

```

vector<vector<int>> combo(vector<int> &cond, int right)
{
    vector<vector<int>> answer;
    vector<int> ds;
    sort(cond.begin(), cond.end());
    solve(0, cond, target, answer, ds);
    return answer;
}

```

Subset Sum

Given a list (array) of N integers, print sums of all subsets in it. Output should be printed in increasing order of sums.

Input : $N = 2$, $A[0] = [2, 3]$

Subsets = $[0], [2], [3], [2, 3]$

Output = $0, 2, 3, 5$

Approach

formula : Number of subset = 2^n where $n = \text{no. of elements}$

$[3, 1, 2], N = 3$

Subsets $\Rightarrow \{\emptyset \rightarrow 0, \{3\} \rightarrow 3, \{1\} \rightarrow 1, \{2\} \rightarrow 2, \{3, 1\} \rightarrow 4$
 $\{3, 2\} \rightarrow 5, \{1, 2\} \rightarrow 3, \{3, 1, 2\} \rightarrow 6$

Output = $0, 1, 2, 3, 4, 5, 6$

We can use Power set for subset generation using Bit Manipulation which take $TC = 2^n \times N$ but this is Brute force soln

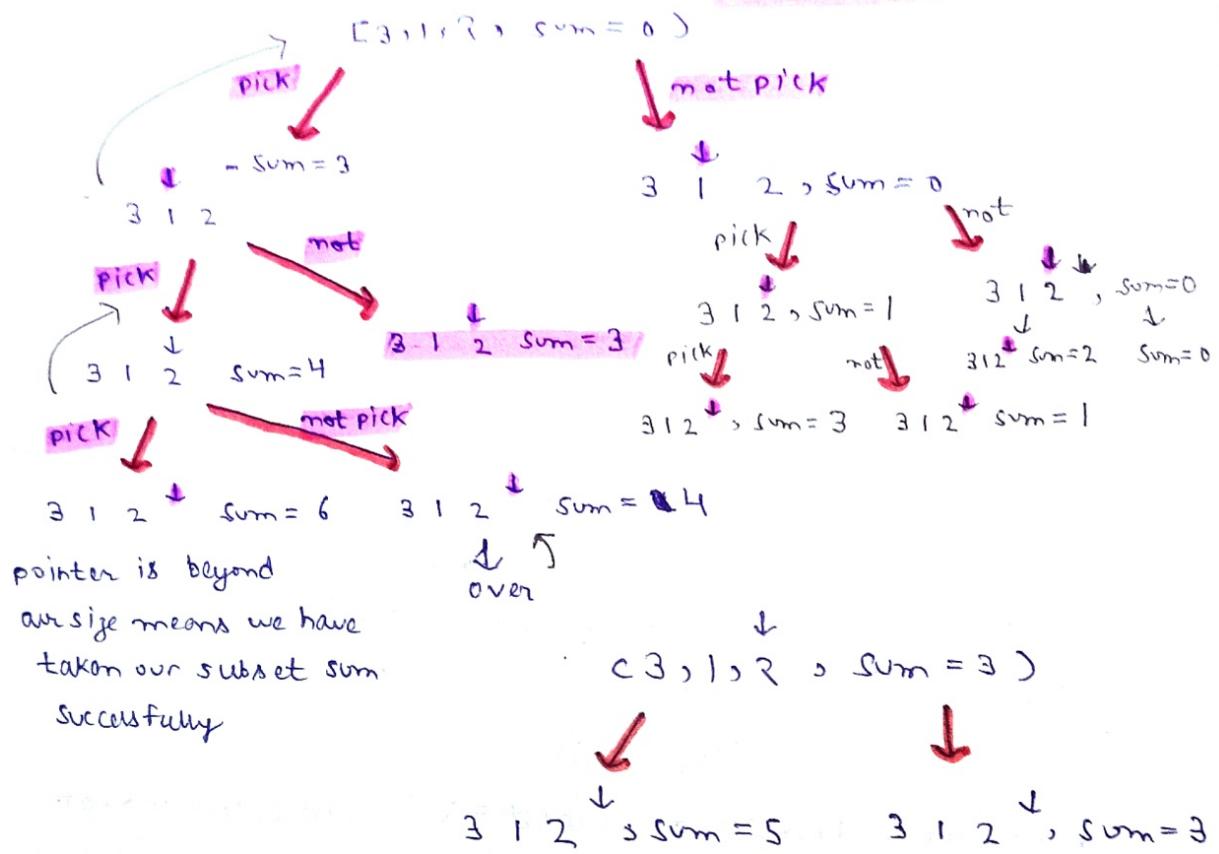
OPTIMISED

$$\text{ITC} = 2^m + 2^m \log(2^m)$$

2^m = size of output

$$\text{ISc} = 2^m$$

arr = [3, 1, 2]



pointer is beyond
arr.size means we have
taken our subset sum
successfully

subset sum = 3

f(ind, s = 0, ans)

pick

not

f(ind + 1, s = 0 + arr[ind], ans) f(ind + 1, s = 0, ans)

|| Base

if C arr.ind == arr.size() {

{

ds.push(subset);

}

Subset - II

Given an integer array numa that may contain duplicates, return all possible subsets [the power set]

Some might not contain duplicate subsets. Return sets in any order.

Input: $\text{numa} = [1, 2, 2]$

Output: $\{\{1\}, \{1\}, \{1, 2\}, \{1, 2, 2\}, \{2\}, \{2, 2\}\}$

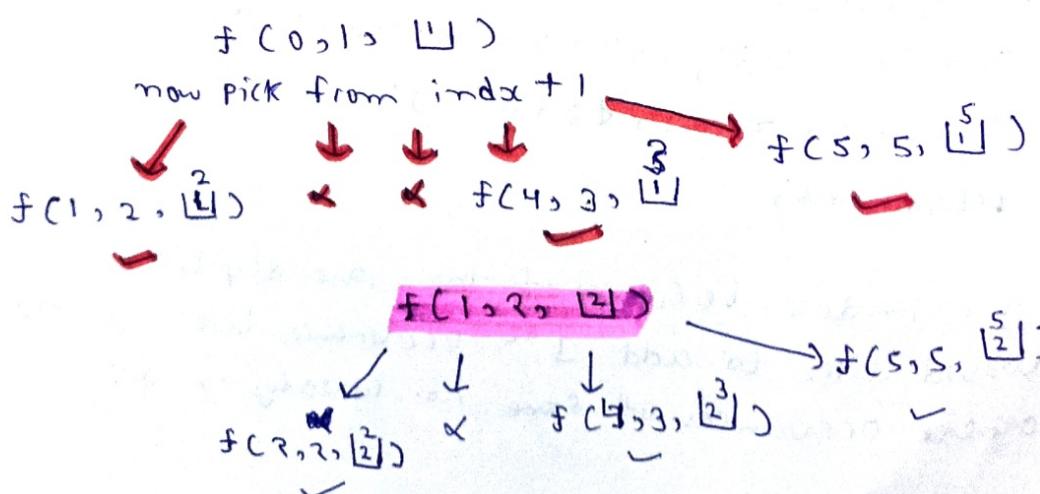
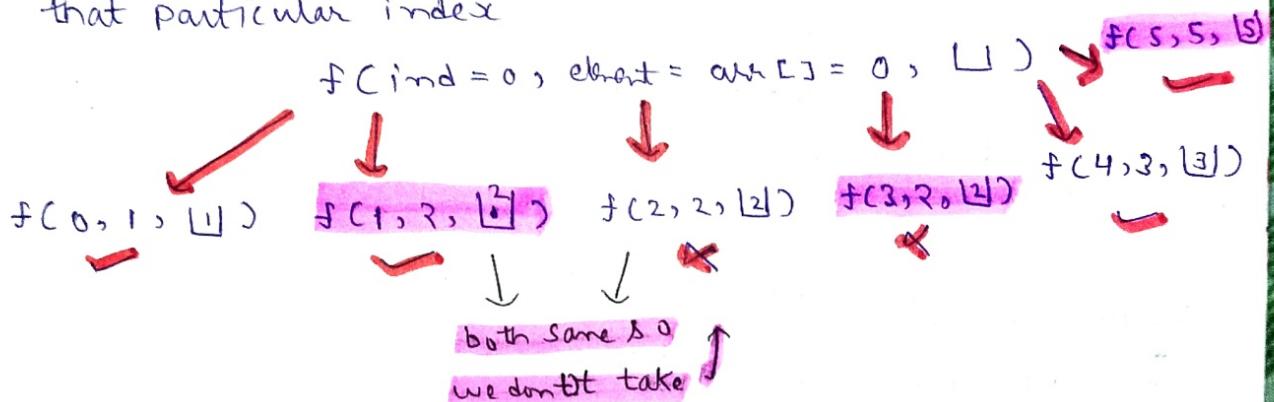
Input $\Rightarrow \text{numa} = [0]$

