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Communication at Opportunity Sim -- Square Boundary Analysis

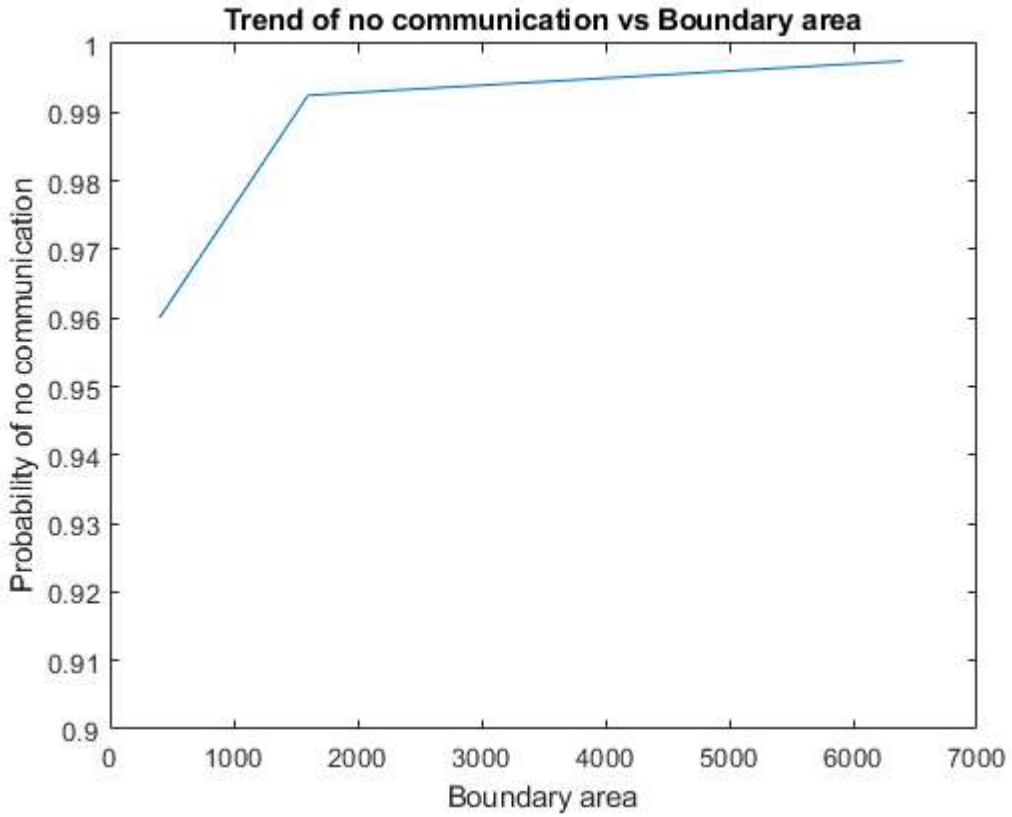
By: Patrick Ledzian Date: 10 April 2022

```
% Overview:
% Generate simulation data to provide insight as to how often agents
% interact when bouncing around in a closed, axis-aligned square boundary.
% Each agent chooses a new random heading (uniform distribution [0, pi)])
% whenever it intersects with a boundary. Longer-term goal is to determine
% what conditions result in reliably connected communications graphs
% between agents, independent of agent starting position. As well as to
% determine how long agents must randomly interact before said
% communication graphs are connected.
%

close all
clear all
clc

a = SimAnalysis();
```

General Analysis -- Infinite path length, single iteration simulations

With square axis-aligned boundaries the chance of random communication between non-coordinating agents appears to be stationary with-respect-to the number of agents. However, the transients behavior (rise-time) is shorter the more agents that are present. Also note that as the area of the boundaries increases the chance of communication goes down. A target for future work is to intelligently manipulate the distribution agents choose new random headings from, maybe from local interactions (comms). This should also be balanced with the transient (rise-time) behavior to meet mission needs (vehicle specs, on-scene time, power management, etc).

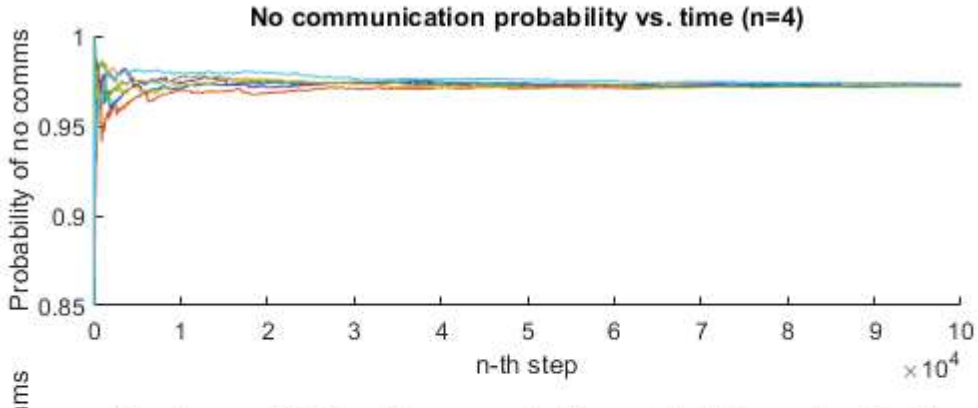
```
xgen = [400, 1600, 6400];
ygen = [0.96, 0.9925, 0.9975];

figure()
plot(xgen, ygen)
xlabel("Boundary area")
ylabel("Probability of no communication")
title("Trend of no communication vs Boundary area")

ylim([0.9 1.0])
```

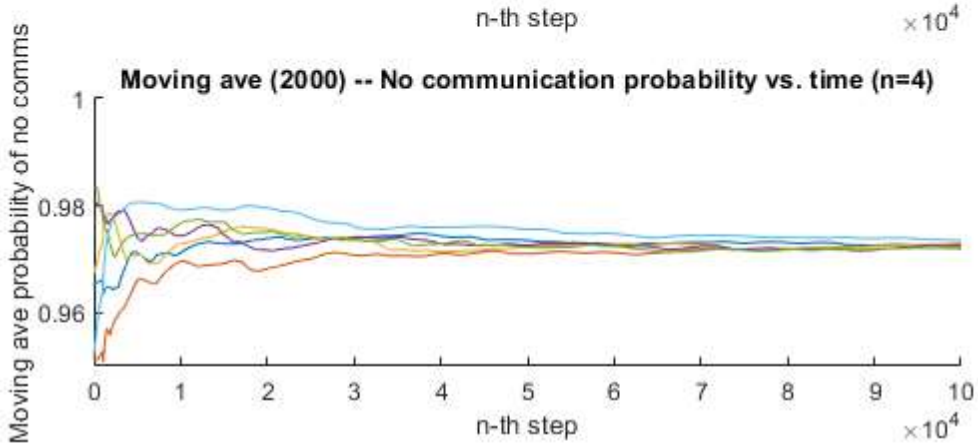


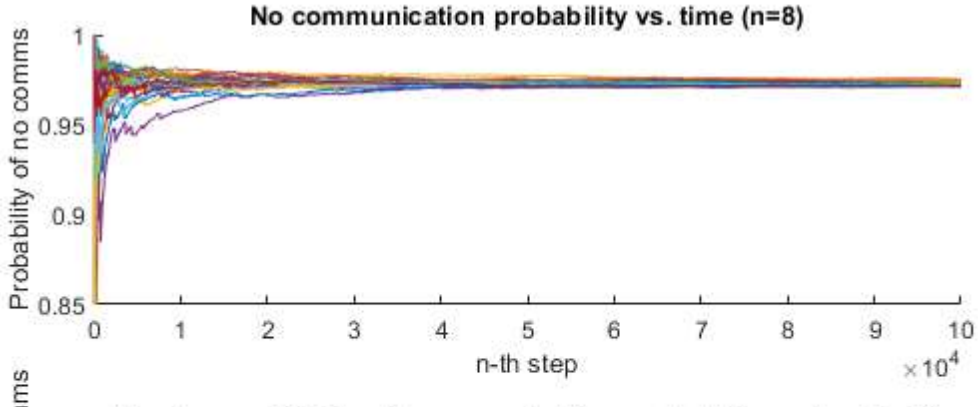
4, 8, 16, 32 Agent Inf Horizon Test in 20x20 Box

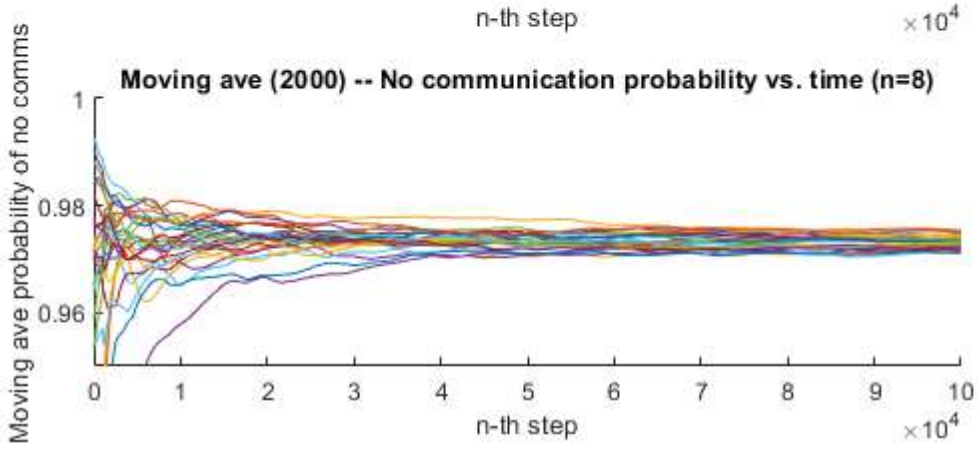
Results: 4-Agent case: converges to [0.970, 0.974] 8-Agent case: converges to [0.969, 0.975] 16-Agent case: converges to [0.969, 0.976] 32-Agent case: converges to [0.969, 0.976]

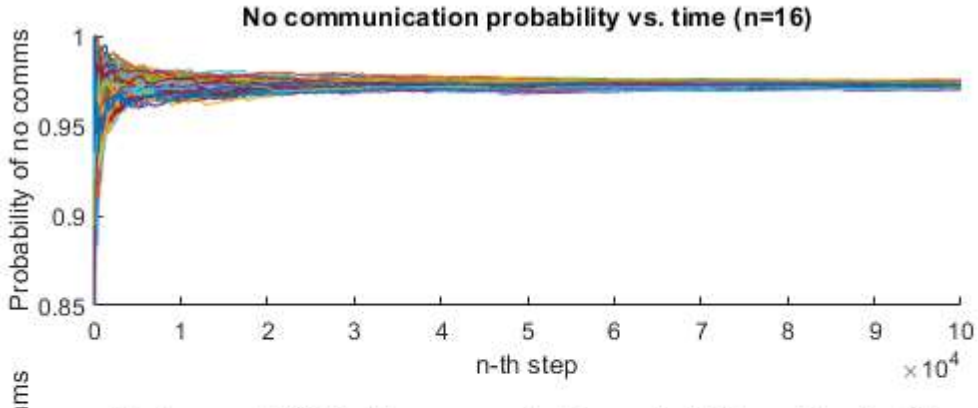
```
bounds = [0 20; 0 20];

a.steadyStateCommProb(bounds, 4, 100000, 1);             % bounds, numAgents, N, sim_itrs
a.steadyStateCommProb(bounds, 8, 100000, 1);
a.steadyStateCommProb(bounds, 16, 100000, 1);
a.steadyStateCommProb(bounds, 32, 100000, 1);

SimAnalysis.clearEmptyFigs();                            % closes figures without titles (for empty ones!)
```

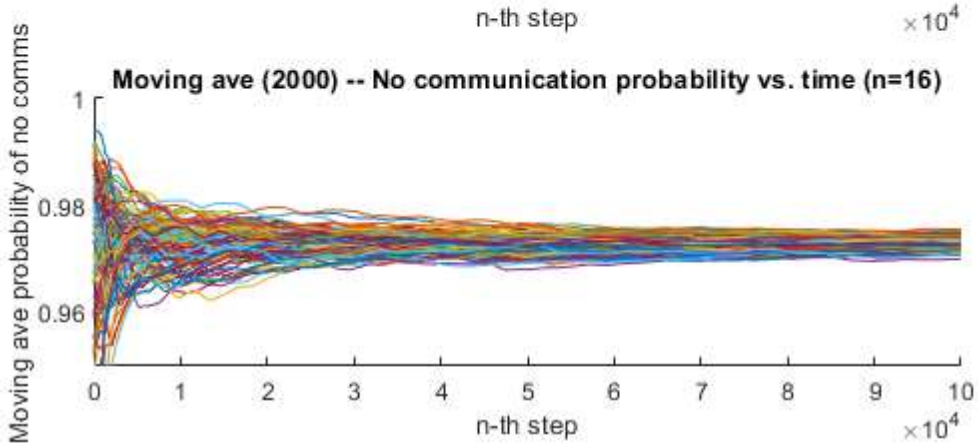

No communication probability vs. time (n=4)
Probability of no comms
1
0.95
0.9
0.85
0
1
2
3
4
5
6
7
8
9
10
n-th step
×10^4

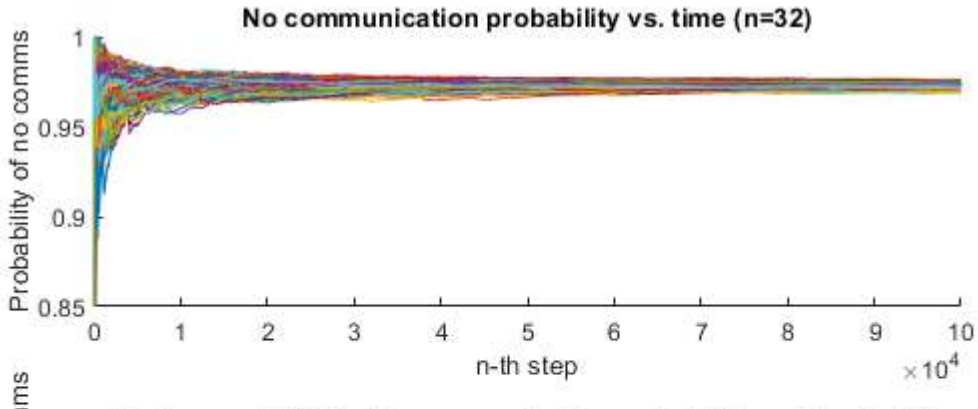

Moving ave (2000) -- No communication probability vs. time (n=4)
Moving ave probability of no comms
1
0.98
0.96
0
1
2
3
4
5
6
7
8
9
10
n-th step
×10^4

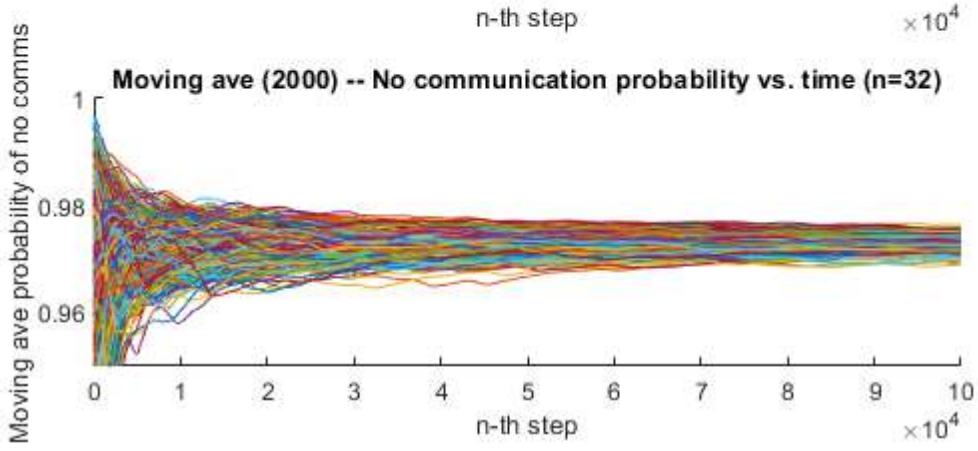

No communication probability vs. time (n=8)
Probability of no comms
1
0.95
0.9
0.85
0
1
2
3
4
5
6
7
8
9
10
n-th step
×10^4


Moving ave (2000) -- No communication probability vs. time (n=8)
Moving ave probability of no comms
1
0.98
0.96
0
1
2
3
4
5
6
7
8
9
10
n-th step
×10^4





