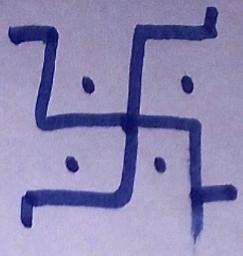


सत्य श्री राम



PLACEMENT

PREP

BEGINS

2020 - 2024

## Lecture 1

(1/4/23)

- ① Understand prob
- ② check given values
- ③ Move towards approach (Divide & Solve)
- ④ Make program of that approach

Pseudo code / flowchart



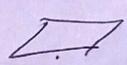
program (HLL) (source code)



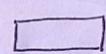
Machine understandable code

Flowchart

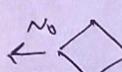
→ terminator (start / end)



→ i/o ke liye



→ processing



→ Decision making

↓ yes

↓ ↑ → Arrows (flow to connect components)



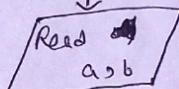
→ connector

Q Sum of 2 no. flowchart

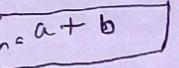
$$a = 5, b = 10$$

$$\text{sum} = a + b = 5 + 10 = 15$$

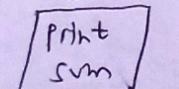
(start)



↓



↓



↓

end

Pseudocode

way of representing code  
which is generic and not  
any language specific.

just code in english language

— x — x — x — x —

① Read 2 no's a and b

② Sum = a + b

③ print sum

or

① read a

② read b

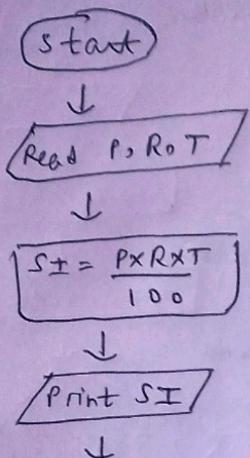
③ let sum = 0

④ sum = a + b

⑤ print sum

Pseudocode / flowchart

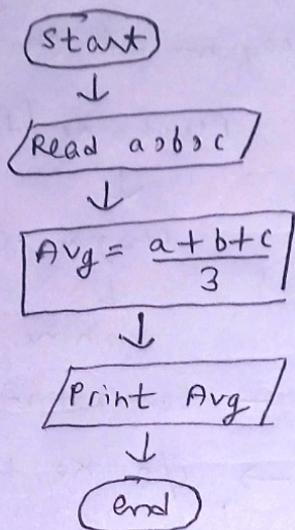
$$SI = \frac{P \times R \times T}{100}$$



for simple interest

flowchart for avg of 3 no.

$$\text{avg} = \frac{a+b+c}{3}$$

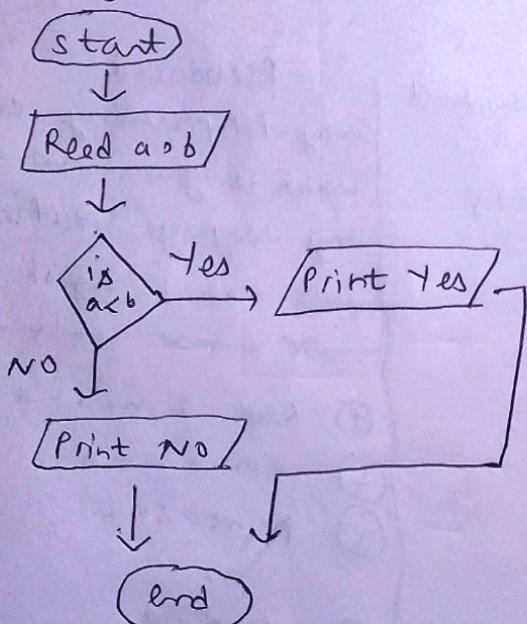


check  $a < b$  or not

print yes else no

i/p  $\rightarrow$  a, b

o/p  $\rightarrow$  yes or no



Pseudocode

① Read a, b

② if  $a < b$

    Print Yes

else

    Print No

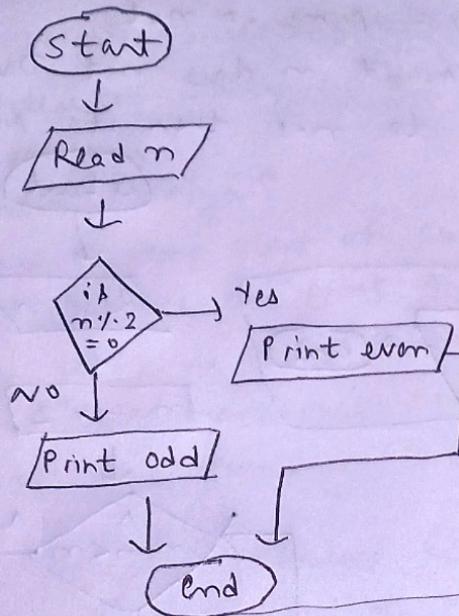
check given no. is odd or even

no.  $n \% 2 == 0$  means even

no.  $n \% 2 != 0$  means odd

$\% \text{ operator} \rightarrow \text{remainder}$

(modulo operator)



