



**Mansoura University**  
**Faculty of Computers and Information**  
**Department of Information System**  
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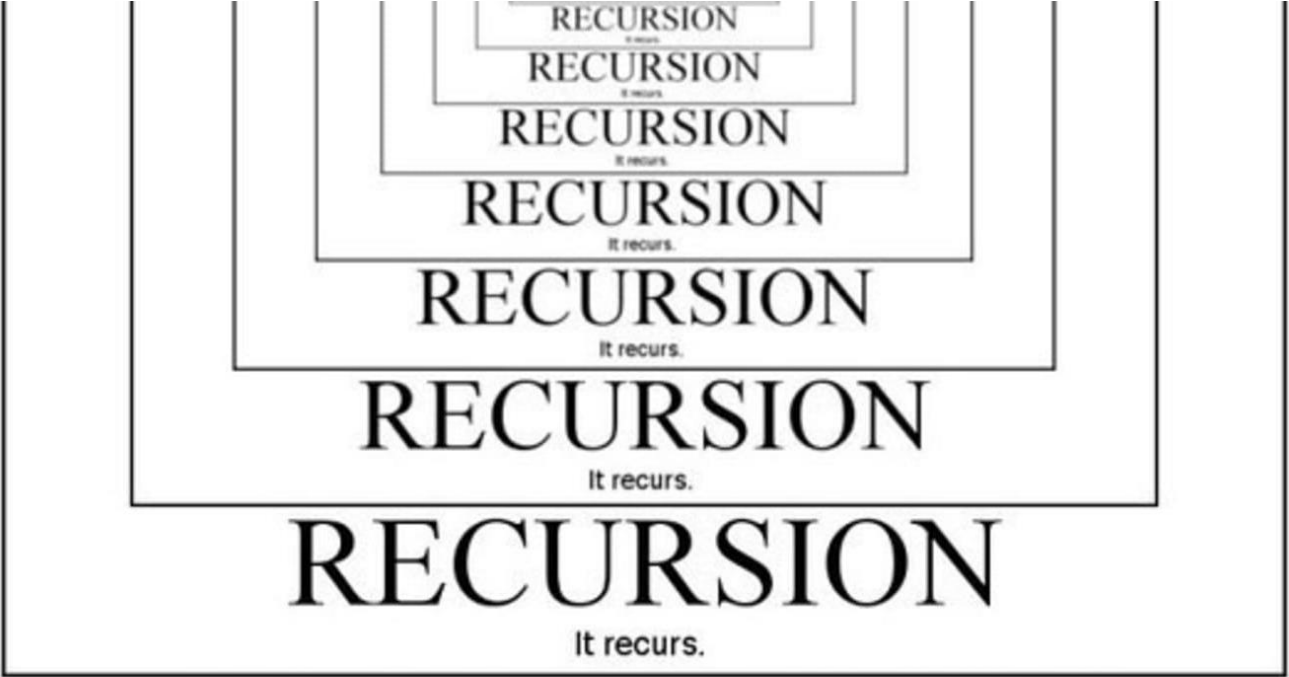


**Course: Data Structure.**

**Grade: Second year**

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# RECURSION



# Recursion

## What is Recursion?

- ❖ Recursion allows a function to call itself. Fixed steps of code get executed again and again for new values.
- ❖ We also must set criteria for deciding when the recursive call ends.

## When to Use Recursion?

- ❖ Recursion is a method of solving problems that involves breaking a problem down into smaller and smaller subproblems until you get to a small enough problem that it can be solved trivially.

# Recursion

## The Three Laws of Recursion:

- ❖ A recursive algorithm must have a **base case**.
- ❖ A recursive algorithm must **change its state** and move toward the base case.
- ❖ A recursive algorithm must call itself, **recursively**.

A **base case** is the **condition** that allows the algorithm to **stop recursing**.

A **change of state** means that some data that the algorithm is using is modified. Usually, the data that represents our problem gets smaller in some way.