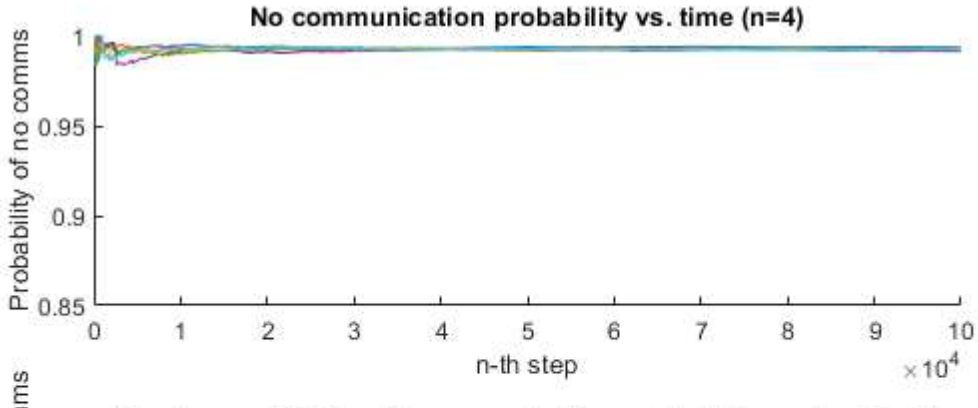


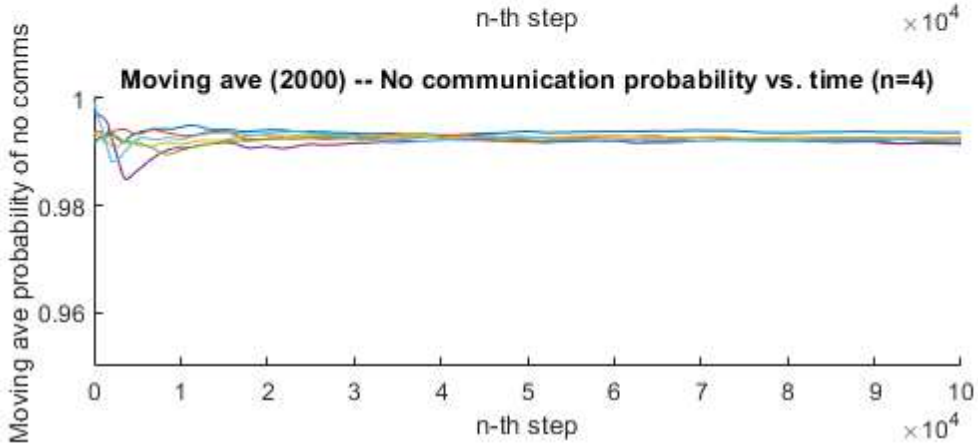


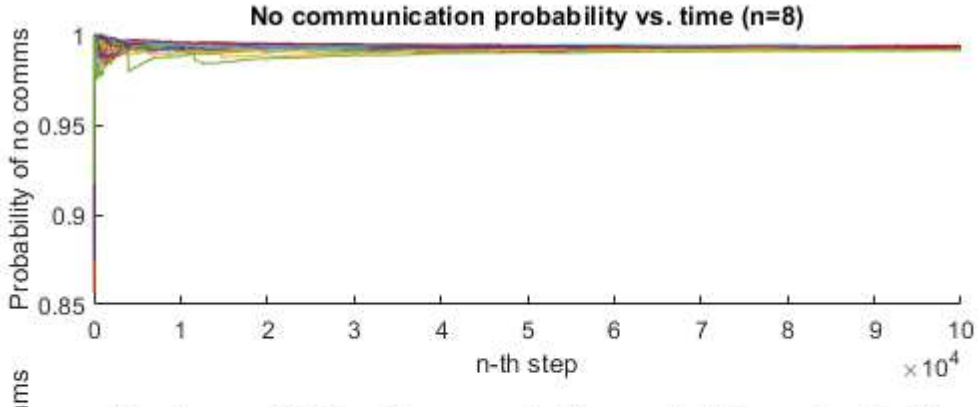
4, 8, 16, 32 Agent Inf Horizon Test in 40x40 Box

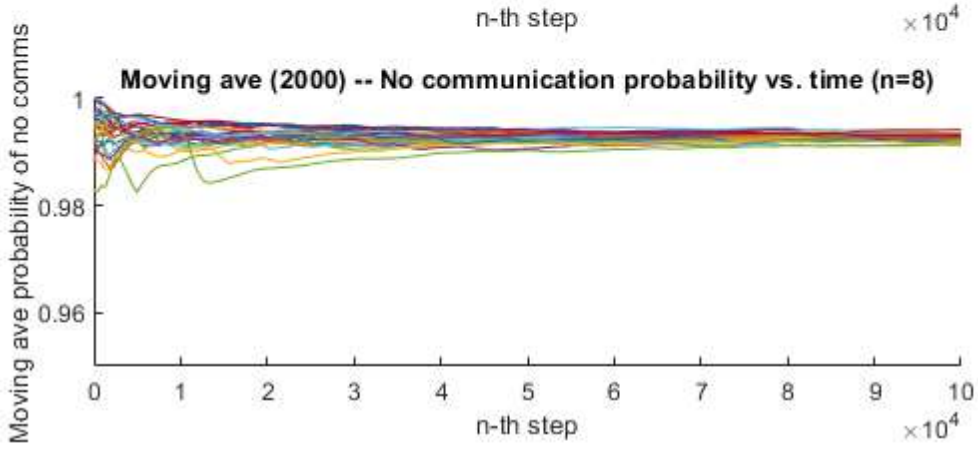
Results: 4-Agent case: converges to [0.991, 0.994] 8-Agent case: converges to [0.990, 0.993] 16-Agent case: converges to [0.991, 0.994] 32-Agent case: converges to [0.990, 0.994]

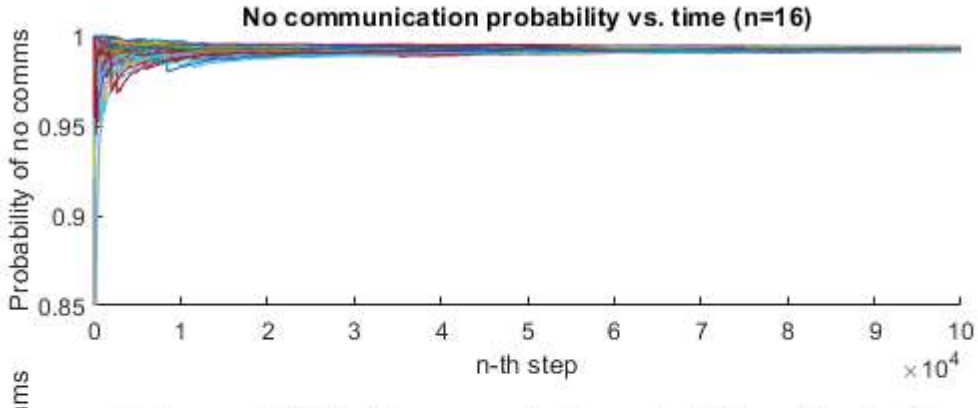
```
bounds = [0 40; 0 40];

a.steadyStateCommProb(bounds, 4, 100000, 1);              % bounds, numAgents, N, sim_itrs
a.steadyStateCommProb(bounds, 8, 100000, 1);
a.steadyStateCommProb(bounds, 16, 100000, 1);
a.steadyStateCommProb(bounds, 32, 100000, 1);

SimAnalysis.clearEmptyFigs();
```

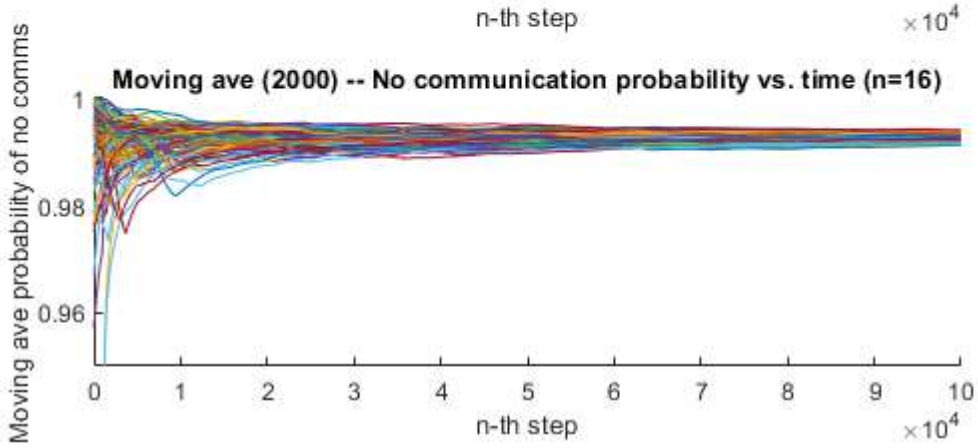

No communication probability vs. time (n=4)
Probability of no comms
1
0.95
0.9
0.85
0
1
2
3
4
5
6
7
8
9
10
n-th step
×10^4

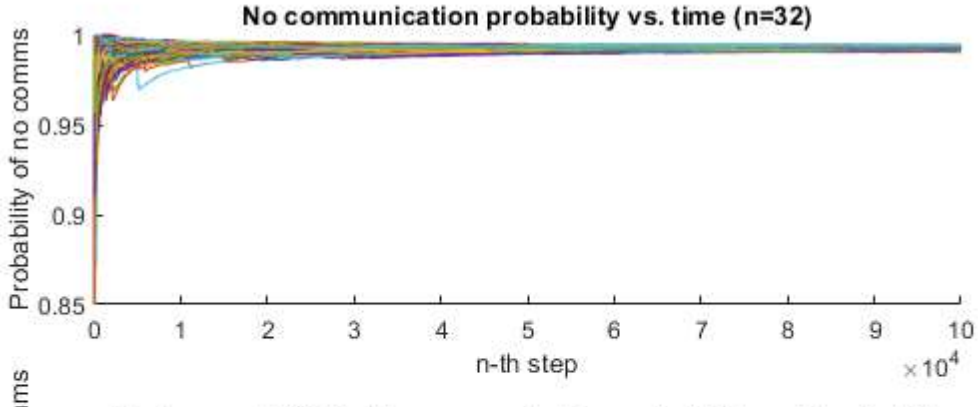

Moving ave (2000) -- No communication probability vs. time (n=4)
Moving ave probability of no comms
1
0.98
0.96
0
1
2
3
4
5
6
7
8
9
10
n-th step
×10^4

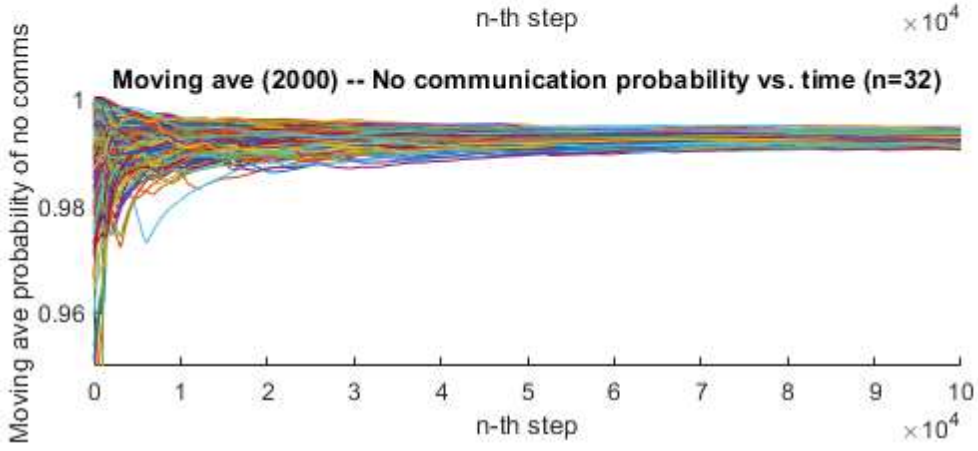

No communication probability vs. time (n=8)
Probability of no comms
1
0.95
0.9
0.85
0
1
2
3
4
5
6
7
8
9
10
n-th step
×10^4


Moving ave (2000) -- No communication probability vs. time (n=8)
Moving ave probability of no comms
1
0.98
0.96
0
1
2
3
4
5
6
7
8
9
10
n-th step
×10^4





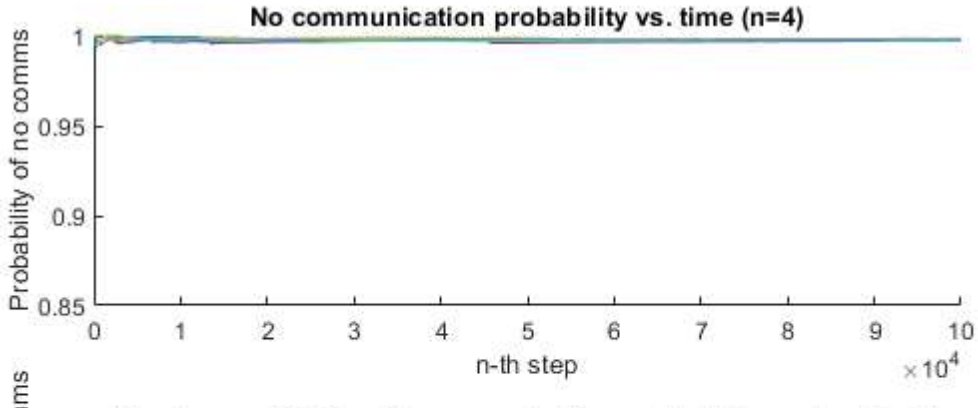


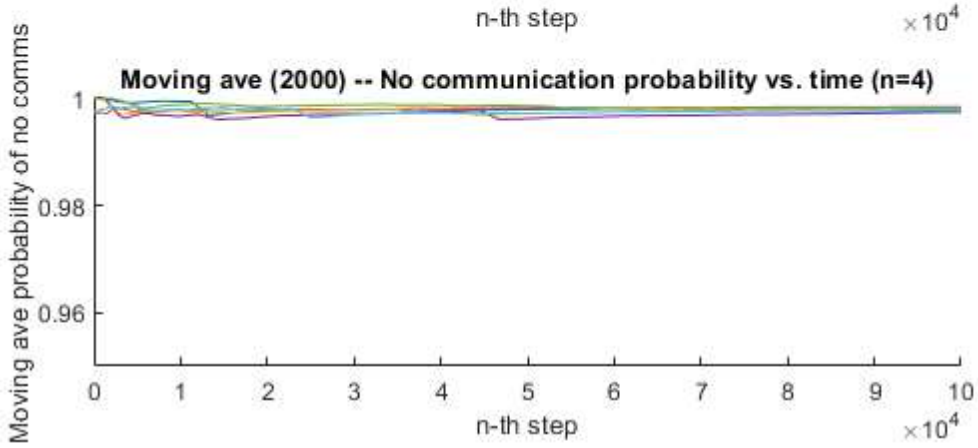


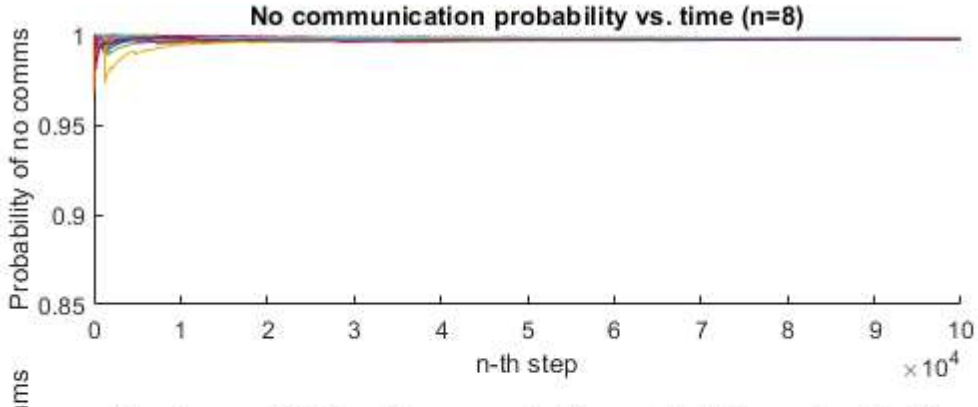
4, 8, 16, 32 Agent Inf Horizon Test in 80x80 Box

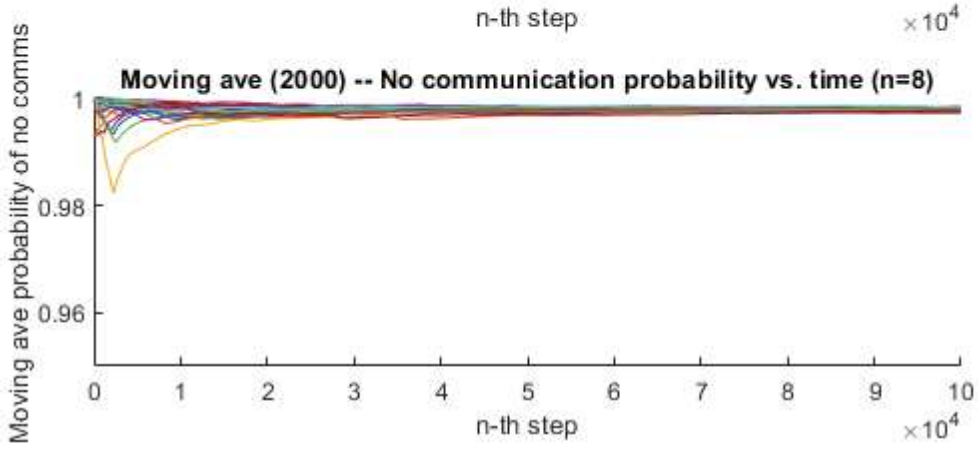
Results: 4-Agent case: converges to [0.997, 0.998] 8-Agent case: converges to [0.997, 0.998] 16-Agent case: converges to [0.996, 0.998] 32-Agent case: converges to [0.996, 0.998]

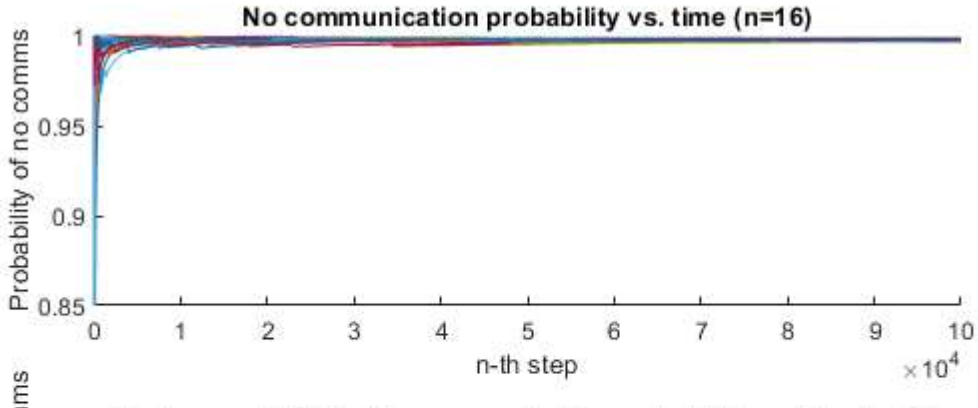
```
bounds = [0 80; 0 80];

a.steadyStateCommProb(bounds, 4, 100000, 1);              % bounds, numAgents, N, sim_itrs
a.steadyStateCommProb(bounds, 8, 100000, 1);
a.steadyStateCommProb(bounds, 16, 100000, 1);
a.steadyStateCommProb(bounds, 32, 100000, 1);

SimAnalysis.clearEmptyFigs();
```