valid triangle or not

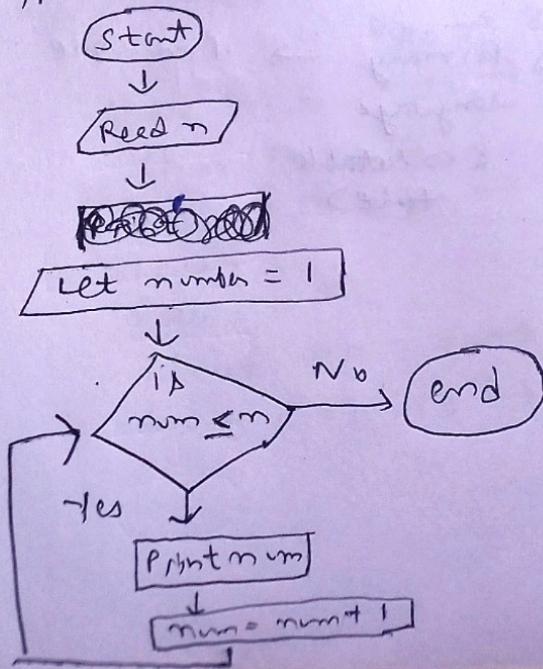
$$a+b > c, b+c > a, c+a > b$$

is our condition

Loops

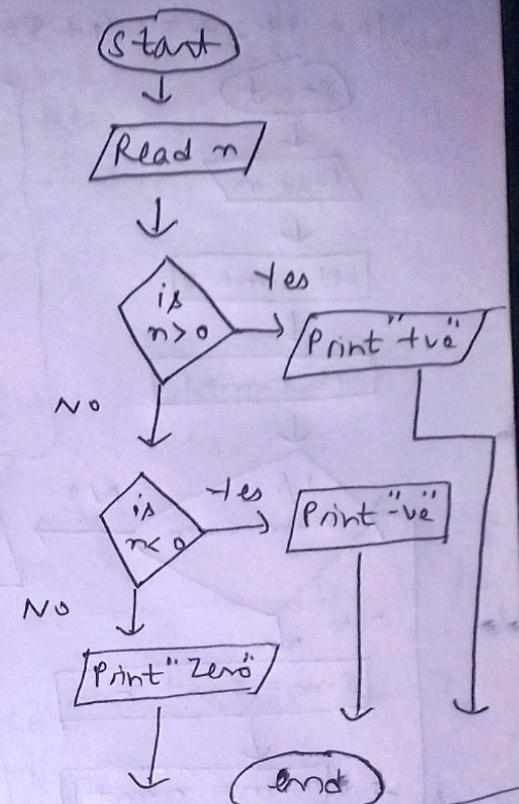
print 1 to N where N = given

i/p  $N = 5$   
o/p  $1, 2, 3, 4, 5$



check given no. is true or

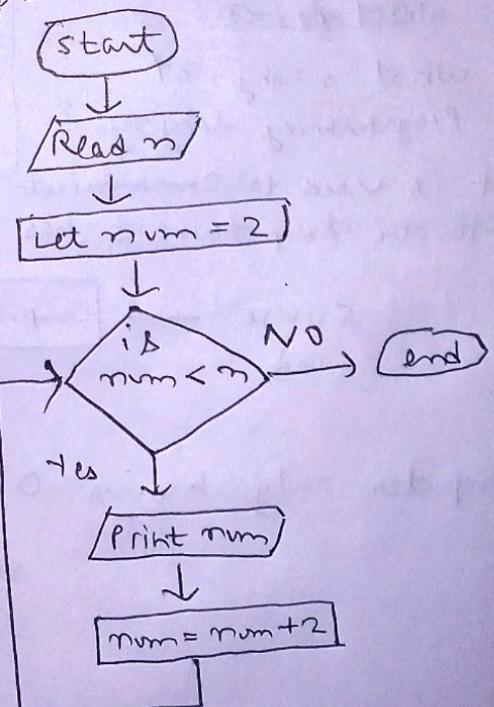
-ve or zero

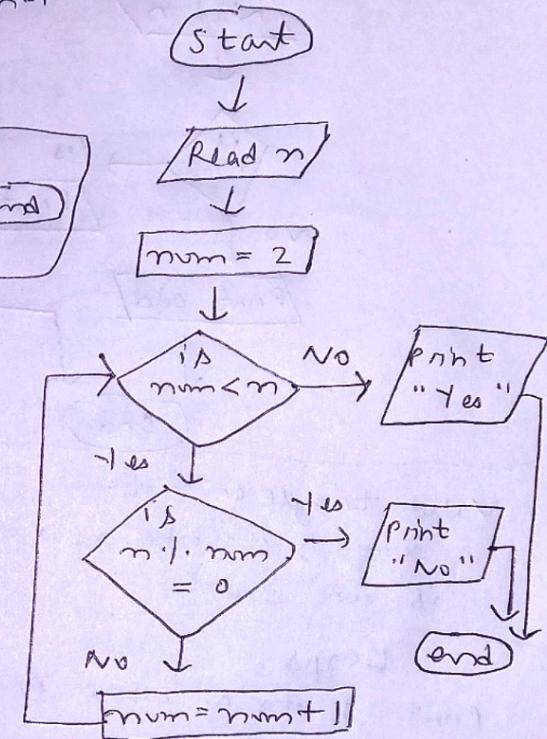
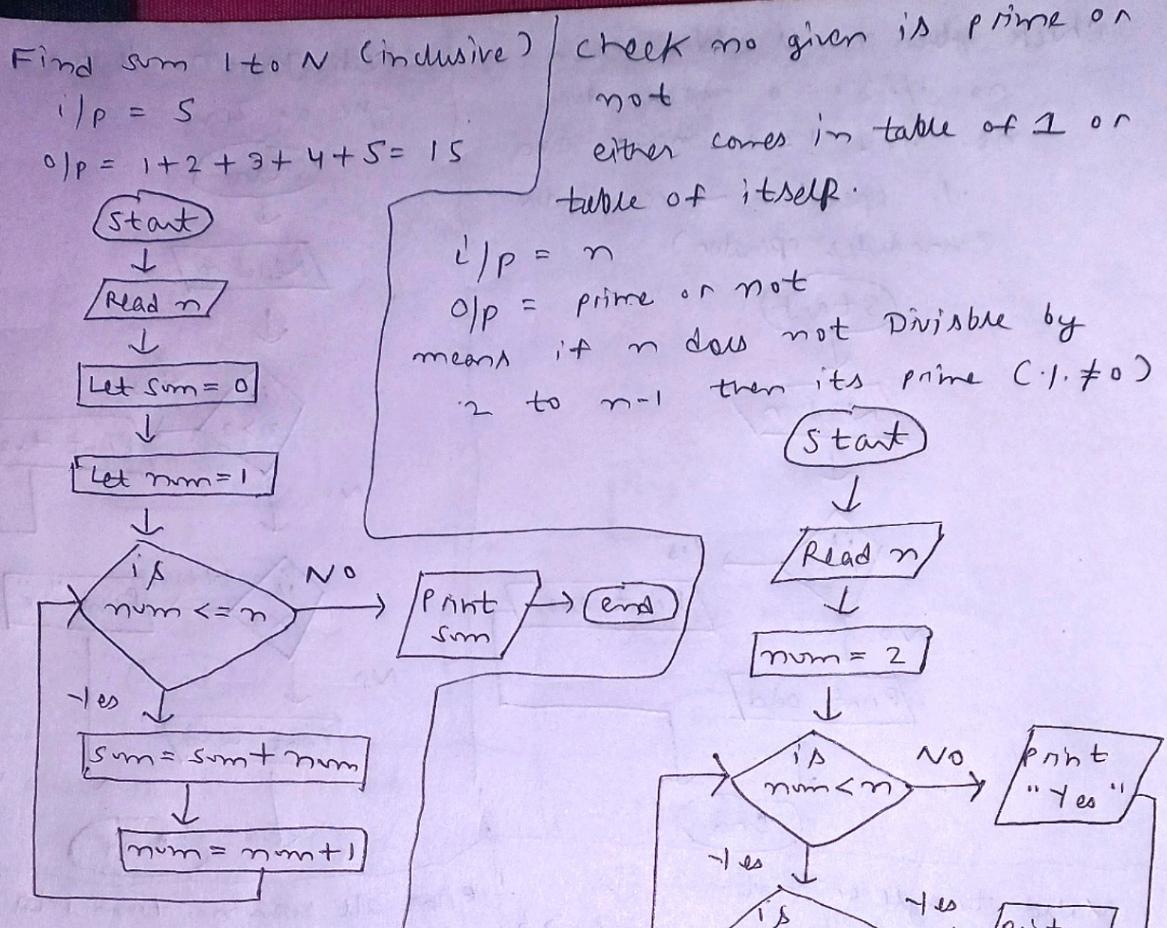


print all even no. from 1 to N

i/p = n

o/p = all even no. b/w 1 to n





~~Lecture 2~~

what's why of  
 Programming language?

It is used to communicate  
 with the computer, it has some rules or semantics

source code  $\rightarrow$  Compiler  $\rightarrow$  Binary language  $\rightarrow$  Run code  
 (executable file)

Computer only knows 0 or 1

## Lecture 2

→ Getting started

Made SRC code using any programming language  
Comp only understand binary language (0 or 1) for that we need  
Compiler then Comp runs or executes that file.

Compiler helps in Translation, error finding

IDE (Integrated Development environment)

→ first program

"Namaste Duniya"

→ There should be some start of code (which is int main())

→ Using cout, we can print anything in C++.

→ To use cout, we need to include Header file

→ We write "using namespace std;" to say, we want to

use std vala namespace as their are many namespaces in

C++.

→ endl means newline (Put cursor to next line)  
printing newline. Or can use "\n"

→ ";" semicolon is used to end the line just like we  
use fullstop(.) in English literature.

→ Data types and variable

To store anything in C++ we need to tell its type so  
that its size can be estimated.

int a  
↓ ↓  
type variable

int → 4 byte → 32 bit

char → 1 byte → 8 bit

char ch = 'a';

bool → 1 byte → 8 bit

True, 1

False, 0

float f = 1.2 → 8 byte

double d = 1.23 → 8 byte

(depend compiler to compiler)

→ There are some rules or convention for variable naming but never put number in starting of variable naming.

int a = 123 ; ✓

int 2a = 123 ; ✗

char a = 'v' ; ✓

→ sizeof() operator to get size of a variable

→ How data stored in memory?

int a = 8 ;

↓  
convert to binary  
(1000)

↓  
0000    0000    0000    1000 (32 bit)

for -ve number?

char ch = 'a'

ASCII values of a = 97

65 - 90 is A - Z

97 - 122 is a - z

→ Type casting (Converting one type of another type)

int a = 'a';

cout << a << endl; o/p = 97

char ch = 98;

cout << ch; o/p = b

integer = 4 byte means 32 bit

max value that can be stored =  $2^{32} - 1$

min value = 0

for char = 1 byte = 8 bit

max value =  $2^8 - 1$

min value = 0

How -ve no. are stored

- ① first bit shows no. is +ve or -ve  
+ve  $\rightarrow$  0, -ve  $\rightarrow$  1

- ① ignore -ve sign
  - ② convert left over thing to binary
  - ③ Take 2s complement and store  
2s comp means first take 1s comp ( $0 \rightarrow 1s, 1 \rightarrow 0$ )  
now add 1 to it

```
int a = -5;
```

$$0 \text{ means } -\infty \\ \text{so print} = -5$$

$$2^{31} - 1 \rightarrow -(2^{31} - 1)$$

$2^{31} - 1$  to  $-(2^{31} - 1)$   
 but 0 and -0 is same so why do we rep  
 it in 2 ways so to save this, we use 2s comp method  
 → default we can store both +ve or -ve in int but  
 unsigned int → only +ve no. (range has increased)

unsigned int a = 111; cout = 111

unsigned abc = 111;      0/p = 111  
                          -111;      0/p = 4294967285

unsigned abc = -11; o/p = 489, -  
by default int has signed value i.e both + or -  
can be stored.

operator

$\therefore \rightarrow$  modulo  $^{opp}$

Arithmetic  $\rightarrow +, -, \times, /$

Arithmetical operators

`int | int = int`

float / int = float

float | int = var  
double | t = double

double | int = double

→ Relational operator  
=, >, <, ≥, ≤, !=

→ Logical operators  
&&, ||, !

→ Bitwise operator

8, |, ^, <<, >>, ~

## Lecture 3

## Conditionals & loops

## Conditionals

```
if (a > b)  
{    cout << "a" ;
```

]

if ( $b > a$ )

```
{     cout << "b";
```

3

if-else block

if ( $a > 0$ )

```
    }  
else {  
    print mat +ve
```

3

## Loops

→ while loop

5

Pattern print

6

② check no. of col in  
each row

③ make relation b/w each row & col. based on P.D.W.

→ cin does not read tab '\t',  
" " = " space", "\n" enter

→ `cin.get();` reads everything whether its space, tab, anything for input.

```
if(c) {  
    if(c) {  
        }  
    if(c) {  
        }  
    if(c)  
    }  
}  
if(c) {  
    }  
else {  
    }  
}  
if(c) {  
    }  
else if(c)  
    }  
else {  
    }  
}  
}
```

# Lecture 4

## Pattern Print

① 1 2 3 4  
1 2 3 4  
1 2 3 4  
1 2 3 4

② 3 2 1  
3 2 1  
3 2 1

③ 1 2 3  
4 5 6  
7 8 9

row = 3

col = 1

Take count

④ X  
X X  
X X X  
X X X X

⑤ 1 2 2  
3 3 3  
4 4 4 4

⑥ 1  
2 3  
4 5 6  
7 8 9 10

⑦ 1  
2 3  
4 5 5  
4 5 6 7

⑧ 1  
2 1  
3 2 1  
4 3 2 1

⑨ A A A  
B B B  
C C C  
⑩ A B C  
A B C  
A B C

⑪ A B C  
B C D  
C D E

⑫ A  
B B  
C C

⑬ A  
B C  
D E F  
G H I F

⑭ A  
B C  
C D E  
D E F G

⑮ D  
C D  
B C D  
A B C D

⑯ \*  
XX  
XX X  
XXX  
XXXX  
space + star

⑰ XXXX  
XXX  
XX  
X

⑱ XXXX  
XX X X  
XX X  
X

MPL  
⑲ 1 1 1  
1 2 2  
1 2 3  
1 2 3 4  
1 2 3 4  
1 2 1  
2 1 1  
3 2 1  
3 2 1

question has  
3 parts

Day 2

Lecture 5

(2 Apr 2023)

Operator & loop

Bitwise operator

AND  $\rightarrow \&$ OR  $\rightarrow |$ NOT  $\rightarrow \sim$ XOR  $\rightarrow ^n$ 

All work in level of bits

X	Y	Z
0	0	0
0	1	0
1	0	0
1	1	1

$a = 5 \rightarrow 101$

$b = 7 \rightarrow 111$

$a \& b \rightarrow 101 = 5$

OR operator ( $\oplus$ )

X	Y	Z
0	0	0
0	1	1
1	0	1
1	1	1

$a = 2 \rightarrow 10$

$b = 4 \rightarrow 100$

$a \oplus b \rightarrow 110 = 6$

$a = 3 \rightarrow 11$

$b = 6 \rightarrow 100$

$a \oplus b \rightarrow 111 = 7$

## (NOT)

X	Z
0	1
1	0

$a = 2 \rightarrow 10 \rightarrow 0000\ldots0010$

int = 4 byte = 32 bit

$\sim a = 111\ldots1101$

How to print  $\sim a$ 

$\sim a = 111\ldots1101$

means -ve

take 2's comp of

$-111\ldots1101$

~~but~~~~Opposite of 1's comp~~

$$\begin{aligned} s_{comp} &= -000\ldots0010 \\ &\quad +1 \\ &= -00\ldots0011 \\ &= -3 \end{aligned}$$

XOR (Dono mai se ek 1)

X	Y	Z
0	0	0
0	1	1
1	0	1
1	1	0

$a = 2 \rightarrow 10$

$a = 5 \rightarrow 101$

$b = 4 \rightarrow 100$

$b = 7 \rightarrow 111$

$a \oplus b = 110$

$a \oplus b = 010$

To get 2A comp we get 1s comp first then add +1 in it.

