



FACULTY OF COMPUTER  
SCIENCE AND ENGINEERING

# FUNCTIONAL DEPENDENCIES AND NORMALIZATION



DATABASES - lectures



# Outline

- Informal Design Guidelines for Relational Databases
- Functional Dependencies (FDs)
- Normal Forms (NFs) for Relational Databases
  - 1NF
  - 2NF
  - 3NF and BCNF
  - 4NF
  - 5NF

# Informal Design Guidelines for Relational Databases

- What is relational database design?
  - The grouping of attributes to form "good" relation schemas
- Two levels of relation schemas
  - The logical "user view" level
  - The storage "base relation" level
- Design is concerned mainly with base relations
- Informal criteria for “good” base relations:
  - Making sure that the semantics of the attributes is clear in the schema
  - Reducing the redundant information in tuples
  - Reducing the NULL values in tuples
  - Disallowing the possibility of generating spurious tuples

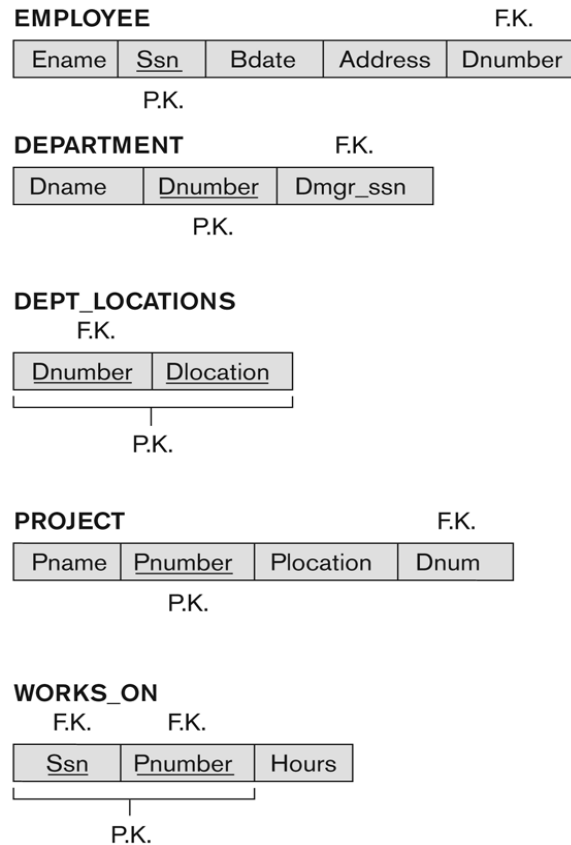


# Semantics of the Relation Attributes

- **GUIDELINE 1** : Informally, each tuple in a relation should represent one entity or relationship instance.
- Attributes of different entities (EMPLOYEEs, DEPARTMENTs, PROJECTs) should not be mixed in the same relation
- Only foreign keys should be used to refer to other entities
- Entity and relationship attributes should be kept apart as much as possible.

Bottom Line: *Design a schema that can be explained easily relation by relation.  
The semantics of attributes should be easy to interpret.*

# Example



**Figure 10.1**  
A simplified COMPANY relational database schema.

A simplified COMPANY relational database schema

**Figure 10.2**  
Example database state for the relational database schema of Figure 10.1.

**EMPLOYEE**

Ename	<u>Ssn</u>	Bdate	Address	Dnumber
Smith, John B.	123456789	1965-01-09	731 Fondren, Houston, TX	5
Wong, Franklin T.	333445555	1955-12-08	638 Voss, Houston, TX	5
Zelaya, Alicia J.	999887777	1968-07-19	3321 Castle, Spring, TX	4
Wallace, Jennifer S.	987654321	1941-06-20	291 Berry, Bellaire, TX	4
Narayan, Ramesh K.	666884444	1962-09-15	975 Fire Oak, Humble, TX	5
English, Joyce A.	453453453	1972-07-31	5631 Rice, Houston, TX	5
Jabbar, Ahmad V.	987987987	1969-03-29	980 Dallas, Houston, TX	4
Borg, James E.	888665555	1937-11-10	450 Stone, Houston, TX	1

**DEPARTMENT**

Dname	<u>Dnumber</u>	Dmgr_ssn
Research	5	333445555
Administration	4	987654321
Headquarters	1	888665555

**DEPT\_LOCATIONS**

<u>Dnumber</u>	<u>Dlocation</u>
1	Houston
4	Stafford
5	Bellaire
5	Sugarland
5	Houston

**WORKS\_ON**

<u>Ssn</u>	<u>Pnumber</u>	Hours
123456789	1	32.5
123456789	2	7.5
666884444	3	40.0
453453453	1	20.0
453453453	2	20.0
333445555	2	10.0
333445555	3	10.0
333445555	10	10.0
333445555	20	10.0
999887777	30	30.0
999887777	10	10.0
987987987	10	35.0
987987987	30	5.0
987654321	30	20.0
987654321	20	15.0
888665555	20	Null

**PROJECT**

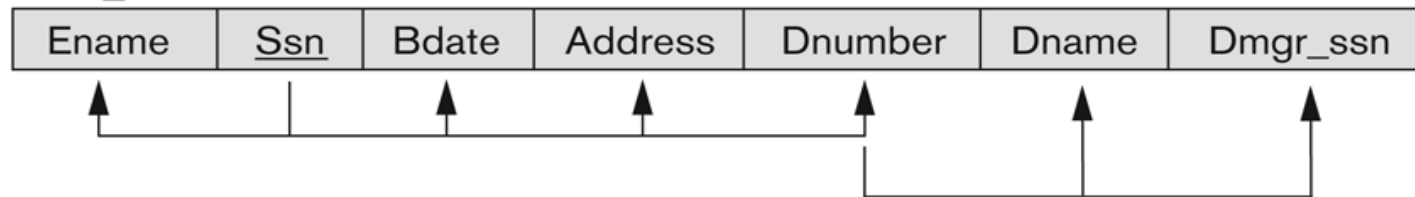
Pname	<u>Pnumber</u>	Plocation	Dnum
ProductX	1	Bellaire	5
ProductY	2	Sugarland	5
ProductZ	3	Houston	5
Computerization	10	Stafford	4
Reorganization	20	Houston	1
Newbenefits	30	Stafford	4



# Easy to Explain Its Meaning

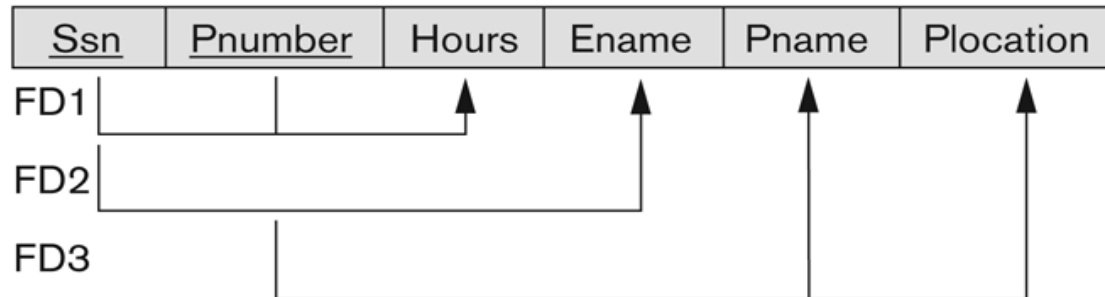
(a)

**EMP\_DEPT**



(b)

**EMP\_PROJ**

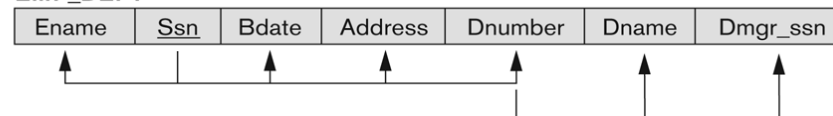


# Redundant Information in Tuples

- Information is stored redundantly
  - Wastes storage
  - Causes problems with update anomalies
    - Insertion anomalies
    - Deletion anomalies
    - Modification anomalies

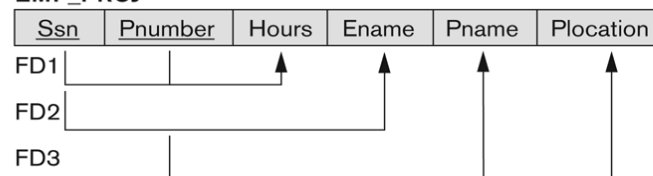
## Example of redundant information in tuples