Output = $\{\{0\}, \{\}\}$

Approach

$[1, 2, 2, 3, 3, 5]$

we can start from any index starting from a index = 0
and an empty DS just same as combination sum = 2
but if $\text{arr}[\text{ind}] == \text{arr}[\text{ind}-1]$ we will not take
that particular index



Code

$$\text{TC} = 2^n \times m \quad \text{SC} = O(2^n) \times k$$

↓ ↓
generating copy each subset to ans
subset

$k = \text{length of subset}$
 $\text{aux space} = O(n)$

|| we do not have base cond'n because this loop below will run till $n-1$ and it automatically gets over once array size exceeded by index

|| we use backtrack step of pop-back

```
void solve(int index, vector<int>& nums, vector<int>& ds, vector<vector<int>>& ans){  
    ans.push_back(ds);  
    for(int i = index; i < nums.size(); i++)  
        if(i != index && nums[i] == nums[i-1]) continue;  
        ds.push_back(nums[i]);  
        solve(i+1, nums, ds, ans);  
        ds.pop_back();  
}
```

```
vector<vector<int>> subset(vector<int>& nums){
```

```
    vector<vector<int>> ans;  
    vector<int> ds;  
    sort(nums.begin(), nums.end());  
    solve(0, nums, ds, ans);  
    return ans;
```

```
}
```

|| $i \neq \text{index}$ because if there are duplicates we would like to add 1st occurrence but not the other occurrences of same no. already in ds.

(1st March) Combination Sum

Given an array of distinct integers candidates and a target integer target, return a list of all unique combinations of candidates where chosen numbers sum to target. You may return combinations in any order. The same number may be chosen from candidates an unlimited number of times. Two combinations are unique if frequency of atleast one of chosen no. is different. It is guaranteed that no. of unique combinations that sum up to target is less than 150 combination of given input.

Input: candidates = [2, 3, 6, 7] target = 7

Output = [2, 2, 3] = 7 and [7].

Input: Candidates = [2, 3, 5] target = 8

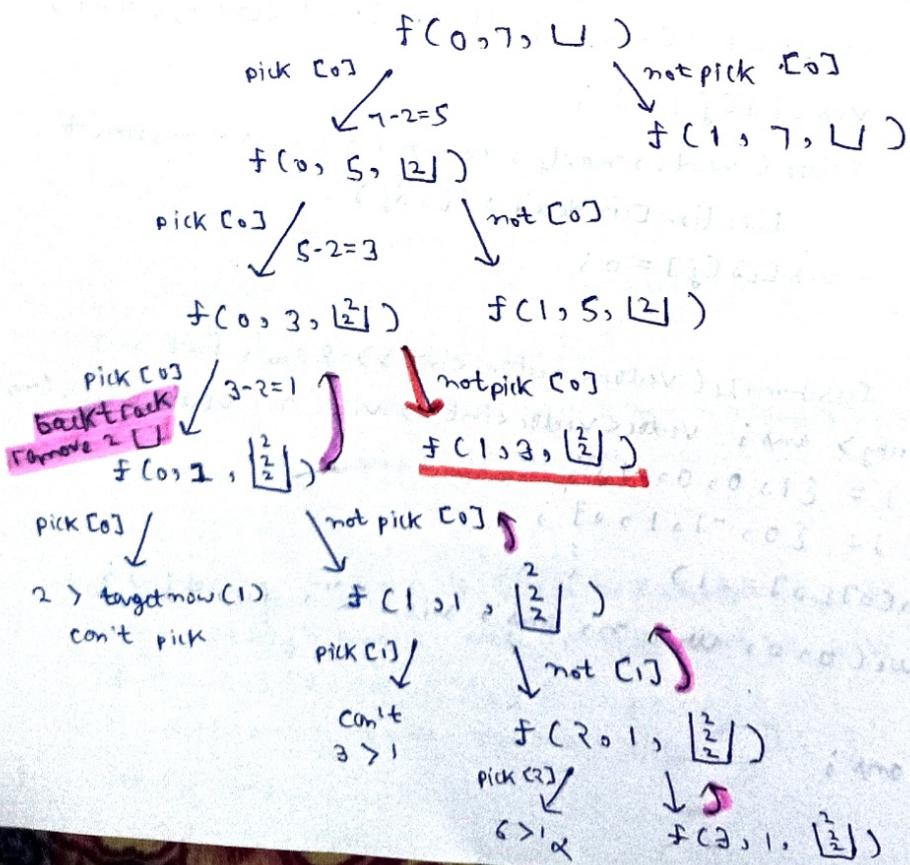
```
output = [[2, 2, 2, 2], [2, 3, 3], [3, 5]]
```

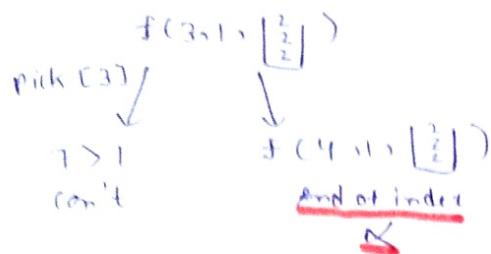
Approach $\| T C = ? \xrightarrow{\text{target}} S C = k \times \infty$
 $\in = \text{no. of combo}$

We will use pick / non pick Approach

We can pick one value multiple times so if we pick a index say c_0 then again next time we still be at c_0 and again we will choose whether we can pick 0 or not. we do till $\text{our arr}[c_0] > \text{target}$.

arr = [2, 3, 6, 7] target = 7





so combination [3, 3, 2] is not valid as

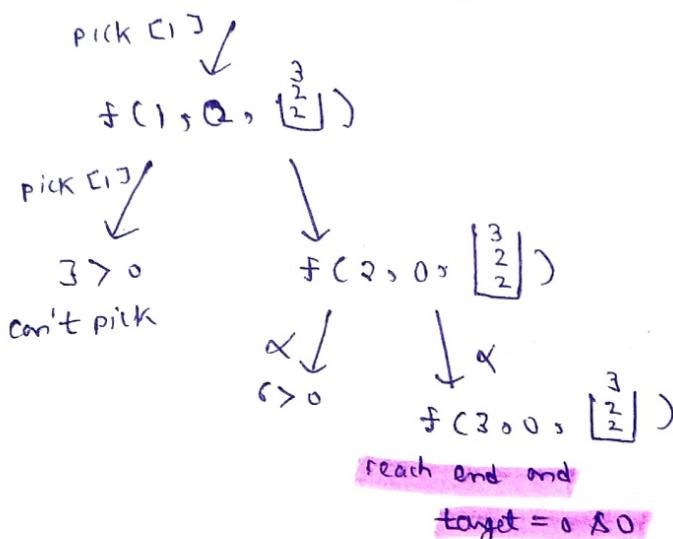
at end when index = last index if not target == 0
means combination not valid so we go back

