

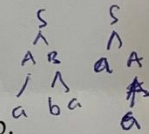
KWAME NKRUMAH UNIVERSITY OF SCIENCE AND TECHNOLOGY, KUMASI
MIDSEMESTER EXAMINATION, 2018/2019
BSc (COMPUTER SCIENCE)
FOURTH YEAR

CSM 484 INTRODUCTION TO COMPILERS **DURATION: 1 HOUR**

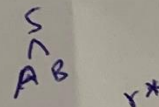
1. a) Find the phrase structure grammar to generate the set $\{0^m 1^n \mid m, n \text{ are nonnegative integers}\}$. [5 Marks]
- b) Differentiate between ^{lexer}lexical analysis and ^{parser}syntactic analysis/parsing. [5 Marks]
- c) Let $V = \{S, A, B, a, b\}$ and $T = \{a, b\}$. Find the language generated by the grammar

$G = \{V, T, S, P\}$ when the set P of productions consists of: [5 Marks]

- i) $S \rightarrow AB, A \rightarrow ab, B \rightarrow bb.$
- ii) $S \rightarrow AB, S \rightarrow aA, A \rightarrow a, B \rightarrow ba.$
- iii) $S \rightarrow AB, S \rightarrow AA, A \rightarrow aB, A \rightarrow ab, B \rightarrow b.$
- iv) $S \rightarrow AA, S \rightarrow B, A \rightarrow aaA, A \rightarrow aa, B \rightarrow bB, B \rightarrow b.$
- v) $S \rightarrow AB, A \rightarrow aAb, B \rightarrow bBa, A \rightarrow \lambda$



lexical analysis is a compiler



2. a) Prove that $(r^*)^* = r^*$. [2 Marks]
- b) Show that the following regular expressions are equivalent: [5 Marks]
- i) $a(a+b)^*$
- ii) $a((a+\lambda)(b+\lambda))^*$
- c) Draw state diagrams for 2(b) (i) and (ii). [6 Marks]
- d) Differentiate between DFA and NFA. [2 Marks]

$(aa+ab)^*$

unique input from one state another

J. K. PANFORD

COMPUTER SCIENCE IV

CSM 484 INTRODUCTION TO COMPILERS

Time Allowed: 1 Hours

Instruction: Answer all questions

- Find a deterministic finite-state automaton (state diagram) that recognizes each of the following sets.
 a) $\{0^*\}$ b) $\{1,00^*\}$ c) $\{1^n \mid n = 3,4,5,\dots\}$
- Fully parenthesize each of the following expressions and show the partial relationships between the sub-expressions.
 a) $k = \sim b - s \uparrow c * g + f \uparrow q * v$
 b) $w = \sim q \uparrow m - p / k \uparrow c - v * a$
- Give the step-by-step generation of machine code (in assembly language) of each of the following algebraic/infix strings using 1-address instruction format.
 a) $c = k + g \uparrow (-(m / q - 2)) + f * v \uparrow w$
 b) $w = \sim (\sim q \uparrow m) + b / c - t * s \uparrow a$

END OF SECOND SEMESTER EXAMINATION 2013-2014

BSc. COMPUTER SCIENCE IV

CSM 484 INTRODUCTION TO COMPILERS

April 2014

[100 Marks]

Time Allowed: 2½ Hours

Instructions: Answer ALL FOUR questions in the answer booklet provided. Each question carries 25marks!