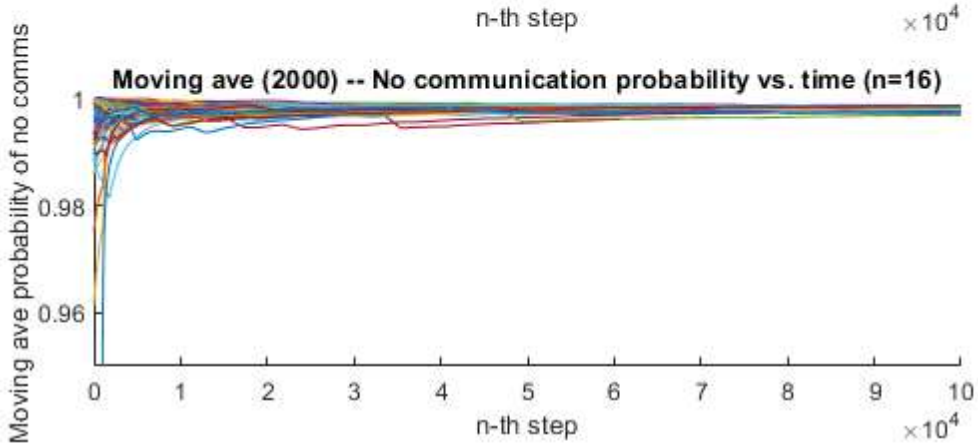

No communication probability vs. time (n=4)
Probability of no comms
1
0.95
0.9
0.85
0
1
2
3
4
5
6
7
8
9
10
n-th step
×10^4

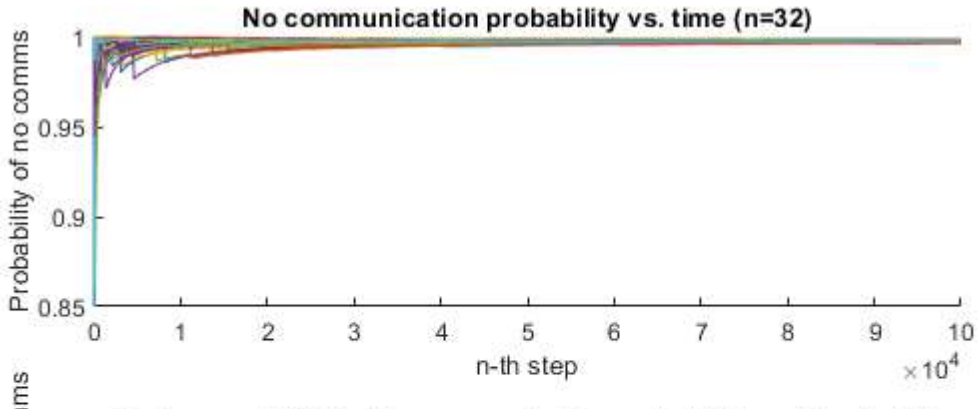

Moving ave (2000) -- No communication probability vs. time (n=4)
Moving ave probability of no comms
1
0.98
0.96
0
1
2
3
4
5
6
7
8
9
10
n-th step
×10^4

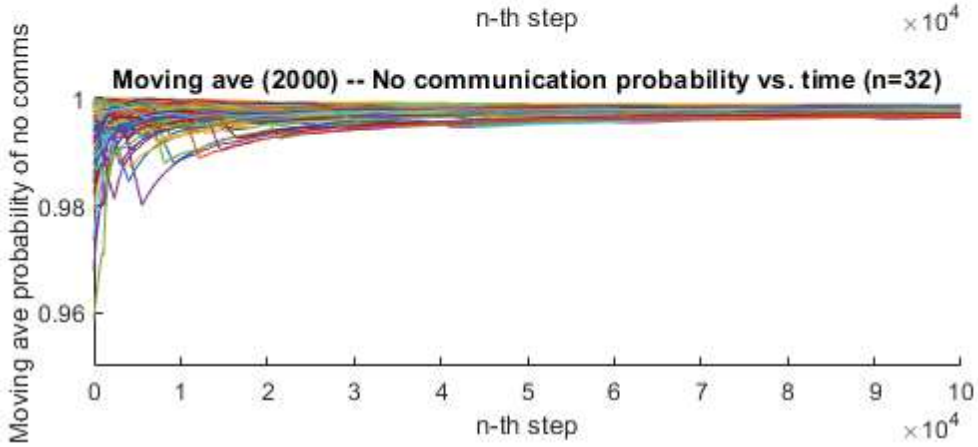

No communication probability vs. time (n=8)
Probability of no comms
1
0.95
0.9
0.85
0
1
2
3
4
5
6
7
8
9
10
n-th step
×10^4


Moving ave (2000) -- No communication probability vs. time (n=8)
Moving ave probability of no comms
1
0.98
0.96
0
1
2
3
4
5
6
7
8
9
10
n-th step
×10^4







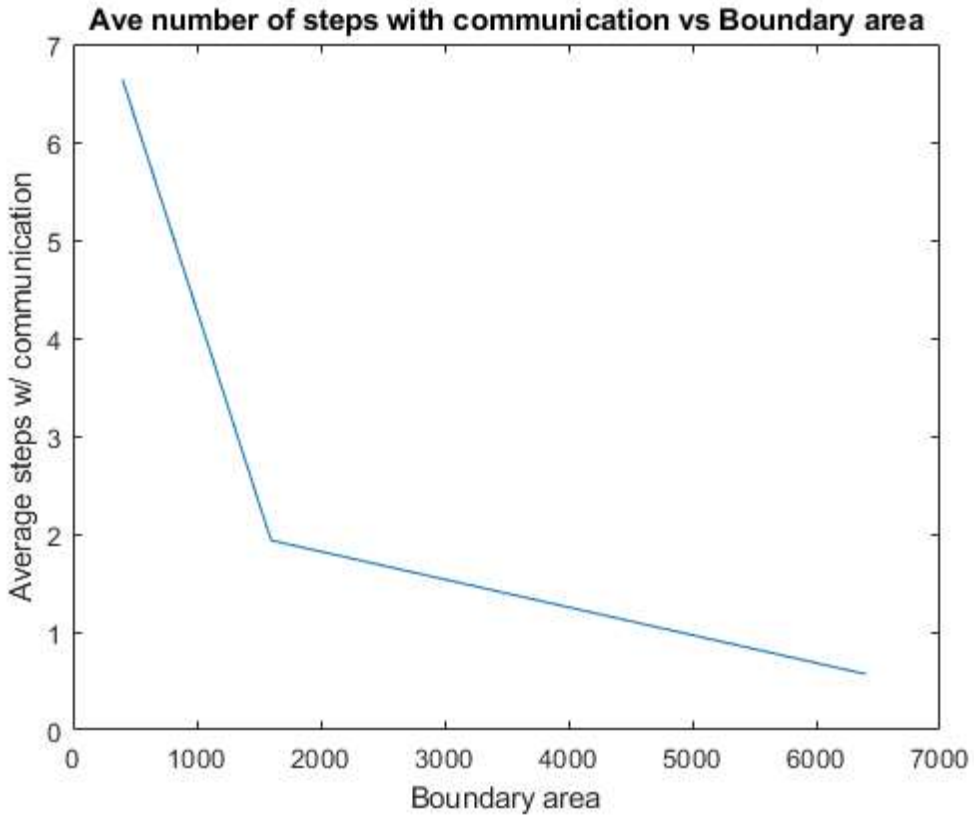


General Analysis -- 240 path length, multi-start simulations

Analysis: For axis-align square boundaries the average number of steps with communication drops off sharply as the boudary area increases, but seems stationary (wrt the mean) to the number of agents. It should be noted that the std. deviation of the average number of steps in communication appears to increase as the number of agents increases. We can also note that the number of multi-start iterations with at least one agent pairing experiencing no communications increases sharply from the 20x20 bounds to

40x40 and beyond. We know that any iteration with two agents experiencing no communication results in an un-connected graph, which needs to be avoided. This is a target for future work.

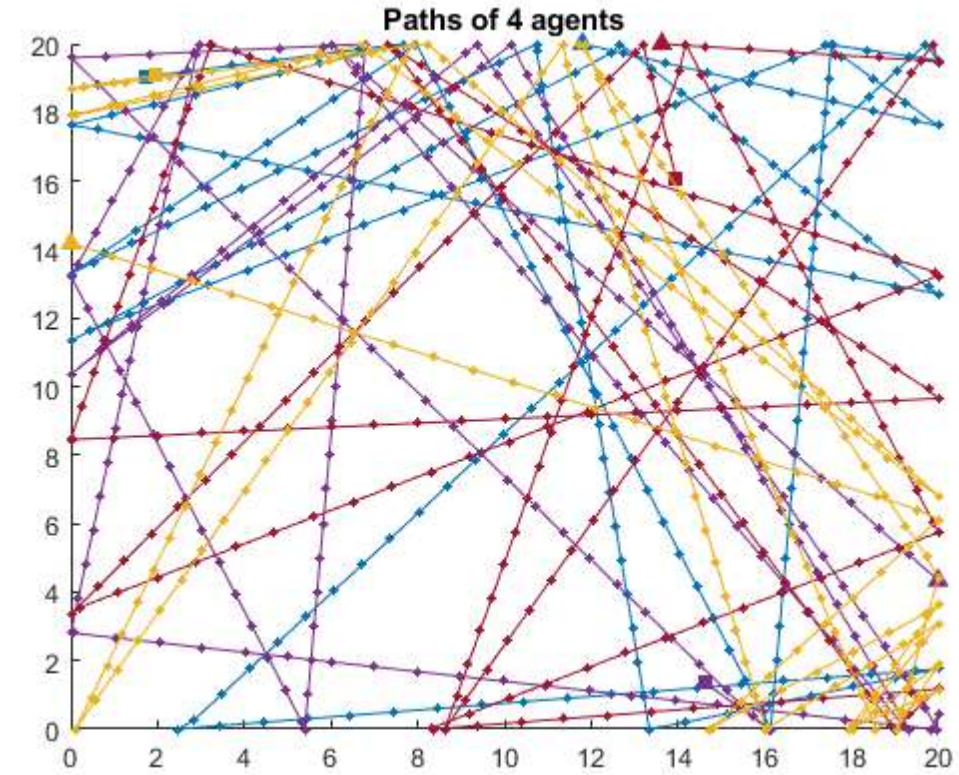
```
xgen = [400, 1600, 6400];
ygen = [6.64, 1.935, 0.57];

figure()
plot(xgen, ygen)
xlabel("Boundary area")
ylabel("Average steps w/ communication")
title("Ave number of steps with communication vs Boundary area")

ylim([0 7.0])
```

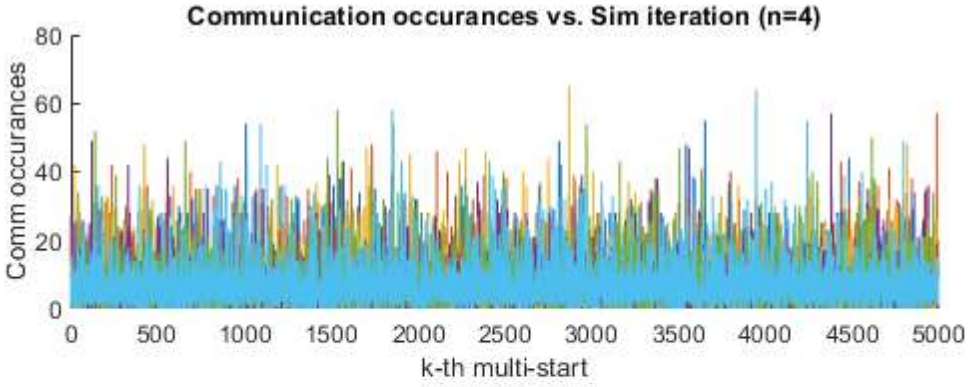


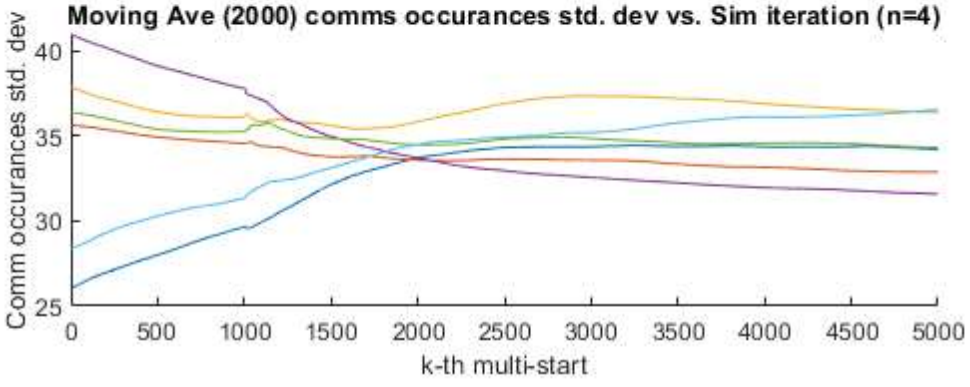
4, 8, 16, 32 Agent Multi-Start Test in 20x20 Box

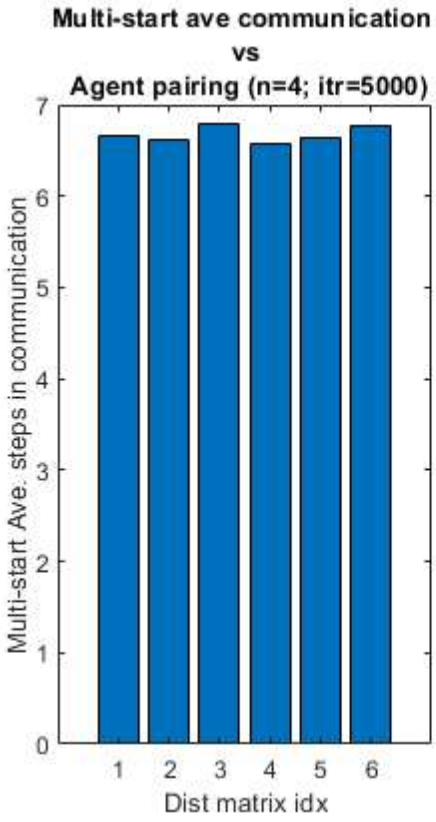
Results: 4-Agent case: ave comms [6.52, 6.75]; no comms itrs [318, 372] 8-Agent case: ave comms [6.51, 6.88]; no comms itrs [297, 388] 16-Agent case: ave comms [6.44, 6.85]; no comms itrs [299, 380] 32-Agent case: ave comms [6.41, 6.92]; no comms itrs [292, 397]

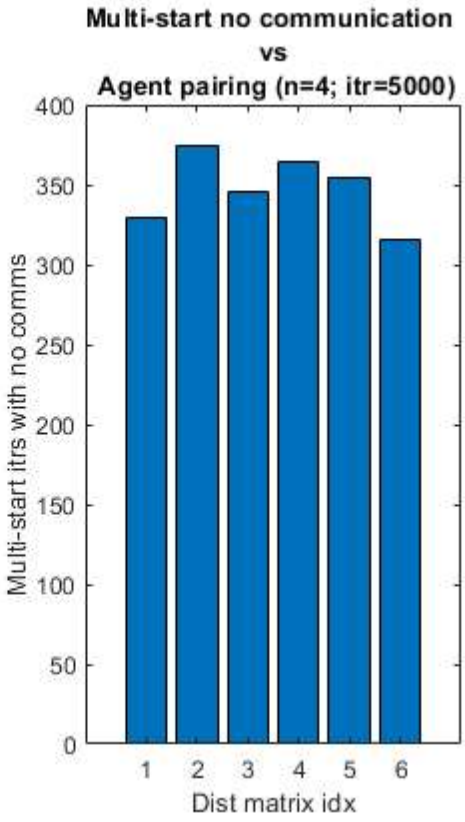
```
bounds = [0 20; 0 20];

a.multiStartData(bounds, 4, 240, 5000);                % bounds, numAgents, N, sim_itrs
a.multiStartData(bounds, 8, 240, 5000);
a.multiStartData(bounds, 16, 240, 5000);
a.multiStartData(bounds, 32, 240, 5000);

SimAnalysis.clearEmptyFigs();
```