We have a problem to solve with a function, but that function solves the problem by calling itself

```
def factorial (n):  
    if n<=1:  
        return 1  
    else:  
        return factorial(n-1)*n
```

```
print(factorial(6))
```

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## FACTORIAL FUNCTION USING RECURSION

```
def binary_search (arr, item):  
    if len(arr)==0:  
        return False  
    else:  
        midpoint=len(arr)//2  
        if arr[midpoint]==item:  
            return True  
        else:  
            if item< arr[midpoint]:  
                return binary_search(arr[:midpoint],item)  
            else:  
                return binary_search(arr[midpoint+1:],item)
```

```
arr=[1,2,6,8,9]  
print(binary_search(arr,4))  
print(binary_search(arr,8))  
print(binary_search(arr,1))
```

False  
True  
True

# RECURSIVE BINARY SEARCH

# BACKTRACKING

## What is Backtracking?

- ❖ Backtracking is a form of recursion. But it involves choosing only option out of any possibilities.
- ❖ In backtracking, if the current solution is not suitable, then we backtrack and try to find other solutions. So, recursion is used.

## When to use Backtracking?

- ❖ Backtracking is used to solve problems that have multiple solutions.

	Recursion	Backtracking
	Recursion does not always need backtracking	Backtracking always uses recursion to solve problems
	A recursive function solves a particular problem by calling a copy of itself and solving smaller subproblems of the original problems.	Backtracking at every step eliminates those choices that cannot give us the solution and proceeds to those choices that have the potential of taking us to the solution.
	Recursion is a part of backtracking itself and it is simpler to write.	Backtracking is comparatively complex to implement.
	Applications of recursion are Tree and Graph Traversal, Towers of Hanoi, Divide and Conquer Algorithms, Merge Sort, Quick Sort, and Binary Search.	Application of Backtracking is N Queen problem, Rat in a Maze problem, Knight's Tour Problem, Sudoku solver, and Graph coloring problems.

## WHAT IS THE DIFFERENCE BETWEEN BACKTRACKING AND RECURSION?



```
def permute (repeat,list1):  
    xy=[]  
    if repeat==1:  
        return list1  
    else:  
        for y in permute(1,list1):  
            for x in permute(repeat-1,list1):  
                xy.append(x+y)  
        return xy
```

```
print(permute(1,['a','b','c','d']))  
print(permute(2,['a','b','c','d']))
```

['a', 'b', 'c', 'd']

['aa', 'ba', 'ca', 'da', 'ab', 'bb', 'cb', 'db', 'ac', 'bc', 'cc', 'dc', 'ad', 'bd', 'cd', 'dd']

# PERMUTE

## EXERCISE

**Q-1:** How many recursive calls are made when computing the sum of the list [2,4,6,8,10]?

A. 6

✗ There are only five numbers on the list, the number of recursive calls will not be greater than the size of the list.

B. 5

✗ The initial call to listsum is not a recursive call.

C. 4

✓ the first recursive call passes the list [4,6,8,10], the second [6,8,10] and so on until [10].

D. 3

✗ This would not be enough calls to cover all the numbers on the list

## EXERCISE

**Q-2:** Suppose you are going to write a recursive function to calculate the factorial of a number.  $\text{fact}(n)$  returns  $n * n-1 * n-2 * \dots$ . Where the factorial of zero is defined to be 1. What would be the most appropriate base case?

A.  $n == 0$

✗ Although this would work there are better and slightly more efficient choices. since  $\text{fact}(1)$  and  $\text{fact}(0)$  are the same.

B.  $n == 1$

✗ A good choice, but what happens if you call  $\text{fact}(0)$ ?

C.  $n >= 0$

✗ This basecase would be true for all numbers greater than zero so  $\text{fact}$  of any positive number would be 1.

D.  $n <= 1$

✓ Good, this is the most efficient, and even keeps your program from crashing if you try to compute the factorial of a negative number.