$a = 4 \rightarrow 100$

$b = 6 \rightarrow 110$

$a \oplus b = 011 = 3$

(Left Shift opp)

$5 \ll 1$

$000 \dots 101 \ll 1$

$0000 \dots 1010 = 10$

$3 \ll 2$

$0000 \dots 11 \ll 2$

$000 \dots 1100 = 12$

$a \ll b$

Shift bits of a by b steps  
bit = 1

Set bit means left shift becomes  
any bigger or

-ve no.

$0100 \dots 0010 \ll 1$

$\frac{1000}{\downarrow} \dots 0100$

Show -ve

(Right Shift opp)

$15 >> 1$

$5 >> 2$

$000 \dots 00101 >> 2$

$000 \dots 00001 = 1$

$5 >> 1 \rightarrow 5/2$

$5 >> 2 \rightarrow 5/2 \times 2$

\* On shifting +ve no. padding  
is done with 0 i.e extra bit  
added on shifting either side is

\* On shifting -ve no., padding  
is compiler dependent.

(Inc | Dec operator)

$i++ \rightarrow$  post inc

$+i \rightarrow$  pre inc

$i-- \rightarrow$  post dec

$-i \rightarrow$  pre dec

$i++ \rightarrow$  use krne ke baad  
mai badha dunga

int  $i = 3, a = 2$

$sum = a + (i++)$

$= 2 + 3 = 5$

but now  $i = 4$

phle purani value use krdo

then inc krdo

$++i \rightarrow$  phle increment phir

use karao

int  $i = 11$

int  $a = ++i = 12$

$a = 2, i = 3$

$sum = a + (++i)$

$= 2 + 4$

$= 6$

someway  $i--$ ,  $--i$  are  
used.

(For loop)

for (int  $i = 0$ ;  $i < n$ ;  
initialisation      condition)

$i++$

updation

{

}

ini, cond, upd nothing  
is necessary we can also  
write it like

for ( $i$  ; )

{

}

but it will run into a  $\infty$   
loop as this for loop does  
not know when to stop.

### (Break)

we can stop this loop using  
break keyword.

```

for ( _____; _____; _____) {
    {
        _____
    }
}

```

### Fibonacci Series

0, 1, 1, 2, 3, 5, 8, 13, ...

$$n = (n-1) + (n-2)$$

```

int a = 0
int b = 1
cout << a << b
for (i=1; i<=n; i++) {
    int next = a+b;
    a = b;
    b = next;
    cout << next;
}

```

### ~~else if~~ Precedence

#### (Continue)

skip a particular iteration  
in the loop.

### (Variable & Scope)

- ★ Declare a variable before using it.
- ★ Without assignment any ~~not~~ garbage value will be assigned to that variable.
- ★ Anything b/w {} will have block scope

★ we cannot redefine any variable.

★ we cannot declare variable of same name inside same block twice.  
but its valid for block inside block.

```
if (true) {
```

```
    int c = 10;
```

```
    if (true)
```

```
{ int c = 11;
```

```
    cout << c << endl;
```

```
    // 11
```

```
}
```

but if we remove it

```
cout << c = 10
```

★ if variable is not found inside block then it will be searched outside whether it declared anywhere else outside or not.

### (Operator Precedence)

★ Use bracket

★ Do not cram table

Q Leetcode Problem

To get last digit of no.  
=  $\text{num} \% 10$

To remove that no. from

Digit =  $\text{num} / 10$

Go on till num ≠ 0

Q Get no. of '1' bits  
in any unsigned integer

\* check last bit and right  
shift by 1 everytime  
till no. becomes 0

\* To check last bit we  
do  $m \& 1$  as

$$1 \& 1 = 1$$

$$0 \& 1 = 0$$

So by  $m \& 1$  we will get  
whether last bit is 0 or 1

## Lecture 6

(Binary & Decimal  
Number System)

Decimal = 1, 2, 3, 4, ...

Binary = 0 or 1

Logic for conversion

①  $m = 10$

→ Divide by 2

→ store remainder

→ repeat above step till  $m = 0$

→ reverse the answer left

$m = 10$

~~+ 0 + 2 = 0~~

Div	Rem
$10/2 \rightarrow 5$	0
$5/2 \rightarrow 2$	1
$2/2 \rightarrow 1$	0
$1/2 \rightarrow 0$	1

$$\text{ans} = 0101$$

now reverse the ans = 1010

②  $m = 7$

Div Rem

$$7/2 = 3 \quad 1$$

$$3/2 = 1 \quad 1$$

$$1/2 = 0 \quad 1$$

$$\text{ans} = 111$$

$$\text{reverse} = 111$$

Binary of 7 = 111

$$1 + 1 + 1 = 7$$

(Another logic)

$$m = 5, 101$$

Binary rep of 5 ?

num & 1 = 1 means odd  
else its even

while( $m \neq 0$ )

{ bit =  $m \& 1$ ; // get rightmost bit

$m = m \gg 1$ ; // Right shift

} int ans = 0

Digit = 1 on  $m \& 1, m \gg 1$

= 0 on  $m \& 1, m \gg 1$

= 101 on  $m \& 1, m \gg 1$

answer =  $(10^0 \times \text{digit}) + \text{answer}$

answer =  $(10^1 \times \text{digit}) + \text{answer}$

answer =  $(10^2 \times \text{digit}) + \text{answer}$

★ If we want to make a no. in same flow i.e

1, 2, 3 given

we want 123

ans = 0 // initialise

ans = (ans \* 10) + digit

★ If we want to make reverse in same flow i.e

1, 2, 3 given

we want = 321

ans = 0

run loop for i = 0 to n

ans = (digit \* 10<sup>i</sup>) + ans

★ Convert binary of no. m

int ans = 0; i = 0;

while (m != 0)

{ int digit = m & 1;

ans = (digit \* pow(10, i))

+ ans;

m = m >> 1;

i++;

}

cout << ans

★ Find Binary of -6

① ignore -ve sign

② Find 2's comp of 6  
i.e 1's comp + 1

★ Binary to Decimal

1 0 1 0 1

$2^4 * 2^3 * 2^2 * 2^1 * 2^0$

if our bit is 1 then consider that '2 ki power' else if its 0, do not consider '2 ki power anything'

```
n = 110
while (n != 0)
{
    bit = n > 1
    if (bit == 1)
    {
        ans = ans + (bit * 2i)
        i++;
    }
}
```

// Code

```
int ans = 0; j = 0;
int m's // in binary i/p
while (m != 0)
```

```
{ int dig = m & 1;
if (dig == 1)
{ ans = ans + pow(2, j);
```

}

m = m / 10;

j++;

}

cout << ans;

★ if we are working on bit level

a) we get last bit

b) we Right shift

★ if we work on digit

level

a) get last digit by .1.10

b) Remove last digit by /10

## Lecture 7

### Leetcode Problem solving

#### ① Reverse Integer

Normal  $\rightarrow$  123  
 $\downarrow$   
 321

If range exceeds return 0

- ① get last digit by  $\cdot 1 \cdot 10$
- ② ans = ans  $\times 10 +$  last digit
- ③ Remove last digit by

$num / 10$

- ④ Repeat above steps till

$m != 0$

now if value > limit then

return 0.

Range =  $[2^{31}, 2^{31}-1]$   
 $\downarrow$   
 INT\_MIN INT\_MAX

if (ans > INT\_MAX)

$\mid 10$

ans < INT\_MIN)

$\mid 10$

{ return 0;

}

- ② Complement of base 10 integer

$n = 5 \rightarrow 101$

$\sim n \rightarrow 010 = 2$

return complement of 5

$n = 7 \rightarrow 111$

$\sim n \rightarrow 000 = 0$

① we need to play with bit

② complement the bits

③ append them in a integer

④ Return that integer.

$n = 5 \rightarrow 0000 \dots 0101$

$\sim n \rightarrow 1111 \dots 1010$

We need a mask to remove

$\Sigma \dots 1 \dots 13$  part

$\sim n \& \text{mask}$

where mask = 0000...0111

then we can achieve the result

- ① To create mask we

first remove last bit

till  $num != 0$

- ② now left shift by 1

- ③ now OR by 1 to attach 1 at the end

{ int m = m;

int mask = 0;

ans = 0;

while ( $m != 0$ )

{ mask = (mask << 1) | 1;

$m = m >> 1$ ;

ans = (ans) & mask;

return ans;

}

### ③ Power of Two

Given any no. tell its True or False based on if its power of 2 or not.

We check from  $2^0$  to  $2^{30}$   
if any one == n return true

as constraint is that

$$2^{-31} \leq n \leq 2^{31}-1$$

(Code)

```
{ int ans = 1;
for(i=0; i<= 30; i++)
{
    if (ans == n)
        { return true;
    }
    if (ans < INT_MAX/2)
        { ans = ans * 2;
    }
}
return false;
}
```

### (Lecture 8)

Switch case & functions

① In switch case default case is not necessary

② Case '  
'

this take int/char but it does not take float/string in switch case

③ Break is important after every case in switch

④ we can write multiple statement inside a case in switch case.

⑤ we can put another switch inside any particular case of a switch case.

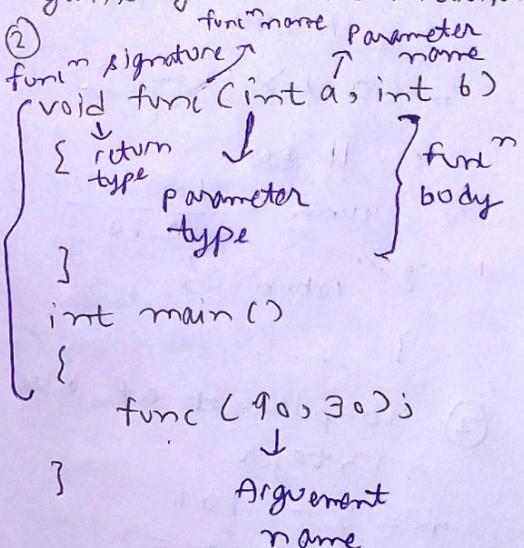
⑥ if-else-if ladder can be converted to switch.