// backtrack cond n

remove 2 from $\boxed{\underline{2}}$

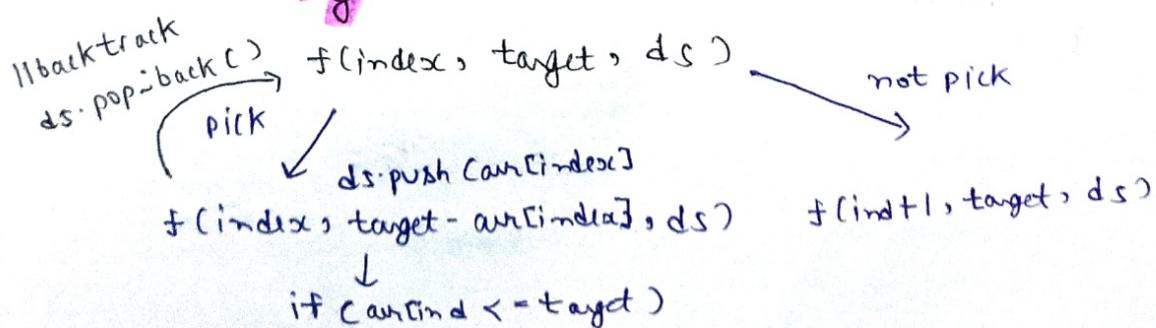
now we go to

$f(1, 3, \boxed{\underline{2}})$



[3, 3, 2] is a combination

algo



// Base case
 $\text{if } (index == n)$
 $\text{if } (target == 0)$
 add combo

```

void solve(int index, vector<int>& arr, int target, vector<vector<int>>& ans)
{
    if (index == arr.size())
    {
        if (target == 0)
        {
            ans.push_back(ds);
        }
        return;
    }

    // Recursive call
    if (arr[index] <= target)
    {
        // pick
        ds.push_back(arr[index]);
        solve(index + 1, arr, target - arr[index], ans, ds);
        ds.pop_back();
    }

    // not pick
    solve(index + 1, arr, target, ans, ds);
}

vector<vector<int>> combination(vector<int>& candidates, int target)
{
    vector<vector<int>> ans;
    vector<int> ds;

    solve(0, candidates, target, ans, ds);
    return ans;
}

```

Combination Sum - II

Given candidates and target , find all unique combinations from candidates where candidate numbers sum to target . Each number in candidates may only be used once in combination . The solution must not contain duplicates .

Input \Rightarrow candidates = [1, 2, 3, 4] target = 8

Output = [[1, 1, 6], [1, 2, 5], [1, 7], [2, 6]] + 1 is repeating because it appear 2 times in input

Note : Return answer in lexicographical order . (sorted)

Approach

$$TC = 2^m \times K \times \log(\text{set size})$$

Brute force

// same as combination 1

```
void solve( int index, vector<int> arr, int target )  
{  
    set<vector<int>> ans, ds;
```

{

// same .

```
if ( arr[ index ] <= target )
```

{

// same

```
solve( index + 1, arr, target - arr[ index ], ans, ds );
```

}

// same

```
solve( index + 1, arr, target, ans, ds );
```

}

```
vector<vector<int>> comb( candidates, target )
```

```
{  
    set<vector<int>> ans;
```

```
    vector<vector<int>> answer;
```

```
    sort( candidates.begin(), candidates.end() );
```

```
    for ( auto it = ans.begin(); it != ans.end(); it++ )
```

{

```
        answer.push_back( *it );
```

}

```
    return answer;
```

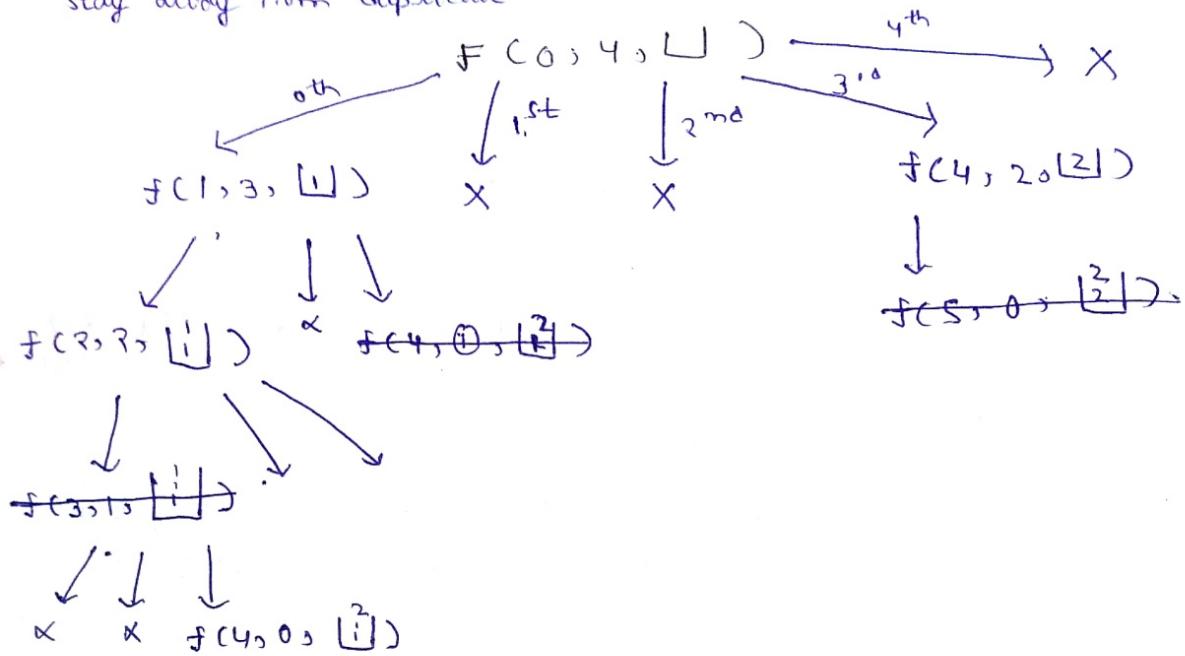
}

Approach 2

$$TC = 2^m \times k \quad SC = k \times x$$

$arr = [1, 1, 1, 2, 2]$ target = 4

we can start with any of index but we want to stay away from duplicate



```

void solve(int index, vector<int> arr, int target, vector<
vector<int>> &ans, vector<int> &ds)
{
    if(target == 0)
    {
        ans.push_back(ds);
        return;
    }
    for(int i = index; i < arr.size(); i++)
    {
        if(i > index && arr[i] == arr[i-1]) continue;
        if(target < arr[i]) break;
        ds.push_back(arr[i]);
        solve(i+1, arr, target - arr[i], ans, ds);
        ds.pop_back();
    }
}

