

# Project 2

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## Setup

```
print("Data structure:")

## [1] "Data structure:"

str(D)

## 'data.frame':    13288 obs. of  1 variable:
## $ X0.4...weight...0.002105263157894737.: chr  "0 12 {'weight': 0.002105263157894737}" "0 18 {'weight': 0.002105263157894737}" ...

print("First few rows:")

## [1] "First few rows:"

head(D)

##      X0.4...weight...0.002105263157894737.
## 1 0 12 {'weight': 0.002105263157894737}
## 2 0 18 {'weight': 0.002105263157894737}
## 3 0 25 {'weight': 0.004210526315789474}
## 4 0 30 {'weight': 0.002105263157894737}
## 5  0 46 {'weight': 0.00631578947368421}
## 6 0 55 {'weight': 0.002105263157894737}

# Load the library
library(igraph)

##
## Attaching package: 'igraph'

## The following objects are masked from 'package:stats':
##
##      decompose, spectrum

## The following object is masked from 'package:base':
##
##      union

library(stringr)

# Format the data
edges_df <- data.frame(
  from = as.numeric(sub("^((\\d+).*)", "\\1", D$X0.4...weight...0.002105263157894737.)),
  to = as.numeric(sub("^((\\d+\\.\\s+(\\d+).*)", "\\1", D$X0.4...weight...0.002105263157894737.)),
  weight = as.numeric(sub(".*'weight':\\s*([0-9.]+).*", "\\1", D$X0.4...weight...0.002105263157894737.))
)
```

```
# Create the graph
g <- graph_from_data_frame(edges_df, directed = TRUE)
```

## Graph Characteristics

### Network Understanding

```
print("Network Order (number of vertices):")

## [1] "Network Order (number of vertices):"
vcount(g)

## [1] 475

# Network size (number of edges)
print("Network Size (number of edges):")

## [1] "Network Size (number of edges):"
ecount(g)

## [1] 13288

# Network density
print("Network Density:")

## [1] "Network Density:"
edge_density(g)

## [1] 0.05901843

# Check strong connectivity
components <- components(g, mode="strong")
cat("\nNumber of strongly connected components:", components$no, "\n")

##
## Number of strongly connected components: 7
cat("Size of largest strongly connected component:", max(components$csize), "\n")

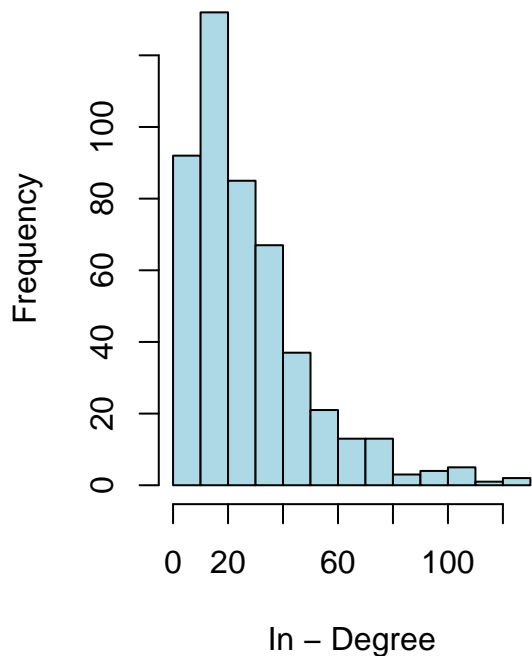
## Size of largest strongly connected component: 469
```

### Degree Distribution

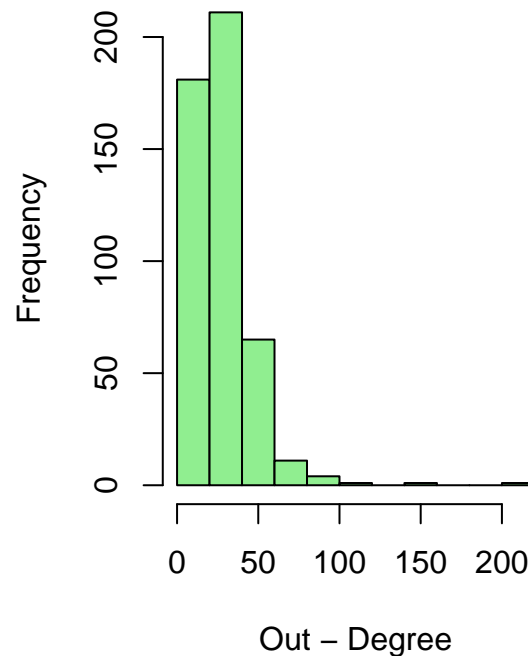
```
# Calculate different degree measures
in_deg <- degree(g, mode="in")
out_deg <- degree(g, mode="out")
total_deg <- degree(g, mode="total")

par ( mfrow = c (1 ,2))
hist ( in_deg , main = " In - Degree Distribution " ,
xlab = " In - Degree " , ylab = " Frequency " , col = " lightblue " )
hist ( out_deg , main = " Out - Degree Distribution " ,
xlab = " Out - Degree " , ylab = " Frequency " , col = " lightgreen " )
```