⑦ if we have a switch case inside a loop and we want to get out of a loop by writing one statement inside switch then it will be exit().

⑧ 'continue' inside switch is not valid.

### (Functions)

① To avoid repetition we use functions. To avoid writing same piece of code again & again we use functions.



Function call stack

Stack = Shadi ki plates.  
(Last In First Out)

PrintCount()

printPrime()

Factorial()

n(r,l)

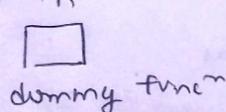
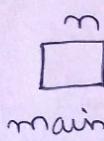
main()

Aapna Kadam hote hi func<sup>n</sup> will  
be out of call stack

(Pass by Value)

The way we pass normally  
is pass by value i.e. value  
will not be updated in

main : (both are different)



dummy func<sup>n</sup>

If we pass m=16 from main  
and make m=12 in dummy, m  
will change only in dummy not  
in main.

Copy of m will be passed to  
dummy, not the original one

(Lecture 9)

(Day 3) (3 April 2023)  
(Arrays)

Array is like a container  
in which we can store variables  
of same type. all element  
should be of same type although  
it can be of type but all same.  
(similar type of item)  
at contiguous memory location  
we can access any element through  
its index.

Indexing starts from zero.

v[0] = first element of array ✓

int v[10];

v[1] = second element of array ✓

if size of array = n

index will go from 0 to n-1

(Initialization)

int a[3] = {5, 7, 11}

or

int a[1000] = {0}

(How to initialise entire array  
with same value?)

int a[5] = {[0...4] = 1};

or

int a[] = {[0...4] = 1};

(How to get no. of element or size  
of an array?)

int n = sizeof(arr) / sizeof(int)

- ★ Uninitialised Array will have default value = 0
  - ★ while passing array as parameter of funcn, mentioning size is not important.

\* Size of array =  $\frac{\text{size of Carr}}{\text{size of (int)}}$

but if size of 15, but it has  
only 2 element initialised then  
this formula will give size=15  
not size=2 so we pass size as a  
parameter to a function also.

★ int arr[~~size~~] ~~xx~~ (BAD)  
int arr[100000] ✓  
always put no. in size never give  
variable.

\* `max()` and `min()` are 2 predefined funcn to find maximum & minimum element of an array

\* (Scope in array)  
actual / original array is passed as  
a parameter to a func<sup>n</sup> whenever  
we pass array as a parameter.  
Any change made inside func<sup>n</sup> to  
array will be reflected in actual  
array also.

\* void func (int arr[])

main ( )  
{ fun (arr) ;  
    }  
} This means we are passing  
address of first block of array  
to fun n so any change made  
will be updated in original  
array also.

## Searching inside Array

## ★ Linear Search.

## ★ Reversing the array

just start = 0

$$\text{end} = \text{size} - 1;$$

while ( $\text{start} < \text{end}$ )

[ Swap (arr[Start],  
arr[End]) ;

`i++;`  
`i--;`

## (Lecture 10) /

### ① Swap Alternate

```
i/p arr[5] = {1, 2, 3, 4, 5}
o/p = {2, 1, 4, 3, 5}

i/p arr[6] = {1, 2, 3, 4, 5, 6}
o/p = {2, 1, 4, 3, 6, 5}

for(i=0; i < size; i++)
{
    if(i+1 < size)
    {
        swap(arr[i], arr[i+1]);
        i++;
    }
}
```

### ② Swap two numbers without using library

we need a dummy variable.

```
temp = arr[1]
arr[1] = arr[0]
arr[0] = temp
```

### ③ Find Unique

1, 3, 4, 1, 3

① Count all numbers and form a Hash table

② XOR,  $a \wedge a = 0$   
 $0 \wedge a = a$

### ④ Find Duplicates in an array

```
int ans = 0
for(i=0 → size)
{
    ans = ans ^ arr[i];
}

for(i=1 → size)
{
    ans = ans ^ arr[i];
}

return ans;
```

### ⑤ Intersection of Arrays

Intersection means resultant array has common element from both arrays

Given: arrays are sorted in non-decreasing order  
if no int present return -1.

```
i/p arr1 = {1, 2, 3}
arr2 = {3, 4}
o/p = {3}
```

① pick every element from arr1 and check in arr2.  
and print common elements.  
but before break change value of that element in arr2.  
so that it does not gets mapped again. (TLE)

② elements are already sorted in inc order so

```
if arr1[i] < arr2[j]
    break;
```

③ (TLE)

④ 1, 2, 2, 2, 3, 4 = arr1

2, 2, 3, 3 = arr2

~~arr1[i] < arr2[j]~~

↓  
i++

arr1[i] == arr2[j]

↳ print  
i++, j++;

arr1[i] > arr2[j]

↳ j++;

[2 pointer approach]

### ⑥ Pair Sum

Find pairs whose sum = S

Given: sum S, return answer in a vector and each pair should be in sorted order.

⑦ for ( $i=0 \rightarrow m-1$ )

{ for ( $i+1 \rightarrow m-1$ )

{ if ( $arr[i] + arr[j] == S$ )

{ // store ans in

{ $\min(C), \max(C)$ }

}

}

}

11 Return all pairs in sorted order of their first values.

sort (C);

return;

for ( $i=0 \rightarrow m-1$ )

{ for ( $j=i+1 \rightarrow m-1$ )

{ if ( $arr[i] + arr[j] == S$ )

{ temp.push( $\min(arr[i], arr[j])$ )

temp.push( $\max(C)$ );

ans.push(temp)

}

}

sort (ans.begin(), ans.end());

return ans;

}

⑧ Triplet with given sum  
Find triplet whose sum is equal to target.

① Use 3 loops

for ( $i=0 \rightarrow m-1$ )

{ for ( $j=i+1 \rightarrow m-1$ )

{ for ( $k=j+1 \rightarrow m-1$ )

{ if ( $arr[i] + arr[j] + arr[k] == S$ )

{

}

}

}

### ⑨ Sort 0 1

Put all zeroes at one side and all 1's at other side.

I/p: 0 0 1 0 1 0 0 0 1

O/p: 0 0 0 0 1 0 1 1 1

⑩ 2 pointer approach

if ( $arr[i] == arr[j]$ )

{ i++;

}

if ( $arr[i] != arr[j]$ )

{ swap

{

- x - x - x - x -

int l = 0, r = n-1;

while (l <= r)

{ while ( $arr[l] == 0$ )

{ i++;

}

while ( $arr[r] == 1$ )

{ j--;

}

`swap(arr[i], arr[n]);`  
`i++, n--;`

}  
 Don't forget to check  
 ( $\text{left} < \text{right}$ ) in all 3  
 Conditions.  
~~— x — x — x — x —~~

### Lecture 11

Time & Space Complexity  
 amt of time taken by an algo  
 as funcn of length of i/p.  
 How to say a algo is good or  
 bad?  
 Based on its Time complexity.

Let say we run any slow algo  
 in fast machine and fast algo in  
 slow machine then its unfair.  
 Time Comp is metric for any algo  
 to be called as optimised.

Big O (upper bound) (Hadd se  
 Hadd itna time legi)



Theta O (for average case comp)



Omega  $\Omega$

O (Kam se Kam) (lower bound)

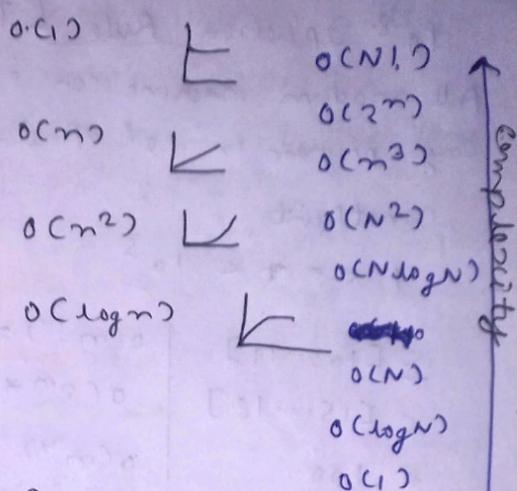
Constant time  $\rightarrow O(1)$

Linear  $\rightarrow O(n)$

Log time  $\rightarrow O(\log n)$

Quadratic time  $\rightarrow O(n^2)$

Cubic time  $\rightarrow O(n^3)$



### Rules

- ① lower degree is always ignored
- ② Constant are always ignored

$$4n^4 + 3n^3 = O(n^4)$$

$$3n^3 + 2n^2 + 5 = O(n^3)$$

$$1200 = O(1)$$

$$\frac{n^3}{500} = O(n^3)$$

$$\frac{n+4}{4} = O(n)$$

- ③ Bahar ek loop Hai then

use +

for ( ) { }  $\Rightarrow O(n)$

for ( ) { }  $\Rightarrow O(n)$

{ }

$$\text{then } O(n+n) = O(n)$$

ek ke andar ek loop Hai

then use \*

for ( ) { }  $\Rightarrow O(n)$

{ for ( ) { }  $\Rightarrow O(n)$

{

}

{ then  $O(n * n) = O(n^2)$

## $10^8$ operation Rule [TLE]

All modern machine can execute any program in  $10^8$  operation /second

Constraints

$$1 \leq n \leq 10^5$$

$$\leq [10 \dots 11]$$

$$O(n!) \Rightarrow O(n^6)$$

$$< [15 \dots 18]$$

$$O(2^n * n^2)$$

$$< 100$$

$$O(n^4)$$

$$< 400$$

$$O(n^3)$$

$$< 2000$$

$$O(n^2 * \log n)$$

$$< 10^4$$

$$O(n^2)$$

$$< 10^6$$

$$O(n \log n)$$

$$< 10^8$$

$$O(n), O(\log n)$$

## Space Complexity

Extra space taken by our algo as function of length of i/p.

\* Variable do not contribute to SC  $\Theta(1)$

\* int arr[5]; // SC:  $O(1)$   
as array is of fixed size

\* int arr[n];  
 $cin >> n$   
// SC:  $O(n)$

\* for loop running n times do not contribute to SC  $\Rightarrow$  it only contribute to TC

## Lecture 12 Binary Search

→ we have already studied linear search

→ we use it for finding a key in an Array

→ Linear search takes  $O(n)$  complexity

→ Binary Search takes  $O(\log n)$   
so it is optimised things used for searching in an Array. (Condition of AS)

→ Binary search always work in monotonic funcn (i.e all rising or all falling order)

- 1) Find mid element of Array
- 2) Compare mid ele with key
- 3) if no, then
  - (possibly) we take either left or right part of mid element and again find its mid.

