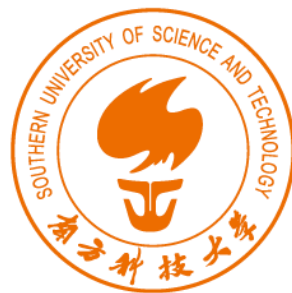


# A novel biophysical model for radical pair mechanism in birds' magnetoreception



2019年5月21日

骆锦威 11410163



# Contents

- Background
- Three Possible Mechanisms
- OCC Model
- Simulations
- Predictions and Discussion

# Background

# First discovery in magnetoreception

## **Magnets Interfere with Pigeon Homing**

**WILLIAM T. KEETON**

Section of Neurobiology and Behavior, Division of Biological Sciences  
University, Ithaca, New York 14850

*Communicated by Donald R. Griffin, October 8, 1970*

**ABSTRACT** Magnets glued to the backs of experienced pigeons often resulted in disorientation when the birds were released from distances of 17-31 miles (27-50 km) under total overcast, whereas no such disorientation occurred during similar releases under clear skies. The magnets did, however, often cause disorientation when first-flight birds were released under sun, and there was some indication of disturbance to experienced pigeons released under sun at longer distances.

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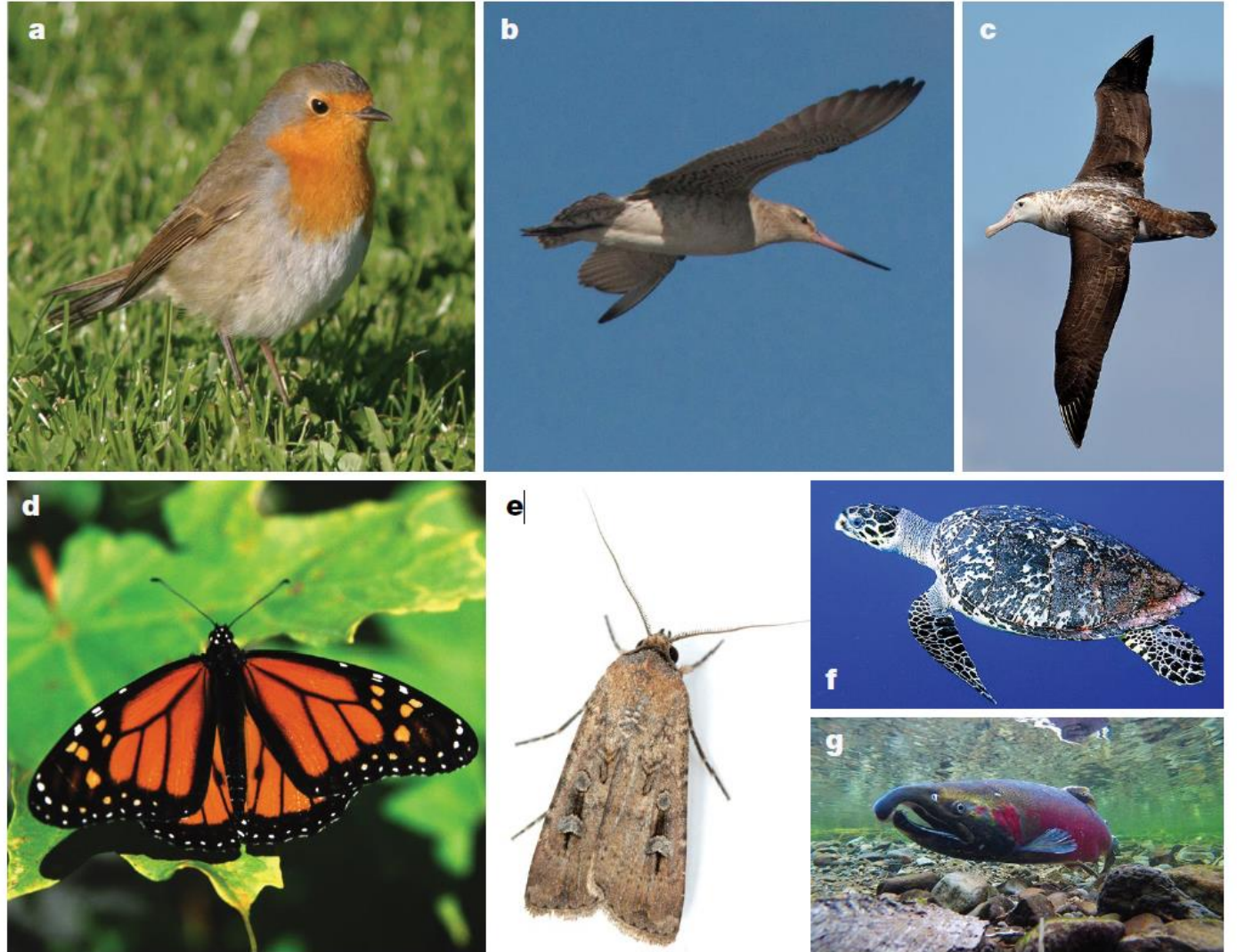
Modified after Ref.[1]

# Magnetic compass is ubiquitous across species

**Vertebrates:** birds, fishes, amphibians, reptiles, mammals.

**Invertebrates:** mollusks, crustaceans, insects.

- *Erithacus rubecula*
- *Limosa lapponica*
- *Diomedea exulans*
- *Danaus plexippus*
- *Agrotis infusa*
- *Eretmochelys imbricate*
- *Oncorhynchus kisutch*



Modified after Ref.[2]