## In – Degree Distribution



## Out – Degree Distribution



## PageRank

```
page_rank <- page_rank (g , weights = E ( g ) $weight , directed = TRUE ) $vector
```

## Hub and Authority Scores

*Note:* The depreciation warning about 'hub\_score' and 'authority\_score' appears to not actually be true.

```
hub_scores <- hub_score(g , scale = TRUE ) $vector # Hub scores
```

```
## Warning: `hub_score()` was deprecated in igraph 2.0.3.
## i Please use `hits_scores()` instead.
## This warning is displayed once every 8 hours.
## Call `lifecycle::last_lifecycle_warnings()` to see where this warning was
## generated.
```

```
auth_scores <- authority_score(g , scale = TRUE ) $vector # Authority scores
```

```
## Warning: `authority_score()` was deprecated in igraph 2.1.0.
## i Please use `hits_scores()` instead.
## This warning is displayed once every 8 hours.
## Call `lifecycle::last_lifecycle_warnings()` to see where this warning was
## generated.
```

## Closeness Centrality

```
harmonic_close <- harmonic_centrality (g , weights = E ( g ) $weight , mode = "out" )
```

## Betweenness Centrality

```
betweenness <- betweenness (g , weights = E ( g ) $weight , directed = TRUE , normalized = TRUE )
```

## Nodes

```
get_top_10 <- function (metric, metric_name) {  
  top_indices <- order ( metric , decreasing = TRUE ) [1:10]  
  data.frame (   
    Metric = rep(metric_name, 10) ,  
    Node = top_indices ,  
    Value = round ( metric [ top_indices ] , 4)  
  )  
}  
  
top_nodes <- rbind (   
  get_top_10 ( in_deg , " In - Degree " ) ,  
  get_top_10 ( out_deg , " Out - Degree " ) ,  
  get_top_10 ( page_rank , " PageRank " ) ,  
  get_top_10 ( harmonic_close , " Harmonic Closeness " ) ,  
  get_top_10 ( betweenness , " Betweenness " ) ,  
  get_top_10 ( hub_scores , " Hub Scores " ) ,  
  get_top_10 ( auth_scores , " Authority Scores " )  
)  
  
# Print results  
print ( " Top 10 nodes by different centrality measures : " )  
  
## [1] " Top 10 nodes by different centrality measures : "  
  
print ( top_nodes )
```

##	Metric	Node	Value
## 322	In - Degree	212	127.0000
## 208	In - Degree	397	121.0000
## 190	In - Degree	36	120.0000
## 111	In - Degree	71	109.0000
## 385	In - Degree	82	108.0000
## 254	In - Degree	172	108.0000
## 269	In - Degree	236	106.0000
## 192	In - Degree	37	105.0000
## 303	In - Degree	151	97.0000
## 147	In - Degree	205	97.0000
## 367	Out - Degree	163	210.0000
## 3221	Out - Degree	212	157.0000
## 393	Out - Degree	121	111.0000
## 71	Out - Degree	157	97.0000
## 399	Out - Degree	383	89.0000
## 436	Out - Degree	355	85.0000
## 179	Out - Degree	94	84.0000
## 2541	Out - Degree	172	79.0000
## 105	Out - Degree	135	75.0000
## 87	Out - Degree	16	71.0000
## 3222	PageRank	212	0.0167
## 1471	PageRank	205	0.0128

```

## 389          PageRank 140      0.0111
## 2691          PageRank 236      0.0107
## 215           PageRank 148      0.0106
## 2081          PageRank 397      0.0089
## 92            PageRank 70       0.0082
## 246           PageRank 78       0.0082
## 113           PageRank 72       0.0080
## 3031          PageRank 151      0.0080
## 17    Harmonic Closeness 25 258396.3888
## 149    Harmonic Closeness 93 197943.6471
## 1111   Harmonic Closeness 71 189102.1252
## 3      Harmonic Closeness 60 188666.1494
## 88     Harmonic Closeness 92 185805.9653
## 428    Harmonic Closeness 39 184838.3983
## 32     Harmonic Closeness 63 180308.9408
## 263    Harmonic Closeness 160 176995.4495
## 3671   Harmonic Closeness 163 171500.8813
## 22     Harmonic Closeness 62 171473.9764
## 1112    Betweenness 71      0.0845
## 3223    Betweenness 212     0.0707
## 171     Betweenness 25      0.0677
## 4281    Betweenness 39      0.0619
## 1472    Betweenness 205     0.0500
## 3672    Betweenness 163     0.0450
## 3032    Betweenness 151     0.0438
## 2542    Betweenness 172     0.0412
## 1131    Betweenness 72      0.0399
## 2151    Betweenness 148     0.0376
## 226     Hub Scores 76       1.0000
## 159     Hub Scores 232      0.8593
## 3991    Hub Scores 383      0.8423
## 164     Hub Scores 442      0.6993
## 129     Hub Scores 412      0.6380
## 220     Hub Scores 233      0.6114
## 118     Hub Scores 294      0.5920
## 440     Hub Scores 433      0.5685
## 354     Hub Scores 239      0.5546
## 3224    Hub Scores 212      0.5460
## 3225    Authority Scores 212 1.0000
## 3891    Authority Scores 140 0.8251
## 2692    Authority Scores 236 0.6272
## 1132    Authority Scores 72  0.5033
## 2461    Authority Scores 78  0.4468
## 2082    Authority Scores 397 0.4260
## 188     Authority Scores 286 0.4085
## 318     Authority Scores 138 0.3433
## 1921    Authority Scores 37  0.3400
## 335     Authority Scores 81  0.3315