EMP\_DEPT



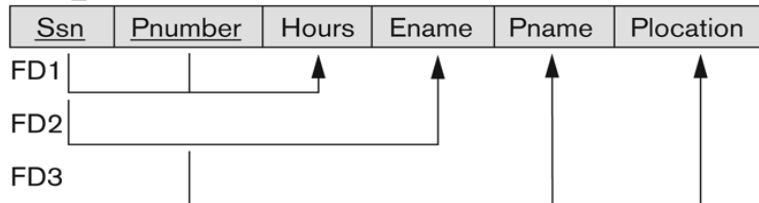
(b)

EMP\_PROJ



# Example – modification anomalies

EMP\_PROJ



EMP\_PROJ

<u>Ssn</u>	<u>Pnumber</u>	Hours	Redundancy		Plocation
			Ename	Pname	
123456789	1	32.5	Smith, John B.	ProductX	Bellaire
123456789	2	7.5	Smith, John B.	ProductY	Sugarland
666884444	3	40.0	Narayan, Ramesh K.	ProductZ	Houston
453453453	1	20.0	English, Joyce A.	ProductX	Bellaire
453453453	2	20.0	English, Joyce A.	ProductY	Sugarland
333445555	2	10.0	Wong, Franklin T.	ProductY	Sugarland
333445555	3	10.0	Wong, Franklin T.	ProductZ	Houston
333445555	10	10.0	Wong, Franklin T.	Computerization	Stafford
333445555	20	10.0	Wong, Franklin T.	Reorganization	Houston
999887777	30	30.0	Zelaya, Alicia J.	Newbenefits	Stafford
999887777	10	10.0	Zelaya, Alicia J.	Computerization	Stafford
987987987	10	35.0	Jabbar, Ahmad V.	Computerization	Stafford
987987987	30	5.0	Jabbar, Ahmad V.	Newbenefits	Stafford
987654321	30	20.0	Wallace, Jennifer S.	Newbenefits	Stafford
987654321	20	15.0	Wallace, Jennifer S.	Reorganization	Houston
888665555	20	Null	Borg, James E.	Reorganization	Houston

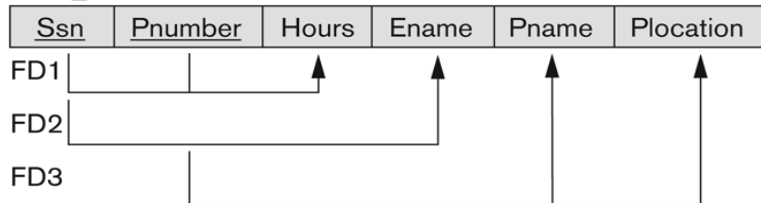
- Changing the name of project number P1 from “Billing” to “Customer-Accounting” may cause this update to be made for all 100 employees working on project P1.





# Example – insertion anomalies

EMP\_PROJ



EMP\_PROJ

<u>Ssn</u>	<u>Pnumber</u>	Hours	Ename	Pname	Plocation
123456789	1	32.5	Smith, John B.	ProductX	Bellaire
123456789	2	7.5	Smith, John B.	ProductY	Sugarland
666884444	3	40.0	Narayan, Ramesh K.	ProductZ	Houston
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Redundancy

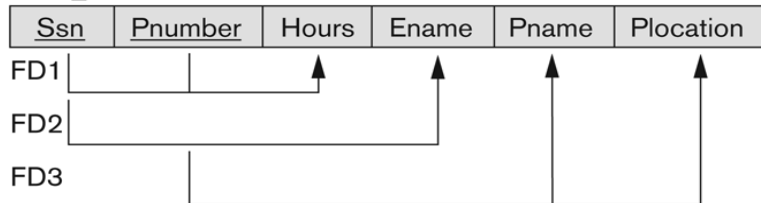
Redundancy

- Cannot insert a project unless an employee is assigned to it.
- Cannot insert an employee unless he/she is assigned to a project.



# Example – deletion anomalies

EMP\_PROJ



EMP\_PROJ

<u>Ssn</u>	<u>Pnumber</u>	Hours	Ename	Pname	Plocation
123456789	1	32.5	Smith, John B.	ProductX	Bellaire
123456789	2	7.5	Smith, John B.	ProductY	Sugarland
666884444	3	40.0	Narayan, Ramesh K.	ProductZ	Houston
453453453	1	20.0	English, Joyce A.	ProductX	Bellaire
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333445555	3	10.0	Wong, Franklin T.	ProductZ	Houston
333445555	10	10.0	Wong, Franklin T.	Computerization	Stafford
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999887777	30	30.0	Zelaya, Alicia J.	Newbenefits	Stafford
999887777	10	10.0	Zelaya, Alicia J.	Computerization	Stafford
987987987	10	35.0	Jabbar, Ahmad V.	Computerization	Stafford
987987987	30	5.0	Jabbar, Ahmad V.	Newbenefits	Stafford
987654321	30	20.0	Wallace, Jennifer S.	Newbenefits	Stafford
987654321	20	15.0	Wallace, Jennifer S.	Reorganization	Houston
888665555	20	Null	Borg, James E.	Reorganization	Houston

- When a project is deleted, it will result in deleting all the employees who work on that project.
- Alternately, if an employee is the sole employee on a project, deleting that employee would result in deleting the corresponding project.



# Redundant Information in Tuples

## ➤ GUIDELINE 2 :

- Design a schema that does not suffer from the insertion, deletion and update anomalies.
- If there are any anomalies present, then note them so that applications can be made to take them into account.

# Null Values in Tuples

## ➤ **GUIDELINE 3 :**

- Relations should be designed such that their tuples will have as few NULL values as possible
- Attributes that are NULL frequently could be placed in separate relations (with the primary key)
- Reasons for nulls:
  - Attribute not applicable or invalid
  - Attribute value unknown (may exist)
  - Value known to exist, but unavailable

# Spurious Tuples

- Bad designs for a relational database may result in erroneous results for certain JOIN operations
- The "lossless join" property is used to guarantee meaningful results for join operations
- **GUIDELINE 4 :**
  - The relations should be designed to satisfy the lossless join condition.
  - No spurious tuples should be generated by doing a natural-join of any relations.

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  - *Design relation schemas so that they can be **joined with equality conditions on attributes that are appropriately related** (primary key, foreign key) pairs in a way that guarantees that no spurious tuples are generated.*



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  - No spurious tuples should be generated by doing a natural-join of any relations.
  - *Design relation schemas so that they can be **joined with equality conditions on attributes that are appropriately related** (primary key, foreign key) pairs in a way that guarantees that no spurious tuples are generated*
  - ***Avoid relations that contain matching attributes that are not (foreign key, primary key) combinations because joining on such attributes may produce spurious tuples***

# Example

**EMP\_LOCS**

<u>Ename</u>	<u>Plocation</u>
P.K.	

**EMP\_LOCS \* EMP\_PROJ1=?**

**EMP\_PROJ1**

<u>Ssn</u>	<u>Pnumber</u>	Hours	Pname	Plocation
P.K.				

**EMP\_LOCS**

Ename	Plocation
Smith, John B.	Bellaire
Smith, John B.	Sugarland
Narayan, Ramesh K.	Houston
English, Joyce A.	Bellaire
English, Joyce A.	Sugarland
Wong, Franklin T.	Sugarland
Wong, Franklin T.	Houston
Wong, Franklin T.	Stafford
Zelaya, Alicia J.	Stafford
Jabbar, Ahmad V.	Stafford
Wallace, Jennifer S.	Stafford
Wallace, Jennifer S.	Houston
Borg, James E.	Houston

**EMP\_PROJ1**

Ssn	Pnumber	Hours	Pname	Plocation
123456789	1	32.5	ProductX	Bellaire
123456789	2	7.5	ProductY	Sugarland
666884444	3	40.0	ProductZ	Houston
453453453	1	20.0	ProductX	Bellaire
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888665555	20	NULL	Reorganization	Houston





# Example

	Ssn	Pnumber	Hours	Pname	Plocation	Ename
	123456789	1	32.5	ProductX	Bellaire	Smith, John B.
*	123456789	1	32.5	ProductX	Bellaire	English, Joyce A.
	123456789	2	7.5	ProductY	Sugarland	Smith, John B.
*	123456789	2	7.5	ProductY	Sugarland	English, Joyce A.
*	123456789	2	7.5	ProductY	Sugarland	Wong, Franklin T.
	666884444	3	40.0	ProductZ	Houston	Narayan, Ramesh K.
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	333445555	3	10.0	ProductZ	Houston	Wong, Franklin T.
	333445555	10	10.0	Computerization	Stafford	Wong, Franklin T.
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\*  
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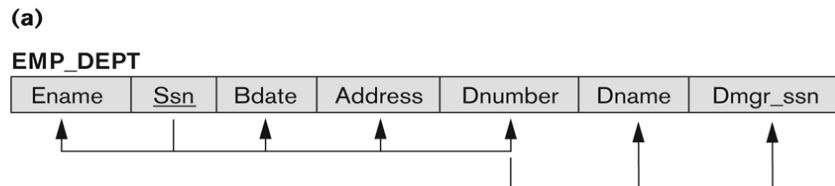
# Functional Dependencies

