# Mathematical Foundations of Computer Graphics & Vision



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# **Today!**

- 1) Handout, exercise 1;
- 2) Next week Handout, exercise 2
- 3) 14.03.2016 Grading exercise 1







#### Reminder!

- 6 homework assignments (70% of the grade in total)
- Oral examination (30% of the grade)

#### Homeworks:

- Individual work!
- Normally you will have 2 weeks to solve each exercise.
- Programming in Matlab
- 3 minute demo sessions







#### Reminder!

- Approximately 3 minutes to show your code and explain what you did or didn't do.

- Prepare in advance to present your work. Present each exercise in order. Already have your computer turned on and ready to go on your turn.

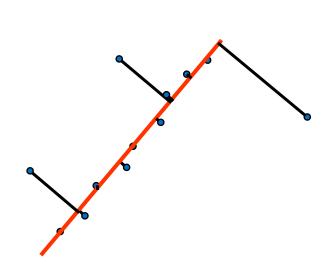
- Presentations during the TA session. Random order, random examiner.







- RANSAC



- -Select 2 points
- -Fit the line
- -Compute the distances
- -Count the nb of inliers
  - -9 out of 13

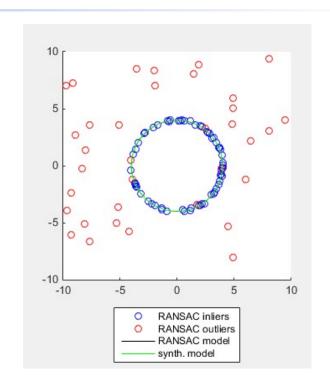






#### RANSAC to detect best circle fit.

- Familiarize yourself with RANSAC;
- Apply RANSAC to detect inliers/outliers in a data set which can be approximated by a circle;
- Observe the efficiency of RANSAC on data sets of various qualities.

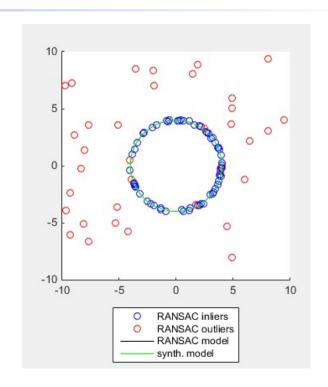








- Input:
  - Data set (N points in 2D)
  - Number of iterations k
  - Threshold value t
- Output:
  - Parameters *r*, *c* of the estimated circle
  - Inliers/Outliers

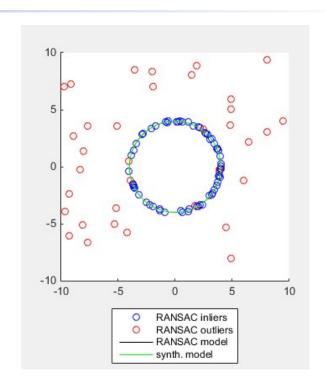








- Synthetic data -> Ground truth solution exists!
- Choose r, c as you want
- Generate N=100 points in the domain [-10,10]x[-10,10]
- Some points are inliers, they are on the circle, but have noise
- Some points are outliers, they are not on the circle at all

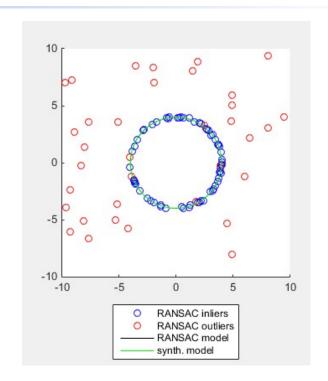








- Make sure that the synthesized inliers are indeed inliers and the synthesized outliers are indeed outliers and then verify the given outlier ratio r
- Total number of points is always N (N=100). So if the ratio of outliers is r = 10%, then 10 points are outliers and 90 points are inliers. If r = 30%, then 30 outliers and 70 inliers.

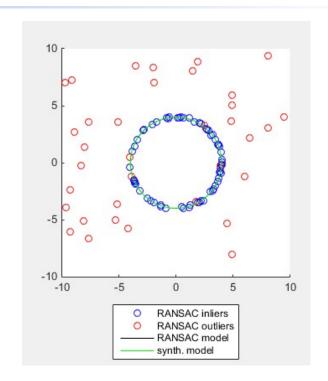








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 Automatically compute the number of RANSAC iterations

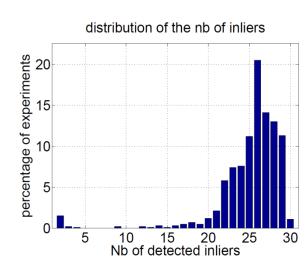
$$N = \frac{\log(1-p)}{\log(1-(1-\varepsilon)^s)}$$
 Outlier ratio Sample size (minimum data) e.g. s=2 for line fitting, s=3 for circle







- Plot results for data sets with r=5,20,30,70% of outliers
- Run RANSAC several times (1000) and plot the distribution of the best number of inliers for each run on a histogram

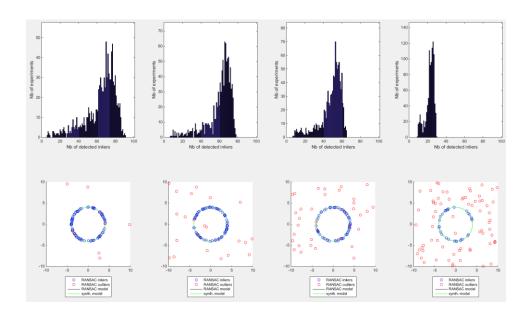








A successful task looks like this:

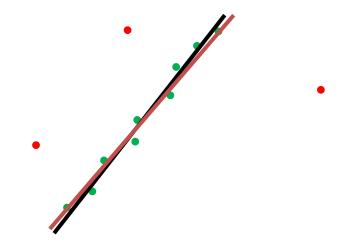








• Line fitting

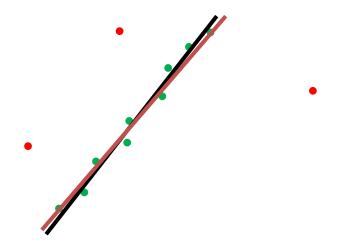








- To generate data points on a line, follow a similar strategy to Part1.
- Add noise
- 0% (none) and 10% of outliers

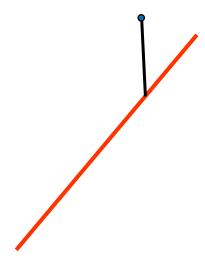








- Vertical cost: p = (px,py)
- d(f,p) = py f(px)



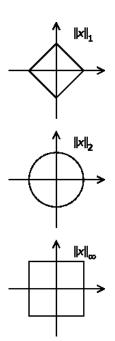






$$|x|_1 = \sum_{i=1}^n |x_i|$$

$$|x|_{\infty} = max_i|x_i|$$



Source - wikipedia







 A successful result looks like this (LP with Linf norm, 10% outliers)

