

12.10.3.17

Lokesh Surana

CLASS 12, CHAPTER 10, EXERCISE 4.8

- 8) If either $\mathbf{a} = \mathbf{0}$ or $\mathbf{b} = \mathbf{0}$ then $\mathbf{a} \times \mathbf{b} = \mathbf{0}$. Is the converse true? Justify your answer with an example.

Solution: False.

Let $\mathbf{a} = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}$ and $\mathbf{b} = \begin{pmatrix} m \\ 0 \\ 0 \end{pmatrix}$ ($m \neq 0$).

Here neither of \mathbf{a} or \mathbf{b} is zero.

$$\begin{aligned} \mathbf{a} \times \mathbf{b} &= \begin{vmatrix} a_{23} & b_{23} \\ a_{31} & b_{31} \\ a_{12} & b_{12} \end{vmatrix} \\ &= \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix} \end{aligned}$$

Justified.