```

```
vector<vector<int>> combo(vector<int> &cond, int target)
{
    vector<vector<int>> answer;
    vector<int> ds;
    sort(cond.begin(), cond.end());
    solve(0, cond, target, answer, ds);
    return answer;
}
```

```
void solve (int index, int sum, vector<int> arr,
           int N, vector<int> &ans)
{
    if(index == N)
    {
        ans.push_back(sum);
        return;
    }
    // pick
    solve(index+1, sum + arr[index], arr, N, ans);

    // not pick
    solve(index+1, sum, arr, N, ans);
}

vector<int> subsetSum (vector<int> arr, int N)
{
    vector<int> ans;
    solve(0, 0, arr, N, ans);
    sort (ans.begin(), ans.end());
    return ans;
}
```

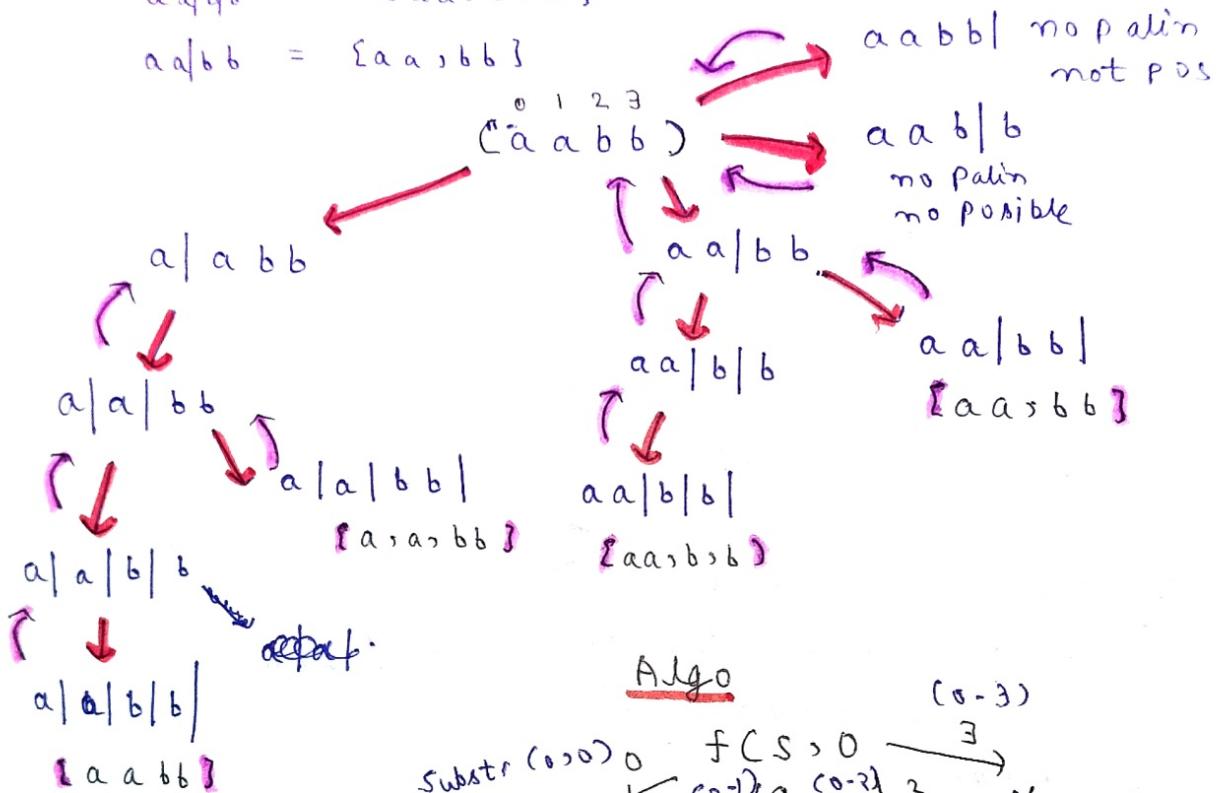
Approach

$$\{ "a|a|b|b" \} = \{ a, a, b, b \}$$

$$a|a|bb = \{a, a, bb\}$$

$$a \sqcup b = \{aa, ab, ba\}$$

$$aabbb = \{aaa,bbb\}$$



Algo

(Check if substring is palindrome or not)

for $C_{ind} \rightarrow m-1$)

{ is palind

7

call recursion

11 bata

if (ind == n)

{ store in ds

```

vector<vector<string>> partition (string s)
{
    vector<vector<string>> res;
    vector<string> ans;
    solve(0, s, res, ans);
    return res;
}

void solve (int index, string s, vector<vector<string>> &res,
           vector<string> ans)
{
    if (index == s.size())
    {
        res.push_back (ans);
        return;
    }

    for (int i = index; i < s.size(); i++)
    {
        if (isPalindrome (s, index, i))
        {
            ans.push_back (s.substr (index, i - index + 1));
            solve (i + 1, s, res, ans);
            ans.pop_back();
        }
    }
}

bool isPalindrome (string s, int start, int end)
{
    while (start <= end)
    {
        if (s[start++] != s[end--])
            return false;
    }
    return true;
}

```

Palindrome Partitioning

Given a string s , partition s , such that every substring of partition is a palindrome. Return all possible palindrome partitioning of s . A palindrome string is a string that reads same backward as forward.

Input: $s = "aab"$

Output: $[["a", "a", "b"], ["aa", "b"]]$

Input: $s = "a"$

Output: $[["a"]]$

Partition Sequence

The set $[1, 2, 3, \dots, n]$ consists total of $n!$ unique permutations. By listing and labelling all permutations in order, we get the following sequence for $n=3$

- | | |
|---------|-------|
| ① "123" | ⑦ 231 |
| ② 132 | ⑤ 312 |
| ③ 213 | ⑥ 321 |

Given n and $k \rightarrow$ return k^{th} permutation sequence.

Input : $n=3, k=3$ output = "213"

Input : $n=4, k=9$ output = "2314"

Input : $n=3, k=1$ output = "123"

Approach

Brute force $\text{TC} = n! \times n$

- ① Generate all permutation using recursion and store in a DS
- ② if the DS in which we've stored the permutations has 0 based indexing then our k^{th} perm = $\text{ds}[k-1]$ after sorting DS

Optimal $\text{TC} = o(n) \times o(n)$ to erase

$n=4$, then no. of perm = $n! = 24$

$\text{SC} = o(n)$

$k=17$

we can start the perm with

1 + $(2, 3, 4)$] 6 (0-5 permutations)

2 + $(1, 3, 4)$] 6 (6-11)

3 + $(1, 2, 4)$] 6 (12-17)

4 + $(1, 2, 3)$] 6 (18-23)

24 unique permutation

we need $k=17$ means 17^{th} permutation

and it will start with 3 as 3 has (12-17 perm)

as there is 0 based indexing so

$k=17$ means 16^{th}

each no. contain 6 permutation so

$$16 / 6 = 2$$

means index = 2 has 16^{th} perm starting for 0 based indexing

$16 \cdot 1 \cdot 6 = 4^{\text{th}}$ sequence from those 6 permutations
given by starting with 3. so now question comes down to

$\{1, 2, 4\}, k=4$ as we already know sequence start
from 3.