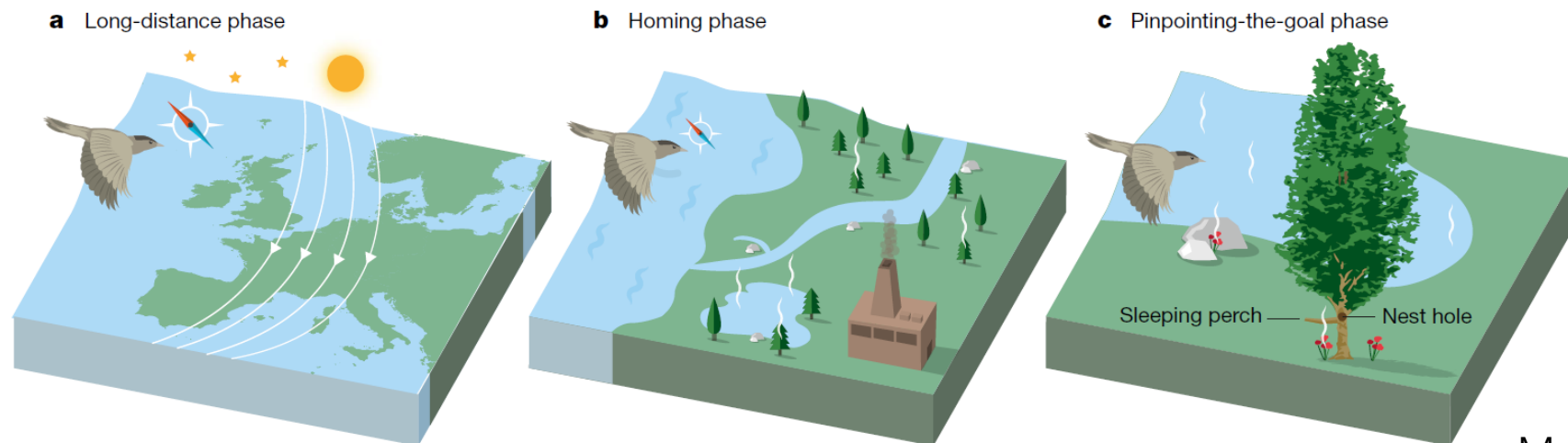
# Multisensory cues for bird navigation

- **Long-distance navigation – Migration maps**

Magnetic compass, sun compass, star compass

- **Homing and pinpointing – Local orientation**

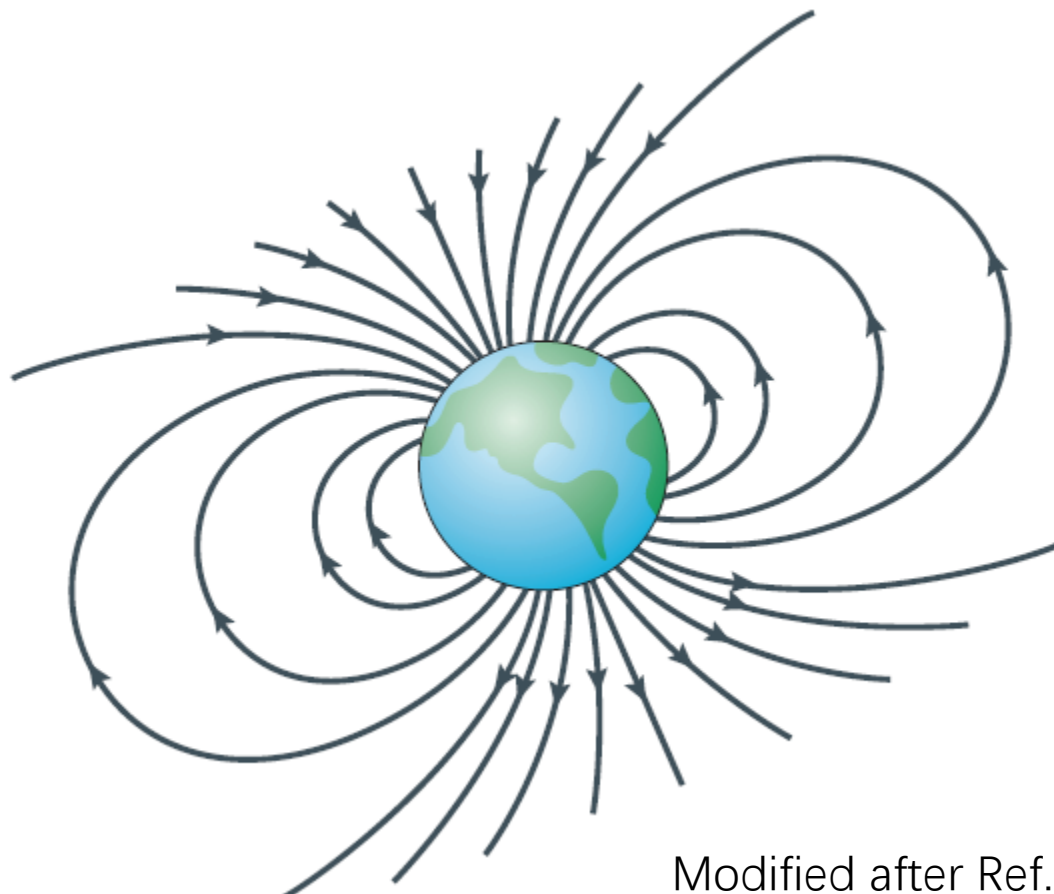
Odors, borders, coast lines, sound, landmarks such as a tree, a small hill, a specific coral



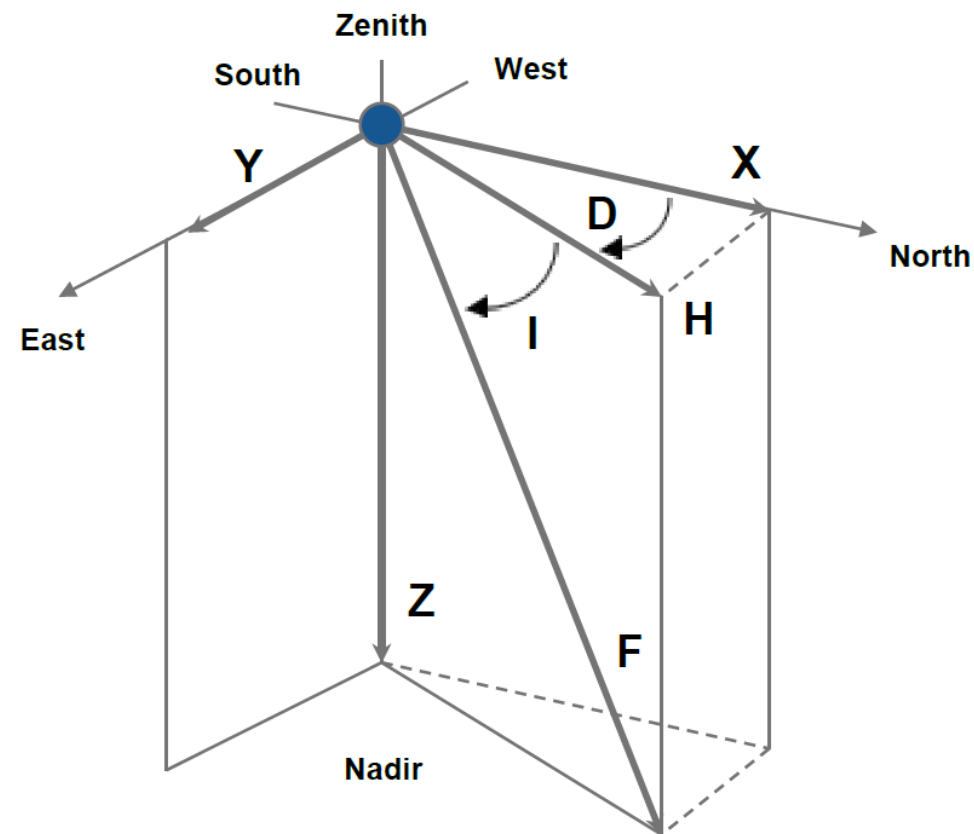
Modified after Ref.[2]

# Earth magnetic fields

- Field strength: 25~60uT



Modified after Ref.[3]



