

Q1) let us take a graph

12 nodes

Level 0

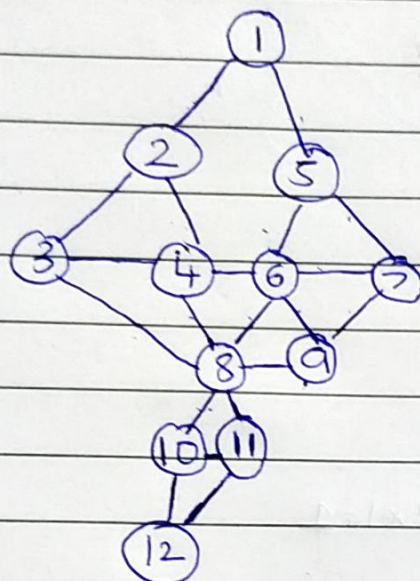
Level 1

level 2

level 3

level 4

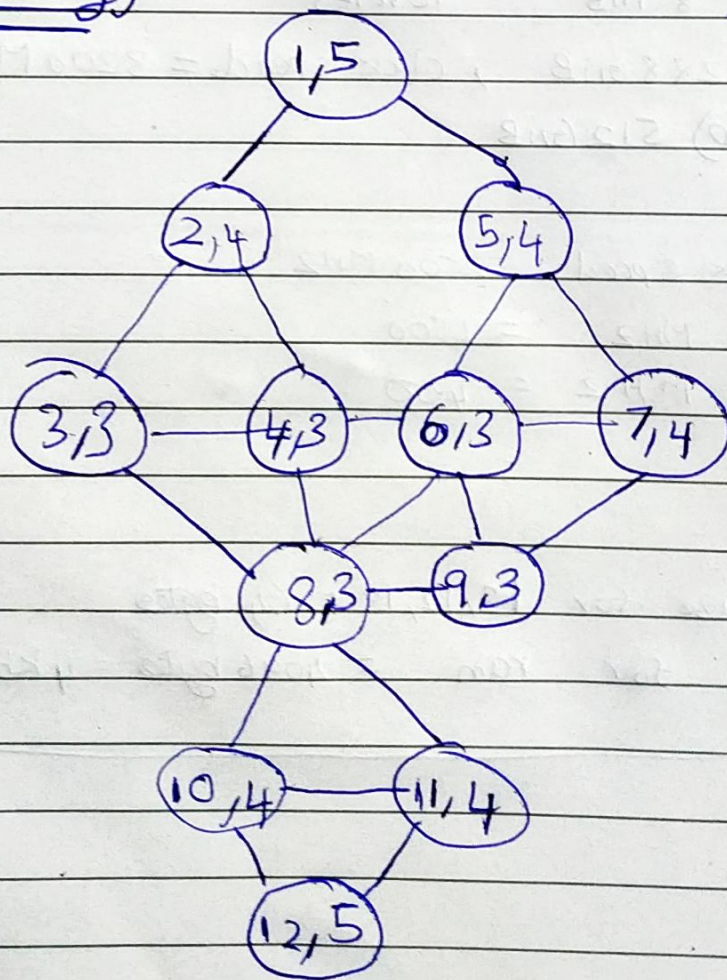
level 5



→ nodes @ 1 20 edges

(node, Eccentricity)

node, ecc graph





(92) eccentricity( $u$ )  $\rightarrow$  longest of [shortest paths from a fixed node  $u$  to all other nodes  $v$  in graph  $G$ ]

$B_i \rightarrow$  max of all eccentricity at level  $i$

Algorithm: ~~Two~~

- 1) Take a node and root the graph at the node
- 2) Now from the bottom most level do a BFS on each node at that level and find ecc. ~~of~~ ~~at~~  
 let  $B_i \rightarrow$  max of all ecc at level  $i$
- 3) if  $B_i > 2C_{i-1}$ , Then we can stop our BFS's as any node above it will not have a ecc greater than ecc of all nodes found till now



For our graph

	$B_i$	Condition ( $B_i > 2(i-1)$ )	Result
level 5: Node 12 $\rightarrow ecc(12) = 5$	$B_5 = 5$	$5 > 2(5-1)$	False
level 4: Node 11 $\rightarrow ecc(11) = 4$ Node 10 $\rightarrow ecc(10) = 4$	$B_4 = 4$	$4 > 2(4-1)$	False
level 3: Node 9 $\rightarrow ecc(9) = 3$ Node 8 $\rightarrow ecc(8) = 3$	$B_3 = 3$	$3 > 2(3-1)$	False
Level 2: Node 7 $\rightarrow ecc(7) = 4$ Node 6 $\rightarrow ecc(6) = 3$ Node 4 $\rightarrow ecc(4) = 3$ Node 3 $\rightarrow ecc(3) = 3$	$B_2 = 4$	$4 > 2(2-1)$	True

So in level 2  $B_2 > 2(2-1) \rightarrow$  so we need not do  
BFS for level 1 nodes

Effectively we do  $(1+9)$  BFS traversals <sup>Rooting</sup>

For example we do very high no of  
traversal even though using IFUR,

One reason is nodes : edges ratio