we can say our permutation will start from

$$\underline{1} + (2, 4)] 2 \text{ permutations } (0-1)$$

$$\underline{2} + (1, 4)] 2 \quad (2-3)$$

$$\underline{4} + (1, 2)] \underline{2} \quad (4-5)$$

$\cdot 6 \text{ i.e. } 3!$ as $n=3$ now

since $k=4$, $\frac{4}{2} = 2$ means index = 2 i.e. 4

$4 \cdot 1 \cdot 2 = 0$ means perm start from 4 at 0th. question

become $\{1, 2\}, k=0$

perm can start with

$$\underline{1} + (2)] 1 \quad (0-0)$$

$$\underline{2} + (\text{empty})] \underline{1} \quad (1-1)$$

$2 \text{ i.e. } 2!$

$0/1 = 0$ i.e. 0th index means perm start with 1

$0 \cdot 1 \cdot 1 = 0$ i.e. $k=0$

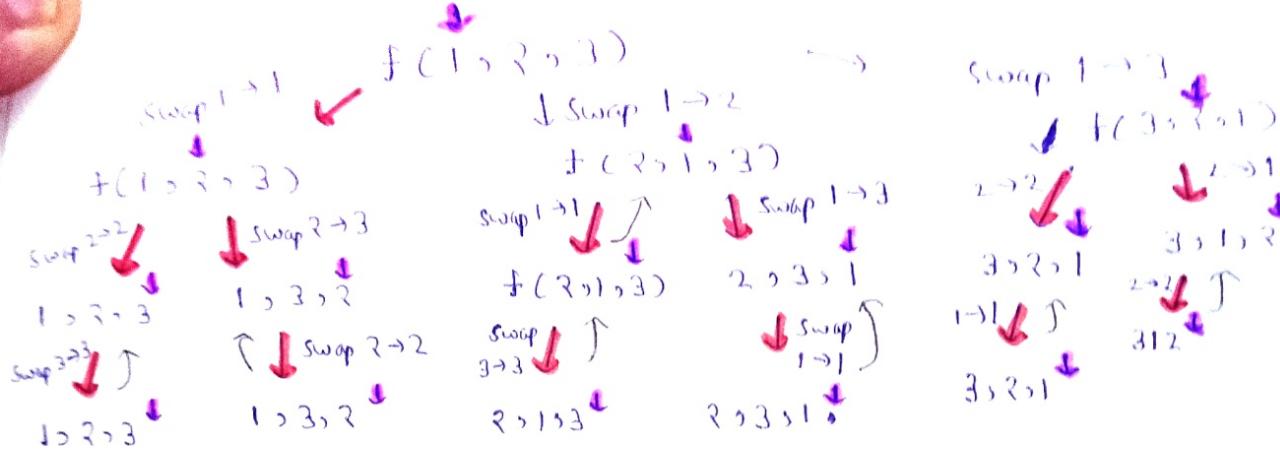
$\{2\}, k=0$

$$\underline{2} + (\text{empty})] 1$$

so out output

3 4 1 2

```
String getPermutation (int n, int k)
{
    int fact = 1;
    vector<int> numbers;
    for (l=1; l < n; l++)
    {
        fact = fact * l;
        numbers.push_back(l);
    }
    numbers.push_back(n);
    k = k - 1;
    while (true)
    {
        ans += to_string(numbers[k / fact]);
        numbers.erase(numbers.begin() + (k / fact));
        if (numbers.size() == 0)
        {
            break;
        }
        k = k % fact;
        fact = fact / numbers.size();
    }
    return ans;
}
```



Permutations

Given an array `nums` of distinct integers, return all possible permutations. You can return answer in any order.

Input : `nums = [1, 2, 3]`

Output = `[[], [1, 2, 3], [1, 3, 2], [2, 1, 3], [2, 3, 1], [3, 1, 2], [3, 2, 1]]`

Input : `nums = [0, 1]`

Output = `[[], [0, 1], [1, 0]]`

Input : `nums = [1]`

Output = `[[], [1]]`

CODE $\text{TC} = O(n!)$ $\text{SC} = O(n!)$

```
void solve (int index, vector<int> &nums, vector<vector<int>> &ans)
{
    if (index == nums.size() - 1)
    {
        ans.push_back (nums);
        return;
    }
    for (int j = index; j < nums.size(); j++)
    {
        swap (nums[index], nums[j]);
        solve (index + 1, nums, ans);
        swap (nums[index], nums[j]);
    }
}
vector<vector<int>> permute (vector<int> &nums)
{
    vector<vector<int>> ans;
    solve (0, nums, ans);
    return ans;
}
```

Power of Three

if there exist an x such that $n = 3^x$

bool isPowerOfThree (int n)

```
{   if (TC = O(log 3(m))) SC = O(log 3(m))  
    if (m == 1) return true;  
    if (m <= 0 || m % 3 != 0) return false;  
    return isPowerOfThree(m/3);  
}
```

Power of Four

bool isPowerOfFour (int n)

```
{   if Recursively TC = O(log 4(m)) SC = O(log 4(m))  
    if (m == 1) return true;  
    if (m <= 0 || m % 4 != 0) return false;  
    return isPowerOfFour(m/4);  
}
```

bool isPowerOfFour (int n)

```
{   if Iterative TC = O(log 4(m)) SC = O(1)  
    if (n == 0) return false;  
    while (n % 4 == 0)  
    {  
        n = n / 4;  
    }  
    return n == 1;  
}
```

Power of Two using Recursion

Given an integer n . Return true if its power of two. otherwise return false.
An integer is power of 2 if there exist an integer x such that $n = 2^x$.

CODE

divide no. by 2 until it reach 1 successfully if not div by 2 or -ve return false.

```
TC = O(log 2(n)) SC: O(log 2(n))

if (n == 1) return 1;
bool isPowerofTwo (int n)
{
    if (n == 1) return true;
    if (n <= 0 || n % 2 != 0) return false;
    return isPowerofTwo(n / 2);
}
```

51. N-Queens

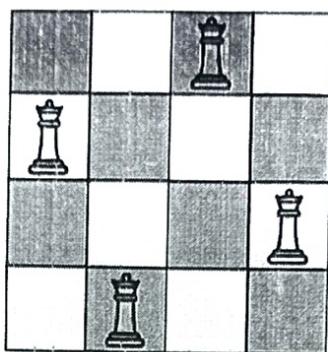
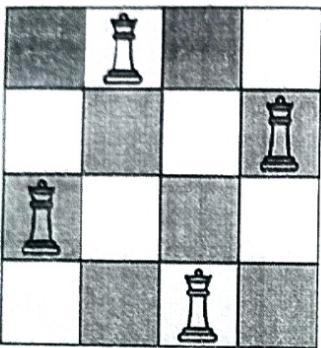
Hard · 5264 · 145 · Add to List · Share

The n-queens puzzle is the problem of placing n queens on an $n \times n$ chessboard such that no two queens attack each other.

Given an integer n , return all distinct solutions to the n-queens puzzle. You may return the answer in any order.

Each solution contains a distinct board configuration of the n-queens' placement, where 'Q' and '.' both indicate a queen and an empty space, respectively.

Example 1:



Input: $n = 4$

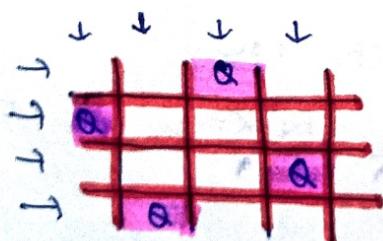
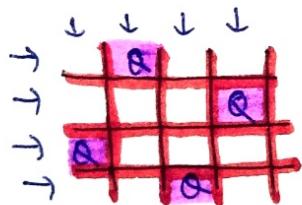
Output: $[["Q__","...Q__","Q__","..Q__"], ["..Q__","Q__","...Q__",".Q__"]]$

