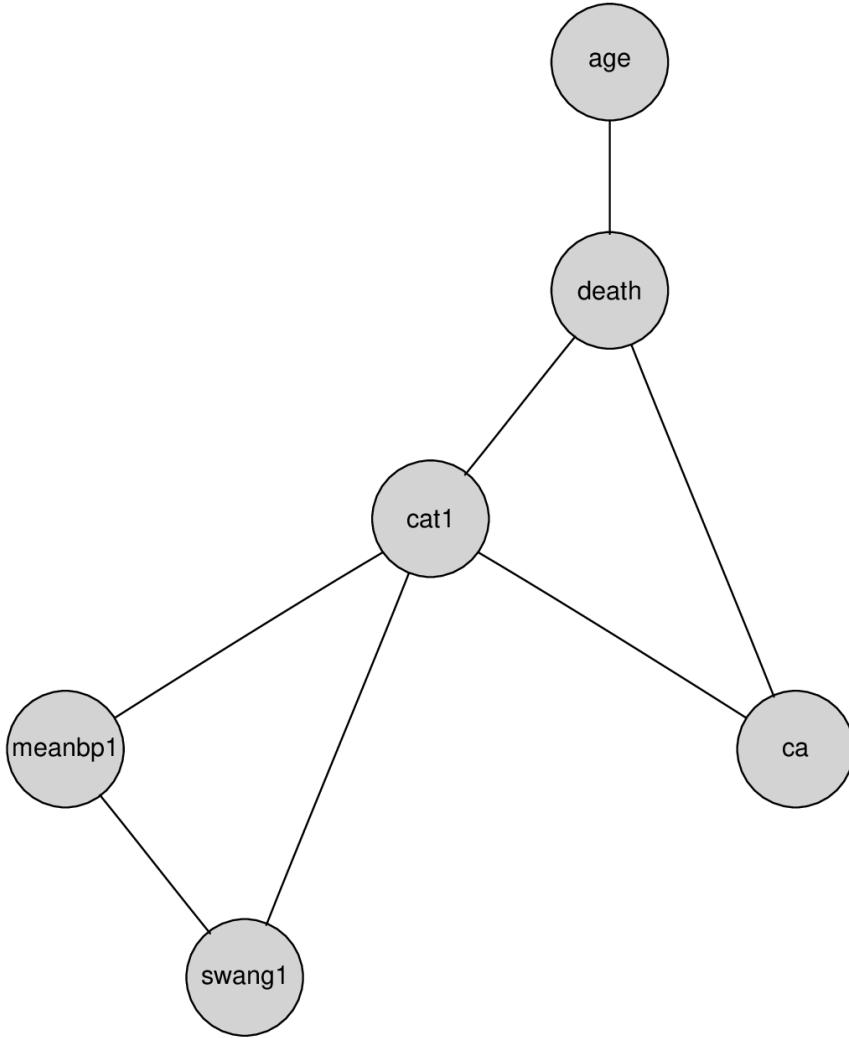
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This is Homework Set 2 of Data Mining

**Number of questions:** 5

- 1** Consider the graphical log-linear model with the following independence graph:  
2 pt.



Which of the following (conditional) independences hold in this model?

- a.  $\text{age} \perp \text{cat1}$
- b.  $\text{swang1} \perp \text{death} \mid \text{cat1}$
- c.  $\text{age} \perp \text{swang1}$
- d.  $\text{death} \perp \{\text{meanbp1}, \text{swang1}\} \mid \{\text{age}, \text{cat1}\}$
- e.  $\text{death} \perp \text{ca}$
- f.  $\text{death} \perp \{\text{meanbp1}, \text{swang1}\} \mid \text{cat1}$
- g.  $\text{swang1} \perp \text{ca} \mid \text{meanbp1}$

- 2** Consider the following table of counts on binary variables  $x$  and  $y$ :

$n(x,y)$	$y=0$	$y=1$
$x=0$	80	20
$x=1$	40	60

Suppose we fit the independence model  $x \perp y$  to this data. Give the fitted counts for:

$(x=0, y=0)$ :

**a.** ..... (0.5 pt.)

$(x=1, y=0)$ :

**b.** ..... (0.5 pt.)

$(x=0, y=1)$ :

**c.** ..... (0.5 pt.)

$(x=1, y=1)$ :

**d.** ..... (0.5 pt.)

- 3** Consider a graphical model M on three binary variables A,B, and C, with independence graph  $G=(K,E)$  with  $K = \{A,B,C\}$  and  $E = \{\{B,C\}\}$ .