1. a) Using a suitable diagram explain the phases of the compilation process.
- b) Describe the types of grammars and give one example under each.
- c) Give 2 advantages of ^{intermediate} immediate representation (IR) of code.
- d) Let G_1 and G_2 be context-free grammars, generating the languages $L(G_1)$ and $L(G_2)$ respectively. Show that there is a context-free grammar generating each of the following sets.
- i) $L(G_1) \cup L(G_2)$ ii) $L(G_1)L(G_2)$ iii) $L(G_1)^*$
2. a) Let V be an alphabet, and let A and B be subsets of V^* with $A \subseteq B$. Show that $A^* \subseteq B^*$.
- b) Determine whether the string 11101 is in each of the following regular sets.
- i) $\{11\}^*\{01\}^*$ ii) $\{111, 000\}\{00, 01\}$ iii) $\{11\}\{1\}^*\{01\}$
- c) Let V be an alphabet, and let A and B be subsets of V^* , show that:
- $$|AB| \leq |A||B|.$$
- d) A context-free grammar is ambiguous if there is a word in $L(G)$ with two derivations that produce different derivation trees, considered as ordered, rooted trees. Show that

the grammar $G = \{V, T, S, P\}$ with $V = \{0, S\}$, $T = \{0\}$, starting state S , and Productions $P = \{S \rightarrow 0S, S \rightarrow S0, \text{ and } S \rightarrow 0\}$ is ambiguous by constructing two different derivation trees for 0^3 .

3. a) Give the step-by-step generation of machine code of the following algebraic/infix strings.

i) $m = -c \uparrow b * q + a + b/r$
 ii) $p = s * b \uparrow c - w/r * d + e$

- b) Give the step-by-step generation of the algebraic string of each of the following Reverse Polish strings, if possible.

i) $x y g \mid a b c * e / + f - e / * + = \Rightarrow$
 ii) $q w m \uparrow a / g s * + \Rightarrow$

$$\begin{aligned} \uparrow &= 4 \\ x/ &= 3 \\ \sim &= 2 \\ + - &= 1 \\ = &= 0 \\ (&= 10 \end{aligned}$$

- c) List 2 advantages of a byte-code over an object code.

4. a) Fully parenthesize each of the following using the PARENTHEZING ALGORITHM step-by-step.

i) $m = -c \uparrow b * q + a + b/r$
 ii) $p = s * b \uparrow c - w/r * d + e$

- b) Draw syntax diagrams for each of the following:

- i) *For* statement
 ii) *If* statement
 iii) *While* statement
 iv) *Try/catch* statement

- c) Explain how a deterministic FSA can be transformed into non-deterministic FSA.

Handwritten notes:
 For statement: $\text{For } i = 1 \text{ To } n \text{ Do } \dots \text{End For}$
 If statement: $\text{If } \text{condition} \text{ Then } \dots \text{Else } \dots \text{End If}$
 While statement: $\text{While } \text{condition} \text{ Do } \dots \text{End While}$
 Try/catch statement: $\text{Try } \dots \text{Catch } \dots \text{End Try}$

Instructions: Answer ALL FOUR questions in the answer booklet provided. Each question carries 25 marks.

1. a) Differentiate between each of the following: [10 Marks - 2½ marks each]

- i) Lexer and Parser
- ii) Symbol table and Lexicons
- iii) Deterministic and Nondeterministic Finite State Automata
- iv) Top-down and Bottom-up parsing

b) i) Construct a phrase-structure grammar that generates all signed decimal numbers, consisting of a sign, either + or -; a nonnegative integer; and a decimal fraction that is either the empty string or a decimal point followed by a positive integer, where initial zeros in an integer are allowed. [5 Marks]

ii) Give the Backus-Naur form (BNF) of the grammar in question 1b(i). [5 Marks]

iii) Construct a derivation tree (syntactic parse tree) for -31.4 in the grammar in 1b(i) using:

α) top-down parsing [2½ Marks]

β) bottom-up parsing [2½ Marks]

2. a) Let V be an alphabet, and let A and B be subsets of V^* with $A \subseteq B$. Show that $A^* \subseteq B^*$. [5 Marks]

b) Determine whether the string 11101 is in each of the following (regular) sets. [6 Marks - 2 marks each]

- i) $\{0, 1\}^*$
- ii) $\{1\}^* \{0\}^* \{1\}^*$
- iii) $\{111\}^* \{0\}^* \{1\}$

c) Find a deterministic finite state automaton (state diagram) that recognizes each of the following sets. [6 Marks - 2 marks each]