- Functional Dependencies (FDs)
  - Are used to specify *formal measures* of the "goodness" of relational designs
  - And keys are used to define **normal forms** for relations
  - Are **constraints** that are derived from the *meaning* and *interrelationships* of the data attributes
  
- FDs are derived from the real-world constraints on the attributes

# Functional Dependencies

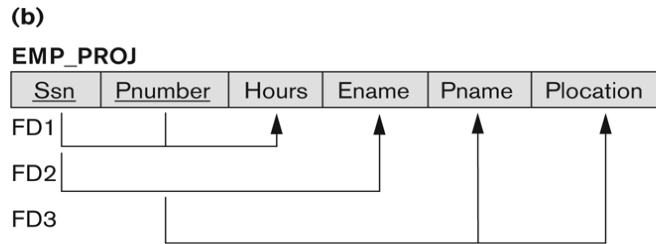
- A set of attributes  $X$  *functionally determines* a set of attributes  $Y$  if the value of  $X$  determines a unique value for  $Y$ 
  - Denoted by  $X \rightarrow Y$
- $X \rightarrow Y$  holds iff whenever two tuples have the same value for  $X$ , they *must have* the same value for  $Y$ 
  - For any two tuples  $t1$  and  $t2$  in any relation instance  $r(R)$ : If  $t1[X]=t2[X]$ , *then*  $t1[Y]=t2[Y]$
- $X \rightarrow Y$  in  $R$  specifies a *constraint* on all relation instances  $r(R)$

# Examples of FD constraints



➤ Social security number determines employee name

$SSN \rightarrow ENAME$



➤ Project number determines project name and location

$PNUMBER \rightarrow \{PNAME, PLOCATION\}$

➤ Employee ssn and project number determines the hours per week that the employee works on the project

$\{SSN, PNUMBER\} \rightarrow HOURS$

# Example

- A functional dependency is a property of the **semantics or meaning of the attributes for all relation states**.
- The database designers will use their understanding of the semantics of the attributes of R—that is, how they relate to one another—to specify the functional dependencies that should hold on **all** relation states (extensions)  $r$  of R

**TEACH**

Teacher	Course	Text
Smith	Data Structures	Bartram
Smith	Data Management	Martin
Hall	Compilers	Hoffman
Brown	Data Structures	Horowitz

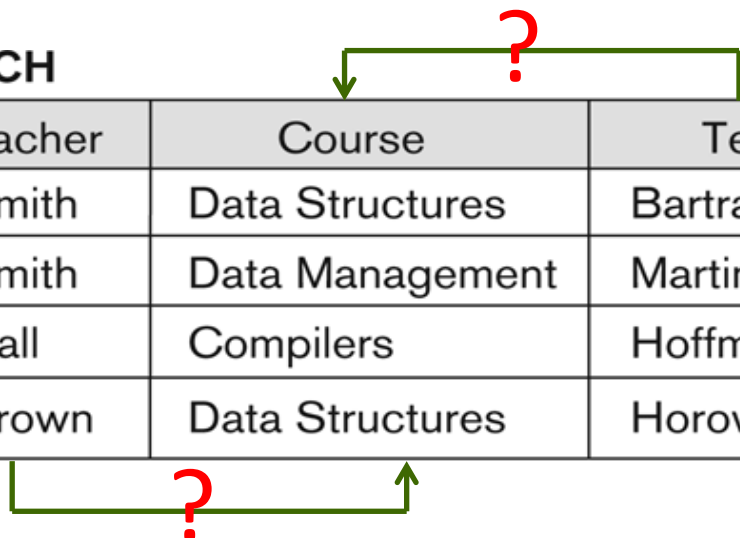
**Figure 10.7**

A relation state of TEACH with a *possible* functional dependency  $\text{TEXT} \rightarrow \text{COURSE}$ . However,  $\text{TEACHER} \rightarrow \text{COURSE}$  is ruled out.

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# Inference Rules for FDs

- Given a set of FDs  $F$ , we can **infer** additional FDs that hold whenever the FDs in  $F$  hold
- Armstrong's inference rules:
  - IR1. (**Reflexive**) If  $Y \text{ subset-of } X$ , then  $X \rightarrow Y$
  - IR2. (**Augmentation**) If  $X \rightarrow Y$ , then  $XZ \rightarrow YZ$ 
    - (Notation:  $XZ$  stands for  $X \cup Z$ )
  - IR3. (**Transitive**) If  $X \rightarrow Y$  and  $Y \rightarrow Z$ , then  $X \rightarrow Z$
- IR1, IR2, IR3 form a **sound** and **complete** set of inference rules
  - All dependencies inferred using these rules hold in all relation states
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a set of attributes always  
determines itself  
or any of its subsets





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  - IR2. (**Augmentation**) If  $X \rightarrow Y$ , then  $XZ \rightarrow YZ$  ↙ adding the same set of attributes to both the left- and right-hand sides of a dependency results in another valid dependency
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  - All possible dependencies can be inferred using these rules repeatedly

# Inference Rules for FDs

- Some additional inference rules that are useful:
  - **Decomposition:** If  $X \rightarrow YZ$ , then  $X \rightarrow Y$  and  $X \rightarrow Z$
  - **Union:** If  $X \rightarrow Y$  and  $X \rightarrow Z$ , then  $X \rightarrow YZ$
  - **Pseudotransitivity:** If  $X \rightarrow Y$  and  $WY \rightarrow Z$ , then  $WX \rightarrow Z$
  
- The last three inference rules, as well as any other inference rules, can be deduced from IR1, IR2, and IR3 (completeness property)

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➤ **Pseudotransitivity:** If  $X \rightarrow Y$  and  $WY \rightarrow Z$ , then  $WX \rightarrow Z$

we can remove attributes from  
the right-hand side of a dependency

➤ The last three inference rules, as well as any other inference rules, can be deduced from IR1, IR2, and IR3 (completeness property)



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➤ **Union:** If  $X \rightarrow Y$  and  $X \rightarrow Z$ , then  $X \rightarrow YZ$

➤ **Pseudotransitivity:** If  $X \rightarrow Y$  and  $WY \rightarrow Z$ , then  $WX \rightarrow Z$

we can combine a set of dependencies  
into a single FD

➤ The last three inference rules, as well as any other inference rules, can be deduced from IR1, IR2, and IR3 (completeness property)

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We can replace a set of attributes  $Y$  on the left hand side of a dependency with another set  $X$  that functionally determines  $Y$

➤ The last three inference rules, as well as any other inference rules, can be deduced from IR1, IR2, and IR3 (completeness property)

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  - **Decomposition:** If  $X \rightarrow YZ$ , then  $X \rightarrow Y$  and  $X \rightarrow Z$
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  - **Pseudotransitivity:** If  $X \rightarrow Y$  and  $WY \rightarrow Z$ , then  $WX \rightarrow Z$

*Cautionary note:*

$XY \rightarrow A$  does *not* necessarily imply either  $X \rightarrow A$  or  $Y \rightarrow A$ .

- The last three inference rules, as well as any other inference rules, can be deduced from IR1, IR2, and IR3 (completeness property)



# Inference Rules for FDs

- **Closure** of a set  $F$  of FDs is the set  $F^+$  of all FDs that can be inferred from  $F$ , including  $F$
- **Closure** of a set of attributes  $X$  **with respect to**  $F$  is the set  $X^+$  of all attributes that are **functionally determined by  $X$**
- $X^+$  can be calculated by repeatedly applying IR1, IR2, IR3 using the FDs in  $F$

# Equivalence of Sets of FDs

- Two sets of FDs  $F$  and  $G$  are **equivalent** if:
  - Every FD in  $F$  can be inferred from  $G$ , and
  - Every FD in  $G$  can be inferred from  $F$
  - Hence,  $F$  and  $G$  are equivalent if  $F^+ = G^+$
- Definition (**Covers**):
  - $F$  **covers**  $G$  if every FD in  $G$  can be inferred from  $F$ 
    - (i.e., if  $G^+ \text{ subset-of } F^+$ )
- $F$  and  $G$  are equivalent if  $F$  covers  $G$  and  $G$  covers  $F$
- There is an algorithm for checking equivalence of sets of FDs





# Minimal Sets of FDs

- A set of FDs is **minimal** if it satisfies the following conditions:
1. Every dependency in  $F$  has **a single attribute for its right-hand side**.
  2. We cannot remove any dependency from  $F$  and have a set of dependencies that is equivalent to  $F$ .
  3. We cannot replace any dependency  $X \rightarrow A$  in  $F$  with a dependency  $Y \rightarrow A$ , where  $Y$  proper-subset-of  $X$  ( $Y$  subset-of  $X$ ) and still have a set of dependencies that is equivalent to  $F$ .
- A **minimal cover** of a set of functional dependencies  $E$  is a *minimal* set of dependencies (in the **standard canonical form** and **without redundancy**) that is equivalent to  $E$ .