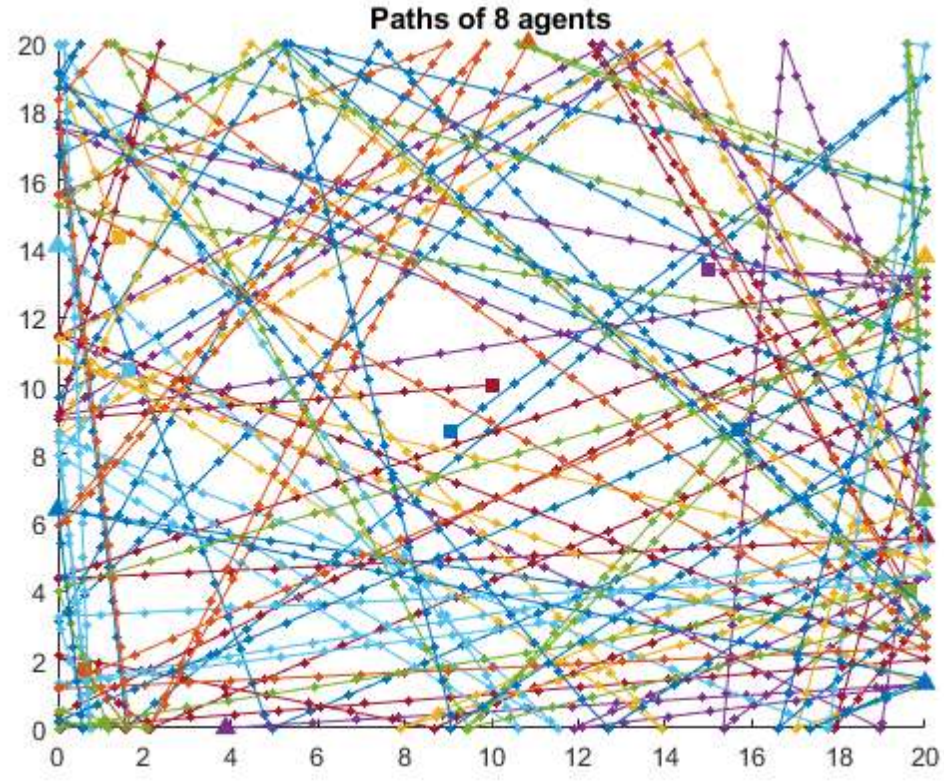

Paths of 4 agents
0
2
4
6
8
10
12
14
16
18
20

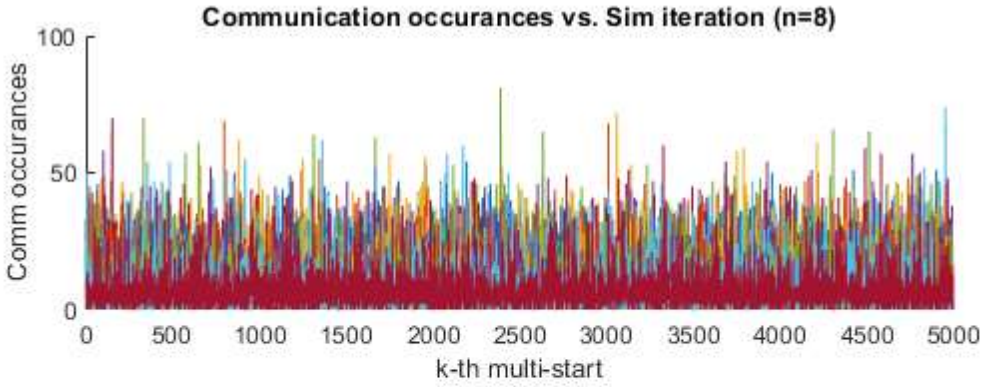

Communication occurances vs. Sim iteration (n=4)
Comm occurances
k-th multi-start
0
20
40
60
80
500
1000
1500
2000
2500
3000
3500
4000
4500
5000

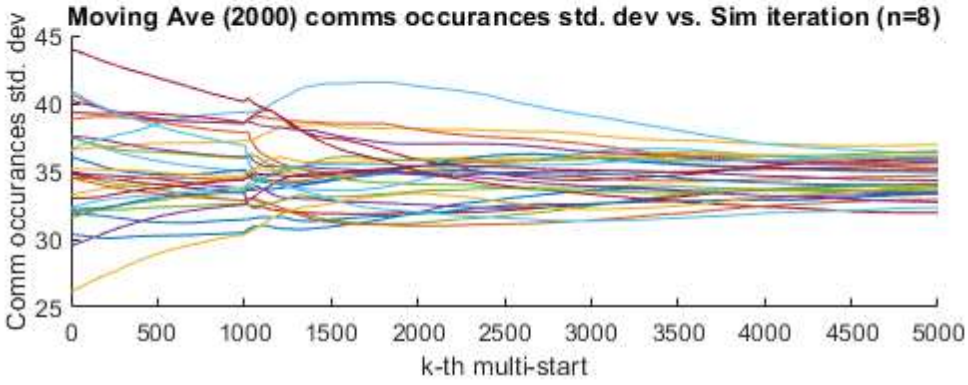

Moving Ave (2000) comms occurances std. dev vs. Sim iteration (n=4)
Comm occurances std. dev
k-th multi-start
25
30
35
40
500
1000
1500
2000
2500
3000
3500
4000
4500
5000

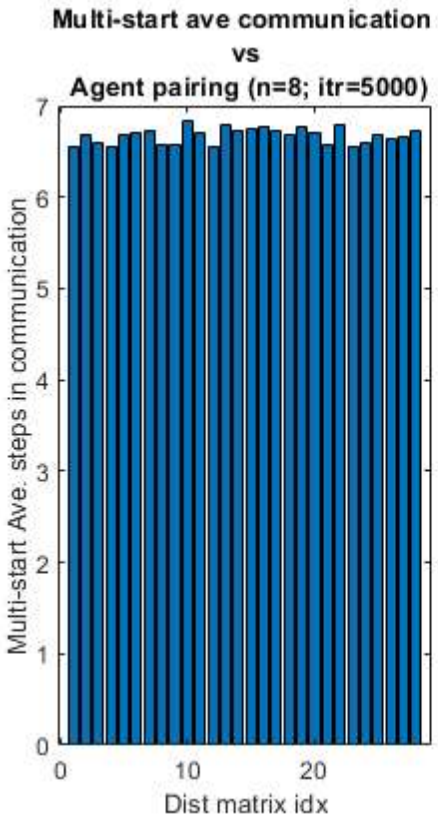

Multi-start ave communication
vs
Agent pairing (n=4; itr=5000)
Multi-start Ave. steps in communication
Dist matrix idx

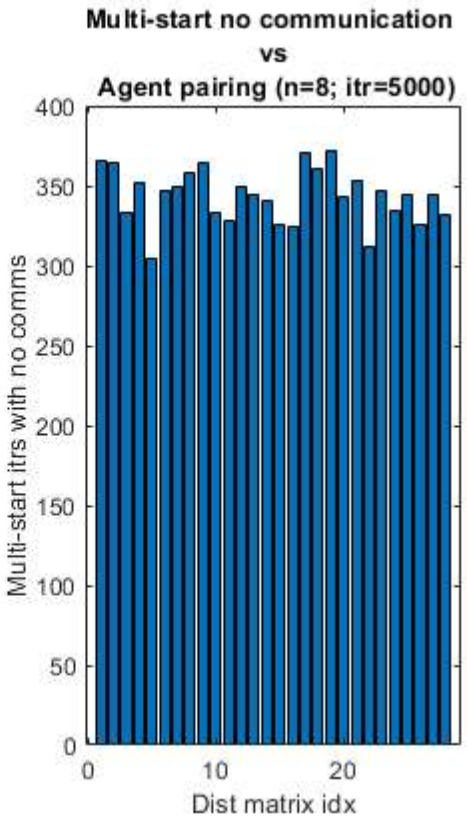

Multi-start no communication
vs
Agent pairing (n=4; itr=5000)
Multi-start itrs with no comms
Dist matrix idx

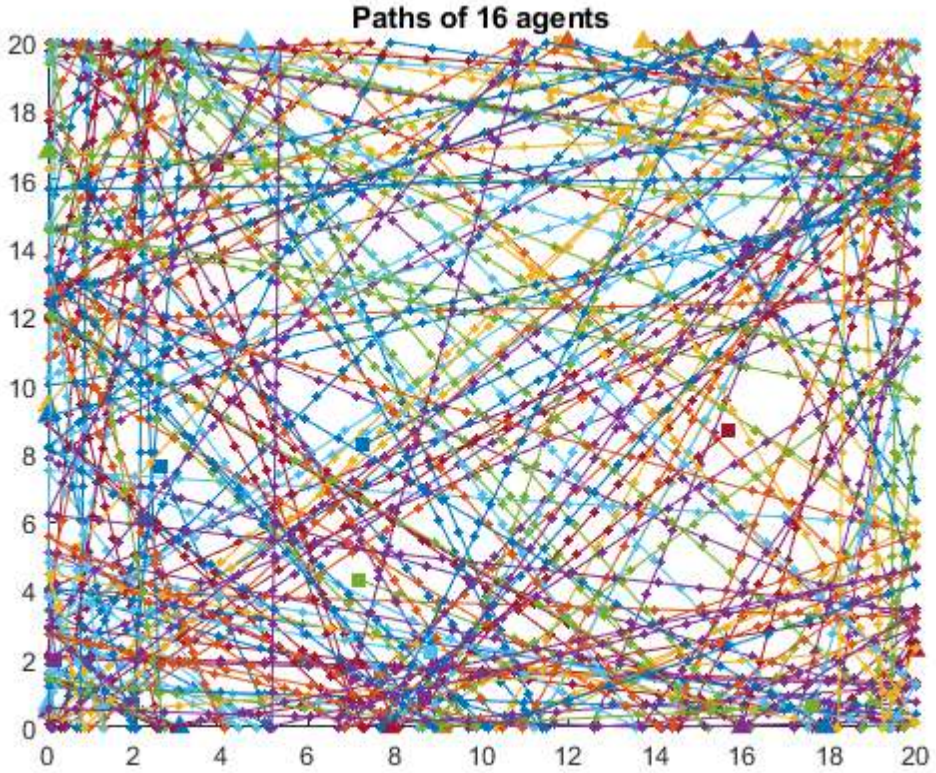

Paths of 8 agents

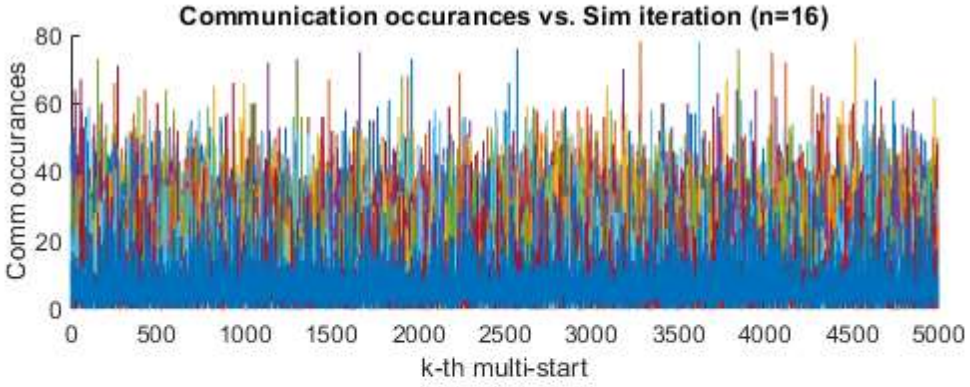

Communication occurances vs. Sim iteration (n=8)
Comm occurances
k-th multi-start

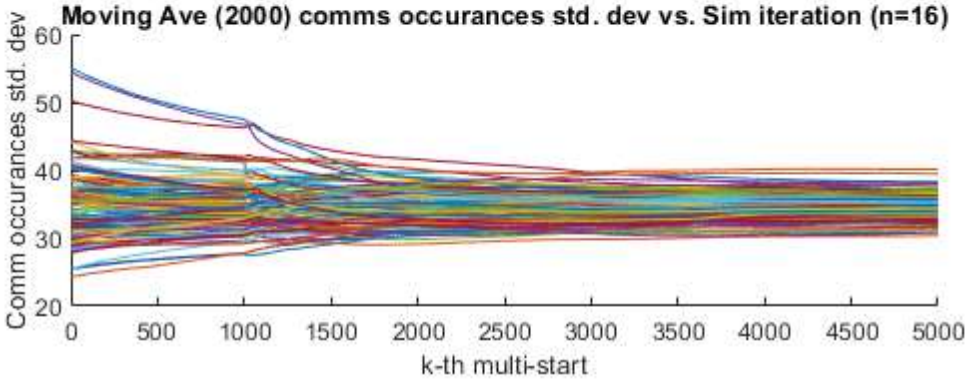

Moving Ave (2000) comms occurances std. dev vs. Sim iteration (n=8)
Comm occurances std. dev
k-th multi-start

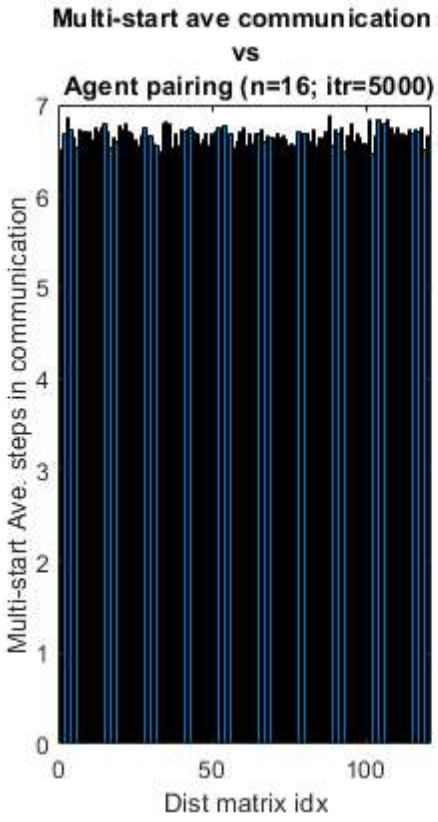

Multi-start ave communication
vs
Agent pairing (n=8; itr=5000)
Multi-start Ave. steps in communication
Dist matrix idx

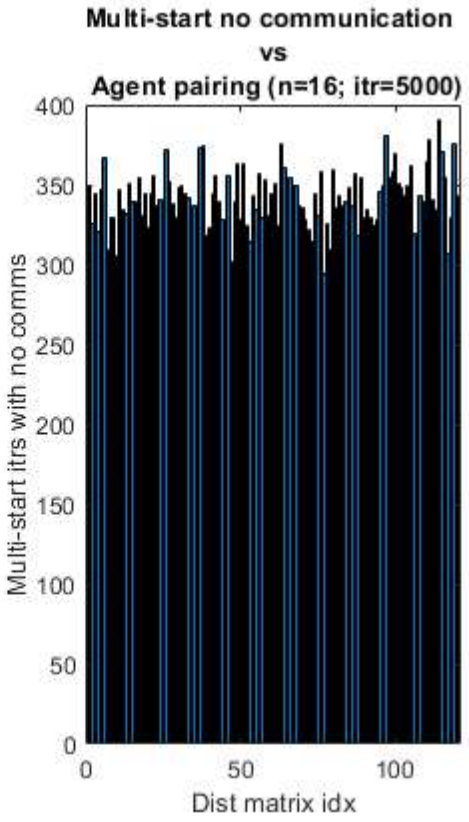

Multi-start no communication
vs
Agent pairing (n=8; itr=5000)
Multi-start itrs with no comms
Dist matrix idx

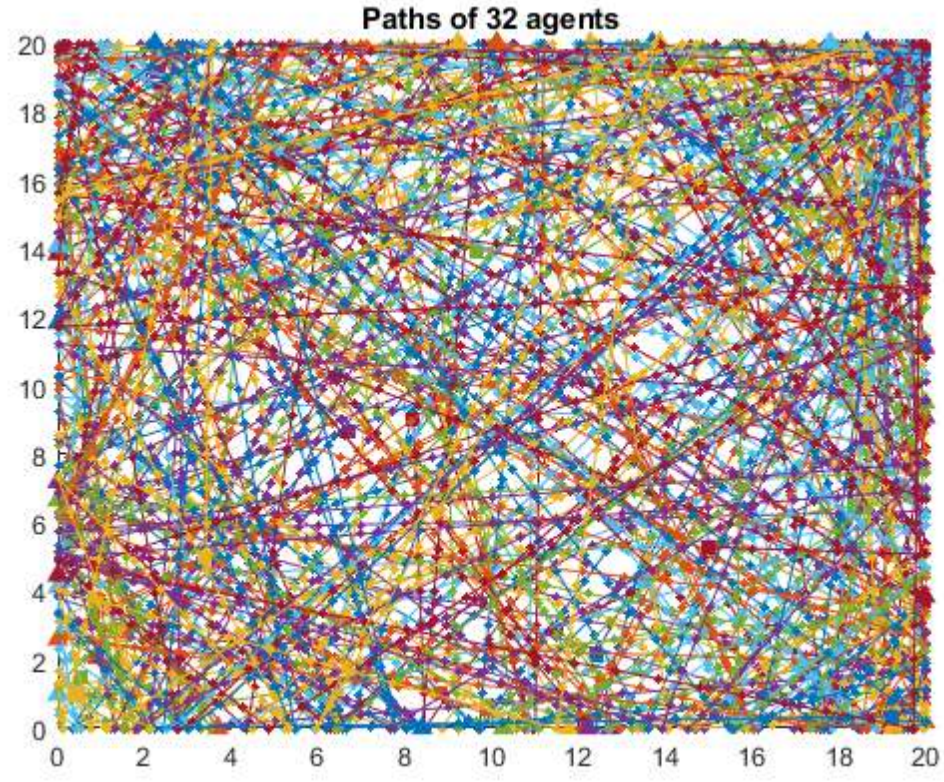

Paths of 16 agents
0
2
4
6
8
10
12
14
16
18
20

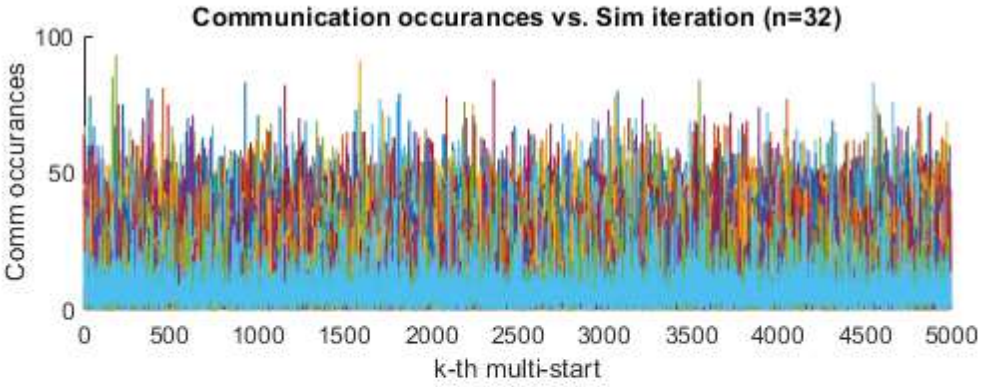

Communication occurances vs. Sim iteration (n=16)
Comm occurances
k-th multi-start
0
20
40
60
80
500
1000
1500
2000
2500
3000
3500
4000
4500
5000