```

```
node_freq <- table(top_nodes$Node)
```

```

# Convert to dataframe and sort
node_freq_df <- data.frame(
  Node = names(node_freq),

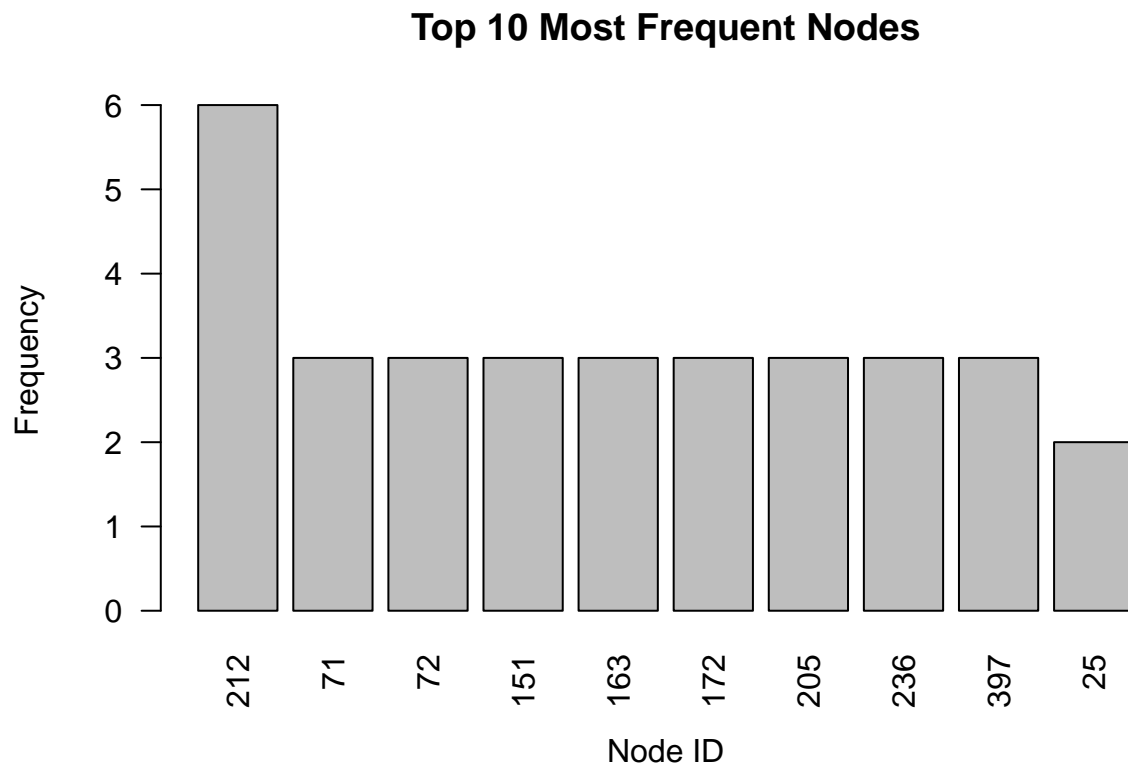
```

```

    Frequency = as.numeric(node_freq)
  )
node_freq_df <- node_freq_df[order(-node_freq_df$Frequency), ]

# Create the plot using base R
barplot(node_freq_df$Frequency[1:10],
        names.arg = node_freq_df$Node[1:10],
        main = "Top 10 Most Frequent Nodes",
        xlab = "Node ID",
        ylab = "Frequency",
        las = 2) # Rotate x-axis labels

```



**Justification**