Magnetic field information

**Inclination**

**Polarity/Declination**

**Intensity**

# Mechanisms

## Three possible mechanisms

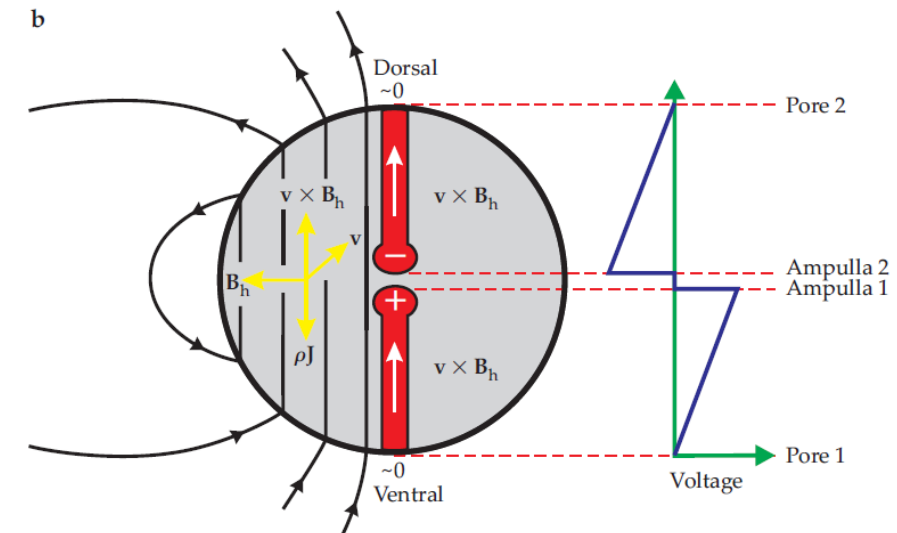
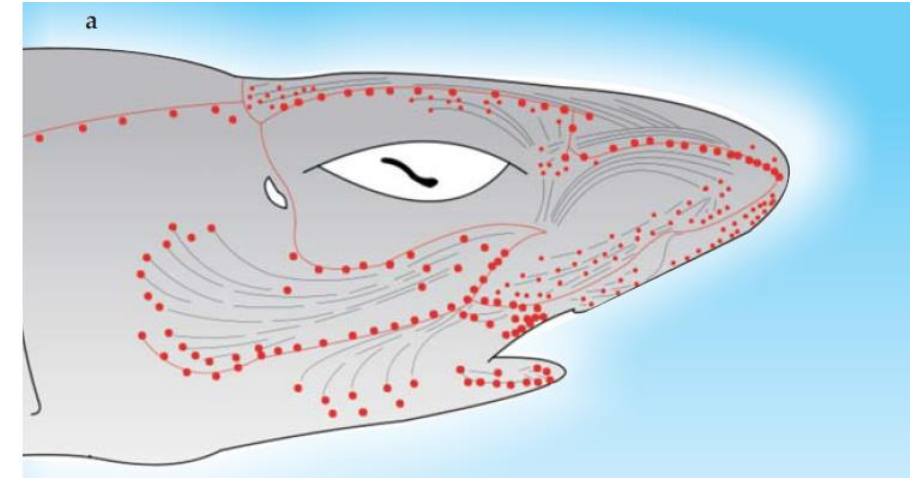
- Electromagnetic induction
- Magnetite based magnetoreception
- Radical based magnetoreception

## Difficulties for verification

- No specific organ is found
- No unique behavioral phenotype
- Multisensory cues coupling
- Adaptation and acclimation
- Multi origins or single origin?



- A unique organ in cartilaginous fish:
- **Ampullae of Lorenzini**
- Jelly-filled pores with electroreceptors
- Moving magnetic field accumulates electric potential on two ampullas via proton flux, which can be detected by electroreceptor cells.
- Elasmobranch species: **sharks, rays and skates.**

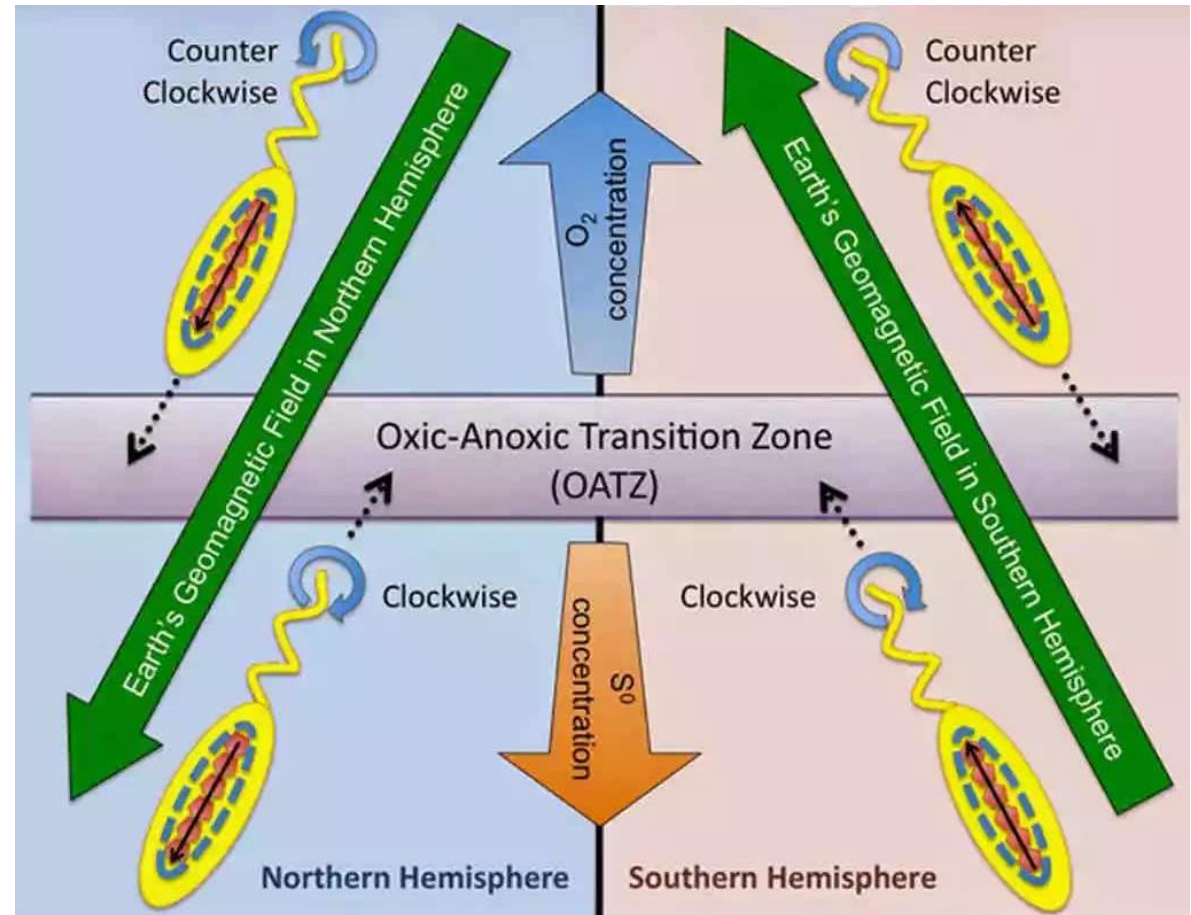
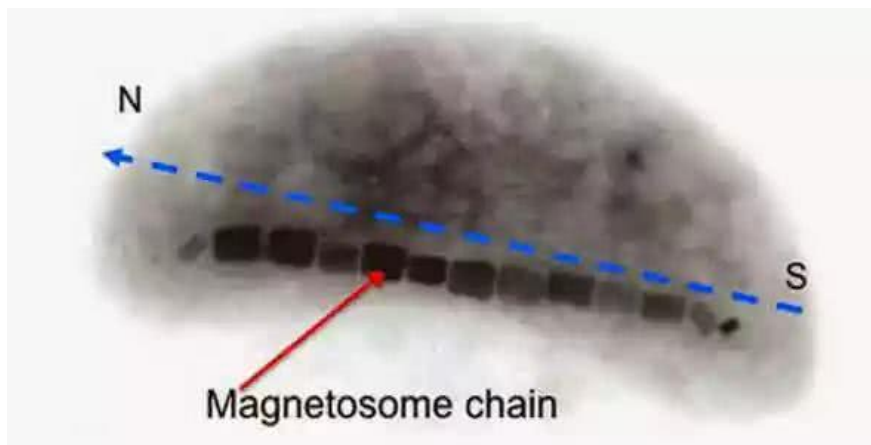