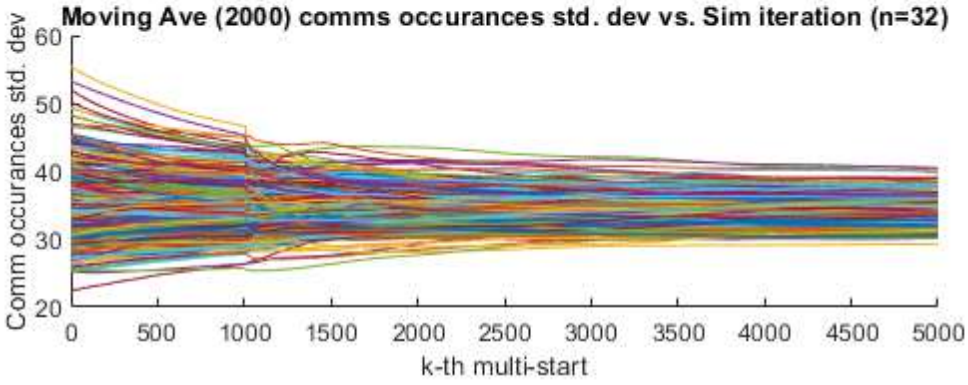

Moving Ave (2000) comms occurances std. dev vs. Sim iteration (n=16)
Comm occurances std. dev
k-th multi-start
20
30
40
50
60
0
500
1000
1500
2000
2500
3000
3500
4000
4500
5000

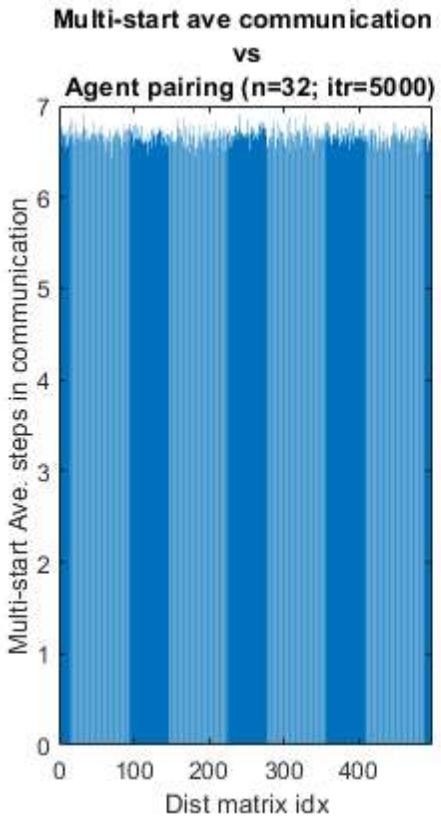

Multi-start ave communication
vs
Agent pairing (n=16; itr=5000)
Multi-start Ave. steps in communication
Dist matrix idx
0
1
2
3
4
5
6
7
0
50
100

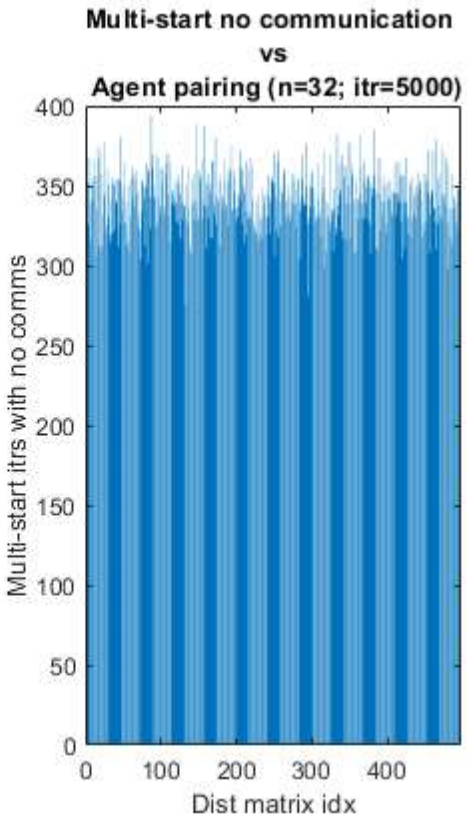

Multi-start no communication
vs
Agent pairing (n=16; itr=5000)
Multi-start itrs with no comms
Dist matrix idx
0
50
100
150
200
250
300
350
400
0
50
100


Paths of 32 agents
0
2
4
6
8
10
12
14
16
18
20
0
2
4
6
8
10
12
14
16
18
20





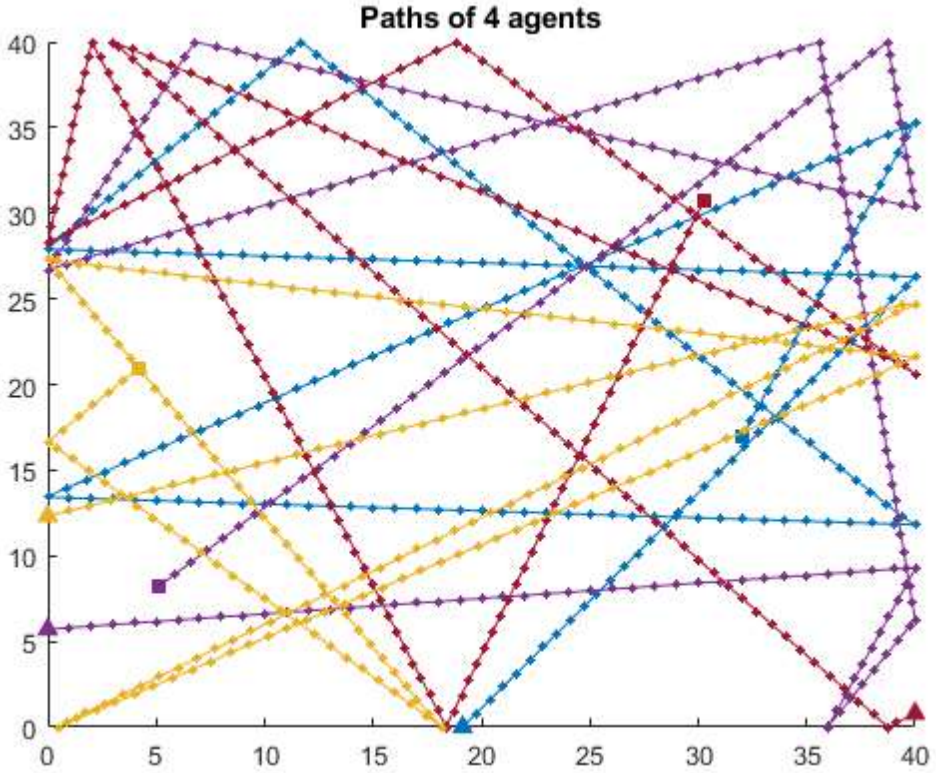


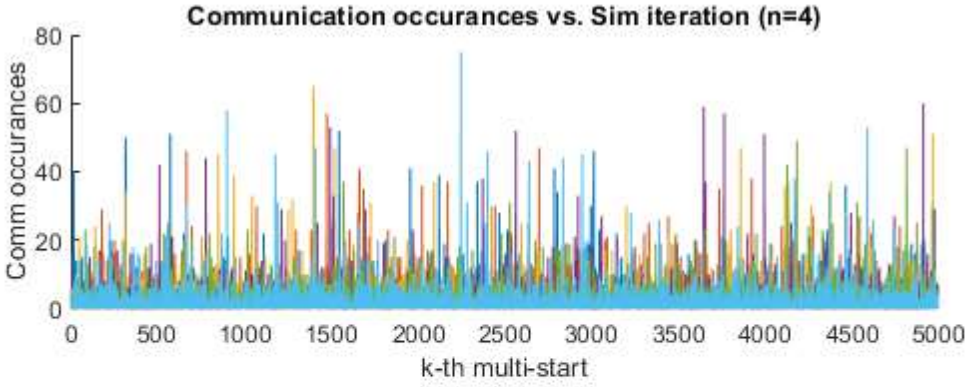


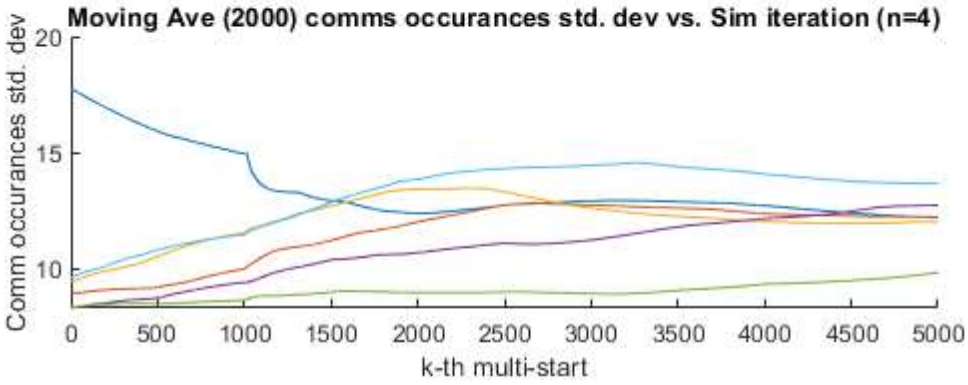
4, 8, 16, 32 Agent Multi-Start Test in 40x40 Box

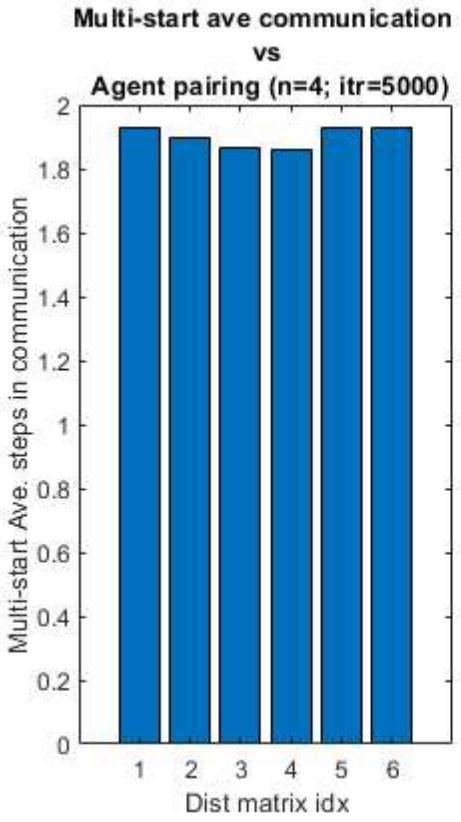
Results: 4-Agent case: ave comms [1.86, 2.01]; no comms itrs [2389, 2474] 8-Agent case: ave comms [1.82, 2.03]; no comms itrs [2342, 2491] 16-Agent case: ave comms [1.82, 2.09]; no comms itrs [2322, 2507] 32-Agent case: ave comms [1.76, 2.06]; no comms itrs [2334, 2515]

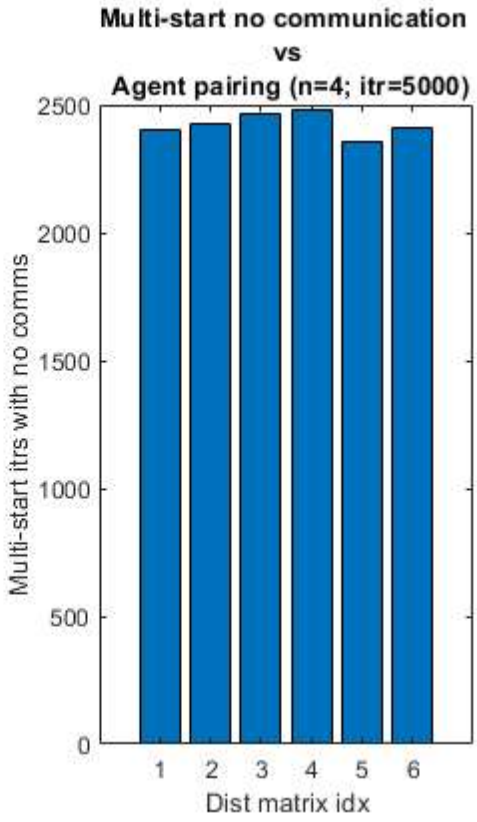
```
bounds = [0 40; 0 40];

a.multiStartData(bounds, 4, 240, 5000);                 % bounds, numAgents, N, sim_itrs
a.multiStartData(bounds, 8, 240, 5000);
a.multiStartData(bounds, 16, 240, 5000);
a.multiStartData(bounds, 32, 240, 5000);

SimAnalysis.clearEmptyFigs();
```

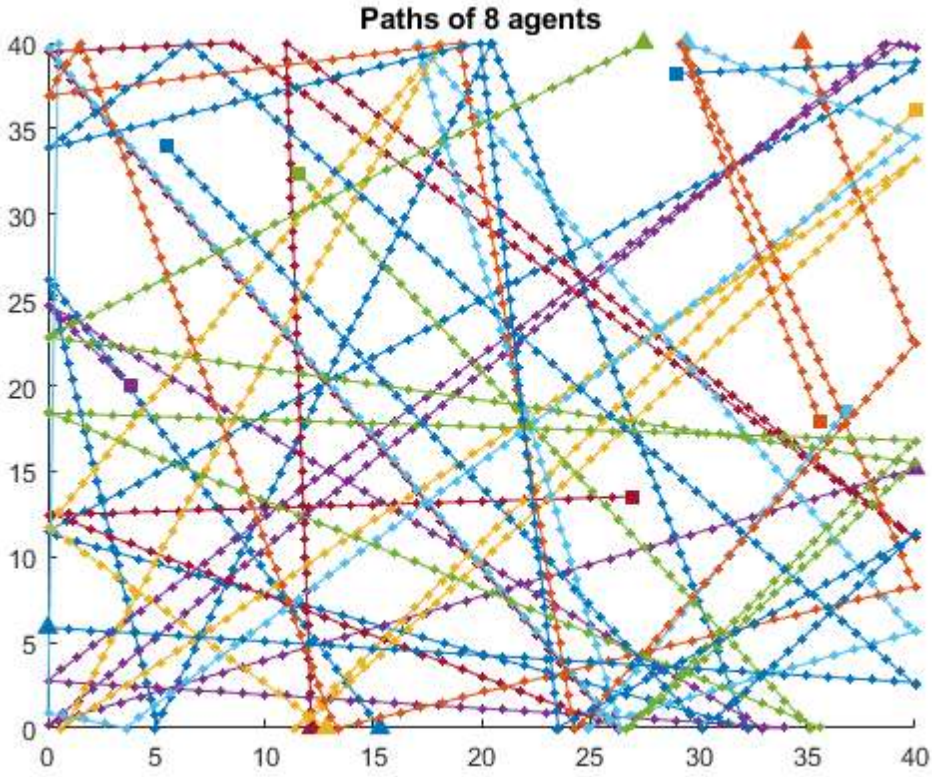

Paths of 4 agents
0
5
10
15
20
25
30
35
40

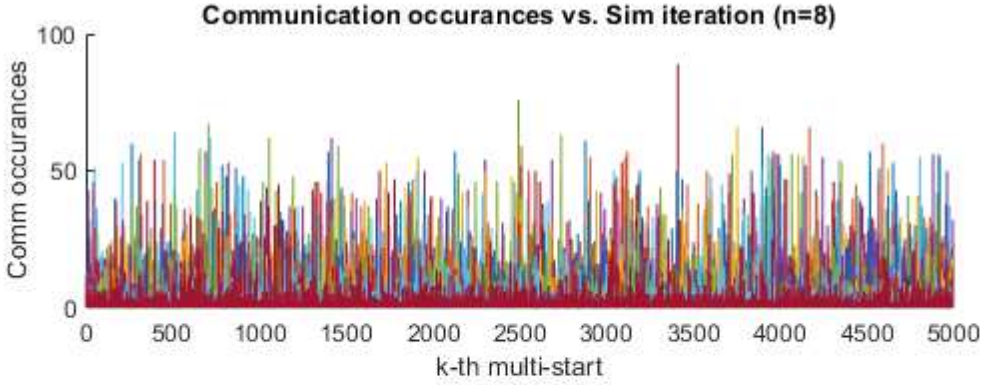

Communication occurances vs. Sim iteration (n=4)
Comm occurances
k-th multi-start
0
20
40
60
80
500
1000
1500
2000
2500
3000
3500
4000
4500
5000