# Minimal Sets of FDs

- A set of FDs is **minimal** if it satisfies the following conditions:
1. Every dependency in  $F$  has a single attribute for its right-hand side.
  2. We cannot remove any dependency from  $F$  and have a set of dependencies that is equivalent to  $F$ .
  3. Ensures that there are no redundancies in the dependencies either by having redundant attributes on the left-hand side of a dependency
- A **minimal cover** of a set of functional dependencies  $E$  is a *minimal* set of dependencies (in the **standard canonical form** and **without redundancy**) that is equivalent to  $E$ .

# Minimal Sets of FDs

- A set of FDs is **minimal** if it satisfies the following conditions:
1. Every dependency in  $F$  has a single attribute for its right-hand side.
  2. Ensures that there are no redundancies in the dependencies either by having a dependency that can be inferred from the remaining FDs in  $F$
  3. We cannot replace any dependency  $X \rightarrow A$  in  $F$  with a dependency  $Y \rightarrow A$ , where  $Y$  proper-subset-of  $X$  ( $Y$  subset-of  $X$ ) and still have a set of dependencies that is equivalent to  $F$ .
- A **minimal cover** of a set of functional dependencies  $E$  is a *minimal* set of dependencies (in the **standard canonical form** and **without redundancy**) that is equivalent to  $E$ .

# Algorithm for Finding a Minimal Cover $F$ for a Set of Functional Dependencies $E$

1. Set  $F := E$ .
2. Replace each functional dependency  $X \rightarrow \{A_1, A_2, \dots, A_n\}$  in  $F$  by the  $n$  functional dependencies  $X \rightarrow A_1, X \rightarrow A_2, \dots, X \rightarrow A_n$ .
3. For each functional dependency  $X \rightarrow A$  in  $F$   
For each attribute  $B$  that is an element of  $X$   
if  $\{F - \{X \rightarrow A\}\} \cup \{(X - \{B\}) \rightarrow A\}$  is equivalent to  $F$   
then replace  $X \rightarrow A$  with  $(X - \{B\}) \rightarrow A$  in  $F$ .
4. For each remaining functional dependency  $X \rightarrow A$  in  $F$   
if  $\{F - \{X \rightarrow A\}\}$  is equivalent to  $F$   
then remove  $X \rightarrow A$  from  $F$ .



# Example

Let the given set of FDs be  $E : \{B \rightarrow A, D \rightarrow A, AB \rightarrow D\}$ . We have to find the minimum cover of  $E$ .

All above dependencies are in canonical form; so we have completed step 1 of the algorithm and can proceed to step 2. In step 2 we need to determine if  $AB \rightarrow D$  has any redundant attribute on the left-hand side; that is, can it be replaced by  $B \rightarrow D$  or  $A \rightarrow D$ ?

Since  $B \rightarrow A$ , by augmenting with  $B$  on both sides (IR2), we have  $BB \rightarrow AB$ , or  $B \rightarrow AB$  (i). However,  $AB \rightarrow D$  as given (ii), hence by the transitive rule (IR3), we get from (i) and (ii),  $B \rightarrow D$ .  $AB \rightarrow D$  may be replaced by  $B \rightarrow D$ .

We now have a set equivalent to original  $E$ , say  $E' : \{B \rightarrow A, D \rightarrow A, B \rightarrow D\}$ .

No further reduction is possible in step 2 since all FDs have a single attribute on the left-hand side.

In step 3 we look for a redundant FD in  $E'$ . By using the transitive rule on  $B \rightarrow D$  and  $D \rightarrow A$ , we derive  $B \rightarrow A$ . Hence  $B \rightarrow A$  is redundant in  $E'$  and can be eliminated.

Hence the minimum cover of  $E$  is  **$\{B \rightarrow D, D \rightarrow A\}$** .



# Normalization of Relations

## ➤ Normalization:

- The process of decomposing unsatisfactory "bad" relations by breaking up their attributes into smaller relations

## ➤ Normal form:

- Condition using keys and FDs of a relation to certify whether a relation schema is in a particular normal form

## ➤ Denormalization:

- The process of storing the join of higher normal form relations as a base relation—which is in a lower normal form



# Normalization of Relations

- 2NF, 3NF, BCNF
  - based on keys and FDs of a relation schema
- 4NF
  - based on keys, multi-valued dependencies : MVDs
- 5NF
  - based on keys, join dependencies : JDs

# Practical Use of Normal Forms

- **Normalization** is carried out in practice so that the resulting designs are of high quality and meet the desirable properties
- The practical utility of these normal forms becomes questionable when the constraints on which they are based are *hard to understand* or to *detect*
- The database designers *need not* normalize to the highest possible normal form
  - (usually up to 3NF, BCNF or 4NF)





# Definitions of Keys and Attributes Participating in Keys

- A **superkey** of a relation schema  $R = \{A_1, A_2, \dots, A_n\}$  is a set of attributes  $S$  *subset-of*  $R$  with the property that no two tuples  $t_1$  and  $t_2$  in any legal relation state  $r$  of  $R$  will have  $t_1[S] = t_2[S]$
- A **key**  $K$  is a **superkey** with the *additional property* that removal of any attribute from  $K$  will cause  $K$  not to be a superkey any more.

# Definitions of Keys and Attributes Participating in Keys

- If a relation schema has more than one key, each is called a **candidate** key.
  - One of the candidate keys is *arbitrarily* designated to be the **primary key**, and the others are called **secondary keys**.
- A **Prime attribute** must be a member of *some* candidate key
- A **Nonprime attribute** is not a prime attribute—that is, it is not a member of any candidate key.

# First Normal Form 1NF

## ➤ Disallows

- composite attributes
- multivalued attributes
- **nested relations**; attributes whose values for an *individual tuple* are non-atomic

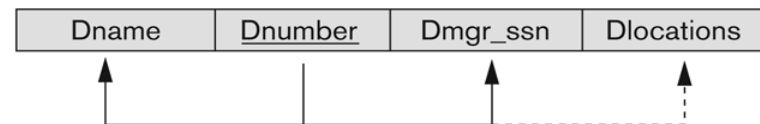
➤ Considered to be part of the definition of relation

# Example

## Normalization into 1NF

(a)

**DEPARTMENT**



(b)

**DEPARTMENT**

Dname	<u>Dnumber</u>	Dmgr_ssn	Dlocations
Research	5	333445555	{Bellaire, Sugarland, Houston}
Administration	4	987654321	{Stafford}
Headquarters	1	888665555	{Houston}

(c)

**DEPARTMENT**

Dname	<u>Dnumber</u>	Dmgr_ssn	<u>Dlocation</u>
Research	5	333445555	Bellaire
Research	5	333445555	Sugarland
Research	5	333445555	Houston
Administration	4	987654321	Stafford
Headquarters	1	888665555	Houston

**Figure 10.8**

Normalization into 1NF.

(a) A relation schema that is not in 1NF. (b)

Example state of relation DEPARTMENT. (c) 1NF

version of the same relation with redundancy.

Can you think of any other solutions to normalize DEPARTMENT?

# Example

Normalizing nested relations into 1 NF

(a)

EMP\_PROJ

Ssn	Ename	Projs	
		Pnumber	Hours

(b)

EMP\_PROJ

Ssn	Ename	Pnumber	Hours
123456789	Smith, John B.	1	32.5
		2	7.5
666884444	Narayan, Ramesh K.	3	40.0
453453453	English, Joyce A.	1	20.0
		2	20.0
333445555	Wong, Franklin T.	2	10.0
		3	10.0
		10	10.0
		20	10.0
999887777	Zelaya, AliciaJ.	30	30.0
		10	10.0
987987987	Jabbar, Ahmad V.	10	35.0
		30	5.0
987654321	Wallace, Jennifer S.	30	20.0
		20	15.0
888665555	Borg, James E.	20	NULL

(c)

EMP\_PROJ1

<u>Ssn</u>	Ename
------------	-------

EMP\_PROJ2

<u>Ssn</u>	<u>Pnumber</u>	Hours
------------	----------------	-------

**Figure 10.9**

Normalizing nested relations into 1NF. (a) Schema of the EMP\_PROJ relation with a *nested relation* attribute PROJS. (b) Example extension of the EMP\_PROJ relation showing nested relations within each tuple. (c) Decomposition of EMP\_PROJ into relations EMP\_PROJ1 and EMP\_PROJ2 by propagating the primary key.



