

# 12.10.3.17

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CLASS 12, CHAPTER 10, EXERCISE 3.17

17) Show that the vectors form the vertices  $\begin{pmatrix} 2 \\ -1 \\ 1 \end{pmatrix}$ ,

$\begin{pmatrix} 1 \\ -3 \\ -5 \end{pmatrix}$  and  $\begin{pmatrix} 3 \\ -4 \\ -4 \end{pmatrix}$  of a right angled triangle.

**Solution:** Let's name the triangle  $ABC$ , where

$\mathbf{A} = \begin{pmatrix} 2 \\ -1 \\ 1 \end{pmatrix}$ ,  $\mathbf{B} = \begin{pmatrix} 1 \\ -3 \\ -5 \end{pmatrix}$  and  $\mathbf{C} = \begin{pmatrix} 3 \\ -4 \\ -4 \end{pmatrix}$ . So sides of triangle are:

$$\mathbf{a} = \mathbf{C} - \mathbf{B} = \begin{pmatrix} 2 \\ -1 \\ 1 \end{pmatrix}$$

$$\mathbf{b} = \mathbf{A} - \mathbf{C} = \begin{pmatrix} -1 \\ 3 \\ 5 \end{pmatrix}$$

$$\mathbf{c} = \mathbf{B} - \mathbf{A} = \begin{pmatrix} -1 \\ -2 \\ -6 \end{pmatrix}$$

If inner product of two vectors is zero, then they are perpendicular. So, we have:

$$\mathbf{a}^\top \mathbf{b} = 2 \cdot (-1) + (-1) \cdot 3 + 1 \cdot 5 = 0$$

$$\mathbf{b}^\top \mathbf{c} = (-1) \cdot (-1) + 3 \cdot (-2) + 5 \cdot (-6) = -35$$

$$\mathbf{c}^\top \mathbf{a} = (-1) \cdot 2 + (-2) \cdot (-1) + (-6) \cdot 1 = -6$$

So,  $\mathbf{a}$  and  $\mathbf{b}$  are perpendicular and therefore triangle  $ABC$  is right angled triangle.