



$$\lambda_1 \in \mathbb{R} \sim \text{exp}(\alpha)$$

$$\lambda_2 \in \mathbb{R} \sim \text{exp}(\alpha)$$

$$\tau \in \mathbb{Z} \sim \text{unif}(n)$$

$$\lambda \in \mathbb{R}^{1 \times n} = \begin{cases} \lambda_1 & t < \tau \\ \lambda_2 & t \geq \tau \end{cases}$$

$$C \in \mathbb{R}^{1 \times n}, C[i] \sim \text{pos}(\lambda[i])$$

probability distributions:

$$P(\lambda_1) \sim \text{exp}(\alpha)$$

$$P(\lambda_2) \sim \text{exp}(\alpha)$$

$$P(\tau) \sim \text{unif}(n)$$

$$P(\lambda | \lambda_1, \lambda_2, \tau) = 1 \quad (\text{given } \lambda_1, \lambda_2, \tau; \tau \text{ is fixed})$$

$$P(C | \lambda) = \prod_{i=0}^n \text{pos}(\lambda[i])$$

Joint distribution: $P(\lambda_1, \lambda_2, \tau, \lambda, C)$

$$= P(\lambda_1) P(\lambda_2) P(\tau) \cdot 1 \cdot \prod_{i=0}^n \text{pos}(\lambda[i])$$

Posterior distribution (Gibbs sampling)

$$P(\lambda_1 | \mathcal{D}) \propto \sum_{\lambda_2} \sum_{\tau} P(\lambda_1, \lambda_2, \tau, \lambda, C)$$