Modified after Ref.[4]

# Magnetite based Magnetoreception

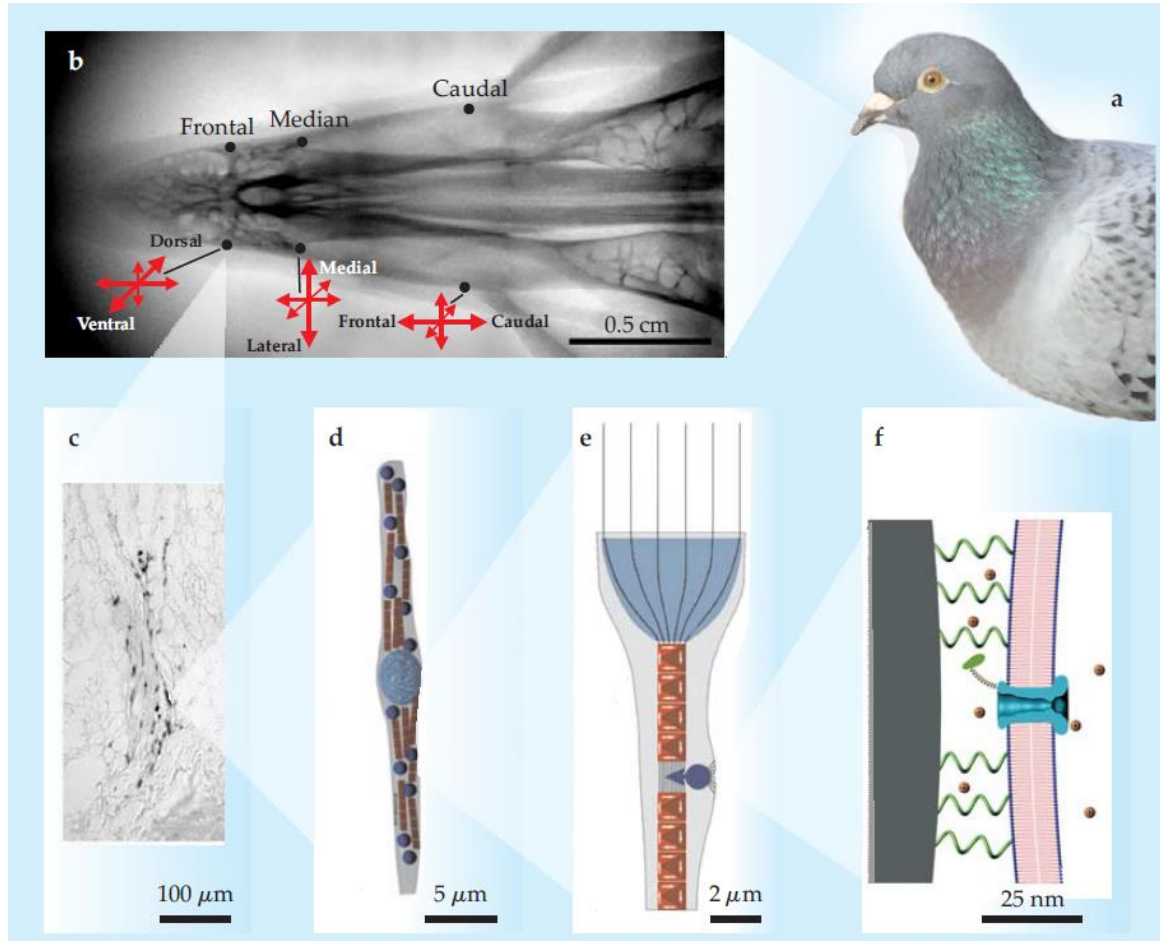
Magnetic force -> Physical rotation

- Magnetotactic bacteria
- A magnetosome chain:
- 15-20  $\text{Fe}_3\text{S}_4$ ,  $\text{Fe}_3\text{O}_4$  crystal
- 30-100nm for each crystal

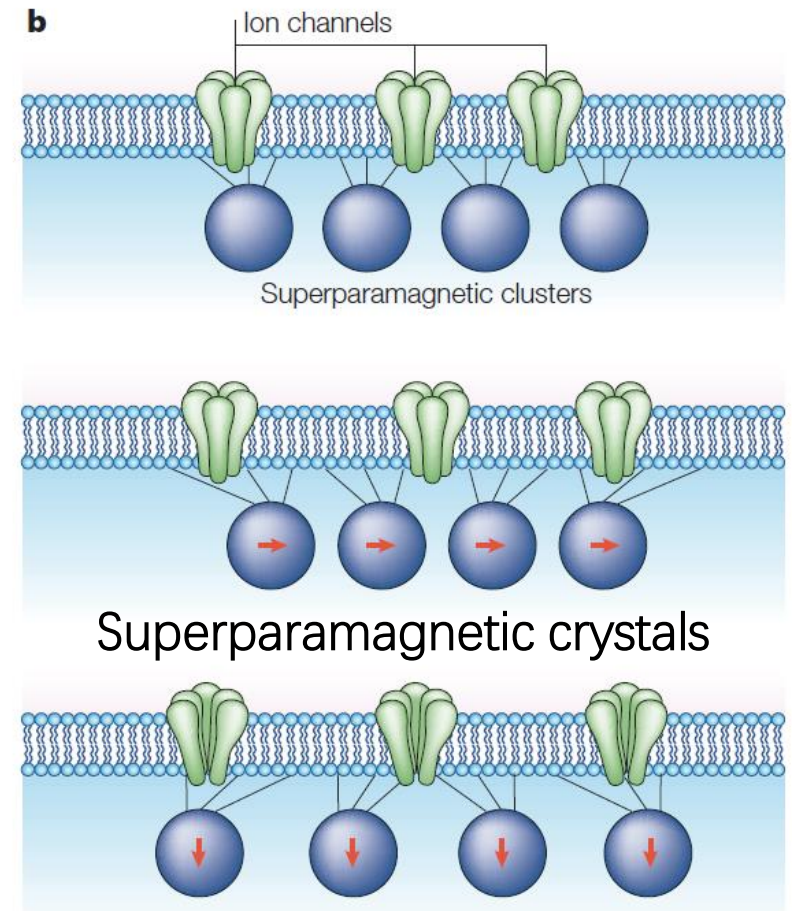


# Magnetite based Magnetoreception

Magnetic information -> Pressure signal -> Electric signal



Modified after Ref.[4]