- 4) Again compare with key if (arr[mid] == key)  
{ return mid; }

$$\begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 \\ 3, 7, 11, 13, 19, 27 \end{matrix}$$

Key = 27

$$\text{mid} = \frac{0+5}{2} = 2, \text{ele} = 11$$

$(11 \neq 27) \Rightarrow 27 > 11 \Rightarrow$  go

in  $\underbrace{3, 4}_{\text{point}}, 5$   
 $13, 19, 27$

$$\text{mid} = 19 \neq 27$$

$$19 < 27$$

$$27$$

$$\text{mid} = \frac{5+5}{2} = 5$$

$$\text{mid} == \text{key}$$

return 5;

4, 8, 16, 22, 34    key = 4  
 0 1 2 3 4

$$\text{mid} = \frac{0+4}{2} = 2, \text{ele} = 16$$

$$16 \neq 4$$

        |  
        4, 8

$$\text{mid} = \frac{0+1}{2} = 0$$

$$4 == 4$$

return 0; // index

5) if Key is not found we return -1.

5, 11, 13, 17, 19, 27    key = 25  
 0 1 2 3 4 5

$$\text{mid} = \frac{0+5}{2} = 2, \text{ele} = 13$$

$$13 \neq 25$$

        13, 19, 27  
        |  |  |  
        3  4  5

$$\text{mid} = \frac{3+5}{2} = 4, \text{ele} = 19$$

$$19 \neq 25$$

        27  
        |  
        5

$$\text{mid} = \frac{5+5}{2} = 5$$

27  $\neq$  25    // Array filled up

return -1; // ele not found

// code

```

    int start=0, end=n-1;
    while(start <= end)
    {
        int mid = (s+e)/2;
        while(s <= e)
        {
            if(arr[mid] == key)
            {
                return mid;
            }
            if(arr[mid] < key)
            {
                start = mid + 1;
            }
            else
            {
                end = mid - 1;
            }
        }
        mid = (s+e)/2;
    }
    return -1;
}

```

### Optimisation in BS

$$\text{mid} = \frac{s+e}{2}$$

We know int has range of  $2^{31}-1$

$$s = 2^{31}-1, e = 2^{31}-1$$

then  $s+e >$  range so

we need to change the formula

$$\left[ s + \left( \frac{e-s}{2} \right) \right] = \text{mid}$$

Complexity of BS =  $O(\log n)$

$$\begin{array}{c}
 \overbrace{\quad\quad\quad}^{\sim O \text{ or } \frac{N}{2^0}} \\
 \downarrow \\
 \overbrace{\quad\quad\quad}^{\sim \frac{N}{2^1}} \\
 \downarrow \\
 \overbrace{\quad\quad\quad}^{\sim \frac{N}{2^2}} \\
 \downarrow \\
 \vdots \\
 \overbrace{\quad\quad\quad}^{\sim \frac{N}{2^K}} = 1
 \end{array}$$

$$N = 2^K$$

$$\log N = K \log 2$$

$$\cancel{K} \cdot \underline{\log N} = K$$

$$\log 2$$

$$\boxed{\log_2 N = K}$$

## Lecture 13

### BS Questions

① First and last posn of an element in sorted array

Q/p: Left most and Right most occurrence of an element

i/p: size = 8

key = 2

Arr = {0, 0, 1, 1, 2, 2, 2, 2}

o/p: first occurrence = 4

last occurrence = 7

if ele do not exist return [-1, -1]

→ Sorted Array Search  
we can use Binary Search  
in  $O(\log n)$

First most      |      Last occurrence  
      acc                  2<sup>nd</sup> part  
      1st part

0, 1, 2, 3, 3, 3, 5      Key = 3  
          1    2    3    4

mid =  $4+0/2 = 2$ , ele = 3  
3 == 3      first occurrence can be  
at index = 2; let store it

now search for another 3 in left  
part of index = 2

so end = mid - 1 and  
store index = 2 for  
first occurrence.

```
if (arr[mid] == key)
{
    ans = mid;
    end = mid - 1;
}
```

// rest all same as  
BS other cases

Last occurrence  
just find the mid  
same as first occurrence  
store mid if  $= \text{key}$   
and start = mid + 1  
if (arr[mid] == key)  
{  
    ans = mid;  
    start = mid + 1;  
}

→ X — X — X —  
DRY RVN

1, 2, 3, 3, 3, 3, 3, 5  
0    1    2    3    4    5    6

Key = 3

mid =  $0+6/2 = 3$

ele = 3

ans = 3

for last occurrence we go  
to Right part of ind = 3

3, 3, 5  
4    5    6

mid =  $0+4/2 = 5$

ans == key, ans = 3

return 3.

→ X — X — X — X — X —

② Find total no. of  
occurrence of an ele in  
an sorted array

we know how to find  
first occurrence and last occur

Total no. = (last ind - first) + 1  
of occ

### ③ Peak Index in a Mountain Array

arr is mountain if arr.length  $\geq 3$

there exist ' $i$ '  $\rightarrow 0 < i < \text{arr.length} - 1$

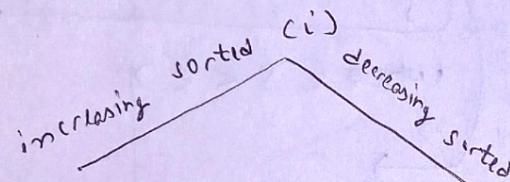
such that

$\text{arr}[0] < \text{arr}[1] \dots < \text{arr}[i]$

$\text{arr}[i] > \text{arr}[i+1] \dots > \text{arr}[n-1]$

Find that index  $i$  (Peak element)

0, 1, 0      |      0, 2, 1, 0



- 1) we can use LS but it take  $O(n)$
- 2) we will use BS, take  $O(\log n)$

i/p [3, 4, 5, 1]

mid =  $0 + 3 / 2 = 1$

ele = 4

{ if ( $\text{arr}[\text{mid}] < \text{arr}[\text{mid} + 1]$ )

{ start = mid + 1;

}

else { end = mid;

} not mid - 1 because our mid can be the peak element also.

}

mid =  $s + (e-s)/2;$

}

3, 4, 5, 1

0 1 2 3

$$\text{mid} = 0 + 3 / 2 = 1$$

$$\text{ele} = 4 < 5$$

$$\text{start} = 1 + 1 = 2$$

$$\text{ele} = 5$$

$$\text{mid} = 2 + 3 / 2 = 2$$

$$\text{ele} = 5$$

$$5 \neq 1$$

$$\text{end} = \text{mid} = 2 \quad \text{index}$$

$$\text{mid} = 2 + 2 / 2 = 2$$

$$2 \neq 1$$

so while ( $s \leq e$ ) ||  $s \leq e$  <sup>not</sup>  $e \leq s$

{

}

return s;

— x — x — x — x — x —

Lecture 14

Binary search Questions.

- ① Find pivot in an array.

pivot means where sum of all no. strictly to left of pivot = sum of all no. strictly to right of pivot.

if index is on left edge's meant left sum = 0, same for right edge return leftmost pivot index.  
return -1 if no such thing exist

i/p: nums: [1, 7, 3, 6, 5, 6]

$$\text{0/p} = \text{left sum} = 1 + 7 + 3 = 11$$
$$\text{right sum} = 6 + 5 = 11$$

0/p = index 3

i/p: nums: [2, 1, -1]

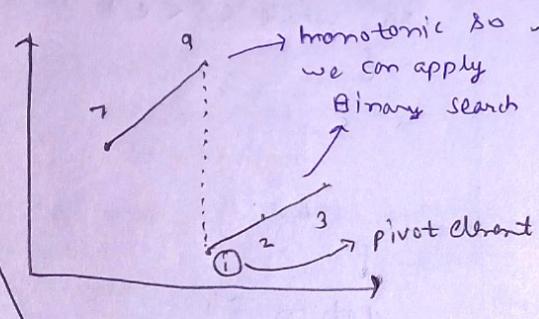
0/p = Left sum = 0 as 2 is leftmost

$$\text{Right} = 1 + (-1) = 0$$

0/p = index = 0.

given: sorted array.

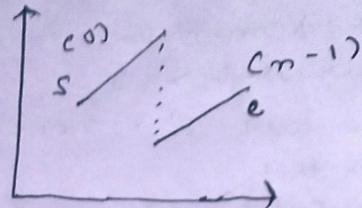
[1, 9, 1, 2, 3]



```
{  
    int right =  
        accumulate(nums.begin,  
                  nums.end(), 0);  
    int left = 0;  
  
    for (i = 0 → n - 1)  
    {  
        if (right = right - nums[i])  
            if (left == right)  
                return i;  
        left += nums[i];  
    }  
    return -1;  
}
```

}

Different question



$$\text{mid} = s + (e - s)/2$$

```
if (arr[mid] >= arr[0])  
{  
    start = mid + 1;  
}  
else {  
    end = mid;  
}
```

```
while (s < e)  
{  
}
```

```
return s;
```

Implementation

$$\text{arr} = \{2, 8, 1, 7, 1\}$$
$$0 \quad 1 \quad 2 \quad 3 \quad 4$$

$$\text{mid} = 0 + 4/2 = 2$$

$$10 > 3$$

$$\text{end} = \text{mid};$$

$$3 ; 8 > 10$$

$$S \quad e$$

$$\text{mid} = 0 + 2/2 = 1$$

$$8 < 10$$

$$\text{start} = 1 + 1 = 2$$

$$10$$

$$S \quad e$$

$$\text{mid} = 2 + 2/2 = 2$$

$$10 < 0$$

and  $> \text{start}$ , loop break

return s or

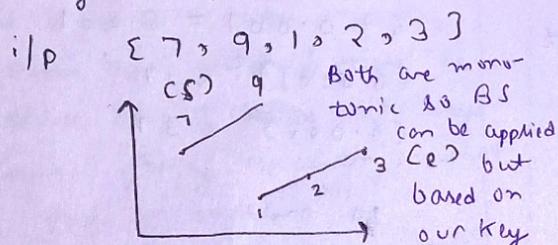
return e

## ② Search in Rotated Sorted Array

given an sorted array and a key  
array is rotated at some pivot  
point unknown to us.

e.g.  $\text{Arr} = [1, 2, 3, 4, 5, 6, 7, 8]$   
Rotated at index = 3:  $[7, 8, 1, 2, 3, 4]$

i/p: index at which K is  
present, if not present  
return -1, no duplicate  
present, Arr can be rotated  
only in right direction.



we can find Pivot and then  
Search for target.

our key can be

$$\text{arr}[\text{pivot}] \leq \text{Target} \leq \text{arr}[n-1]$$

or

$$\text{arr}[0] \leq \text{Target} \leq \text{arr}[\text{pivot}]$$

1) Find pivot

2) then apply Binary Search  
accordingly based on,  
which side key is present of  
pivot

"get pivot C"

|| now binary search code

if ( $\text{Arr}[\text{pivot}] \leq \text{Arr}[n-1]$ )

{ return BinarySearch(

arr, pivot, n-1, k)

}

else {

return BS( arr, 0, pivot, k )

}

## ③ Square root of a number

Given an positive integer N, return its square root  
if 'N' is not a perfect square, then floor value of  
 $\sqrt{N}$ .

i/p:  $N = 27$

o/p:  $\sqrt{27} = 5.2 \approx 5$

i/p:  $N = 8$

o/p:  $\sqrt{8} = 2.8 \approx 2$

Code

### ① Brute force

check for square of each  
no. close to N.