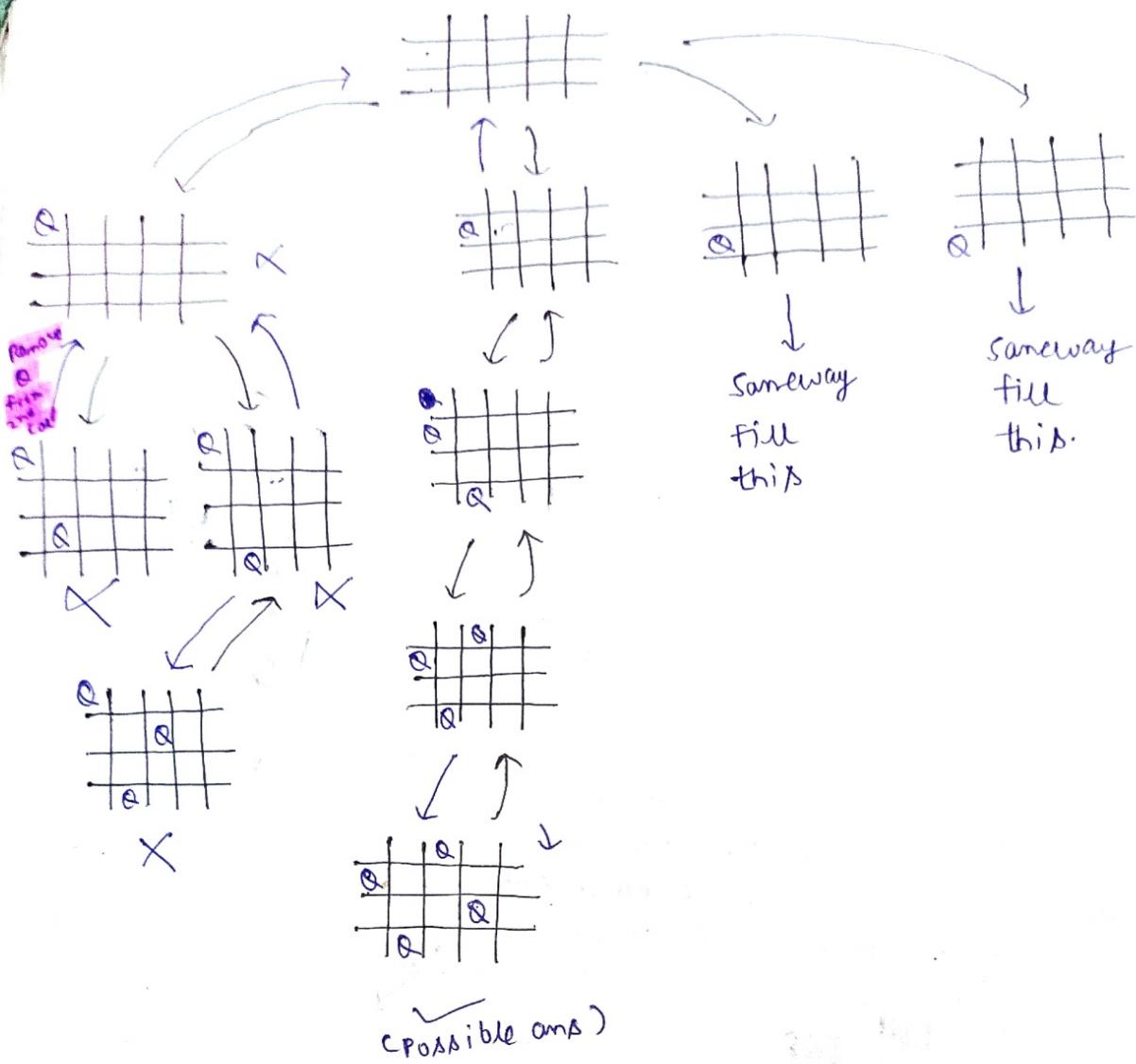
Explanation: There exist two distinct solutions to the 4-queens puzzle as shown above

N Queens

- ① Every row should have one Queen
- ② every col should have one Queen
- ③ None of Queen should attack each other

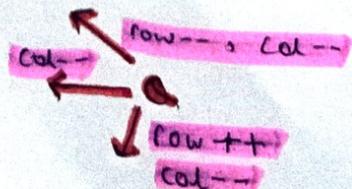
Queen can attack in 8 Directions





Algo

- ① we are filling Queens in each row
- ② Going inside each column and checking is it safe to place Queen there.
- ③ if we reach col end we return
- ④ while returning we make that box again empty.
- ⑤ while filling to check is it safe or not just check in 3 Dirⁿ



```

bool isSafe (int row, int col, vector<string> board, int n)
{
    // check in all 3 direction
    int duprow = row;
    int dupcol = col;

    // upward in left
    while (row >= 0 && col >= 0)
    {
        if (board[row][col] == 'Q') return false;
        row--; col--;
    }

    // straight on left
    row = duprow; col = dupcol;
    while (col >= 0) {if (board[row][col] == 'Q') return false; col--;}

    // downward on left
    row = duprow; col = dupcol;
    while (row < n && col >= 0)
    {
        if (board[row][col] == 'Q') return false; row++; col--;
    }

    return true;
}

void ways (int col, vector<string> &ans, vector<vector<string>> &board, int n)
{
    // base case
    if (col == n)
    {
        ans.push_back(board); return;
    }

    for (int row = 0; row < n; row++)
    {
        if (isSafe (row, col, board, n))
        {
            board[row][col] = 'Q';
            ways (col + 1, ans, board, n);
            board[row][col] = '.'; // backtrack step
        }
    }
}

vector<vector<string>> NQueen (int n)
{
    vector<string> board(n);
    vector<vector<string>> ans (n);
    string s (n, '.'); // empty string
    for (int i = 0; i < n; i++)
    {
        board[i] = s;
    }
    ways (0, ans, board, n);
    return ans;
}

```

37. Sudoku Solver

Hard 4682 145 Add to List Share

Write a program to solve a Sudoku puzzle by filling the empty cells.

A sudoku solution must satisfy all of the following rules:

1. Each of the digits 1-9 must occur exactly once in each row.
2. Each of the digits 1-9 must occur exactly once in each column.
3. Each of the digits 1-9 must occur exactly once in each of the 9 3x3 sub-boxes of the grid.

The '.' character indicates empty cells.

Example 1:

5	3		7					
6			1	9	5			
	9	8				6		
8				6				3
4			8		3			1
7				2			6	
	6				2	8		
			4	1	9			5
			8			7	9	

Example 1:

5	3		7					
6			1	9	5			
	9	8				6		
8				6				3
4			8		3			1
7				2			6	
	6				2	8		
		4	1	9				5
			8			7	9	

Input: board = [[5, 3, '.', '.', '7', '.', '.', '.', ''], [6, '.', '1', '9', 5, '.', '.', '.', ''], [7, '.', '2', '8', '.', '.', '3', '.', ''], [8, '.', '6', '.', '4', '2', '1', '5', ''], [9, '.', '7', '3', '8', '5', '4', '6', ''], [1, '9', '8', '3', '4', '2', '5', '6', '7'], [2, '8', '5', '9', '7', '6', '1', '4', '2', '3], [3, '4', '2', '6', '8', '5', '3', '7', '9', '1'], [4, '7', '1', '3', '9', '2', '4', '8', '5', '6'], [5, '9', '6', '1', '5', '3', '7', '2', '8', '4], [6, '2', '8', '7', '4', '1', '9', '6', '3', '5'], [7, '3', '4', '5', '2', '8', '6', '1', '7', '9]]
Output: [[5, 3, 4, 6, 7, 8, 9, 1, 2], [6, 7, 2, 1, 9, 5, 3, 4, 8], [1, 9, 8, 3, 4, 2, 5, 6, 7], [8, 5, 9, 7, 6, 1, 4, 2, 3], [4, 2, 6, 8, 5, 3, 7, 9, 1], [7, 1, 3, 9, 2, 4, 8, 5, 6], [9, 6, 1, 5, 3, 7, 2, 8, 4], [2, 8, 7, 4, 1, 9, 6, 3, 5], [3, 4, 5, 2, 8, 6, 1, 7, 9]]
Explanation: The input board is shown above and the only valid solution is shown below:

5	3	4	6	7	8	9	1	2
6	7	2	1	9	5	3	4	8
1	9	8	3	4	2	5	6	7
8	5	9	7	6	1	4	2	3
4	2	6	8	5	3	7	9	1
7	1	3	9	2	4	8	5	6
9	6	1	5	3	7	2	8	4
2	8	7	4	1	9	6	3	5
3	4	5	2	8	6	1	7	9

SUDOKU SOLVER

Rules of Sudoku

- ① It is 9x9 board where there are 3x3 boxes which are 9 in number.
- ② The digit 1-9 appears only once in each row.
- ③ The digit 1-9 appears only once in each col.
- ④ Digits 1-9 appears only once in any 3x3 box.

