

- For a spacecraft trajectory around the earth, $r = 10,000$ km when the true anomaly is 30° , and $r = 30,000$ km when the true anomaly is 105° . Calculate the eccentricity. [≈ 1.22]
- At a given instant, a spacecraft has the position and velocity vectors $\mathbf{r}_0 = 7000 \hat{i}$ (km) and $\mathbf{v}_0 = 7 \hat{i} + 7 \hat{j}$ (km/s) relative to an earth-centered non-rotating frame. $\{\mu = 3,98,600 \text{ km}^3/\text{s}^2\}$
 - (a) What is the true anomaly of the initial point? [$\approx 99.208^\circ$]
 - (b) What is the position vector after the true anomaly increases by 90° ? [$\approx 43183 \hat{j}$ (km)]
- For a hyperbolic orbit, find the eccentricity in terms of the radius at periapsis r_p , the hyperbolic excess speed, and μ . [$e = 1 + r_p v_\infty^2/\mu$]
- Let F be the center of the circle of radius $2a$. Consider a point F' located inside the circle such that the distance $FF' = 2ae$, where $e < 1$. Join F and F' to a point Q on the circle. Draw the perpendicular bisector of QF' , meeting QF at P . Show that, as the point Q moves around the circle, the point P traces out an ellipse with eccentricity e , with F and F' as foci. [Join PF' then show $PF+PF'=2a$]