# Second Normal Form 2NF

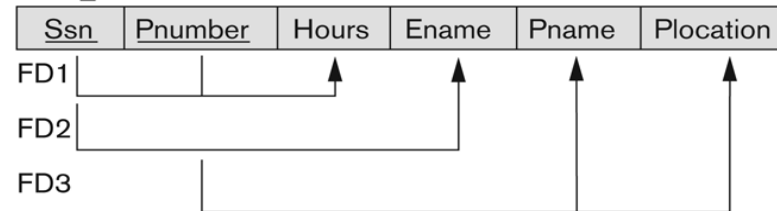
- Uses the concepts of **FDs, primary key**
- Definitions
  - **Prime attribute:** An attribute that is member of the primary key K
  - **Full functional dependency:** a FD  $Y \rightarrow Z$  where removal of any attribute from Y means the FD does not hold any more
- A relation schema R is in **second normal form (2NF)** if **every non-prime attribute A in R is fully functionally dependent on the primary key**

# Example

## Normalizing into 2NF

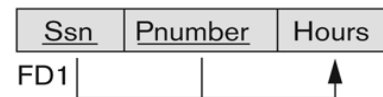
- $\{SSN, PNUMBER\} \rightarrow HOURS$  is a full FD since neither  $SSN \rightarrow HOURS$  nor  $PNUMBER \rightarrow HOURS$  hold
- $\{SSN, PNUMBER\} \rightarrow ENAME$  is not a full FD (it is called a **partial dependency**) since  $SSN \rightarrow ENAME$  also holds

EMP\_PROJ

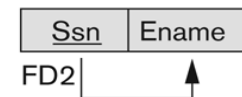


2NF Normalization

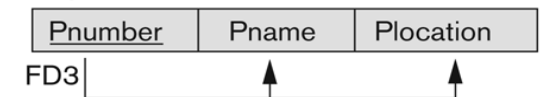
EP1



EP2



EP3



# Third Normal Form 3NF

## ➤ Definition:

➤ **Transitive functional dependency:** a FD  $X \rightarrow Z$  that can be derived from two FDs  $X \rightarrow Y$  and  $Y \rightarrow Z$

➤ A relation schema  $R$  is in **third normal form (3NF)** if it is in 2NF *and* no non-prime attribute  $A$  in  $R$  is *transitively dependent on the primary key*

## ➤ NOTE:

➤ In  $X \rightarrow Y$  and  $Y \rightarrow Z$ , with  $X$  as the primary key, we consider this a problem only if  $Y$  is not a candidate key.

➤ When  $Y$  is a candidate key, there is no problem with the transitive dependency.

➤ E.g., Consider EMP (SSN, Emp#, Salary ).

➤ Here,  $SSN \rightarrow Emp\# \rightarrow Salary$  and  $Emp\#$  is a candidate key.



# Third Normal Form 3NF

## ➤ Definition:

- **Transitive functional dependency:** a FD  $X \rightarrow Y$  that can be derived from two FDs  $X \rightarrow Z$  and  $Z \rightarrow Y$
- *There exists a set of attributes  $Z$  in  $R$  that is **neither a candidate key nor a subset of any key of  $R$***
- A relation schema  $R$  is in **third normal form (3NF)** if it is in 2NF *and* no non-prime attribute  $A$  in  $R$  is transitively dependent on the primary key

# Third Normal Form 3NF

## ➤ Examples:

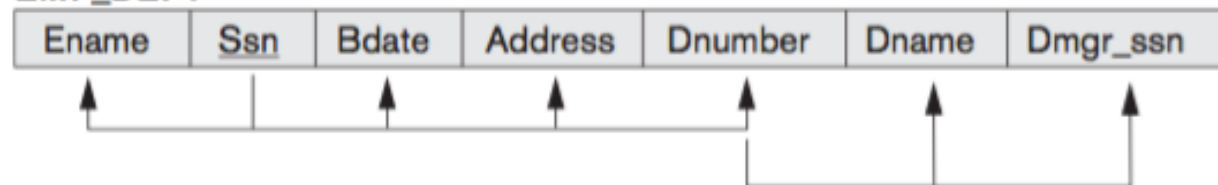
➤ SSN  $\rightarrow$  DMGRSSN is a **transitive** FD

➤ Since SSN  $\rightarrow$  DNUMBER and DNUMBER  $\rightarrow$  DMGRSSN hold

➤ SSN  $\rightarrow$  ENAME is **non-transitive**

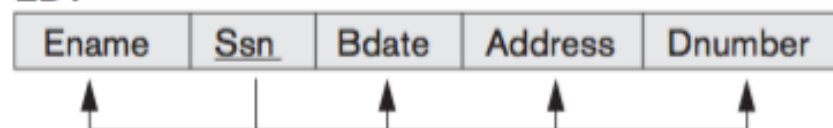
➤ Since there is no set of attributes X where SSN  $\rightarrow$  X and X  $\rightarrow$  ENAME

EMP\_DEPT

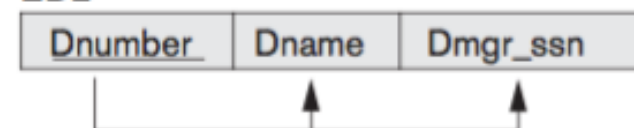


3NF Normalization

ED1



ED2



# Normal Forms Defined Informally

- 1<sup>st</sup> normal form
  - All attributes depend on **the key**
- 2<sup>nd</sup> normal form
  - All attributes depend on **the whole key**
- 3<sup>rd</sup> normal form
  - All attributes depend on **nothing but the key**

# SUMMARY OF NORMAL FORMS based on Primary Keys

Normal Form	Test	Remedy (Normalization)
<b>First (1NF)</b>	Relation should have no multivalued attributes or nested relations.	Form new relations for each multivalued attribute or nested relation.
<b>Second (2NF)</b>	For relations where primary key contains multiple attributes, no nonkey attribute should be functionally dependent on a part of the primary key.	Decompose and set up a new relation for each partial key with its dependent attribute(s). Make sure to keep a relation with the original primary key and any attributes that are fully functionally dependent on it.
<b>Third (3NF)</b>	Relation should not have a nonkey attribute functionally determined by another nonkey attribute (or by a set of nonkey attributes). That is, there should be no transitive dependency of a nonkey attribute on the primary key.	Decompose and set up a relation that includes the nonkey attribute(s) that functionally determine(s) other nonkey attribute(s).

# General Normal Form Definitions (For Multiple Keys)

- The above definitions consider the primary key only
- The following more general definitions take into account relations with multiple candidate keys
- A relation schema  $R$  is in **second normal form (2NF)** if every non-prime attribute  $A$  in  $R$  is fully functionally dependent on *every* key of  $R$

# General Normal Form Definitions

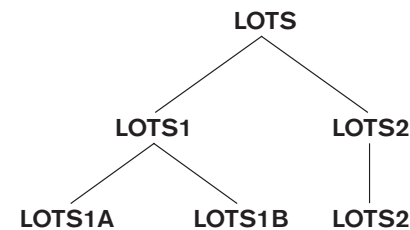
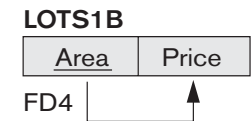
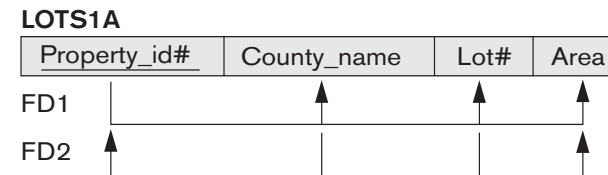
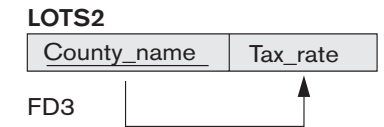
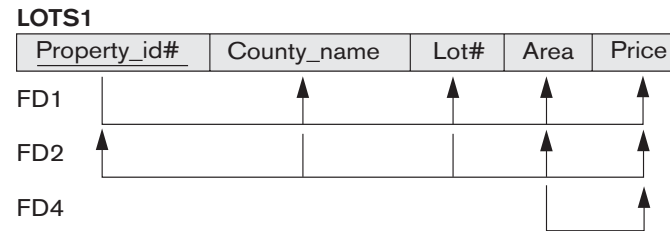
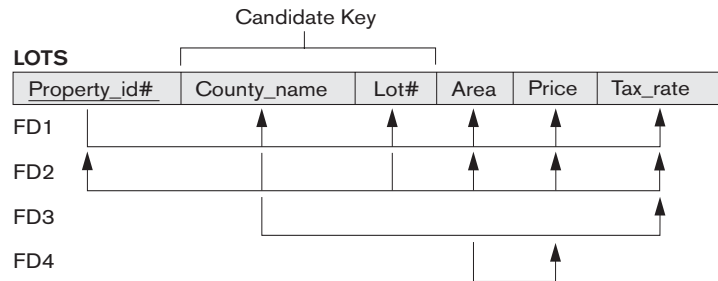
## ➤ Definition:

- **Superkey** of relation schema  $R$  - a set of attributes  $S$  of  $R$  that contains a key of  $R$
  - A relation schema  $R$  is in **third normal form (3NF)** if whenever a FD  $X \rightarrow A$  holds in  $R$ , then either:
    - (a)  $X$  is a superkey of  $R$ , or
    - (b)  $A$  is a prime attribute of  $R$
- if every nonprime attribute of  $R$  meets both of the following conditions:  
It is fully functionally dependent ON EVERY KEY of  $R$ .  
It is nontransitively dependent ON EVERY KEY of  $R$ .