- i) $\{0\}$
- ii) $\{1, 00\}$
- iii) $\{1^n \mid n = 2, 3, 4, \dots\}$

d) A context-free grammar is ambiguous if there is a word in $L(G)$ with two derivations that produce different derivation trees, considered as ordered, rooted trees. Show that the grammar $G = (V, T, S, P)$ with $V = \{0, S\}$, $T = \{0\}$, starting state S , and production $P = \{S \rightarrow 0S, S \rightarrow S0, \text{ and } S \rightarrow 0\}$ is ambiguous by constructing two different derivation trees.

a) Using the parenthesizing algorithm, fully parenthesize each of the following, and show the spatial relationship between the expression and the subexpressions:

i) $w = -b \uparrow c + d - f / (-m \times k) \uparrow -c$ [6 Marks]

ii) $-h + w / s - k \uparrow c - t \times d \uparrow m$ [5 Marks]

b) Using 1-address instruction format convert each of the following algebraic strings into machine (code in assembly language).

i) $w = ((-s \uparrow d) / c) \times b - ((-d \uparrow -m) + 2)$ [7 Marks]

ii) $d - k / h + (-t \uparrow b) \uparrow (d / e \times f) - k$ [7 Marks]

4. a) Convert each of the following infix strings into Reverse Polish strings: [10 Marks – 5 marks each]

i) $p = -g \uparrow c + r - f / (-m \times k) \uparrow -c$

ii) $w - k / h + (-t \uparrow r) \uparrow (d / e \times s) - k$

b) Draw a syntax diagram, in C/C++ or Java, for each of the following:

i) statement [4 Marks]

ii) for statement [2 Marks]

iii) while statement [2 Marks]

iv) try/catch statement [2 Marks]

c) Suppose that A and B are finite subsets of V^* , where V is an alphabet. Is it necessary true that $|AB| = |BA|$? Explain. [5 Marks]

$$A = \{a\} \quad B = \{b\}$$

$$AB = \{ab\}$$

$$BA = \{ba\}$$

CSM 484 Introduction to Compilers

April, 2011

[100 Marks]

Time Allowed: 3 Hours

Instruction: Answer ALL questions in the answer booklet provided. All questions carry equal marks.

1. a) i. Differentiate between TOP-DOWN and BOTTOM-UP parsing. [1 Marks]
- ii. List the phases of the compilation process, and briefly explain the phases. [4 Marks]

- b) Give the BOTTOM-UP parsing, if possible, of the following strings using the syntactic definitions in APPENDIX A. [20 Marks – 5 Marks each]

i. $QZ = W + (LB - KT) / DIX + SAM$

ii. $45 \text{ IF } U / S - DN + RAT .GT. 47.5 * Q \text{ THEN } 80$

iii. $AZ \uparrow (A + CD / BAT) + ELS * SLE$

iv. $ABC + EF * (CAT + KIJ) / 50.75$

2. a) Find a deterministic finite-state automaton (state diagram) that recognizes each of the following. [9 Marks – 3 Marks each]

$\alpha) \{0\}$ $\beta) \{1,00\}$ $\gamma) \{1^n \mid n = 2,3,4,\dots\}$

- b) Draw a detailed syntax diagram in Java for each of the following: [12 Marks – 3 Marks each]

