

- For a spacecraft trajectory around the earth,  $r = 10,000$  km when the true anomaly is  $30^\circ$ , and  $r = 30,000$  km when the true anomaly is  $105^\circ$ . Calculate the eccentricity. [  $\approx 1.22$  ]
- At a given instant, a spacecraft has the position and velocity vectors  $r_0 = 7000 \hat{i}$  ( km ) and  $v_0 = 7 \hat{i} + 7 \hat{j}$  ( km/s ) relative to an earth-centered non-rotating frame.  $\{\mu = 3,98,600 \text{ km}^3/\text{s}^2\}$ 
  - What is the true anomaly of the initial point? [  $\approx 99.208^\circ$  ]
  - What is the position vector after the true anomaly increases by  $90^\circ$ ?  
[  $\approx 43183 \hat{j}$  (km) ]
- For a hyperbolic orbit, find the eccentricity in terms of the radius at periapsis  $r_p$ , the hyperbolic excess speed, and  $\mu$ . [  $e = 1 + r_p v_\infty^2 / \mu$  ]
- Let F be the center of the circle of radius  $2a$ . Consider a point  $F'$  located inside the circle such that the distance  $FF' = 2ae$ , where  $e < 1$ . Join F and  $F'$  to a point Q on the circle. Draw the perpendicular bisector of  $QF'$ , meeting  $QF$  at P. Show that, as the point Q moves around the circle, the point P traces out an ellipse with eccentricity  $e$ , with F and  $F'$  as foci. [Join  $PF'$  then show  $PF+PF'=2a$  ]