

Test 7: Translate and evaluate the following statements (If QL is given, translate it into English. When English is give, translate it to QL.)

P	Q	9	T
1	3	R	E
I	J	8	2
F	B	5	M

**UD** {x : x is in the grid.}

**referent** Each letter in the grid is referred to by the lower-cased version of the same letter.

**s** The number 1.

**Nx** x is a number.

**Tx** ..letter.

**Vx** ..vowel.

**Cx** ..consonant.

**Ex** .. even.

**Dx** .. odd.

**Axy** x is above y.

**Uxy** ..under..

**Rxy** ..right of..

**Lxy** ..left of..

**Gxy** ..greater than..

**Oxy**  $\{(x, y) : y = x + 1\}$

**Sxy** ..subsequent to..

Notes: Spatial predicates do not imply directly. E.g.,  $Apm$  is true even though  $p$  is not directly above  $m$ . Only 2, 3 and 5 are prime.  $G$  is a relation between numbers only.  $S$  is a relation between letters only.  $Sea$  is true because  $e$  comes after  $a$  in the alphabet. No number other than 1 has a name and you may not introduce any.

**Hint:** Be absolutely sure to interpret and translate definite descriptions correctly.

1. The odd number between two consonants is greater than 1.
2. The number 3 exists.
3. Some number is *immediately* above a letter.
4. No consonant except for 'R' is above two different numbers.
5. There are no more than two numbers to the right of the letter E.
6.  $\exists x(Nx \wedge Gxs \wedge \forall z((z \neq s \wedge z \neq x) \rightarrow \neg Gxz))$
7.  $\exists x \exists y \exists z[(Lxy \wedge Rzy \wedge Dy) \wedge \forall u((Lxu \wedge Rzu \wedge Du) \rightarrow u = y)]$
8.  $\exists x(Nx \wedge Lxm \wedge Rxb \wedge Dx \wedge \forall y((Ny \wedge Lym \wedge Ryb) \rightarrow y = x))$