### ② if $N = 27$

our o/p will be b/w 0 - 27

0 - 27 is our search space

0, 1, 2, 3, ..., 27 is

monotonic, means we can

apply BS here

```

if 18 * 18 > N
then 19 * 19 or 20 * 20 > N
So our search space reduced
to 0 - 17.

if (mid * mid > num)
{
    end = mid - 1;
}

mid = 8
8 * 8 < N
7 * 7 < N so
start = mid + 1

if (mid * mid < N)
{
    ans = mid // store it
    start = mid + 1;
}

if (mid * mid == N)
{
    return mid;
}

```

But if mid =  $2^{31}-1$  then  
 $mid * mid >$  out of range  
so long long int mid;  
long long int square =  
 mid \* mid;  
long long int ans;

How to find floor  
value of a decimal value

$$6 + 0.1 = 6.1 * 6.1 \\ 6.1 * 6.2 < 37 \\ \vdots \\ 6.3 \rightarrow (6.3)^2 < 37$$

Summary

$$6.3 + 0.01 \rightarrow 6.31 \\ (6.31)^2 < 37 \\ (6.33)^2 < 37 \\ \text{if we want precision till} \\ 3 \text{ digit we do} \\ 6 + 0.001 = 6.001 \\ (6.001)^2 < 37 \\ (6.002)^2 < 37 \\ \vdots \\ \text{so on}$$

```

double precision(int n, int
precision, int IntValue)
{
    double factor = 1;
    double ans = IntValue;
    for (i=0; i < precision; i++)
    {
        factor = factor / 10;
        for (j=IntValue; j < *j < n;
            j = j + factor)
        {
            ans = j;
        }
    }
    return ans;
}

```

## Lecture 15

### Advanced Binary Search Problems

#### (1) Book Allocation Problem

Lokesh study for test happening in  $N$  days. To score good read  $M$  chapters.  $i^{th}$  chapter take  $TIME[i]$  to study. Ayush has  $100 \times 100$  sec in day. He always study sequentially  $i+1$  only after completing  $i^{th}$ .

If he starts a chapter then he completes it on same day. He divide his work in  $N$  days to  $\downarrow$  amount of time he studies in a day.

Find that minimal time he divide his  $M$  chapters in  $N$  days.

Given: Array representing no. of pages in books.

$$\text{no. of student} = m$$

Allocate books to students such that allocation is continuous, each student gets atleast one book.

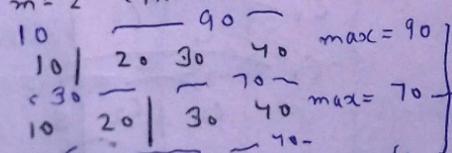
Each book should be allocated to a student, allocate books such that max amount from no. of pages allocated to student is minimum.

#### Solution

ip:  $10, 20, 30, 40$

$$n = 4 \text{ (no. of book)}$$

$$m = 2 \text{ (no. of student)}$$



$$\min(90, 70, 60)$$

$$o/p = 60$$

The array is not sorted here.

So How to apply BS?

We will  $\downarrow$  the search space

Let say  $\min = 0$

$\max = \text{sum of all ele of array}$   
 $(\max - \min)$  is our search space.

Let us check whether our mid i.e.  $\text{mid} = \text{start} + \min / 2$  is possible answer or not?

$$m = \text{no. of student} = 2$$

$$\text{mid} = 50$$

$$10 \quad 20 \quad 30 \quad 40$$

$$I \rightarrow 10 + 20 = 30 \checkmark$$

~~50~~

$$10 + 20 + 30 > 50 \times$$

(10, 20) first partition

$$II \rightarrow 30 \checkmark$$

$$30 + 40 > 50 \times$$

(30) is second partition

III  $\rightarrow$  we only have 2 students

so 50 is not a possible

so m so values  $< 50$  not

possible then start = mid + 1

Search Space is now

$$51 \quad \underline{\hspace{10mm}} \quad 100$$

$$\text{mid} = 75$$

$$I \rightarrow 10 + 20 + 30 \checkmark$$

$$II \rightarrow 40 \checkmark$$

75 can be possible sol<sup>n</sup> as for  $m=2$ , we've successfully allotted the books. So values  $> 75$  are also possible so end = mid - 1

as we need minimum and

so 1) Store ans

2) end = mid - 1

51 — 74

mid = 52

I → 10 + 20 + 30 ✓

II → 40 ✓

end = 62

end = mid - 1

51 — 61

mid = 56

I → 10 + 20 + ✓

II → 30 + 40 ✗

start = mid + 1

57 — 61

mid = 59

I → 10 + 30 ✓

II → 30 + 40 ✗

start = mid + 1

60 — 61

mid = 60

I → 10 + 20 + 30 ≤ 60

II → 40 ≤ 60

(60 is our answer)

end = mid - 1

= 59

start > end so loop breaks

return ans ;

## ② Painter's Partition Problem.

N = no. of boards

each element rep length of each board, k = no. of painter available to paint these boards, each unit of board takes 1 unit time. Return area of min time to get the job done of painting N boards

such that any painter will paint continuous section of boards only.

5, 5, 5, 5

K = 2

no. of painter = no. of student  
no. of pages = no. of boards  
minimum time when  
each board takes one unit  
of time to paint.

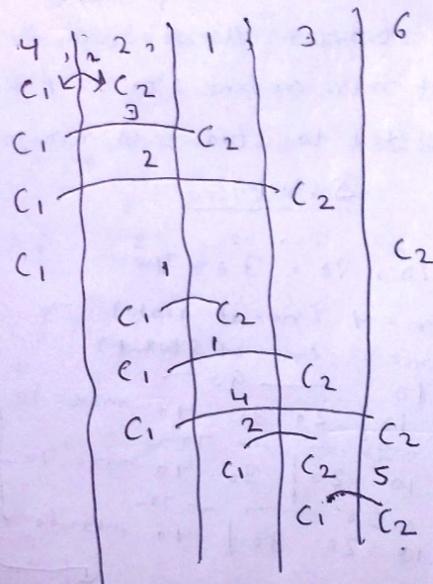
II Same as Book allocation  
problem

## ③ Aggressive Cows

Given array of N integers  
each ele denote posn of  
stall, K = no. of cows  
assign stalls to K cows such  
that min dist b/w any 2  
cows is max possible

IP = arr: {4, 2, 1, 3, 6}

K = 2 (C1, C2)



$$0/p = \max(3, 3+7, 3, 1+1, 4) \\ 2, 5, 3) = 5$$

maximum of minimum distance  
b/w 2 cows.

Search Space

$$\min \text{ dist} = 0$$

$$\max \text{ dist} = \max \text{ val of arr} - \min \text{ val of arr} \\ = 6 - 1 = 5$$

$$\text{mid} = 0 + 5/2 = 2$$

1) Store possible ans

2) Do start = mid + 1 as we need max value in our answer

place first cow at a pos^n

now place second cow such that  $(\text{dist}_{2^{\text{nd}}} - \text{dist}_{1^{\text{st}}} \leq \text{mid})$

$$\text{Dist} > \text{mid}$$

$$\{ \text{and} = \text{mid} - 1$$

}

till start < end

but at the beginning

Sort the vector first

$\xrightarrow{x} \xrightarrow{x} \xrightarrow{x} \xrightarrow{x}$   
lecture 16 (sorting)

Selection Sort

1) Easiest sorting algorithm

$$\text{arr}[] = \{1, 7, 9, 2, 3, 0\}$$

$$\text{Sorted arr}[] = \{0, 1, 2, 3, 7, 9\}$$

What?

There are different rounds in each round, we pick smallest element and put it in its right place.

$$\text{arr}[] = \{64, 25, 12, 22, 11\}$$

Round 1

$$64, 25, 12, 22, 11 \\ i=0$$

put smallest value of arr in  
 $i=0$

$$11, 25, 12, 22, 64 \\ i=1$$

Round 2

put min value of 25, 12, 22,  
64 at  $i=1$  pos^n

$$11, 12, 25, 22, 64 \\ i=2$$

Round 3

put smallest val at  $i=2$

$$11, 12, 22, 25, 64 \\ i=3$$

Round 4

$$11, 12, 22, 25, 64 \\ i=4$$

Round 5 (not needed)

$$11, 12, 22, 25, 64$$

Total element = n

no. of rounds =  $n - 1$

algo

Code

```
// do not consider
for(i=0 ; i<n-1 ; i++) {
    start element
    { minInd = i // let first ind to
        for(j=i+1 ; j<n ; j++)
            if(arr[j] < arr[minInd])
                { minInd = j;
                }
        swap(arr[minInd], arr[i])
    }
}
```

### Examples

1) 6 2 8 4 10

2 6 8 4 10

2 4 8 6 10

2 4 6 8 10

2) 4 3 2 1

1 3 2 4

1 2 3 4

### Space Complexity

$$= O(1)$$

### Time Complexity

$$1 + 2 + 3 + \dots + (n-2) + (n-1)$$

$$= \frac{n(n-1)}{2} = \frac{n^2 - n}{2}$$

$$= O(n^2)$$

Best Case TC = array already

Sorted =  $O(n^2)$

Worst Case TC =  $O(n^2)$

When to use?