5	3	4	6	7	8	9	1	2
6	7	2	1	9	5	3	4	8
8	5	9	7	6	1	4	2	3
4	2	6	8	5	3	7	9	1
7	1	3	9	2	4	8	5	6
9	6	1	5	3	7	2	8	4
2	8	7	4	1	9	6	3	5
3	4	5	2	8	6	1	7	9
1	9	8	3	4	2	5	6	7

- ① We have to fill empty places in given sudoku keeping above condⁿ in mind.
- ② we will try to fill the free spot with every no. b/w 1-9 Keeping in mind all above condⁿ.
- ③ we check empty places in row-wise fashion and then try all possibility in it
- ④ if answer is not possible, we remove filled no. this is our backtrack step. → return false.
- ⑤ if we do not get any empty spot left means all spot filled successfully return true.
- ⑥ if we have successful ans, don't remove filled no. during backtrack because we just want to return one valid answer.

```

void solveSudoku (vector<vector<char>> &board)
{
    solve (board);
}

bool solve (vector<vector<char>> &board)
{
    for (i = 0; i < board.size(); i++)
    {
        for (j = 0; j < board[0].size(); j++)
        {
            if (board[i][j] == '.')
            {
                for (char c = '1'; c <= '9'; c++)
                {
                    if (isValid (board, i, j, c))
                    {
                        board[i][j] = c;

                        if (solve (board))
                            return true;
                    }
                }
            }
        }
    }

    return false;
}

bool isValid (vector<vector<char>> &board, int row, int col, char c)
{
    for (i = 0; i < 9; i++)
    {
        if (board[i][col] == c)
            return false;
        if (board[row][i] == c)
            return false;
    }

    // special formula to check in 3x3 matrix
    if (board[3 * (row / 3) + i / 3][3 * (col / 3) + i % 3] == c)
        return false;
    }

    return true;
}

```

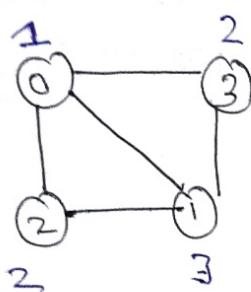
M - Coloring Problem

Given an undirected graph and an integer M, The task is to determine if graph can be colored with at most M colours such that no two adjacent vertices of graph are colored with same colour. Here colouring of graph means the assignment of colors to all vertices. Print 1 if it is possible to colour vertices and 0 otherwise.

Input: $N=4$, $M=3$, $E=5$

Edges [] = $\{(1,2), (2,3), (3,4), (4,1), (1,3)\}$;

Output = 1, it is possible to colour given graph using 3 colours

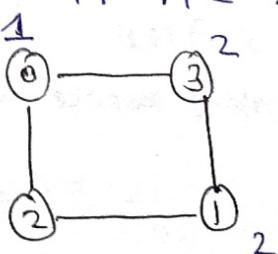


Approach

if $M=3$

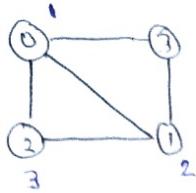
Return 1 as no 2 adjacent vertices have same colour

if $M=2$



Return 0 as we can satisfy adjacent vertices cond'n using only 2 colours.

We will use recursion and will try out every colour of each vertex keeping in mind that two adjacent vertices do not have same colour.



$f(0)$
 colour 1 \downarrow $f(0)$ True
 $f(1)$ \downarrow $f(1)$ True
 \times \downarrow $f(2)$ $f(2)$ True
 \times \downarrow $f(3)$ $f(3)$ True
 \times \downarrow $f(4)$ $f(4)$ True
 So we reach till end
 means return true

Now we can try $f(1)$ with other colours also, $f(0)$ with other colours also but we do not need to as we need to return True only if its possible else return False.

Pseudo code

$T C \rightarrow N^m$ SC $\rightarrow O(N)$
 $+ O(N)$

$f(\text{mode})$

{

 if ($\text{mode} == N$) return True;

 for ($\text{col} = 1 \rightarrow m$)

 if ($\text{possible} \rightarrow v$)

$\{\text{color}[\text{mode}] = \text{col}\}$

 if ($f(\text{mode} + 1) == T$)

 return T;

$\text{color}[\text{mode}] = 0$;

$\{\text{backtrack if that color does not work remove it}$

$\}$

 return False; $\{\text{not possible to colour with M colors}\}$

}

code

```

bool isSafe (int node, int color[], bool graph[10][10],  

            int m, int v, int i)
{
    for (int k = 0; k < v; k++)
    {
        if (k != node && graph[k][node] == 1 &&  

            color[k] == i) // to check if adjacent  

            // vertex has same colour or not
        {
            return false;
        }
    }
    return true;
}

bool solve (int nodes, bool graph[10][10], int color[])
            , int m, int v)
{
    if (node == v) // base case
    {
        return true;
    }

    for (int i = 1; i <= m; i++) // to fill  

        // colours
    {
        if (isSafe(nodes, color, graph, m, v, i))
        {
            color[node] = i; // if safe fill  

            // colour
            if (solve (node + 1, graph, color, m, v))
            {
                return true; // call for next  

                // mode
            }
            color[node] = 0; // if failed  

            // backtrack and  

            // make colour = 0
        }
    }
    return false;
}

```

```
bool Graphcolor (bool graph [10][10], int m,  
                  int v)  
{  
    int color [v] = {0}; // make color array to store  
    if (solve (0, graph, color, m, v))  
        colours  
    {  
        return true;  
    }  
    return false;  
}
```

Rat in a Maze

22nd Feb

Consider a rat placed at $(0,0)$ in a square matrix of order $N \times N$. It has to reach destination at $(N-1, N-1)$. Find all possible paths that rat can take to reach from source to destination. The directions in which rat can move are 'U' (up), 'D' (down), 'L' (left), 'R' (right). Value 0 at a cell in matrix represents that it is blocked and rat cannot move to it while value 1 at cell in matrix represent that rat can travel through it.

Note: In a path, no cell be visited more than one time.