The observed counts are given in the following table:

A	B	C	$n(A,B,C)$
1	1	1	40
1	1	0	10
1	0	1	5
1	0	0	50
0	1	1	30
0	1	0	5
0	0	1	20
0	0	0	40

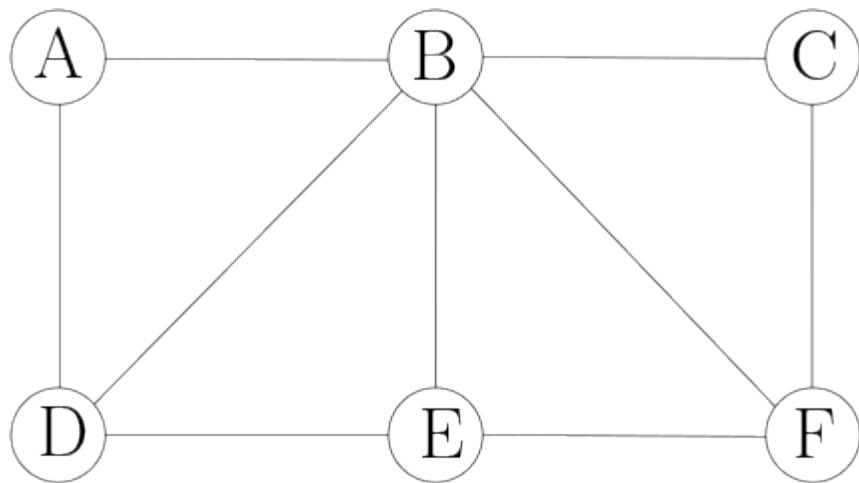
Answer the following questions (do not round your answer):

The fitted count  $\hat{n}(1, 1, 1)$  according to model M is: **a.** .....(1 pt.)

The fitted count  $\hat{n}(0, 1, 0)$  according to model M is: **b.** .....(1 pt.)

- 4** We are performing a hill-climbing search in the space of decomposable models.  
2 pt. Neighboring models are obtained by either adding an edge to the current model, or removing an edge from the current model.

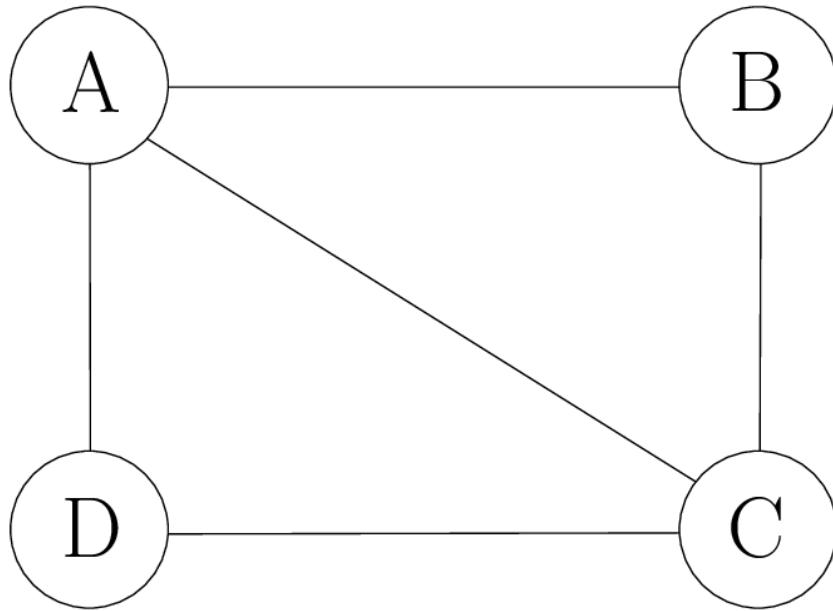
The current model is given in the following figure:



Which of the following operations produce a valid neighbor? (0 or more answers may be correct)

- a. Remove the edge between B and D
- b. Add an edge between A and E
- c. Add an edge between A and F
- d. Remove the edge between B and F
- e. Add an edge between C and D
- f. Remove the edge between A and D
- g. Remove the edge between B and E

- 5 Consider the graphical log-linear model  $M_1$  on binary variables A,B,C, and D, with independence graph:



1 pt. a. The formula for the maximum likelihood fitted counts of  $M_1$  is given by:

- a. 
$$\frac{n(A, B, C)n(A, C, D)}{n(A)n(C)}$$
- b. 
$$\frac{n(A, B, C)n(A, C, D)n(A, C)}{n(A)n(C)}$$
- c. 
$$\frac{n(A, B, C)n(A, C, D)}{n(A, C)}$$
- d. 
$$\frac{n(A, B)n(B, C)n(A, C)n(C, D)n(A, D)}{n(A)n(B)n(C)n(D)}$$

Consider the model  $M_0$  obtained by removing the edge between A and C from  $M_1$ . How many parameters (u-terms) are eliminated by this change?

The number of eliminated u-terms is: b. .... (1 pt.)

Thank you, goodbye!