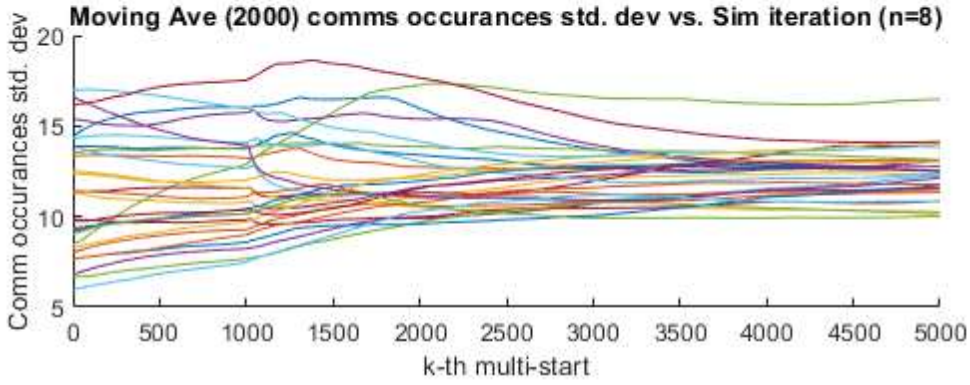

Moving Ave (2000) comms occurances std. dev vs. Sim iteration (n=4)
Comm occurances std. dev
k-th multi-start
10
15
20
0
500
1000
1500
2000
2500
3000
3500
4000
4500
5000

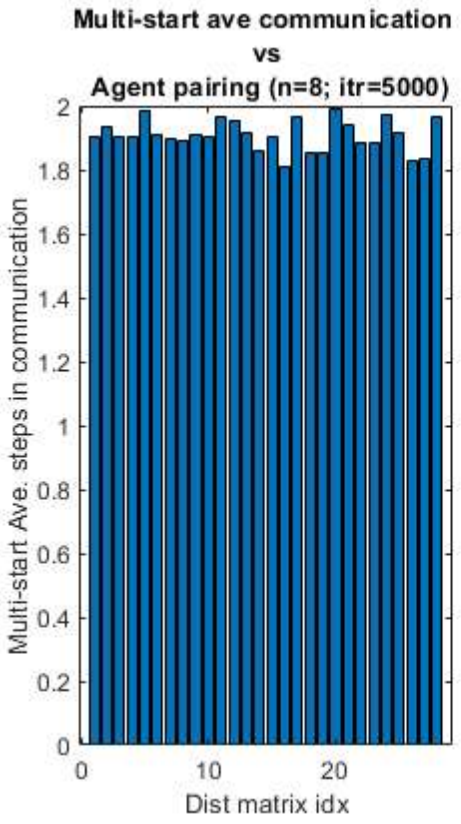

Multi-start ave communication
vs
Agent pairing (n=4; itr=5000)
Multi-start Ave. steps in communication
Dist matrix idx

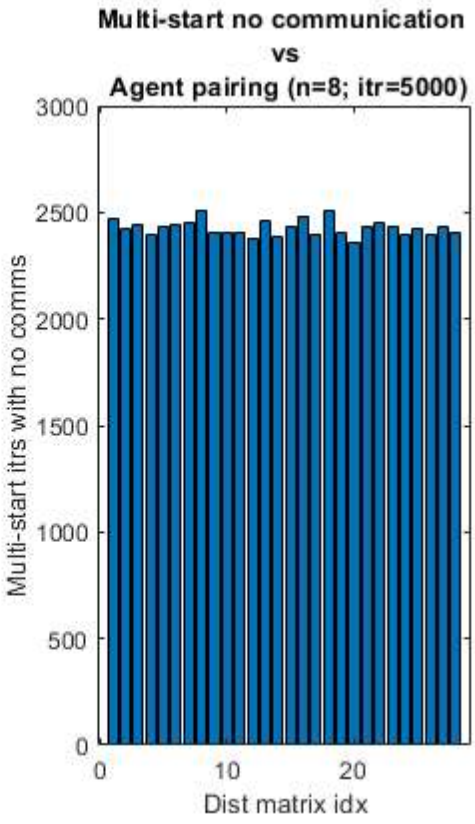

Multi-start no communication
vs
Agent pairing (n=4; itr=5000)
Multi-start itrs with no comms
Dist matrix idx

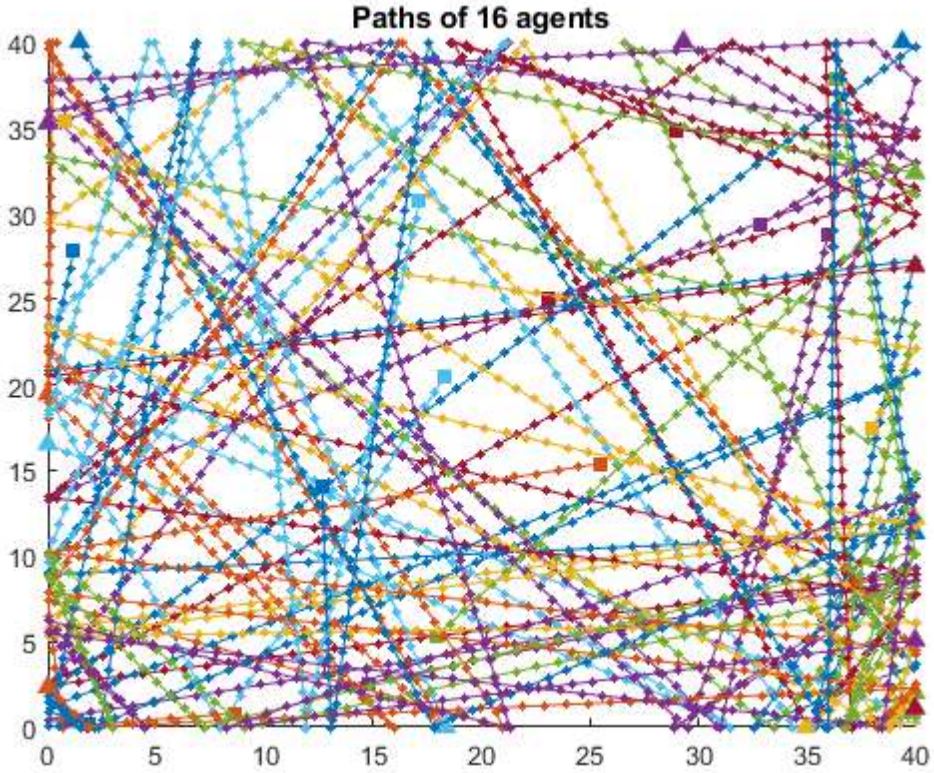

Paths of 8 agents

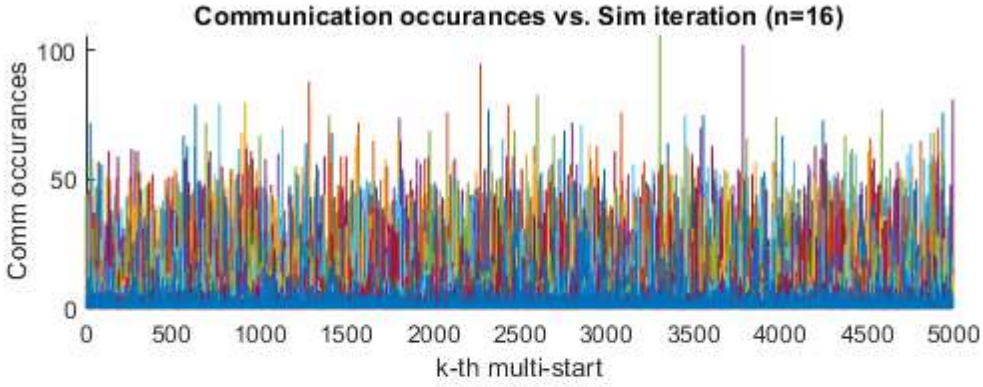

Communication occurances vs. Sim iteration (n=8)
Comm occurances
k-th multi-start

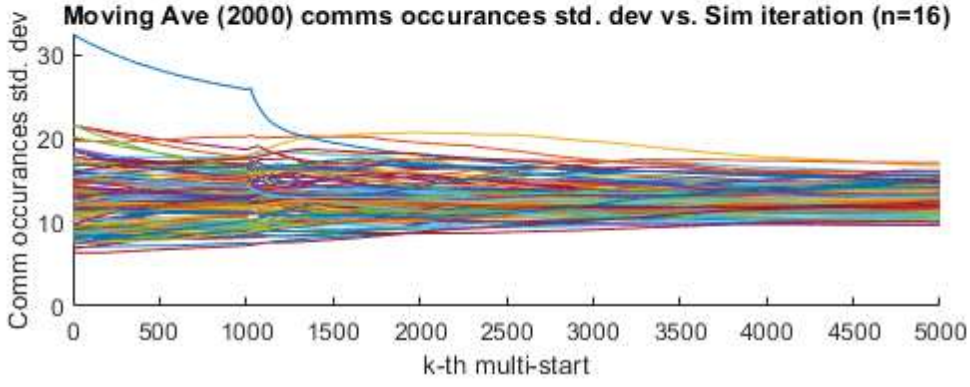

Moving Ave (2000) comms occurances std. dev vs. Sim iteration (n=8)
Comm occurances std. dev
k-th multi-start

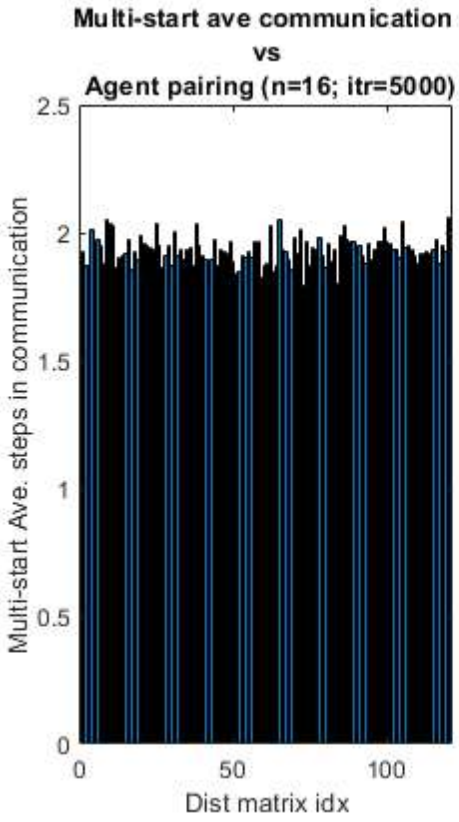

Multi-start ave communication
vs
Agent pairing (n=8; itr=5000)
Multi-start Ave. steps in communication
Dist matrix idx

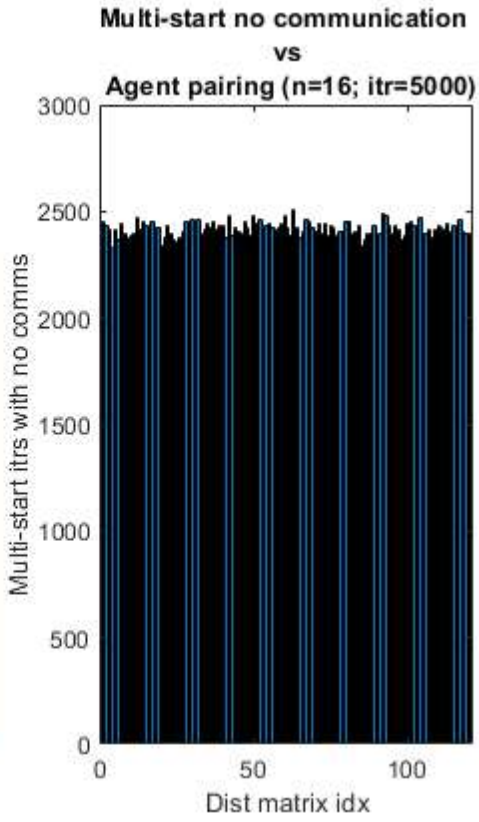

Multi-start no communication
vs
Agent pairing (n=8; itr=5000)
Multi-start itrs with no comms
Dist matrix idx

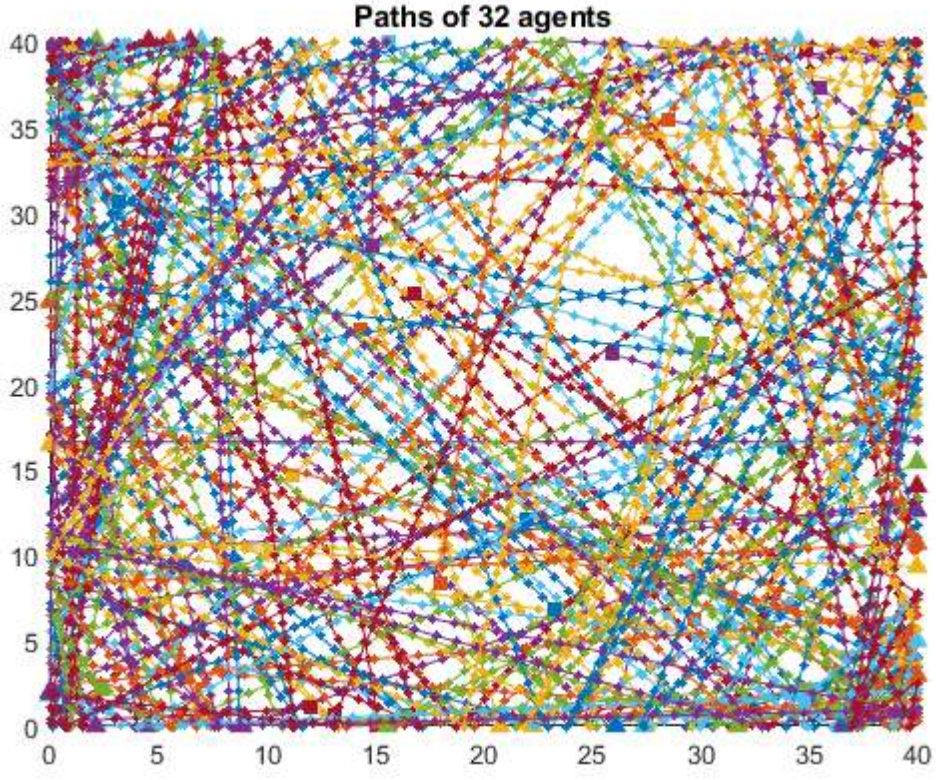

Paths of 16 agents
0
5
10
15
20
25
30
35
40

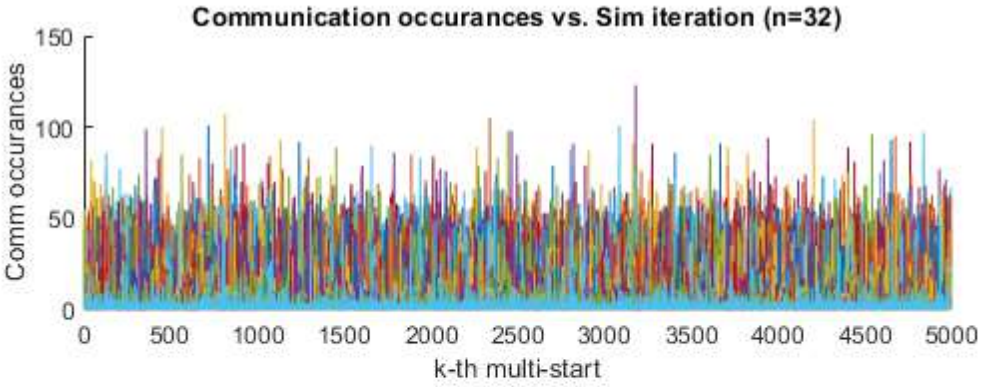

Communication occurances vs. Sim iteration (n=16)
Comm occurances
0
50
100
0
500
1000
1500
2000
2500
3000
3500
4000
4500
5000
k-th multi-start

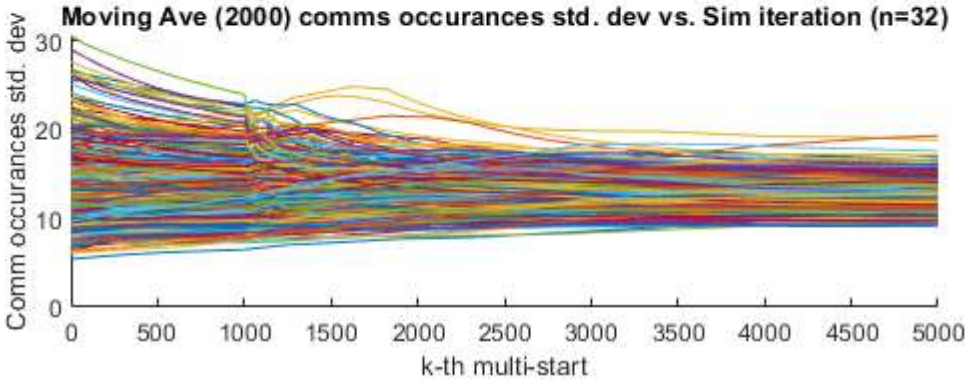

Moving Ave (2000) comms occurances std. dev vs. Sim iteration (n=16)
Comm occurances std. dev
0
10
20
30
0
500
1000
1500
2000
2500
3000
3500
4000
4500
5000
k-th multi-start