➤ NOTE: Boyce-Codd normal form disallows condition (b) above

# Example

## Successive Normalization of LOTS into 2NF and 3NF



1NF

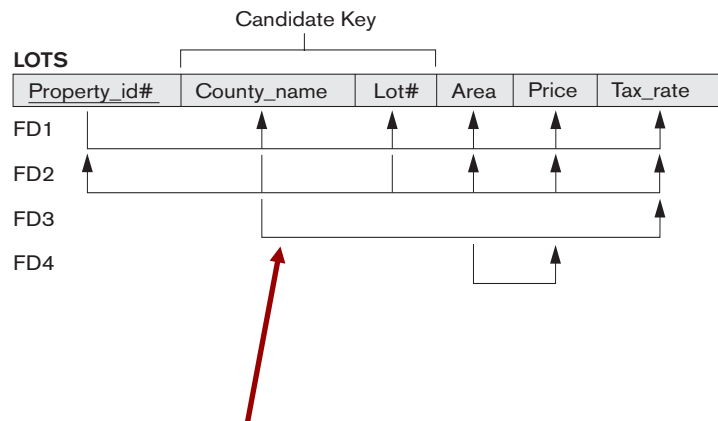
2NF

3NF

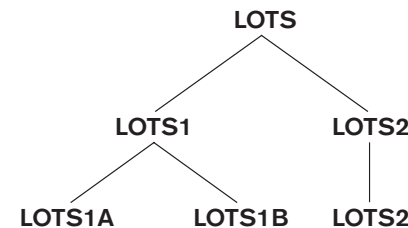
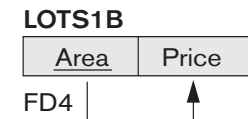
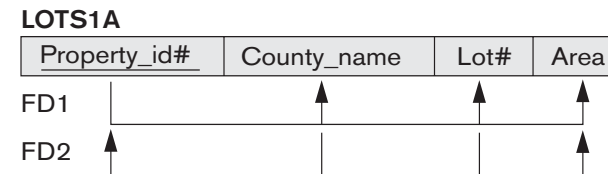
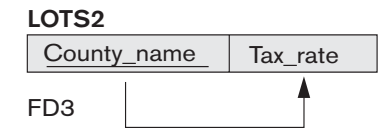
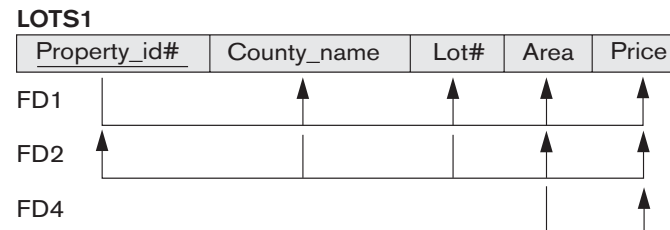


# Example

## Successive Normalization of LOTS into 2NF and 3NF



violates the general definition of 2NF  
 because Tax\_rate is **partially dependent** on  
 the candidate key {County\_name, Lot#}



1NF

2NF

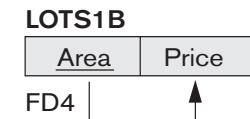
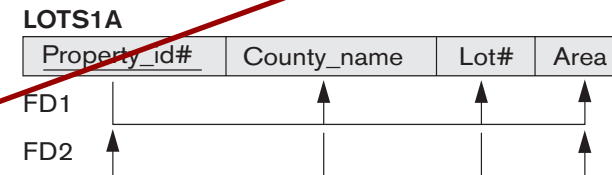
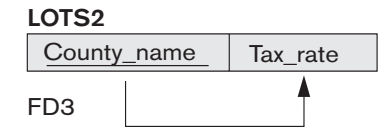
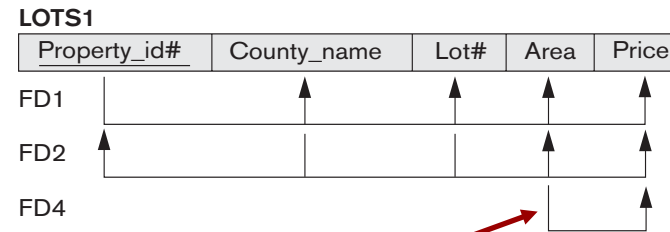
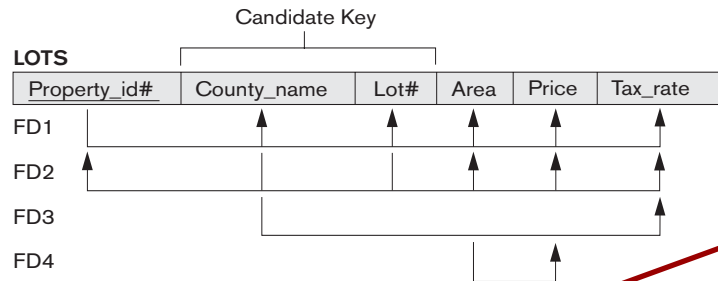
3NF



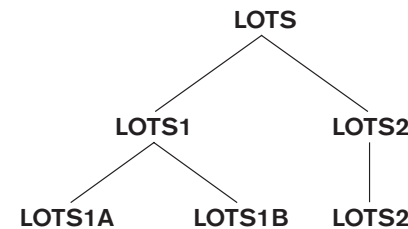


# Example

## Successive Normalization of LOTS into 2NF and 3NF



FD4 in LOTS1 violates 3NF because Area is not a superkey and Price is not a prime attribute in LOTS1.



1NF

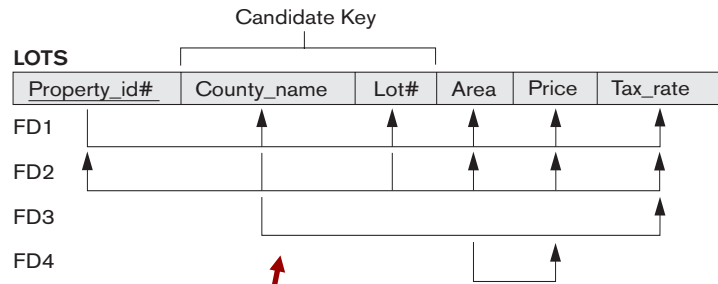
2NF

3NF

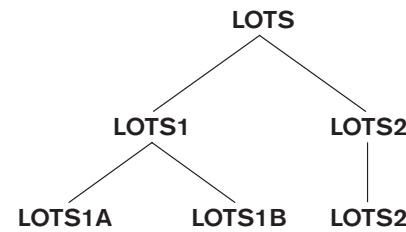
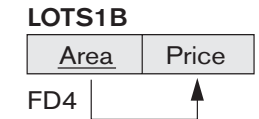
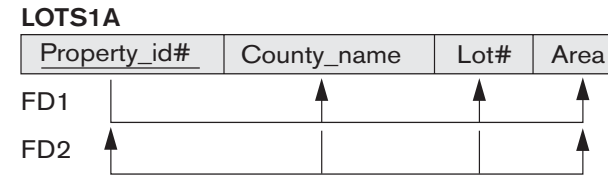
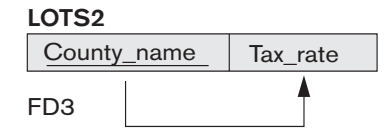
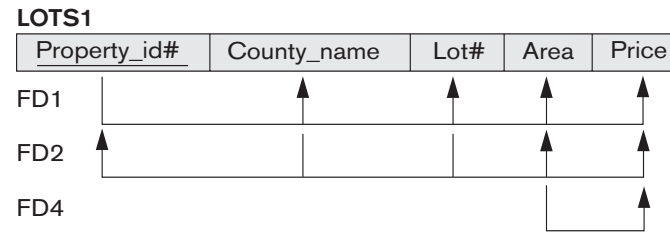


