



IMPROVER METHOD – PT. 4

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PERMUTATION OF THE LAST LAYER (PLL)

“Beginner” method used 2 simple algorithms

- 16-move combination of **Anti-Sune** and **Niklas** for corner permutation (**CPLL**)
- 17-move combination of **Anti-Sune** and its left-handed mirror for edge permutation (**EPLL**)

“Improver” method will use 4 shorter but less intuitive algorithms

- 11-move and 14-move algorithms for corner permutation (**Jb-Perm** and **Na-Perm**) – **R U L** moves
- 11-move algorithms for edge permutation (**Ua-Perm** and **Ub-Perm**) – **R U** moves

The new algorithms will be slightly trickier to learn but well worth the effort!

- The combination of **Anti-Sune** and **Niklas** will be shortened to 11 moves – optimised **Jb-Perm**
- The **Ua-Perm** and **Ub-Perm** algorithms will be speed-optimised to 11 moves – **R U** only

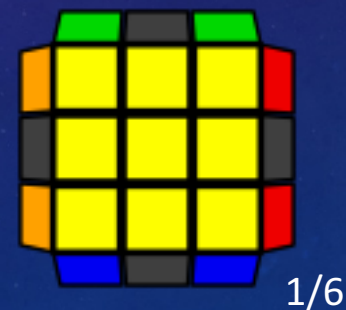


CORNER PERMUTATION OF THE LAST LAYER (CPLL)

There are 3 possible cases during CPLL including the “**solved**” case

The cases that need to be solved are the “**diagonal corner swap**” and the “**adjacent corner swap**”

The “**adjacent**” corner swap is the most common CPLL as it occurs in **4/6** solves



CPLL ALGORITHMS

To change the permutation of corners you will use a mixture of **R U L** moves

- The first **CPLL** algorithm (adjacent corner swap) is **R U2 R' U' R U2 L' U R' U' L**
 - It may not be immediately obvious but it is actually the beginner algorithm after cancellations – see square brackets
 - It starts with the **Anti-Sune** algorithm that was used during **OCLL** – **R U2 R' U' R [U' R']**
 - It ends with the **Niklas** algorithm which manipulates two **F2L pairs** – **[R U'] L' U R' U' L [U]**
 - The combination of these two algorithms is the **Jb-Perm** which swaps 2 diagonal LL corners + 2 LL edges
- The second **CPLL** algorithm (diagonal corner swap) is **(R U' L U2' R' U L') (R U' L U2' R' U L')**
 - This is a 7-move algorithm which manipulates two **F2L pairs**, executed twice – **R U' L U2' R' U L'**
 - The repetition of this algorithm is the **Na-Perm** which swaps 2 adjacent LL corners + 2 LL edges



ADJACENT CORNER SWAP

The “**adjacent**” corner swap can be recognised by the “**headlights**” on one side (shown in orange below)

Approach: “**Adjacent corner swap**” -> “**solved**”

Setup: Ensure the “**Headlights**” are on the left before executing the **CPLL** algorithm

Algorithm: **R U2 R' U' R U2 L' U R' U' L**



Adjacent Swap



Solved

DIAGONAL CORNER SWAP

The “**diagonal**” corner swap can be recognised by the absence of “**headlights**”

Approach: “**Diagonal corner swap**” -> “**solved**”

Setup: No setup required... just execute the algorithm

Algorithm: **(R U' L U2' R' U L') (R U' L U2' R' U L')**



Diagonal Swap



Solved

CPLL EFFICIENCY

“Beginner” – 1 algorithm – $(R U^2 R' U^2') (U R U' R') (R U' L' U) (R' U' L U)$

- **Adjacent Corner Swap** 16 moves, 2 looks
- **Diagonal Corner Swap** 33 moves, 4 looks
- **“Weighted Average”** 16.2 moves, 2.2 looks



Diagonal



Adjacent

“Improver” – 2 algorithms – $R U^2 R' U' R U^2 L' U R' U' L$ and $(R U' L U^2' R' U L') (R U' L U^2' R' U L')$

- **Adjacent Corner Swap** 11 moves, 1 look
- **Diagonal Corner Swap** 14 moves, 1 look
- **“Weighted Average”** 9.7 moves, 1 look