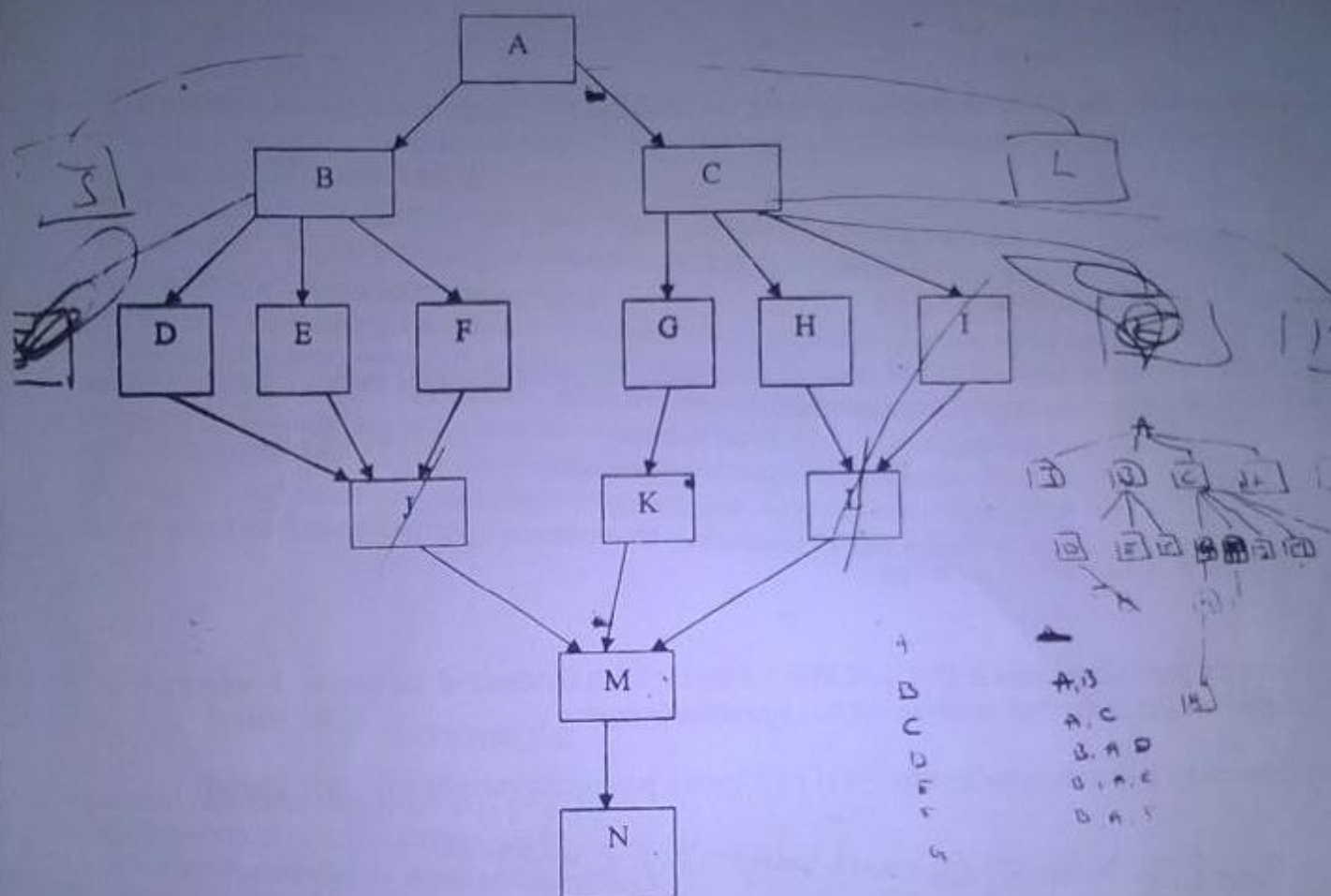
i) *try/catch* statement

ii) *if* statement

iii) *for* statement

iv) *method* declaration

- c) Optimize the following blocks of code using the *dominator tree* algorithm. A, B, C, ..., N are statement blocks. [4 Marks]



3. a) Determine whether the string 11101 is in each of the following sets. [5 Marks]

i) $\{0, 1\}^*$

ii) $\{1\}^* \{0\}^* \{1\}^*$

iii) $\{11\}^* \{01\}^*$

iv) $\{11\}^* \{1\}^* \{01\}$

v) $\{111\}^* \{0\}^* \{1\}$

- b) Give the step-by-step generation of REVERSE POLISH STRING of each of the following algebraic strings: [10 Marks – 5 Marks each]

i. $q = a + b / c + d * e - g \uparrow r$

ii. $w = -z \uparrow b * c + d - r - g$

- c) Give the step-by-step generation of the algebraic string of each of the following Reverse Polish strings

if possible:

[10 Marks - 5 Marks each]

- i. $x y g + a b c * e / + f - e / + =$
- ii. $e f c \uparrow a + d r / + *$

4. a) Fully parenthesize the following strings using the PARENTHEZING ALGORITHM step-by-step, and show the spatial relationship between the expression and the sub-expressions:

[10 Marks - 5 Marks each]

- i. $n = -q \uparrow r * s + a + b / g$
- ii. $p = s + b * c + w / r * d + e$

$$p = (s + (b * c) + (w / r) * (d + e))$$

b) Give the step-by-step generation of machine code of the following algebraic strings using the rules in APPENDIX B and an appropriate algorithm:

[10 Marks - 5 Marks each]

- i. $w = a * b * c + z / y \uparrow t$
- ii. $d = -q \uparrow v + r * s \uparrow a / b - m$

c) i) Give the production rules in BNF or EBNF for the set of all fractions of the form a / b , where a is a signed integer in decimal notation and b is a positive integer. [2½ Marks]

ii) Construct a syntactic parse tree for $+311 / 17$ for the production rules in c(i). [2½ Marks]

$$\langle \text{fraction} \rangle ::= \langle \text{signed integer} \rangle / \langle \text{integer} \rangle$$

$$\langle \text{signed integer} \rangle ::= \langle \text{sign} \rangle \langle \text{integer} \rangle$$

$$\langle \text{sign} \rangle ::= + | -$$

$$\langle \text{integer} \rangle ::= \langle \text{digits} \rangle | \langle \text{digit} \rangle \langle \text{integer} \rangle$$

$$\langle \text{digits} \rangle ::= 0 | 1 | \dots | 9$$

$$+311 / 17$$

APPENDIX A

$\langle \text{null} \rangle ::= b$ ($b \equiv$ blank or space)
 $\langle \text{sign} \rangle ::= + \mid - \mid \langle \text{null} \rangle$
 $\langle \text{prefix operator} \rangle ::= \langle \text{sign} \rangle$
 $\langle \text{alphabetic character} \rangle ::= A \mid B \mid C \mid \dots \mid Z$
 $\langle \text{zero digit} \rangle ::= 0$
 $\langle \text{non zero digit} \rangle ::= 1 \mid 2 \mid 3 \mid \dots \mid 9$
 $\langle \text{digit} \rangle ::= \langle \text{zero digit} \rangle \mid \langle \text{non zero digit} \rangle$
 $\langle \text{replacement sign} \rangle ::= =$
 $\langle \text{relational operator} \rangle ::= .EQ. \mid .GT. \mid .LE. \mid .GE. \mid .NE. \mid .LT.$
 $\langle \text{line number} \rangle ::= \{ \langle \text{digit} \rangle \}^2 \langle \text{non zero digit} \rangle \mid \{ \langle \text{non zero digit} \rangle \}^3 \mid \langle \text{non zero digit} \rangle \{ \langle \text{digit} \rangle \}^2$
 $\langle \text{constant} \rangle ::= \langle \text{sign} \rangle \{ \langle \text{digit} \rangle \} \mid \langle \text{constant} \rangle . \{ \langle \text{digit} \rangle \} \mid \langle \text{constant} \rangle E \{ - \mid + \}^1 \{ \langle \text{digit} \rangle \}^2$
 $\langle \text{variable} \rangle ::= \{ \langle \text{alphabetic character} \rangle \}^4$
 $\langle \text{term} \rangle ::= \langle \text{constant} \rangle \mid \langle \text{variable} \rangle \mid (\langle \text{expression} \rangle) \mid \{ \langle \text{prefix operator} \rangle \}^1 \langle \text{term} \rangle$
 $\langle \text{involution factor} \rangle ::= \langle \text{term} \rangle \mid \langle \text{term} \rangle \uparrow \langle \text{term} \rangle$
 $\langle \text{multiplying factor} \rangle ::= \langle \text{involution factor} \rangle \mid \langle \text{multiplying factor} \rangle \{ * \mid / \}^1 \langle \text{involution factor} \rangle$
 $\langle \text{expression} \rangle ::= \langle \text{multiplying factor} \rangle \mid \langle \text{expression} \rangle \{ + \mid - \}^1 \langle \text{multiplying factor} \rangle$
 $\langle \text{if statement} \rangle ::= \text{IF } \langle \text{expression} \rangle \langle \text{relational operator} \rangle \langle \text{expression} \rangle \text{ THEN } \langle \text{line number} \rangle$
 $\langle \text{arithmetic statement} \rangle ::= \langle \text{variable} \rangle \langle \text{replacement sign} \rangle \langle \text{expression} \rangle$
 $\langle \text{referenced statement} \rangle ::= \langle \text{line number} \rangle \langle \text{if statement} \rangle \mid \langle \text{line number} \rangle \langle \text{arithmetic statement} \rangle$