# Example

## Successive Normalization of LOTS into 2NF and 3NF



The transitive and partial dependencies that violate 3NF can be removed *in any order*



1NF

2NF

3NF



# BCNF (Boyce-Codd Normal Form)

- A relation schema  $R$  is in **Boyce-Codd Normal Form (BCNF)** if whenever an **FD  $X \rightarrow A$**  holds in  $R$ , then  **$X$  is a superkey** of  $R$
- Each normal form is strictly stronger than the previous one
  - Every 2NF relation is in 1NF
  - Every 3NF relation is in 2NF
  - Every BCNF relation is in 3NF
- There exist relations that are in 3NF but not in BCNF
- The goal is to have each relation in BCNF (or 3NF)

# Example

(a)

LOTS1A

<u>Property_id#</u>	County_name	Lot#	Area
---------------------	-------------	------	------



BCNF Normalization

LOTS1AX

<u>Property_id#</u>	Area	Lot#
---------------------	------	------

LOTS1AY

<u>Area</u>	County_name
-------------	-------------

Assume

- **DeKalb County** are only 0.5, 0.6, 0.7, 0.8, 0.9, and 1.0 acres
- **Fulton County** are restricted to 1.1, 1.2, ..., 1.9, and 2.0 acres

Satisfies 3NF since County\_name is prime attribute

(b)

R

<u>A</u>	<u>B</u>	C
----------	----------	---



**Figure 10.12**

Boyce-Codd normal form. (a) BCNF normalization of LOTS1A with the functional dependency FD2 being lost in the decomposition. (b) A schematic relation with FDs; it is in 3NF, but not in BCNF.

# Example

(a)

LOTS1A

<u>Property_id#</u>	County_name	Lot#	Area
---------------------	-------------	------	------



BCNF Normalization

LOTS1AX

<u>Property_id#</u>	Area	Lot#
---------------------	------	------

LOTS1AY

<u>Area</u>	County_name
-------------	-------------

Assume

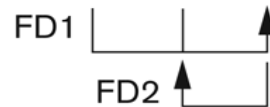
- **DeKalb County** are only 0.5, 0.6, 0.7, 0.8, 0.9, and 1.0 acres
- **Fulton County** are restricted to 1.1, 1.2, ..., 1.9, and 2.0 acres

if  $X \rightarrow A$  holds in a relation schema  $R$  with  $X$  not being a superkey and  $A$  being a prime attribute,  $R$  will be in 3NF but not in BCNF

(b)

$R$

<u>A</u>	<u>B</u>	C
----------	----------	---



**Figure 10.12**

Boyce-Codd normal form. (a) BCNF normalization of LOTS1A with the functional dependency FD2 being lost in the decomposition. (b) A schematic relation with FDs; it is in 3NF, but not in BCNF.

# Example

A relation TEACH that is in 3NF but not in BCNF

TEACH

<u>Student</u>	<u>Course</u>	Instructor
Narayan	Database	Mark
Smith	Database	Navathe
Smith	Operating Systems	Ammar
Smith	Theory	Schulman
Wallace	Database	Mark
Wallace	Operating Systems	Ahamad
Wong	Database	Omiecinski
Zelaya	Database	Navathe
Narayan	Operating Systems	Ammar

FD2

FD1

A relation **NOT** in BCNF should be decomposed so as to meet this property, while possibly forgoing the preservation of all functional dependencies in the decomposed relations

# Achieving the BCNF by Decomposition

- Three possible decompositions for relation TEACH
  - {student, instructor} and {student, course}
  - {course, instructor } and {course, student}
  - {instructor, course } and {instructor, student}
- All three decompositions will lose FD1.
  - We have to settle for sacrificing the functional dependency preservation. But we cannot sacrifice the non-additivity property after decomposition.
- Out of the above three, only the 3rd decomposition will not generate spurious tuples after join (and hence has the non-additivity property).



# Multivalued Dependencies

## Definition:

$X$  multidetermines  $Y$



- A **multivalued dependency (MVD)**  $X \twoheadrightarrow Y$  specified on relation schema  $R$ , where  $X$  and  $Y$  are both subsets of  $R$ , specifies the following constraint on any relation state  $r$  of  $R$ : If two tuples  $t_1$  and  $t_2$  exist in  $r$  such that  $t_1[X] = t_2[X]$ , then two tuples  $t_3$  and  $t_4$  should also exist in  $r$  with the following properties, where we use  $Z$  to denote  $(R - (X \cup Y))$ :

- $t_3[X] = t_4[X] = t_1[X] = t_2[X]$ .
- $t_3[Y] = t_1[Y]$  and  $t_4[Y] = t_2[Y]$ .
- $t_3[Z] = t_2[Z]$  and  $t_4[Z] = t_1[Z]$ .

- An MVD  $X \twoheadrightarrow Y$  in  $R$  is called a **trivial MVD** if (a)  $Y$  is a subset of  $X$ , or (b)  $X \cup Y = R$ .





# Multivalued Dependencies

$Ename \twoheadrightarrow Pname$

$Ename \twoheadrightarrow Dname$

EMP

<u>Ename</u>	<u>Pname</u>	<u>Dname</u>
Smith	X	John
Smith	Y	Anna
Smith	X	Anna
Smith	Y	John
Brown	W	Jim
Brown	X	Jim
Brown	Y	Jim
Brown	Z	Jim
Brown	W	Joan
Brown	X	Joan
Brown	Y	Joan
Brown	Z	Joan
Brown	W	Bob
Brown	X	Bob
Brown	Y	Bob
Brown	Z	Bob



# Multivalued Dependencies

## ➤ Inference Rules for Functional and Multivalued Dependencies:

- IR1 (reflexive rule for FDs): If  $X \supseteq Y$ , then  $X \rightarrow Y$ .
- IR2 (augmentation rule for FDs):  $\{X \rightarrow Y\} \mid = XZ \rightarrow YZ$ .
- IR3 (transitive rule for FDs):  $\{X \rightarrow Y, Y \rightarrow Z\} \mid = X \rightarrow Z$ .
- IR4 (complementation rule for MVDs):  $\{X \twoheadrightarrow Y\} \mid = X \twoheadrightarrow (R - (X \cup Y))$ .
- IR5 (augmentation rule for MVDs): If  $X \twoheadrightarrow Y$  and  $W \supseteq Z$  then  $WX \twoheadrightarrow YZ$ .
- IR6 (transitive rule for MVDs):  $\{X \twoheadrightarrow Y, Y \twoheadrightarrow Z\} \mid = X \twoheadrightarrow (Z - Y)$ .
- IR7 (replication rule for FD to MVD):  $\{X \rightarrow Y\} \mid = X \twoheadrightarrow Y$ .
- IR8 (coalescence rule for FDs and MVDs): If  $X \twoheadrightarrow Y$  and there exists  $W$  with the properties that
  - (a)  $W \cap Y$  is empty, (b)  $W \rightarrow Z$ , and (c)  $Y \supseteq Z$ , then  $X \rightarrow Z$ .

Armstrong's rules

MVD-related

Relate FD and MVD



# Fourth Normal Form 4NF

## Definition:

- A relation schema  $R$  is in **4NF** with respect to a set of dependencies  $F$  (that includes functional dependencies and multivalued dependencies) if, for every *nontrivial* multivalued dependency  $X \twoheadrightarrow Y$  in  $F^+$ ,  $X$  is a superkey for  $R$ .
- Reminder:  $F^+$  is the (complete) set of all dependencies (functional or multivalued) that will hold in every relation state  $r$  of  $R$  that satisfies  $F$ . It is the **closure** of  $F$ .

# Example

**Figure 16.4**

Decomposing a relation state of EMP that is not in 4NF. (a) EMP relation with additional tuples. (b) Two corresponding 4NF relations EMP\_PROJECTS and EMP\_DEPENDENTS.