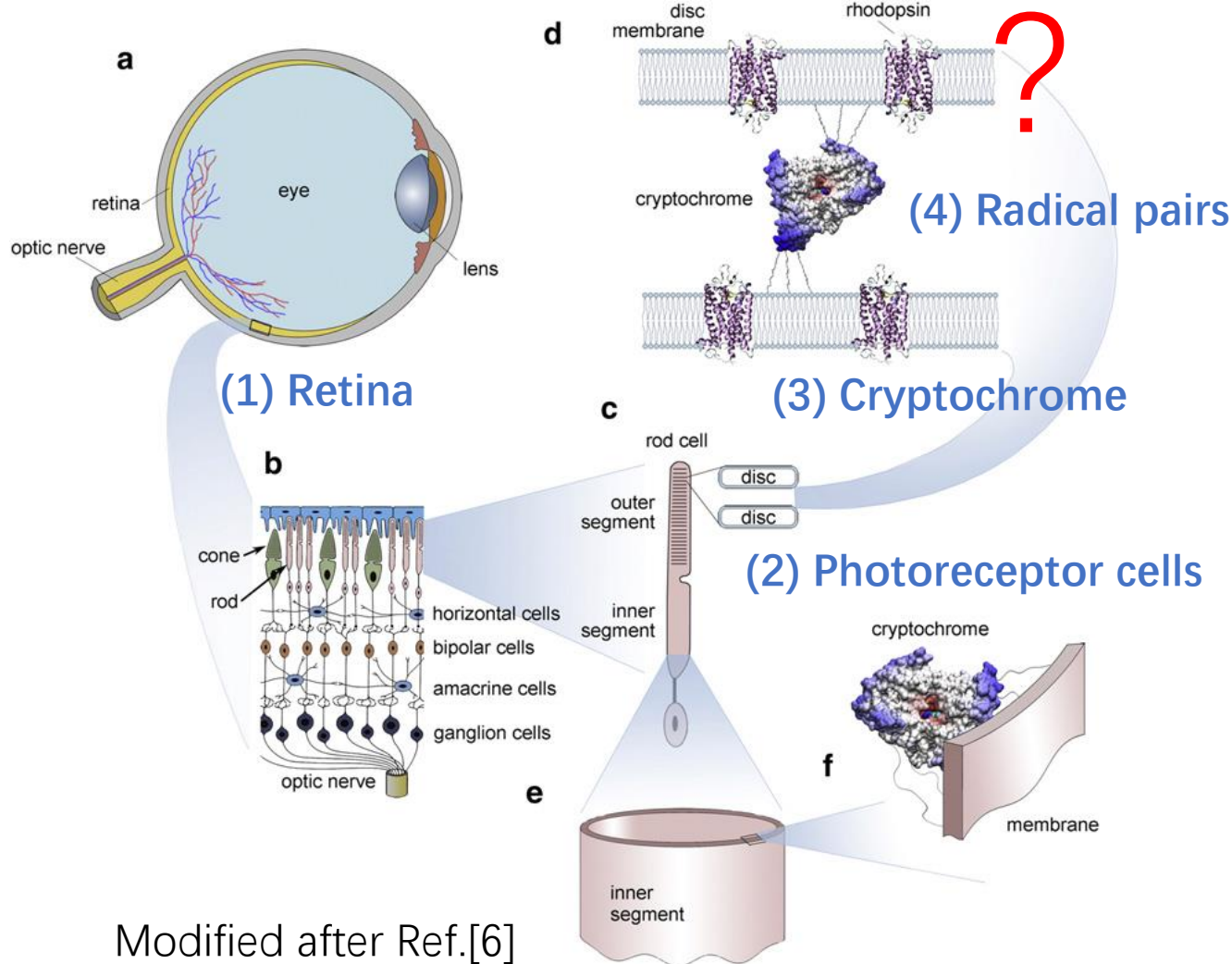
Modified after Ref.[3]



# Radical based magnetoreception

Magnetic information -> Chemical signal -> Electric signal

## (5) Visual pathway



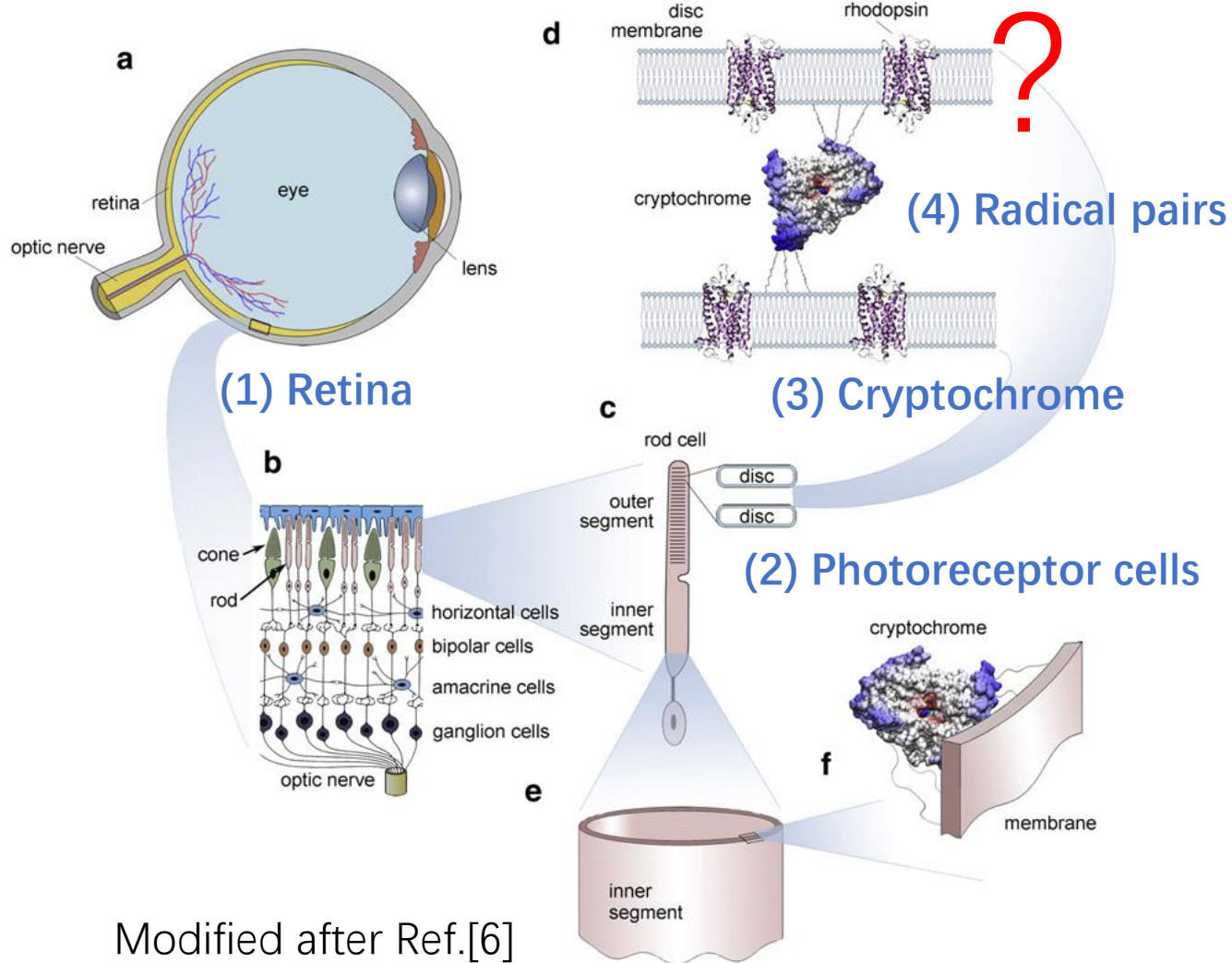
- 1) A **neural connection** between night vision and magnetic sensing in European robin.[12]
- 2) Different wavelength of incident light can **disrupt magnetic orientation** of European robin.[13,14]
- 3) The magnetic compass of European robin is a **inclination compass with  $<5^\circ$  precision**, which can be explained by radical pair mechanism instead of any other hypothesis.[15,16]
- 4) Cryptochrome is the **only protein family** that can form a **light-induced radical pair**.