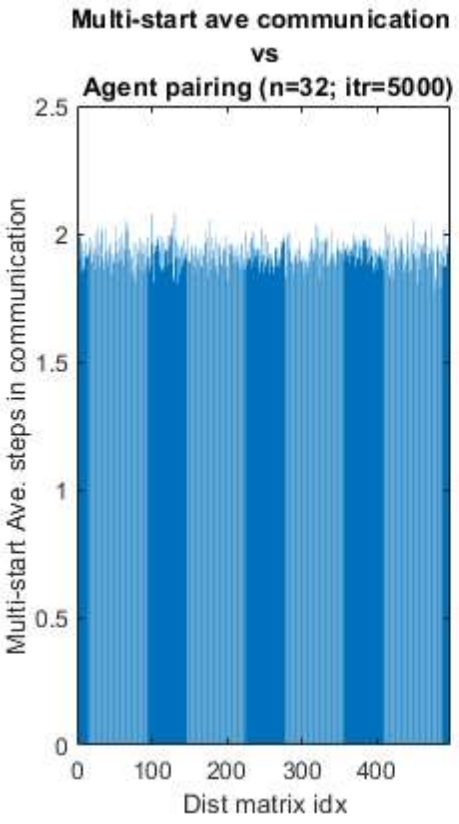

Multi-start ave communication
vs
Agent pairing (n=16; itr=5000)
Multi-start Ave. steps in communication
Dist matrix idx
0
0.5
1
1.5
2
2.5
0
50
100

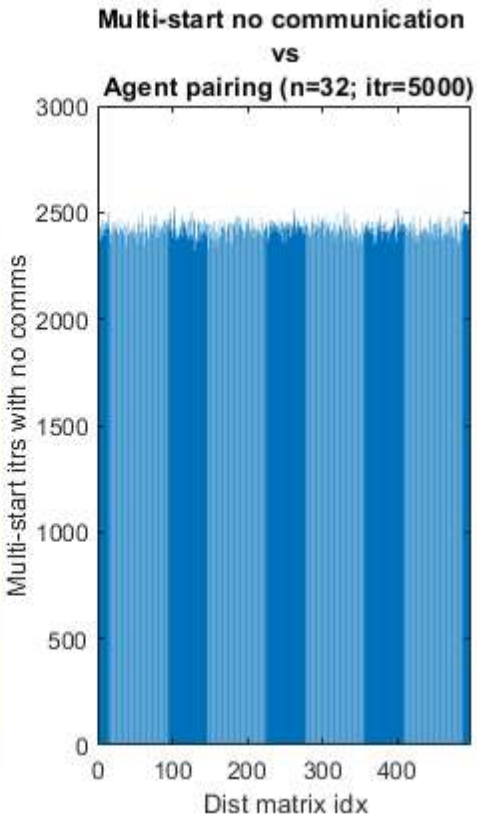

Multi-start no communication
vs
Agent pairing (n=16; itr=5000)
Multi-start itrs with no comms
Dist matrix idx
0
500
1000
1500
2000
2500
3000
0
50
100


Paths of 32 agents
0
5
10
15
20
25
30
35
40







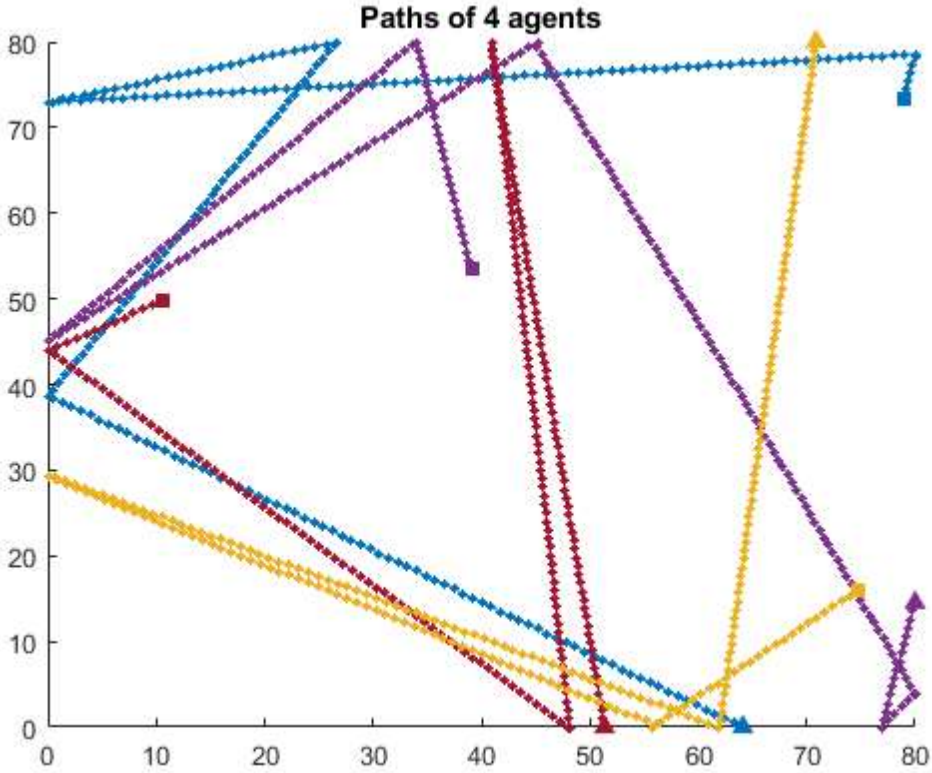


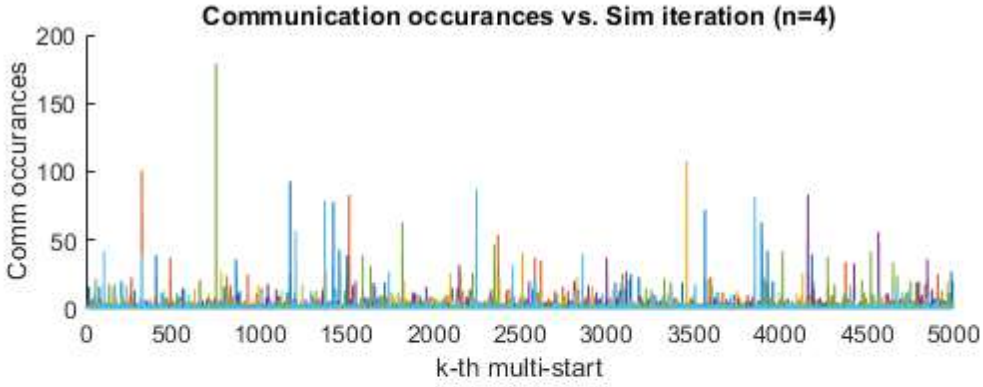
4, 8, 16, 32 Agent Multi-Start Test in 80x80 Box

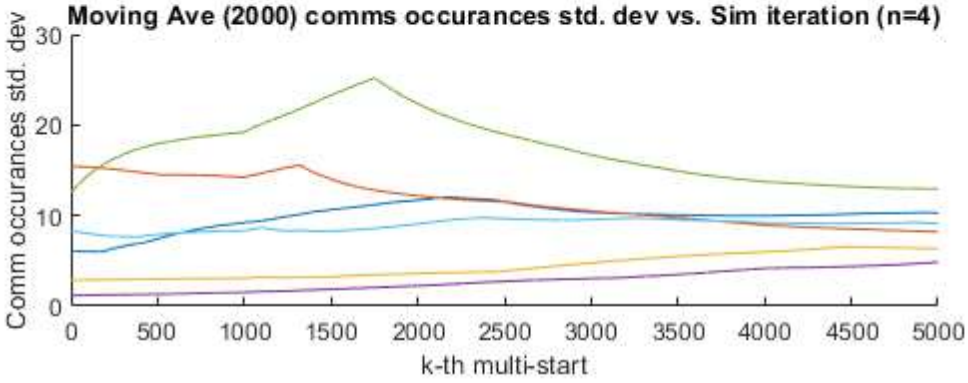
Results: 4-Agent case: ave comms [0.53, 0.61]; no comms itrs [4064, 4119] 8-Agent case: ave comms [0.49, 0.62]; no comms itrs [4031, 4140] 16-Agent case: ave comms [0.49, 0.69]; no comms itrs [4034, 4145] 32-Agent case: ave comms [0.49, 0.72]; no comms itrs [4026, 4166]

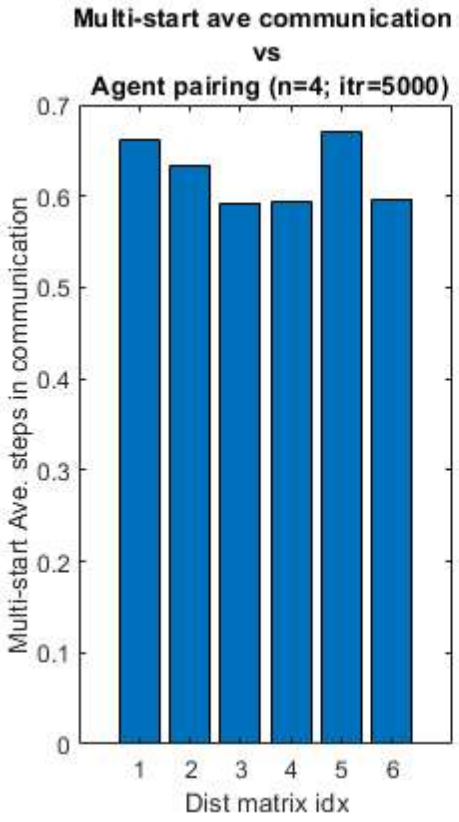
```
bounds = [0 80; 0 80];

a.multiStartData(bounds, 4, 240, 5000);                 % bounds, numAgents, N, sim_itrs
a.multiStartData(bounds, 8, 240, 5000);
a.multiStartData(bounds, 16, 240, 5000);
a.multiStartData(bounds, 32, 240, 5000);

SimAnalysis.clearEmptyFigs();


disp('Done')
```

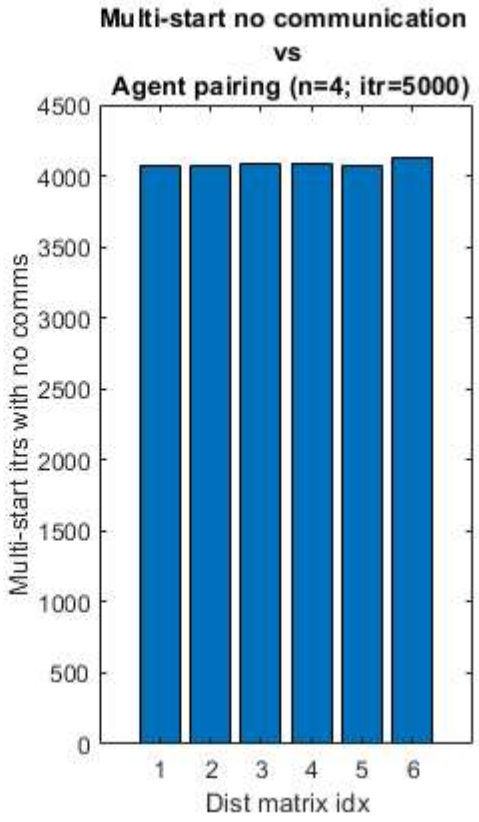
```
Done
```

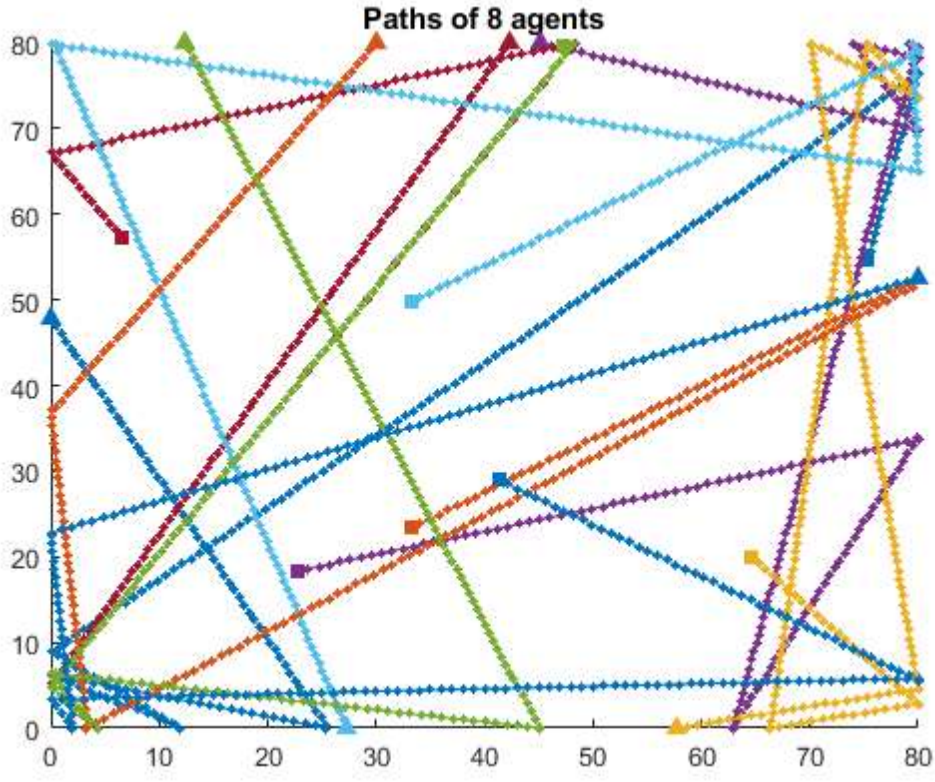

Paths of 4 agents
0
10
20
30
40
50
60
70
80

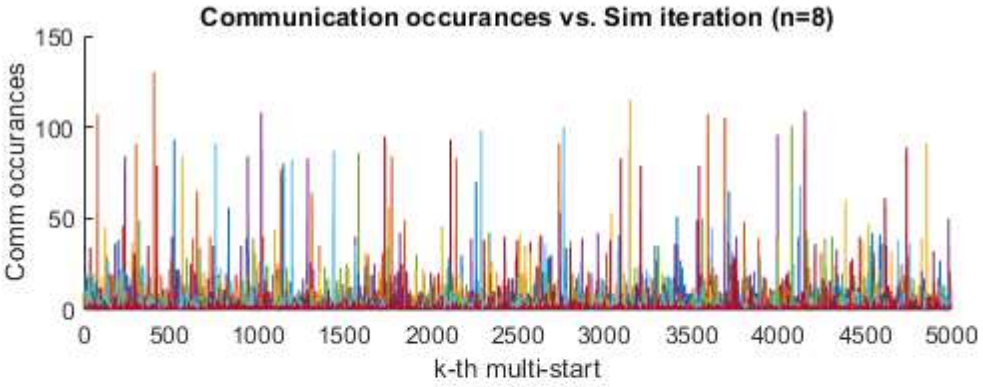

Communication occurances vs. Sim iteration (n=4)
Comm occurances
k-th multi-start
0
50
100
150
200
500
1000
1500
2000
2500
3000
3500
4000
4500
5000

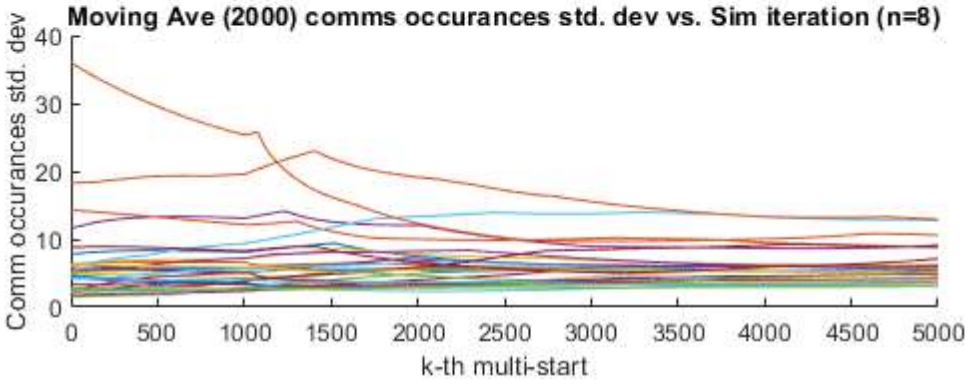

Moving Ave (2000) comms occurances std. dev vs. Sim iteration (n=4)
Comm occurances std. dev
k-th multi-start
0
10
20
30
500
1000
1500
2000
2500
3000
3500
4000
4500
5000

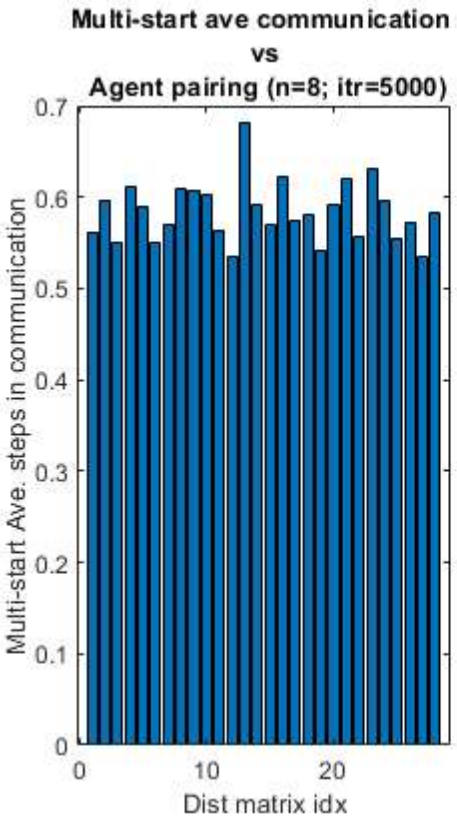

Multi-start ave communication
vs
Agent pairing (n=4; itr=5000)
Multi-start Ave. steps in communication
Dist matrix idx
0
0.1
0.2
0.3
0.4
0.5
0.6
0.7
1
2
3
4
5
6

