

ECE 340 Homework # 1

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1 Problem 1

Solve 5 section 1.2: Out of the students in a class, 60% are geniuses, 70% love chocolate, and 40% fall into both categories. Determine the probability that a randomly selected student is neither a genius nor a chocolate lover.

Solution:

Let G and C be the events that the chosen student is a genius and a chocolate lover, respectively. We have $P(G) = 0.6$, $P(C) = 0.7$, and $P(G \cap C) = 0.4$. We are interested in $P(G^c \cap C^c)$, which is obtained with the following calculation:

$$P(G^c \cap C^c) = 1 - P(G \cup C) = 1 - (P(G) + P(C) - P(G \cap C)) = 1 - (0.6 + 0.7 - 0.4) = 0.1$$

2 Problem 2

Peter, John and Mary are in a group of 6 students to be seated at random in a row of 6 chairs. Find the probability that Peter, John and Mary will be seated together in consecutive chairs.

Solution:

There are $6! = 720$ ways 6 people can sit in a row.

If the Peter, John and Mary are regarded as a unit, then we can first order the objects B, G1, G2, G3, where B is the unit of the Peter, John and Mary, and G1, G2, G3 are the other 3 people. There are $4!$ ways to do this.

Then the Peter, John and Mary can be ordered in $3!$ ways.

Thus total ways in which Peter, John and Mary can be seated together is $4!3! = 144$.

Probability: $144/720 = 0.2$.