Modified after Ref.[6]

# Radical based magnetoreception

Magnetic information -> Chemical signal -> Electric signal

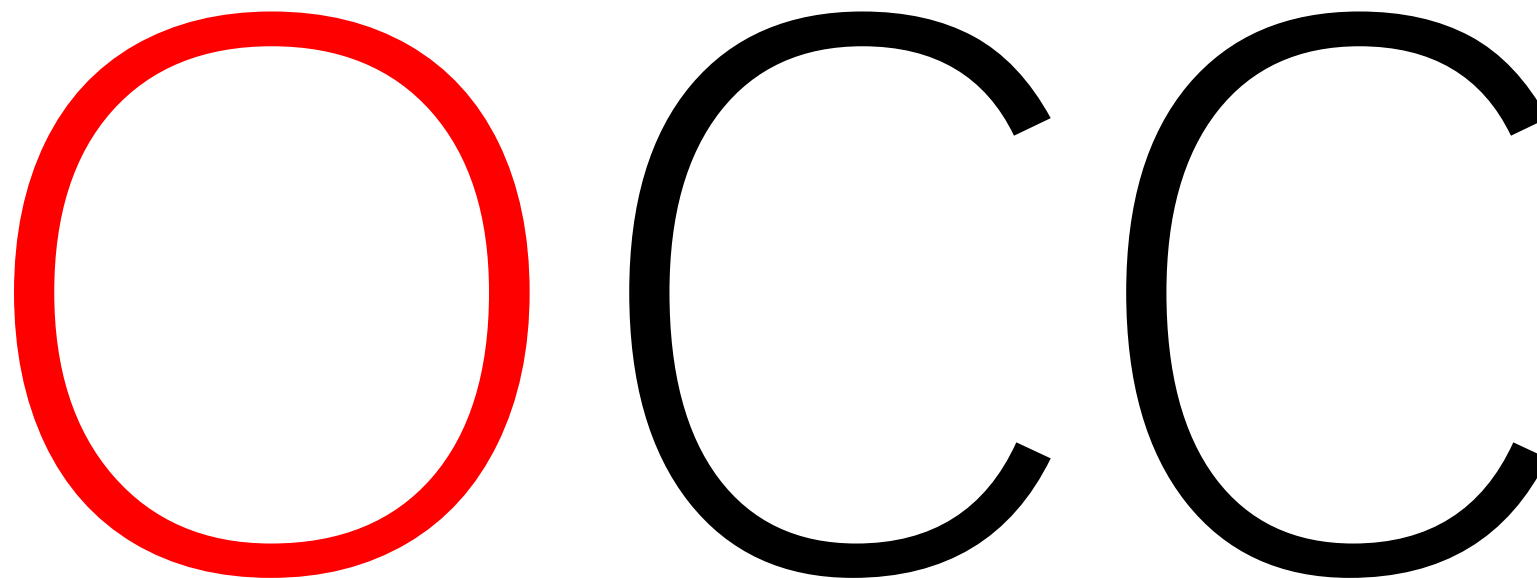
## (5) Visual pathway



Modified after Ref.[6]

- 5) **Cry4 protein**, a member of cryptochrome family, is found recently located on the **outer segment** in cones in birds' retina.[17]
- 6) A popular hypothesis of (4)-(5) is an noncanonical biological pathway of visual system that can modulate night vision. **No such signaling pathway** is found till now.
- 7) We propose that no downstream signaling involved and instead a photon competition plays a key role. A novel biophysical model:

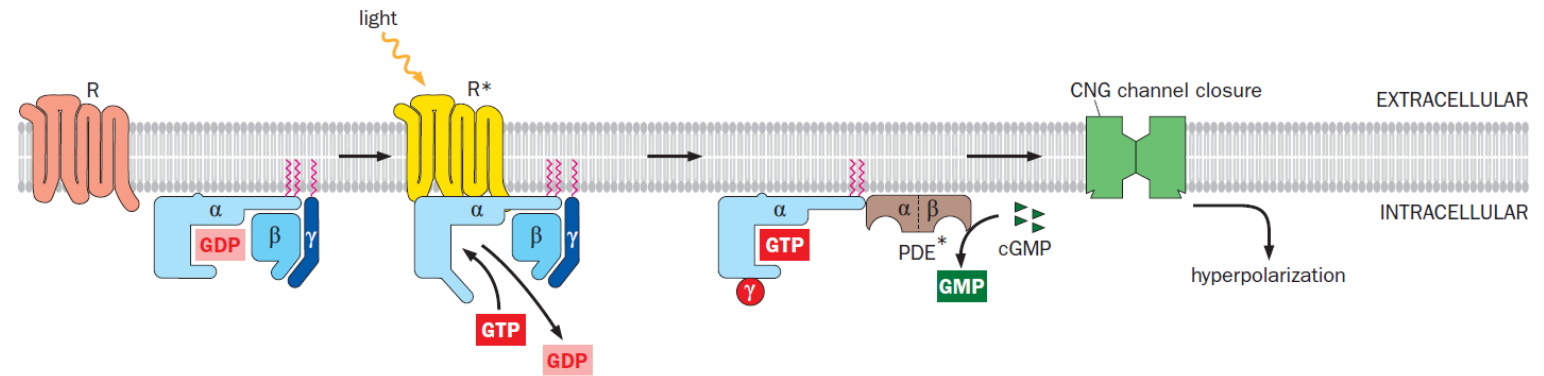
**Opsin-Cryptochrome competition model(OCC model).**