APPENDIX B

$\langle \text{operator in input string} \rangle ::= + \mid - \mid * \mid / \mid \uparrow$
 $\langle \text{unary operator in input string} \rangle ::= \sim \mid -$
 $\langle \text{replacement operator in input string} \rangle ::= =$
 $\langle \text{temporary storage location} \rangle ::= \{ [\alpha 1 \mid \alpha 2 \mid \alpha 3 \mid \alpha 4 \mid \alpha 5 \mid \alpha 6 \mid \alpha 7 \mid \alpha 8 \mid \alpha 9 \mid \alpha 10] \}^1$
 $\langle \text{operator in generated instruction} \rangle ::= \text{ADD} \mid \text{SUB} \mid \text{MUL} \mid \text{DIV} \mid \text{EXP}$
 $\langle \text{operand} \rangle ::= a \mid b \mid c \mid \dots \mid z$
 $\langle \text{operand1} \rangle ::= \langle \text{operand} \rangle$
 $\langle \text{operand2} \rangle ::= \langle \text{operand} \rangle$

PRODUCTION RULES (ALGEBRAIC STRING TO MACHINE CODE)

- a) $\langle \text{operand1} \rangle \langle \text{operator in input string} \rangle \langle \text{operand2} \rangle$
 $\rightarrow \text{LDA } \langle \text{operand1} \rangle$
 $\quad \langle \text{operator in generated instruction} \rangle \langle \text{operand2} \rangle$
 $\quad \text{STOR } \langle \text{temporary storage location} \rangle$

DEPARTMENT OF COMPUTER SCIENCE
MIDSEMESTER EXAMINATION 2014
CSM 484 INTRODUCTION TO COMPILERS Time Allowed: 45 Minutes

1. a) Find a deterministic FSA that recognizes each of the following sets.

- ii) $\{0\}$ ii) $\{1, 00\}$ iii) $\{1^n \mid n = 2, 3, 4, \dots\}$

b) Let V be an alphabet, and let A and B be subset of V^* with $A \subseteq B$. show that $A^* \subseteq B^*$.

c) Show that the grammar $G = \{V, T, S, P\}$ with $V = \{0, S\}$, $T = \{\emptyset\}$, starting state S , and productions $S \rightarrow \emptyset S$, and $S \rightarrow 0$ is ambiguous by constructing two different derivation or parse trees for 0^3 .

2. a) Fully parenthesize each of the following using the parenthesizing algorithm:

(iii) $k = -b \uparrow m + q * s - w / f$

(i) $t = w \uparrow s - d / q \uparrow - g * b$

b) Convert 2(a) (i) and (ii) into Reverse Polish notation.

c) Write a method in C++ or Java that accepts an input algebraic string and generate a syntactic parse tree.

1. 4
+ 1 3
~ 2
+ - 1
~ 0