When size of array is small  
and no memory constraints

We can consider Selection Sort

$\xrightarrow{x} \xrightarrow{x} \xrightarrow{x} \xrightarrow{x} \xrightarrow{x}$

### Lecture 17

#### Bubble Sort

We have an array

10 1 7 6 14 9

There are multiple rounds

Round 1 (This is 1<sup>st</sup> pass)

Compare 10 and 1

If  $10 > 1$ , swap (10, 1)

1, 10, 7, 6, 14, 9

Round 2

Compare 10, 7

1, 7, 10, 6, 14, 9

Round 3

1, 7, 6, 10, 14, 9

Round 4

1, 7, 6, 10, 14, 9

Compare 14, 9

1, 7, 6, 10, 9, 14

In 1<sup>st</sup> Pass, 1<sup>st</sup> largest element will come at its right place.

2<sup>nd</sup> Pass

Last element is already sorted & ignore it

1 7 6 10 9 14

1 6 7 10 9 14

1 6 7 9 10 14

sorted

### 3<sup>rd</sup> Pass

3<sup>rd</sup> largest element will come at its right pos<sup>n</sup> now.

1 6 7 9 10 14

1 6 7 9 10 14

1 6 7 9 10 14

1 6 7 9 10 14  
Sorted

Same way we do 4<sup>th</sup> & 5<sup>th</sup> Pass, when no. of element = 6 = n  
no. of Passes = 5 = n-1

### Code

In every i<sup>th</sup> round of pass of bubble sort, we fix i<sup>th</sup> largest element in its right position.

In every round we are leaving one element from last of array.

$j \rightarrow 0 \rightarrow (n-1)$   
 $0 \rightarrow (n-2)$   
 $0 \rightarrow (n-3)$   
 $\vdots$   
 $0 \rightarrow 1$

so ( $j=0 \rightarrow (n-i)$ )

```
for (i=1, i<n; i++)  
{  for (j=0; j<n-i; j++)  
    { if (arr[j] > arr[j+1])  
        {  
            swap(arr[j], arr[j+1])  
        }  
    }  
}  
if (ci=0  $\rightarrow i < n-1$ )  
then cj=0  $\rightarrow j < n-i-1$ 
```

Time Complexity:

In outer loop we do

(n-1) Comparison

(n-2)

$$\vdots$$
$$1 = \frac{n(n-1)}{2} = O(n^2)$$

Space Complexity = O(1)

Optimisation? if

In my round ~~no~~. during comparison is done means there are no swaps, means array already sorted.

for (i=1  $\rightarrow i < n$ )

{ bool swapped = false;

for (j=0  $\rightarrow j < n-i$ )

{ if ( )

{ swap();

swapped = true;

}

} if (swapped == false)  
{ break; }

}

Best Case TC =  $O(n)$   
 Lecture 18  
 Insertion Sort

### Card example

We have 4 cards, each card has some number, we get card one by one. We want to keep these cards in our hand in a sorted order.

{4 12 11 20}

We have 4  
 {4}

We have 12,  $4 < 12 \{4, 12\}$

We have 11,  $4 < 11, 11 < 12$

{4, 11, 12}

We have 20,

$4 < 20, 12 < 20, 11 < 20$

So {4, 11, 12, 20} is our

Sorted array

### Another example

{10 1 7 4 8 2 11}

Round 1 {10} ~~1 7 4 8 2 11~~

Round 2,  $1 < 10, \{1, 10\}$

Round 3,  $1 < 7, 10 > 7, \{1, 7, 10\}$

R 4,  $4 < 7, 4 > 1, 4 < 10,$   
 {1, 4, 7, 10}

R 5,  $8 > 7, 8 < 10, 8 > 10, 8 > 4$   
 , {1, 4, 7, 8, 10}

R 6, {1, 2, 4, 7, 8, 10}

R 7, {1, 2, 4, 7, 8, 10, 11}

Op = {1, 2, 4, 7, 8, 10, 11}  
 (R7 can be ignored)

No. of element = 7 = n  
 No. of round = n = 17 = 6  
 We need not to swap  
 We need to shift elements here.

### Code

```
for (i=1 → i<n)
{ int temp = arr[i];
  // store it so that we can shift
  int j = i-1;
  // compare with prev elements
  for ( ; j>=0; j--)
  { if (arr[j] > temp)
    { // shift
      arr[j+1] = arr[j];
    }
    else { // Hold on
      break;
    }
  }
  arr[j+1] = temp;
}
```

### Why Insertion Sort?

It is most adaptable  
 means we do less repetitive work for sorting.

It is stable.

9, 3, 3', 5, 7, 5', 3, 1, 3  
 || unsorted

1, 2, 3, 3', 3'', 5, 5', 6, 9  
 || stable

1, 2, 3'', 3', 3'', 5', 5,  
 6, 9 || unstable

stable means preserves the order of records with equal keys.

Insertion, Bubble Sort are stable algs.

Quick Sort, Selection Sort are unstable sorting algs

Adaptive algos

Algo which changes its behaviour at time it is run, based on available info.

Space Comp = O(1)

Time Comp = O(n<sup>2</sup>)

Best Case Comp = O(n)

Worst Case Comp = O(n<sup>2</sup>)

— x — x — x — x —

Lecture 19

C++ STL

(complete code in github  
m's theory)

— x — x — x — x —

Lecture 20

Question on Arrays

① Reverse an array

arr[] = {1, 2, 3, 4}

↓  
{4, 3, 2, 1}

Given = array and pos<sup>m</sup>  
Reverse array after m<sup>th</sup>

pos<sup>m</sup>.

take start = 0

end = n - 1

Swap(arr[start], arr[end])

till start < end

{ 4    3    2    1 } = arr[]

    i                j

{ 1    3    2    4 }

    i                j

{ 1    2    3    4 }

int s = 0, e = size - 1;

while (s < e)

{ swap(arr[s], arr[e]);

s++;

e--;

2) Merge Sorted Array

arr1[] = {1, 3, 5, 7, 9}

arr2[] = {2, 4, 6}

merge both sorted array into a third array which is also sorted

arr3[] = {1, 2, 3, 4, 5, 6, 7, 9}

arr1[] = {1, 3, 5, 7, 9}

arr2[] = {2, 4, 6}

Compare i and j<sup>o</sup> and jo

chota Hain usko daal denge.

arr3[] mai-

i < 2 ; arr3 = {1}, i++

3 > 2 , arr3 = {1, 2}, j++

3 > 4 , arr3 = {1, 2, 3}, i++

5 < 4 , arr3 = {1, 2, 3, 4}, j++

5 > 6 , arr3 = {1, 2, 3, 4, 5}, i++

7 < 6 , arr3 = {1, 2, 3, 4, 5, 6}

j++.

now j is out of range so the array in which elements are left just make while loop and copy elements in it.

```

size of arr1 = m
size of arr2 = n
int i=0, j=0, k=0
vector<int> num3(m+n);
while (i < m & j < n)
{
    if (num1[i] < num2[j])
    {
        num3[k++] = num1[i++];
    }
    else {
        num3[k++] = num2[j++];
    }
}
while (i < m)
{
    num3[k++] = num1[i++];
}
while (j < n)
{
    num3[k++] = num2[j++];
}
for (i=0; i < num3.size(); i++)
{
    num1[i] = num3[i];
}

```

### ③ Move Zeros

Given an array, move all 0's to end of it while maintaining order of non zero elements.

$$I/P = [0, 1, 0, 3, 12]$$

$$O/P = [1, 3, 12, 0, 0]$$

means Keep all non-zero element sorted. and shift all 0's to end of array.

2 pointer approach

$$0, 1, 0, 3, 12, 0$$

move 1<sup>st</sup> non-0 value at i=0  
 so 2<sup>nd</sup> , , , , i=1  
 so 3<sup>rd</sup> , , , , i=2

~~Self explanation~~

if we encounter 0, ignore  
 if we encounter non-0,  
 swap.  
 int i = 0;  
 for (j=0 → j < num.size())  
 {
 if (num[j] != 0)
 {
 swap (num[j],  
 num[i]);  
 i++;
 }
 }

— X — X — X —  
 Lecture 2/1

### ① Rotate Array

Given an array, rotate array by k steps

$$I/P = [1, 7, 9, 11], k=2$$

$$O/P = [9, 11, 1, 7]$$

$$I/P = [-1, -100, 3, 99], k=2$$

$$O/P = [3, 99, -1, -100]$$

\* 1..n my no gives o/p b/w [0 - (n-1)] always

\* Array index is always b/w [0 - (n-1)]

$$[1, 12, 3, 4, 5], k=3$$

Let say we want to shift 15 by k=3 steps

current index of 15 = n-1

$$3 \text{ step from } n-1 \rightarrow n \rightarrow n+1 \rightarrow n+2$$

but array size = n

$$\therefore (n+2) \cdot 1 \cdot n = 2$$

We get correct posn of 15 after rot<sup>n</sup> like this.

$$\text{arr}[(i+k) \% n] = \text{arr}[i]$$

will shift  $i^{\text{th}}$  term by  $k$  steps in cyclic way in an array.

```
vector<int> temp;
for (i=0 → i<nums.size())
{ temp[(i+k) % nums.size()] =
    nums[i];
}
```

$\text{nums} = \text{temp};$

We take temp so that values do not get overwritten in  $\text{nums}$  array.

② Check if array is sorted and Rotated.

There may be duplicates in original array.

i/p = {3, 4, 5, 1, 2}

o/p = true

There can be 3 cases

I Sorted, but not Rotated  
 $\{1, 2, 3, 4, 5\}$

II Rotated, but not sorted  
 $\{3, 4, 5, 1, 2\}$

III neither sorted nor rotated  
 $\{3, 5, 7, 1, 6\}$

~~Case Cases~~

IV all elements are equal  
 $\{1, 1, 1\}$

```
{ int count = 0;
int n = nums.size();
for (i=1 → i < n)
{ if (nums[i-1] > nums[i])
    { count++;
}
if (nums[n-1] > nums[0])
{ count++;
}
}
return count <= 1;
```

③ Sum of 2 Arrays

2 arrays given arr1,  
arr2. add them

arr1 = [1, 2, 3, 4]

arr2 = [6]

$$\begin{array}{r} \text{o/p} = \begin{array}{cccc} 1 & 2 & 3 & 4 \\ + & & & 6 \\ \hline 1 & 2 & 4 & 0 \end{array} \end{array}$$

o/p = [1, 2, 4, 0]

i/p arr1 = {1, 2, 3}

arr2 = {9, 9}

$$\begin{array}{r} \text{o/p} = \begin{array}{ccc} 1 & 2 & 3 \\ + & 9 & 9 \\ \hline 2 & 2 & 2 \end{array} \end{array}$$

o/p = {2, 2, 2}

1) we start adding from last element of array.

