

## SL Rules

### Modus Ponens ( $\rightarrow E$ )

$$\begin{array}{|l} P \rightarrow Q \\ P \\ \hline Q \end{array}$$

### Conjunction Introduction ( $\wedge I$ )

$$\begin{array}{|l} P \\ Q \\ \hline (P \wedge Q) \end{array}$$

### Conjunction Elimination ( $\wedge E$ )

$$\begin{array}{|l} (P \wedge Q) \\ \hline P \\ Q \end{array}$$

### Disjunction Introduction ( $\vee I$ )

$$\begin{array}{|l} (P) \\ \hline P \vee Q \end{array}$$

### Disjunction Elimination ( $\vee E$ )

$$\begin{array}{|l} P \vee Q \\ \neg P \\ \hline Q \end{array}$$

### Biconditional Elimination ( $\leftrightarrow E$ )

$$\begin{array}{|l} (P \leftrightarrow Q) \\ \hline P \rightarrow Q \end{array}$$

### Negation Elimination ( $\neg E$ )

$$\begin{array}{|l} \neg \neg P \\ \hline P \end{array}$$

## Hypothetical Rules

### Reiteration ( $R$ )

$$\begin{array}{|l} *1 \\ \hline P \\ P \end{array}$$

### Conditional Introduction ( $\rightarrow I$ )

$$\begin{array}{|l} | \quad n. P \\ | \quad \hline | \quad \vdots \\ | \quad m. Q \\ P \rightarrow Q \end{array}$$

### Reductio ad Absurdum(RAA)

$$\begin{array}{|l} | \quad n. P \\ | \quad \hline | \quad \vdots \\ | \quad m. Q \\ | \quad m' \neg Q \\ \neg P \end{array}$$

### *Argument by Cases (AC)(First Form)*

$$\begin{array}{|l} P \vee Q \\ P \rightarrow R \\ Q \rightarrow R \\ R \end{array}$$

For 2nd form , first prove  $P \rightarrow R$  and  $Q \rightarrow R$   
using ( $\rightarrow I$ )

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<sup>1</sup>Not a hypothetical rule but often used together.