Solved

EDGE PERMUTATION OF THE LAST LAYER (EPLL)

There are 5 possible cases during EPLL including the “**solved**” case

4 misplaced edges require the most effort to solve when you only know a couple of algorithms



4/12



4/12



2/12



1/12



1/12

EPLL ALGORITHMS

To change the permutation of edges we will only use **R U** moves

- The first **EPLL** algorithm that will be used is **R U' R U R U R U' R' U' R2**
 - It is a conjugation of an algorithm that can be used during **F2L – R U' (R U R U R U' R' U' R' U') U R'**
 - The **R U'** is referred to as a “**setup**” move and the **U R'** will undo the setup
 - Applying cancellations results in the **Ua-Perm** which is a counter-clockwise “**3-cycle**” of LL edges
- The second **EPLL** algorithm that will be used is **R2 U R U R' U' R' U' R' U R'**
 - It is a conjugation of an algorithm that can be used during **F2L – R U' (U R U R U R' U' R' U' R') U R'**
 - The **R U'** is referred to as a “**setup**” move and the **U R'** will undo the setup
 - Applying cancellations results in the **Ub-Perm** which is a clockwise “**3-cycle**” of LL edges

Note how the two algorithms are both an “**inverse**” of each other



3 MISPLACED EDGES

There are 2 **EPLL** cases with 3 misplaced edges and they can be recognised by the "**bar**" (green below)

Approach: "**Ua-Perm**" or "**Ub-Perm**" -> "**Solved**"

Setup: Ensure the "**Bar**" is at the **back** before executing the **EPLL** algorithm

Algorithm: **R U' R U R U R U' R' U' R2** or **R2 U R U R' U' R' U' R' U R'** – depending on the case



Ua-Perm



Solved



Ub-Perm



Solved

4 MISPLACED EDGES

There are 2 **EPLL** cases with 4 misplaced edges and they take the most effort to solve

Approach: “**Z-Perm**” or “**H-Perm**” -> “**Ua-Perm**” -> “**Solved**”

Setup: Avoid the “**Ua-Perm**” by setting up the Z-Perm correctly before executing the **EPLL** algorithm

Algorithm: **R U' R U R U R U' R' U' R2** – twice, remembering to **AUF** prior to execution



H-Perm

or



Z-Perm



Ua-Perm



Solved

EPLL EFFICIENCY

“Beginner” – 1 algorithm – **$(R\ U2\ R'\ U2')\ (U\ R\ U'\ R')\ U\ (L'\ U2\ L\ U2')\ (U'\ L'\ U\ L)$**

- **3 Misplaced Edges** – **Ua** or **Ub** 17 or 35 moves, 2 or 4 looks
- **4 Misplaced Edges** – **Z** or **H** 34 or 35 moves, 4 looks
- **“Weighted Average”** 25.9 moves, 3.1 looks

“Improver” – 2 algorithms – **$R\ U'\ R\ U\ R\ U\ R\ U'\ R'\ U'\ R2$** and **$R2\ U\ R\ U\ R'\ U'\ R'\ U'\ R'\ U\ R$**

- **3 Misplaced Edges** – **Ua** or **Ub** 11 moves, 1 look
- **4 Misplaced Edges** – **Z** or **H** 23 moves, 2 looks
- **“Weighted Average”** 13.1 moves, 1.3 looks



Ua-Perm



Ub-Perm



Z-Perm



H-Perm



Solved

PLL EFFICIENCY

“Beginner” – 2 algorithms – beginner **Jb-Perm** + beginner **Ub-Perm**

- **“Worst Case”** 68 moves, 8 looks
- **“Weighted Average”** 42.1 moves, 5.3 looks

“Improver” – 4 algorithms – **Jb-Perm** + **Na-Perm** + **Ua-Perm** + **Ub-Perm**

- **“Worst Case”** 37 moves, 3 looks
- **“Weighted Average”** 22.8 moves, 2.3 looks

Comparison

- **“Worst Case”** “Improver” method saves **31** moves, **5** looks → **45.6%** saving
- **“Weighted Average”** “Improver” method saves **19.3** moves, **3** looks → **45.9%** saving



CONGRATULATIONS!



**Practice
Makes
Perfect**