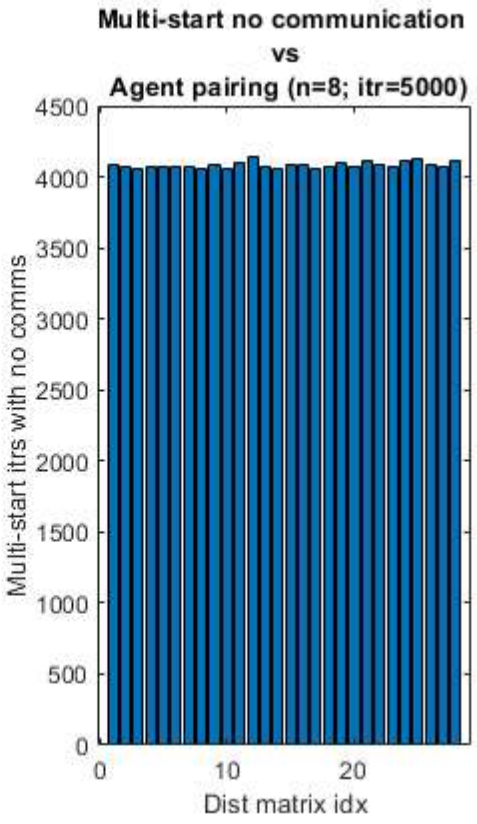

Multi-start no communication
vs
Agent pairing (n=4; itr=5000)
Multi-start itrs with no comms
Dist matrix idx
0
500
1000
1500
2000
2500
3000
3500
4000
4500
1
2
3
4
5
6

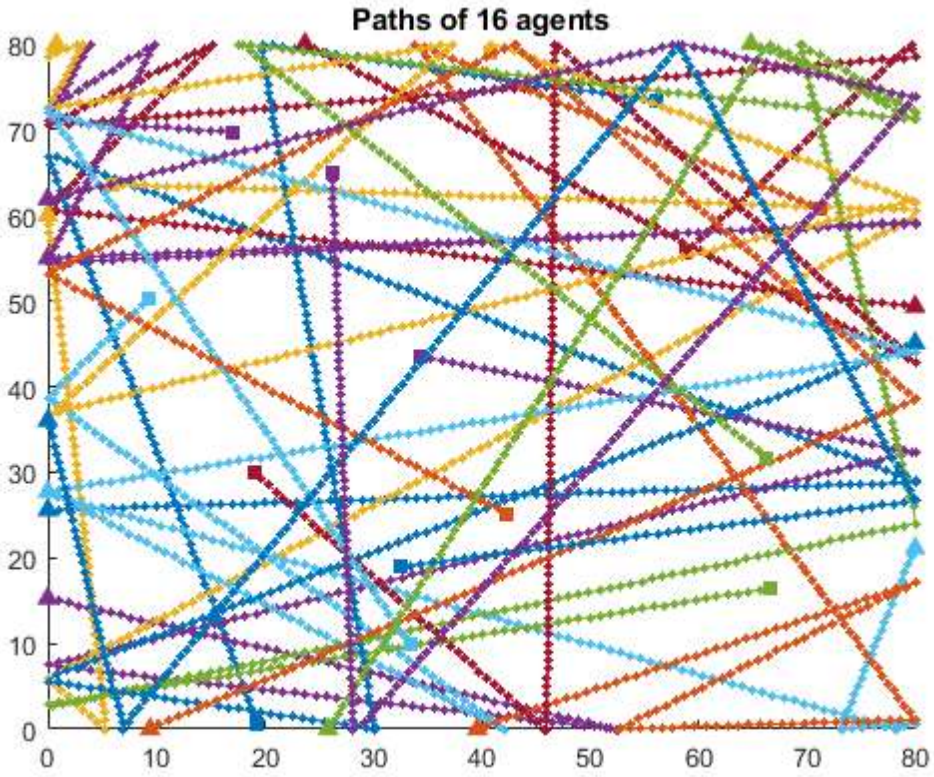

Paths of 8 agents
0
10
20
30
40
50
60
70
80

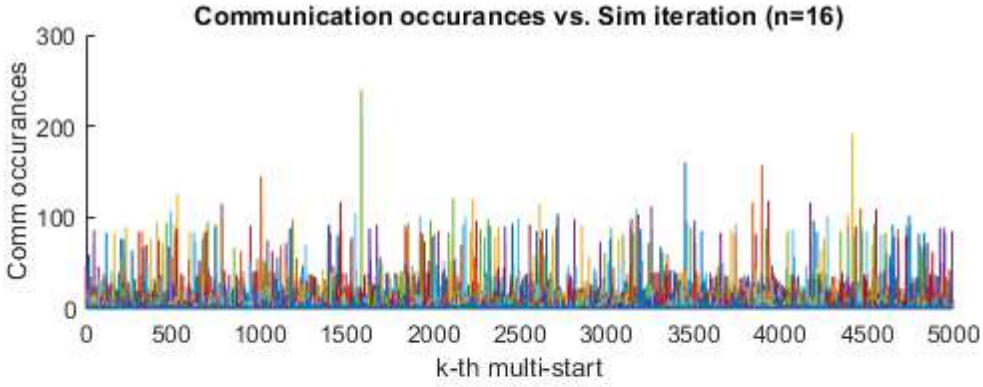

Communication occurances vs. Sim iteration (n=8)
Comm occurances
k-th multi-start

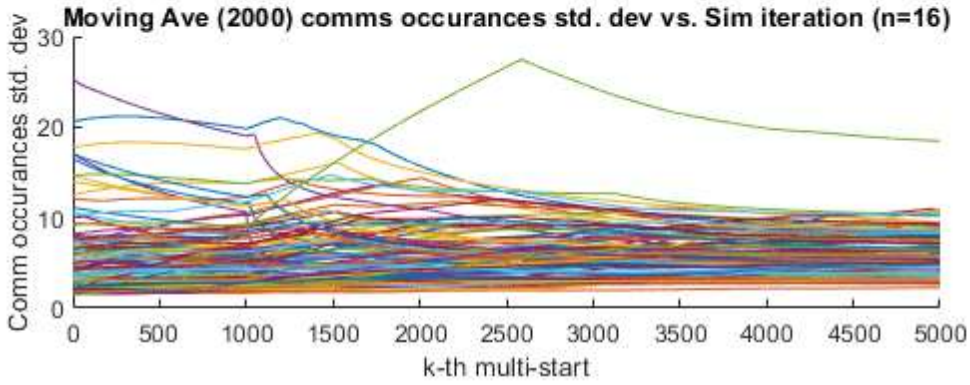

Moving Ave (2000) comms occurances std. dev vs. Sim iteration (n=8)
Comm occurances std. dev
k-th multi-start

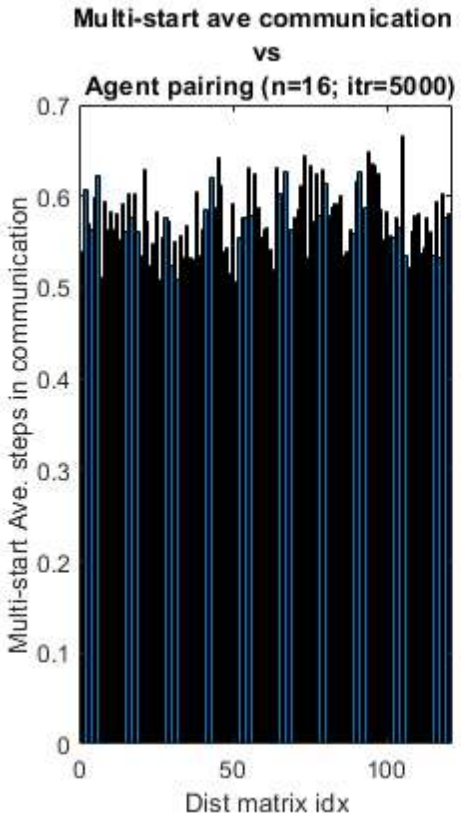

Multi-start ave communication
vs
Agent pairing (n=8; itr=5000)
Multi-start Ave. steps in communication
Dist matrix idx

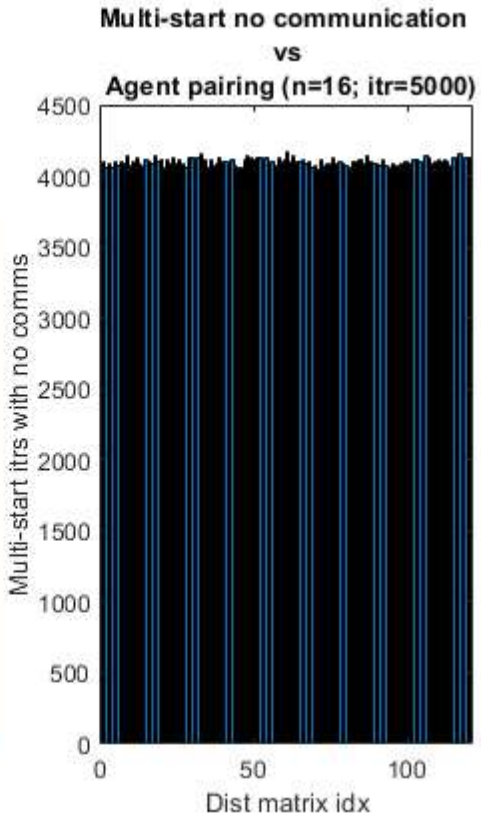

Multi-start no communication
vs
Agent pairing (n=8; itr=5000)
Multi-start itrs with no comms
Dist matrix idx

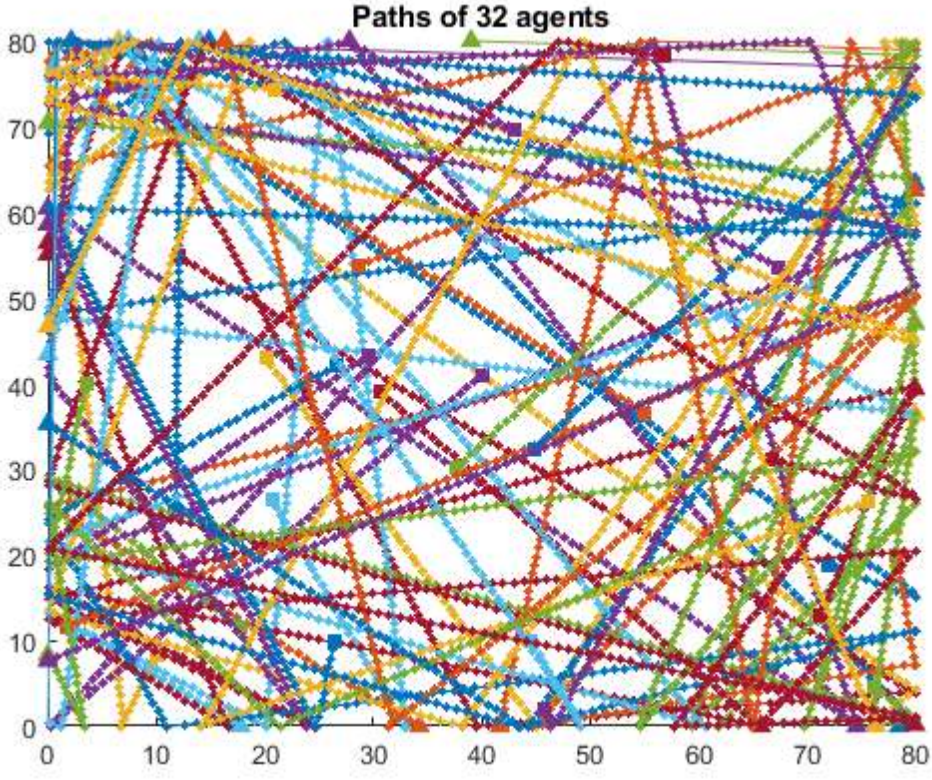

Paths of 16 agents
0
10
20
30
40
50
60
70
80

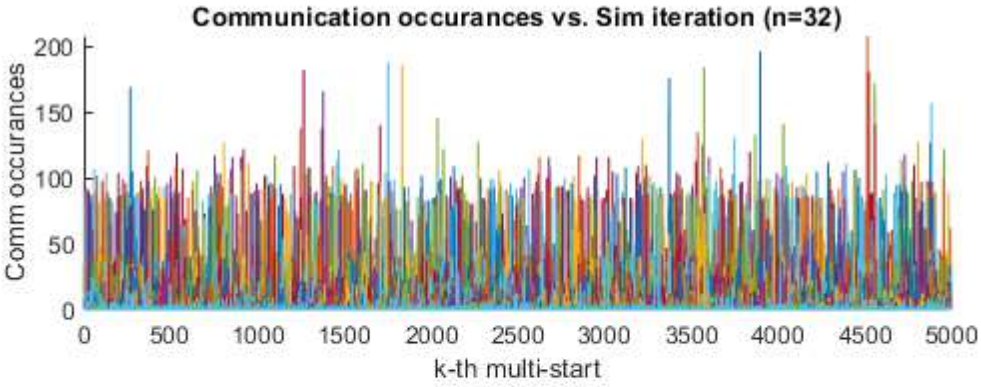

Communication occurances vs. Sim iteration (n=16)
Comm occurances
0
100
200
300
0
500
1000
1500
2000
2500
3000
3500
4000
4500
5000
k-th multi-start

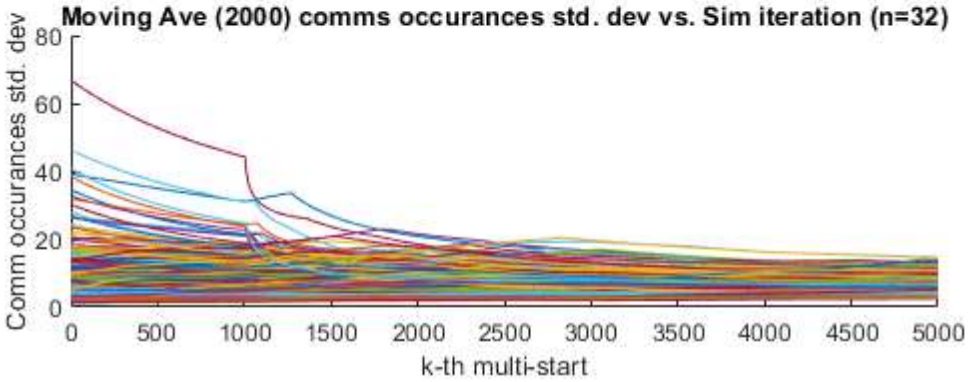

Moving Ave (2000) comms occurances std. dev vs. Sim iteration (n=16)
Comm occurances std. dev
0
10
20
30
0
500
1000
1500
2000
2500
3000
3500
4000
4500
5000
k-th multi-start

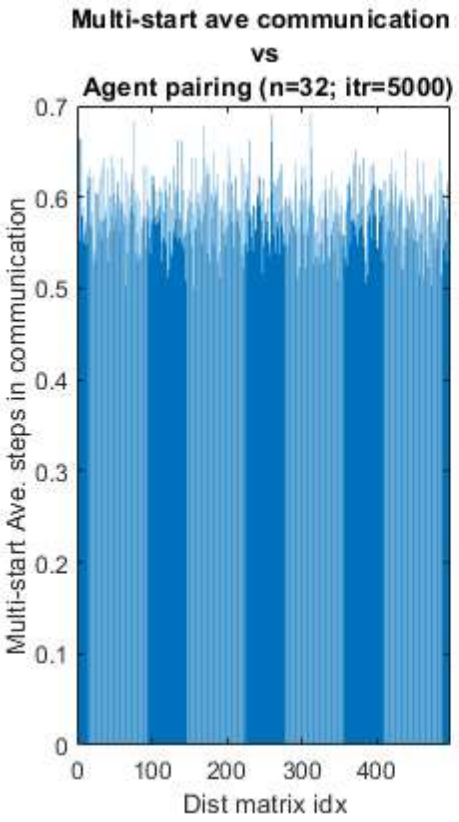

Multi-start ave communication
vs
Agent pairing (n=16; itr=5000)
Multi-start Ave. steps in communication
Dist matrix idx
0
0.1
0.2
0.3
0.4
0.5
0.6
0.7
0
50
100

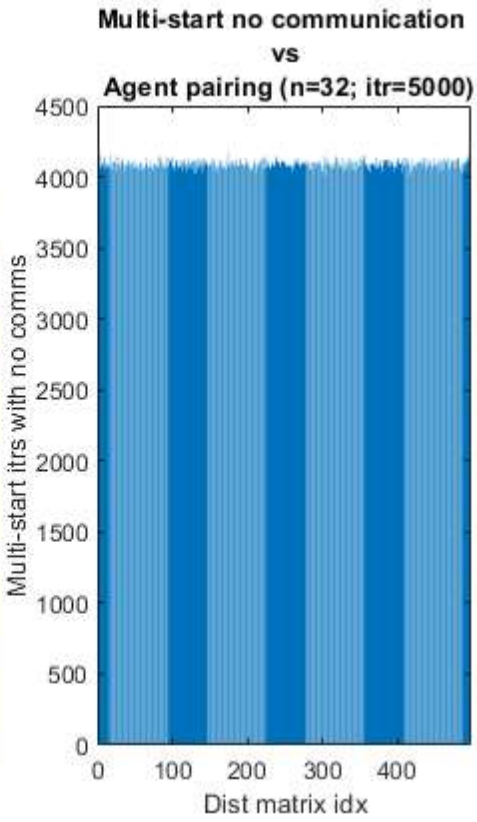

Multi-start no communication
vs
Agent pairing (n=16; itr=5000)
Multi-start itrs with no comms
Dist matrix idx
0
500
1000
1500
2000
2500
3000
3500
4000
4500
0
50
100


Paths of 32 agents
0
10
20
30
40
50
60
70
80









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