Example 1:

Input :

$N = 4$

$m[][] = \{ \{1, 0, 0, 0\}, \{1, 1, 0, 1\}, \{1, 1, 0, 0\}, \{0, 1, 1, 1\} \};$

Output = DDRDRDRR DRDDDRR

Approach

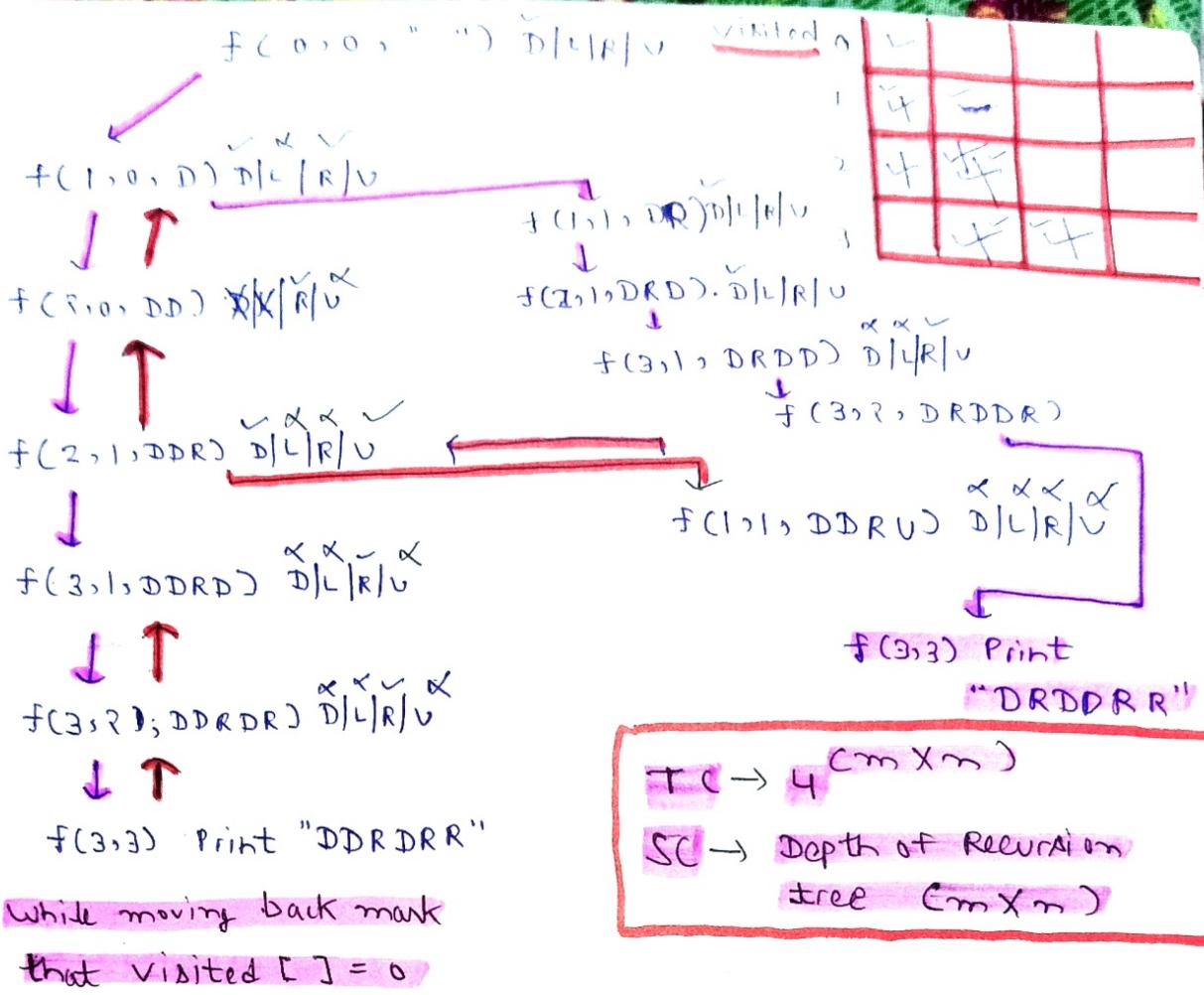
Note : Answer should follow Lexographical order

$D < L < R < U$

- ① we take visited Array for each block which is visited
- ② we travel all ways in all direcⁿ we can.
- ③ we will follow lexic. order i.e $D < L < R < U$
- ④ whenever we take a path make visited[Path] = 1 as we can visit one mode only one time

	0	1	2	3
0	1	0	0	0
1	1	1	0	1
2	1	1	0	0
3	0	1	1	1

4x4



Pseudo code

① we will write code for each direction D, L, R, U and recursion will work in each one of it.

② while going

UP → i - 1

Down → i + 1

Left → j - 1

Right → j + 1

we check visited [U|D|L|R][i|j] each time if its 0 and mage[U|D|L|R][i|j] == 1

then mark visited [] [] == 1

Recursion call

visited [] [] == 0 // backtrack step

CODE

```

void solve(int i, int j, vector<vector<int>> &m, int n, vector<string>
&ans, vector<vector<int>> &vis, string motion)
{
    if (i == m - 1 && j == n - 1)
    {
        ans.push_back(motion);
        return;
    }

    // Downward means i+1
    if (i + 1 < n && !vis[i][j] && m[i + 1][j] == 1)
    {
        vis[i][j] = 1;
        solve(i + 1, j, m, n, ans, vis, motion + 'D');
        vis[i][j] = 0;
    }

    // Left means j-1
    if (j - 1 >= 0 && !vis[i][j - 1] && m[i][j - 1] == 1)
    {
        vis[i][j] = 1;
        solve(i, j - 1, m, n, ans, vis, motion + 'L');
        vis[i][j] = 0;
    }

    // Right means j+1
    if (j + 1 < n && !vis[i][j + 1] && m[i][j + 1] == 1)
    {
        vis[i][j] = 1;
        solve(i, j + 1, m, n, ans, vis, motion + 'R');
        vis[i][j] = 0;
    }

    // Upward means i-1
    if (i - 1 >= 0 && !vis[i - 1][j] && m[i - 1][j] == 1)
    {
        vis[i][j] = 1;
        solve(i - 1, j, m, n, ans, vis, motion + 'U');
        vis[i][j] = 0;
    }
}

vector<string> findPath(vector<vector<int>> &m, int n)
{
    vector<string> ans; vector<vector<int>> vis(n, vector<int>(m, 0));
    if (m[0][0] == 1)
    {
        solve(0, 0, m, n, ans, vis, "");
    }
    return ans;
}

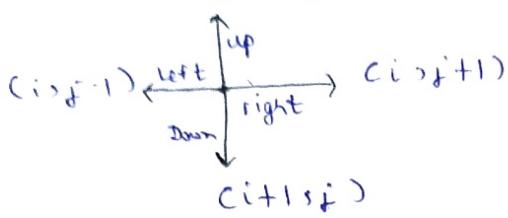
```

Simpler Code

$di[] = \{1, 0, 0, -1\}$

$dj[] = \{0, -1, 1, 0\}$

$(i-1, j)$



	D	L	R	U
di[i]	+1	+0	+0	-1
dj[i]	0	-1	+1	+0

CODE

```

void solve( int i, int j, vector<vector<int>> arr, int m, vector<string>
&ans, vector<vector<int>> &vis, string motion, int di[], int dj[])
{
    if (i == m - 1 && j == m - 1)
    {
        ans.push_back(motion);
        return;
    }
    string direction = "DLRV";
    for (int index = 0; index < 4; index++)
    {
        int nexti = i + di[index];
        int nextj = j + dj[index];
        if (nexti >= 0 && nextj >= 0 && nexti < m && nextj < m
            && !vis[nexti][nextj] && arr[nexti][nextj] == 1)
        {
            vis[i][j] = 1;
            solve(nexti, nextj, arr, m, ans, vis, motion +
                direction[index], di, dj);
            vis[i][j] = 0;
        }
    }
}

vector<string> searchmaze( vector<vector<int>> &arr, int n)
{
    vector<string> ans;
    vector<vector<int>> vis(n, vector<int>(n, 0));
    int di[] = {1, 0, 0, -1};
    int dj[] = {0, -1, 1, 0};
    if (arr[0][0] == 1)
    {
        solve(0, 0, arr, n, ans, vis, "", di, dj);
    }
    return ans;
}

```