**(a) EMP**

<u>Ename</u>	<u>Pname</u>	<u>Dname</u>
Smith	X	John
Smith	Y	Anna
Smith	X	Anna
Smith	Y	John
Brown	W	Jim
Brown	X	Jim
Brown	Y	Jim
Brown	Z	Jim
Brown	W	Joan
Brown	X	Joan
Brown	Y	Joan
Brown	Z	Joan
Brown	W	Bob
Brown	X	Bob
Brown	Y	Bob
Brown	Z	Bob

**(b) EMP\_PROJECTS**

<u>Ename</u>	<u>Pname</u>
Smith	X
Smith	Y
Brown	W
Brown	X
Brown	Y
Brown	Z

**EMP\_DEPENDENTS**

<u>Ename</u>	<u>Dname</u>
Smith	Anna
Smith	John
Brown	Jim
Brown	Joan
Brown	Bob

Ename  $\twoheadrightarrow$  Pname

Ename  $\twoheadrightarrow$  Dname

# Lossless (Non-additive) Join Decomposition into 4NF Relations

➤ Whenever we decompose a relation schema  $R$  into  $R_1 = (X \cup Y)$  and  $R_2 = (R - Y)$  based on an MVD  $X \twoheadrightarrow Y$  that holds in  $R$ , the decomposition has the nonadditive join property

## ➤ PROPERTY LJ1'

➤ The relation schemas  $R_1$  and  $R_2$  form a lossless (non-additive) join decomposition of  $R$  with respect to a set  $F$  of functional *and* multivalued dependencies if and only if :

➤  $(R_1 \cap R_2) \twoheadrightarrow (R_1 - R_2)$

➤ **or** by symmetry, if and only if:

➤  $(R_1 \cap R_2) \twoheadrightarrow (R_2 - R_1).$



# Lossless (Non-additive) Join Decomposition into 4NF Relations

➤ Whenever we decompose a relation schema  $R$  into  $R_1 = (X \cup Y)$  and  $R_2 = (R - Y)$  based on an MVD  $X \twoheadrightarrow Y$  that holds in  $R$ , the decomposition has the nonadditive join property

## ➤ PROPERTY LJ1'

➤ The relation schemas  $R_1$  and  $R_2$  form a lossless (non-additive) join decomposition of  $R$  with respect to a set  $F$  of functional *and* multivalued dependencies if and only if :

➤  $(R_1 \cap R_2) \twoheadrightarrow (R_1 - R_2)$

➤ or by symmetry, if and only if:

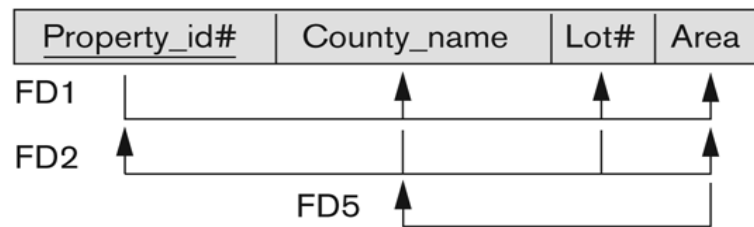
➤  $(R_1 \cap R_2) \twoheadrightarrow (R_2 - R_1).$

Decomposed TECH relation into  
{instructor, course} and {instructor, student}

# Example

(a)

LOTS1A



BCNF Normalization

LOTS1AX



LOTS1AY

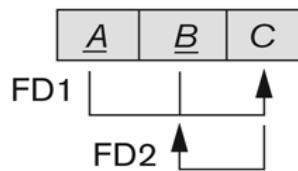


- DeKalb County are only 0.5, 0.6, 0.7, 0.8, 0.9, and 1.0 acres
- Fulton County are restricted to 1.1, 1.2, ..., 1.9, and 2.0 acres

$$(R_1 \cap R_2) \twoheadrightarrow (R_2 - R_1).$$

(b)

R



**Figure 10.12**

Boyce-Codd normal form. (a) BCNF normalization of LOTS1A with the functional dependency FD2 being lost in the decomposition. (b) A schematic relation with FDs; it is in 3NF, but not in BCNF.



# Multivalued Dependencies and 4NF

## Algorithm 11.5: Relational decomposition into 4NF relations with non-additive join property

**Input:** A universal relation  $R$  and a set of functional and multivalued dependencies  $F$ .

1. Set  $D := \{R\}$ ;
2. While there is a relation schema  $Q$  in  $D$  that is not in 4NF do
  - { choose a relation schema  $Q$  in  $D$  that is not in 4NF;
  - find a nontrivial MVD  $X \twoheadrightarrow Y$  in  $Q$  that violates 4NF;
  - replace  $Q$  in  $D$  by two relation schemas  $(Q - Y)$  and  $(X \cup Y)$ ;
  - };



# Join Dependencies

## Definition:

- A **join dependency (JD)**, denoted by  $JD(R_1, R_2, \dots, R_n)$ , specified on relation schema  $R$ , specifies a constraint on the states  $r$  of  $R$ .
- The constraint states that every legal state  $r$  of  $R$  should have **a non-additive join decomposition** into  $R_1, R_2, \dots, R_n$ ; that is, for every such  $r$  we have

$$*(\pi_{R_1}(r), \pi_{R_2}(r), \dots, \pi_{R_n}(r)) = r$$

**Note:** an MVD is a special case of a JD where  $n = 2$ .

- A join dependency  $JD(R_1, R_2, \dots, R_n)$ , specified on relation schema  $R$ , is a **trivial JD** if one of the relation schemas  $R_i$  in  $JD(R_1, R_2, \dots, R_n)$  is equal to  $R$ .

# Fifth Normal Form 5NF

## Definition:

- A relation schema  $R$  is in **fifth normal form (5NF)** (or **Project-Join Normal Form (PJNF)**) with respect to a set  $F$  of functional, multivalued, and join dependencies if,
  - for every nontrivial join dependency  $JD(R_1, R_2, \dots, R_n)$  in  $F^+$  (that is, implied by  $F$ ), every  $R_i$  is a superkey of  $R$ .

# Example

(c) The relation SUPPLY with no MVDs is in 4NF, but not in 5NF if it has the JD(R1, R2, R3)

(d) Decomposing the relation SUPPLY into the 5NF relations R1, R2 and R3.

No nonadditive join decomposition of  $R$  into *two* relation schemas, but there may be a nonadditive join decomposition into *more than two* relation schemas

(c) **SUPPLY**

SNAME	PARTNAME	PROJNAME
Smith	Bolt	ProjX
Smith	Nut	ProjY
Adamsky	Bolt	ProjY
Walton	Nut	ProjZ
Adamsky	Nail	ProjX
Adamsky	Bolt	ProjX
Smith	Bolt	ProjY

(d) **R1**

SNAME	PARTNAME
Smith	Bolt
Smith	Nut
Adamsky	Bolt
Walton	Nut
Adamsky	Nail

**R2**

SNAME	PROJNAME
Smith	ProjX
Smith	ProjY
Adamsky	ProjY
Walton	ProjZ
Adamsky	ProjX

**R3**

PARTNAME	PROJNAME
Bolt	ProjX
Nut	ProjY
Bolt	ProjY
Nut	ProjZ
Nail	ProjX

# Example

- (c) The relation SUPPLY with no MVDs is in 4NF, but not in 5NF if it has the JD(R1, R2, R3)  
(d) Decomposing the relation SUPPLY into the 5NF relations R1, R2 and R3.

(c) **SUPPLY**

SNAME	PARTNAME	PROJNAME
Smith	Bolt	ProjX
Smith	Nut	ProjY
Adamsky	Bolt	ProjY
Walton	Nut	ProjZ
Adamsky	Nail	ProjX
Adamsky	Bolt	ProjX
Smith	Bolt	ProjY

Multiway decomposition into 5NF

(d) **R1**

SNAME	PARTNAME
Smith	Bolt
Smith	Nut
Adamsky	Bolt
Walton	Nut
Adamsky	Nail

**R2**

SNAME	PROJNAME
Smith	ProjX
Smith	ProjY
Adamsky	ProjY
Walton	ProjZ
Adamsky	ProjX

**R3**

PARTNAME	PROJNAME
Bolt	ProjX
Nut	ProjY
Bolt	ProjY
Nut	ProjZ
Nail	ProjX

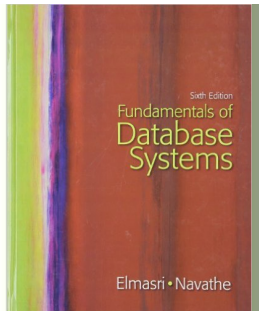
# Short summary

- Informal Design Guidelines for Relational Databases
- Functional Dependencies (FDs)
- Normal Forms Based on Primary Keys
- General Normal Form Definitions (For Multiple Keys)
- BCNF (Boyce-Codd Normal Form)
- Multivalued Dependencies
- 4NF, 5NF

# Possible exam questions

- Identify FDs by applying the inference rules
- Find the minimal cover for a given set of FDs
- For a given table, keys, and set of FDs check if the relation schema is in a required normal form (with explanation)
- Normalize a given relation schema/table

# Bibliography



➤ **Chapter 15**

➤ **Chapter 16**



➤ **Chapter 3**

