

Sept. 8, 2017

HW02: #14, §1.3 & #33, §1.5

& Problems from class $P(\text{sick} | \text{test}+) = .95$

- 14) We roll two fair 6-sided dice. Each one of the 36 possible outcomes is assumed to be equally likely.

$$a) \frac{\# \text{favorable}}{\# \text{total}} = \frac{6}{36} = \frac{1}{6} \boxed{\approx 16\%}$$

$$b) \text{sum} < 4$$

rolls: $(1,1), (1,2), (2,1), (2,2), (3,1), (1,3)$

$$\frac{2}{6} \text{ are less than } 4 \therefore \frac{1}{3} \boxed{= 33\%}$$

$$c) (6,6), (6,1), (1,6) \quad 11 \text{ outcomes}$$

$$\frac{11}{36} = .305 \boxed{\approx 30.5\%}$$

$$d) \text{Six pairs, 30 options.}$$

$$\frac{10}{30} = \frac{1}{3} \boxed{\approx 33\%}$$

- 33) They could flip the coin twice -
 if you get T-H, go to the opera.
 or if you get H-T, see a movie.
 If you get H-H / T-T, flip again.

$$3) P(\text{Sick}) = .03 = 3\%$$

$$\Rightarrow P(\text{Healthy}) = .97 = 97\%$$

$$* P(\text{Sick} | \text{Test Positive}) = .95$$

* What we want - 95% confidence

$$P(\text{Test Positive} | \text{Sick}) = .98 = 98\%$$

$$P(\text{Test Positive} | \text{Healthy}) = .02 = 2\%$$

$$P(\text{Sick} | \text{Test Positive}) = \frac{P(+|S)P(S)}{P(+|S)P(S) + P(+|H)P(H)}$$

$$\left(.95 = \frac{.98(.03)}{.98(.03) + P(+|H)(.97)} \right) [.98(.03) + P(+|H)(.97)]$$

$$= .9215(P(+|H)) = .00147$$

$$\boxed{P(T|H) = .0016}$$