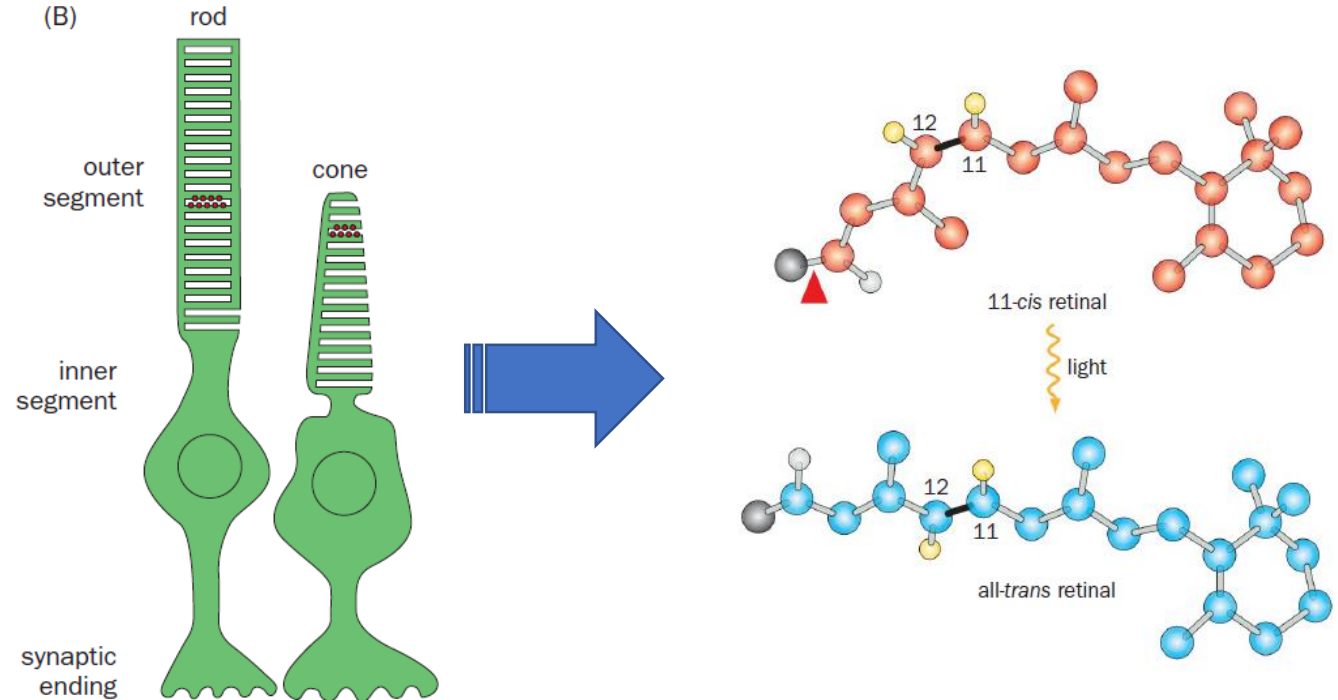
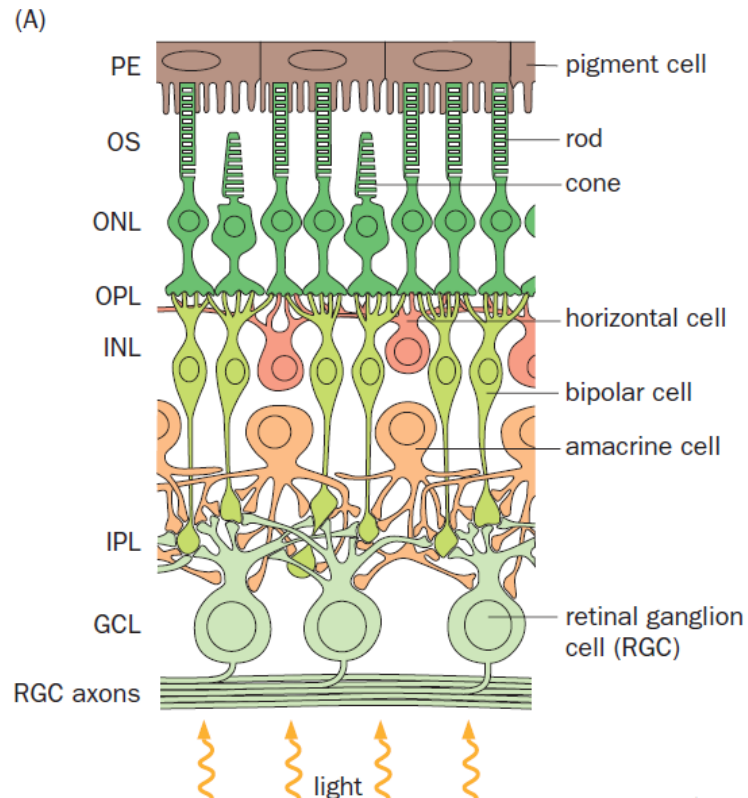
Opsin, Visual system



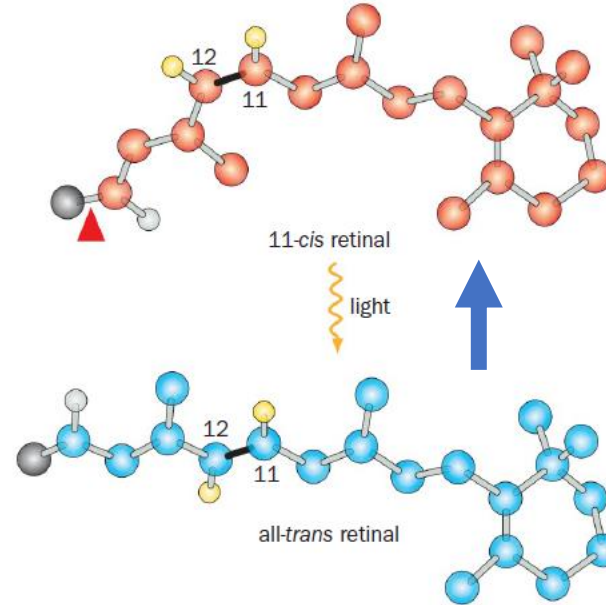
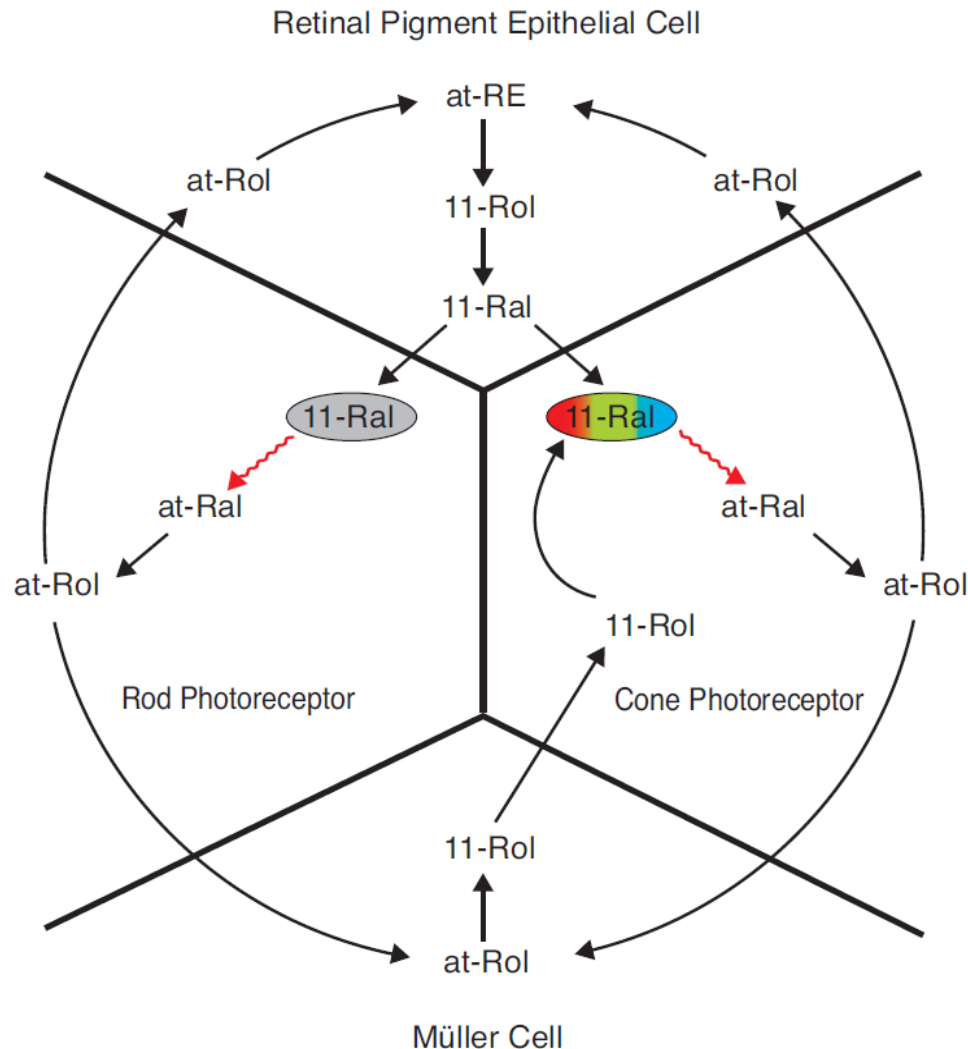
# Light perception