3 cases may arise

1) arr1 is large, arr2 is small

$$\text{arr1} = \boxed{1 \ 2 \ 3 \ 4}$$

$$\text{arr2} = \boxed{\begin{matrix} \text{there will} \\ \text{be missed} \end{matrix}} \ 6$$

2) arr2 is large, arr1 is small

$$\text{arr1} =$$

$$\boxed{1 \ 2 \ 3 \ 4}$$

$$\text{arr2} =$$

$$\boxed{1 \ 2 \ 3 \ 4}$$

3) both arr1 and arr2 has same length

$$\text{arr1} =$$

$$\boxed{9 \ 9 \ 9}$$

$$\text{arr2} =$$

$$\boxed{9 \ 9 \ 9}$$

Carry will be missed

$$\text{Carry} = \text{Sum} / 10$$

$$\text{Sum} = \text{Sum} \cdot 1 \cdot 10$$

$$\text{arr}[i] = \text{Sum}$$

for example:  $2 + 13 = 16$

$$\text{Carry} = 16 / 10 = 1$$

$$\text{Sum} = 16 \cdot 1 \cdot 10 = 6$$

$$\text{arr}[i] = 6$$

At the end our arr will be stored in reverse order so just reverse the o/p array.

### Code

```
vector<int> addC(a: int n, b: int m)
{
    i = n - 1, j = m - 1
    carry = 0, ans<int> ans;
    while (i >= 0 && j >= 0)
    {
        sum = a[i] + b[j] +
            carry;
    }
```

$$\text{carry} = \text{sum} / 10;$$

$$\text{sum} = \text{sum} \cdot 1 \cdot 10;$$

ans.push\_back(sum);

i--;

j--;

}

|| 1<sup>st</sup> case when arr1 large  
while (i >= 0)

$$\{ \text{sum} = a[i] + \text{carry};$$

$$\text{carry} = \text{sum} / 10;$$

$$\text{sum} = \text{sum} \cdot 1 \cdot 10;$$

ans.push\_back(sum);

i--;

}

|| 2<sup>nd</sup> Case

while (j >= 0)

$$\{ \text{sum} = b[j] + \text{carry};$$

{ rest same

j--;

}

|| 3<sup>rd</sup> Case

while (carry)

$$\{ \text{int sum} = \text{carry};$$

$$\text{carry} = \text{sum} / 10;$$

$$\text{sum} = \text{sum} \cdot 1 \cdot 10;$$

ans.push\_back(sum);

}

return reverse(ans);

vector<int> reverse (ans)

{ s = 0, e = ans.size - 1;

while (s < e)

{ swap (ans[s++], ans[e--])

}

return ans;

}

## Lecture 22

### Strings, char arrays

- 1) `char a = 'z'` // variable of character type  
'z' but we can store only a single character, to store multiple characters we use string.
- 2) 1D char type array is called string
- 3) 

```
int a[10]; // int array
char ch[10]; // char array
cin >> n; // int input
cin >> arr[i];
char name[20]; // char array declared
cin >> name; // char array i/p
```
- 4) null character '\0' is used as a terminator in char array or string which signifies where string is ending.
- 5) It will print string till '\0' null character.
- 6) O/p char array?  
`cout << name;` // will print character by character
- 7) AB soon as compiler sees '\0' it will stop printing.
- 8) cin stops execution when it sees space, tab ~~\t~~, '\t' or newline '\n'.

~~Ques~~

### Q) Length of string

```
start counting from index=0
stop at '\0' (null char)
int count = 0;
for (i=0; name[i] != '\0'; i++)
{
    count++;
}
return count;
```

### Q) Reverse a string

```
int s=0, e= n-1;
n = length of string
while (s < e)
{
    swap(s++, name[e--]);
}
```

### Q) check Palindrome

a string whose reverse is same as original string.

NITIN  $\rightleftharpoons$  NITIN  
 NOON  $\rightleftharpoons$  NOON

Question statement : skip all special characters in the string  
 Q) make string to lowercase

### 1) Reverse the string

```
for (i=0; i < s.length(); i++)
{
    char ch = s[i];
    if (ch <= 'Z' & ch >= 'A')
    {
        ch = ch - ('A' - 'a');
        s[i] = ch;
    }
}
```

### 2) Compare original string & Reversed string by putting pointer at 0<sup>th</sup> index on both

```

if (isalnum(s[i]) == 0)
{
    ++i;
}
else if (isalnum(reverseString[s[j]])) == 0)
{
    ++j;
}
else if (s[i] == reverseString[j])
{
    ++i;
    ++j;
}
else {
    return false;
}
}
return true;
}

```

12) String is a class which has some methods & properties.

String stores data internally in form of null terminated C-strings, but in normal usage does not allow us to access the null terminator.

We can use push-back, pop-back, find, compare etc methods in a string also.

13) We have some in-built funn in string.

13) Diff b/w string and char array  
String is used as single entity & Single data type.  
In char array each element is a separate entity.  
String can be stored in random order in memory, char array stored in contiguous location.

String is a class so can use in-built funn but char array can't  
String can be concatenated using + or concat() but char array can't  
String is immutable (immutable means strings with same ~~content~~ content share storage in a single pool to minimize creating copy of some value) hence one string is created its content can't be changed, changing its content will lead to generation of new string. but char array are mutable.

14) Reverse words in a string - II  
In a ~~word~~ string words are given in space separated manner.  
Reverse every word of string such that spaces are intact.

- 1) Reverse string function  
by using
- 2) Start & End Kya and  
stored that words in a  
temp string till space is  
encountered.
- 3) Reverse temp string
- 4) pushback that temp string  
in answer and store  
that many spaces in  
resultant string.
- 5) As soon as i get  
'\0' reverse string  
again

15) Return minimum  
occurring character in a  
I/p string  
print character occ max times  
if more than one character do  
so then print lexicographically  
smaller character first.

String = test  
 $t \rightarrow 2$      $\{$      $t = o/p$   
 $e \rightarrow 1$      $\}$   
 $s \rightarrow 1$

we have total 26 characters  
we make array of size 26  
and store count in it  
we consider 'a' & 'A' with  
some block in that array  $int arr[26] = \{0\}$   
 $for(i=0; i < s.length(); i++)$   
 $\{ if(s[i] is lowercase)$   
 $\{ num = ch - 'a' ; \} || ch = s[i]$   
 $\}$   
 $arr[num]++;$

```

if(s[i] is uppercase)
{
    num = ch - 'A';
}
arr[num]++;
}
int max = -1;
int ans = 0;
for(i = 0 → < 26)
{
    if(max < arr[i])
    {
        maxi = arr[i];
        ans = i;
    }
}
return ans + 'a';

```

16) cin.getline  
To get spaces also stored in  
char array to take I/P

use  
`cin.getline(string, string  
length);`

17) In-built string func  
 1) length    `strlen(name);`  
 2) Compare    `strcmp(s1, s2);`  
 3) Copy    `strcpy(destination str  
, source string);`

18) Replace Spaces.  
Replace all spaces in a string S  
put @40.

I/p: My Name is Khan  
 O/p: My@40Name@40 is @40 Khan.  
 $if(str[i] == ' ')$   
 $\{ temp.pushback('@');$   
 $\quad \quad \quad ('4')$   
 $\quad \quad \quad ('0')$   
 $\}$   
 $else \{ temp.push(str[i]);$   
 $\}$

19) Remove all occ of a string.

Given string  $s$  and part  
Remove all occ of part from  $s$   
by starting from leftmost occ  
of part and remove it from  $s$ .  
Part is a substring.

i/p:  $s = \underline{d}aa\underline{bc}baab\underline{c}bc$   
part = "abc"

after removing abc

$s = da\underline{b}a\underline{abc}bc$

again removing abc

$s = da\underline{b}\underline{abc}$

again some work

$s = dab$

o/p = dab

Code

$s.find(part)$  is used to  
find whether 'part' string is  
present in string ' $s$ ' or not.  
if present, it gives first occ-  
urrence of part in  $s$ .

$s.erase(part.begin(), part.end())$   
is used to erase some part of  
string  $s$  from part.begin to end

while ( $s.length() != 0 \text{ AND } s.find(part) < s.length()$ )

{  
 $s.erase(s.find(part), part.length());$

}

return  $s$ ;

20) Permutation in string

Given two strings  $s_1$  and

$s_2$ , return true if  $s_2$

contains a permutation of  
 $s_1$  or false otherwise.

Return true, if  $s_1$ 's  
permutation is substring of  $s_2$ .

$s_2 = eid\underline{ba}000$

$s_1 = ab$

O/p = true

1) store count of  $s_1$  in  
an char arr[26];

2) make a window of size  
of  $s_1.length$ .

3) Search within that window  
in  $s_2$  and compare with  
arr[26] whether the  
characters are same or not.

21) Remove all adjacent  
Duplicates in a string  
given string in lowercase,  
remove element which are dupli-  
cates & adjacent to each other.

i/p:  $s = \underline{a}b\underline{b}a\underline{c}a$

o/p:  $s = \underline{a}\underline{b}\underline{b}\underline{a} \underline{c} \underline{a} \underline{c} a$

o/p: ca

i/p: a z z c c z y

z z y

o/p: ay

```

string ans;
ans.push(s[0]);
for(i=0 → i < s.length())
{
    if(s[i] == ans.back())
    {
        ans.popback();
    }
    else
    {
        ans.pushback(s[i]);
    }
}
return ans;

```

## 22) string compression

i/p: a, a, b, b, b, c, c, c

o/p: a → 2  
b → 3  
c → 3

o/p: {a, 2, b, 3, c, 3}

if any character appear only 1 time, then count is not needed, just o/p the character only.

i/p: a, a, b, c, c, d, d, d

o/p = {a 2 b 1 c 2 d 3}

Approach

- 1) Take count of character
- 2) if count == 1, print char directly
- 3) if (count > 1)
  - 1) if ( < 10 )
    - 1) if print char with count
  - 2) if count is 2 digit no.

```

    { // convert to single digit and
        do the same
        // print char with count
    }
}

```

// ans should be stored in some i/p array, no extra space to be taken.

### Code

```

i=0; ansInd = 0;
n = chars.size();
while(i < n)
{
    j = i+1;
    while(j < n && chars[i] == chars[j])
    {
        j++;
    }
    // store all char in array
    chars[ansInd + i] = chars[i];
    int count = j - i;
    if(count > 1)
    {
        string cnt = to_string(count);
        for(char ch: cnt)
        {
            chars[ansInd + i] = ch;
        }
    }
    i = j;
}
return ansInd;
}

```