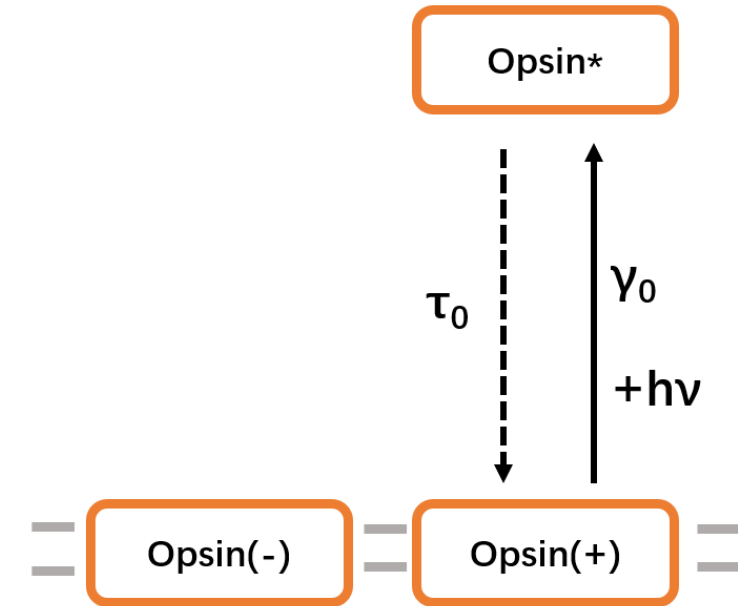
## Phototransduction cascade



# A cone visual cycle: cis-retinal $\leftrightarrow$ trans-retinal



Retinal in a rhodopsin



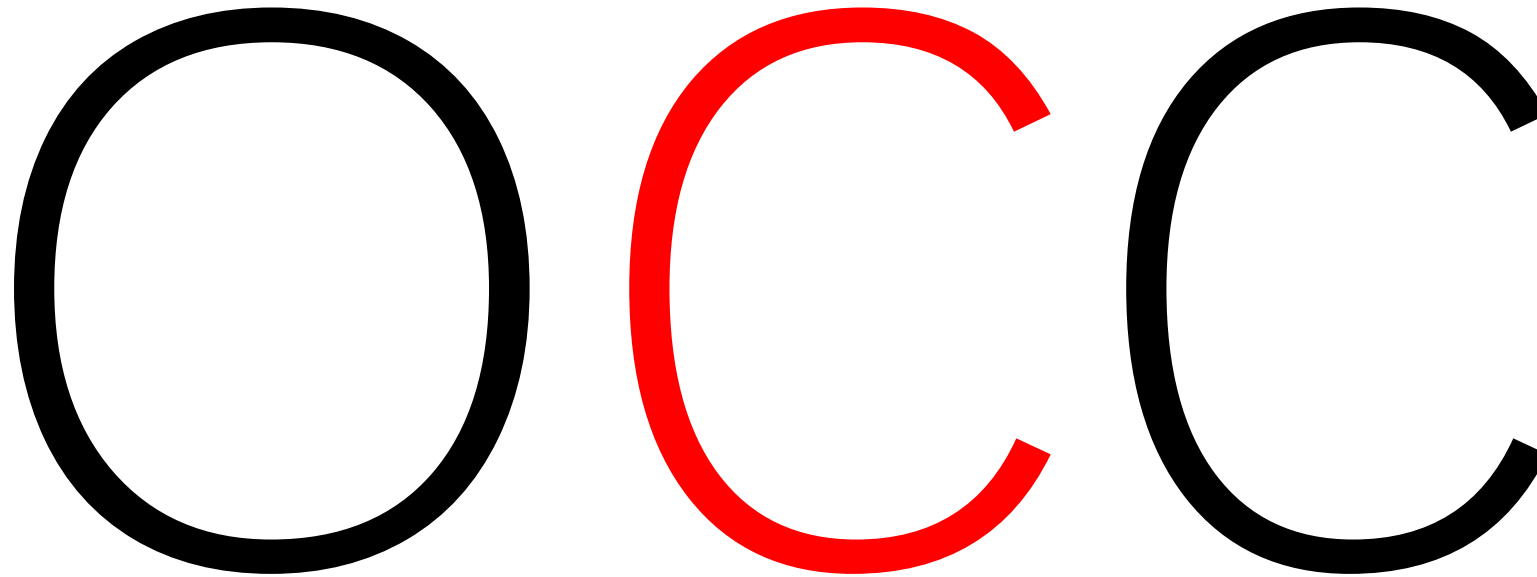
**Abbreviations:** at-RE, *all-trans*-retinyl esters; at-Ral, *all-trans*-retinal; at-Rol, *all-trans*-retinol; 11-Ral, 11-*cis*-retinal; 11-Rol, 11-*cis*-retinol.

Modified after Ref.[7,8]

# Photoreceptor proteins responsible for vision

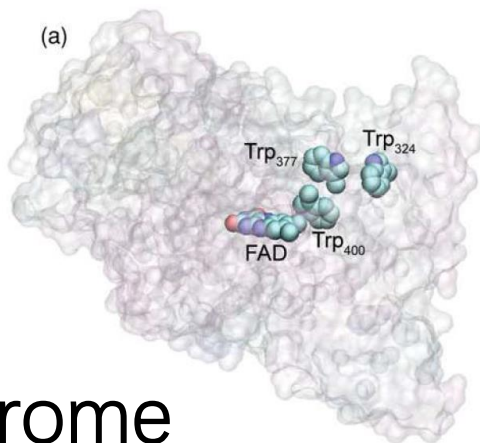
Name	Abbr.	Photo receptor	$\lambda_{\max}$	Color
Long-wave sensitive	LWS	Cone	500–570 nm	Green, yellow, red
Short-wave sensitive 1	SWS1	Cone	355–445 nm	Ultraviolet, violet
Short-wave sensitive 2	SWS2	Cone	400–470 nm	Violet, blue
Rhodopsin-like 2	Rh2	Cone	480–530 nm	Green
Rhodopsin-like 1 (vertebrate rhodopsin)	Rh1	Rod	~500 nm	Blue–green

**Cryptochrome can absorb one photon with wavelength ranging from 400-565nm.**

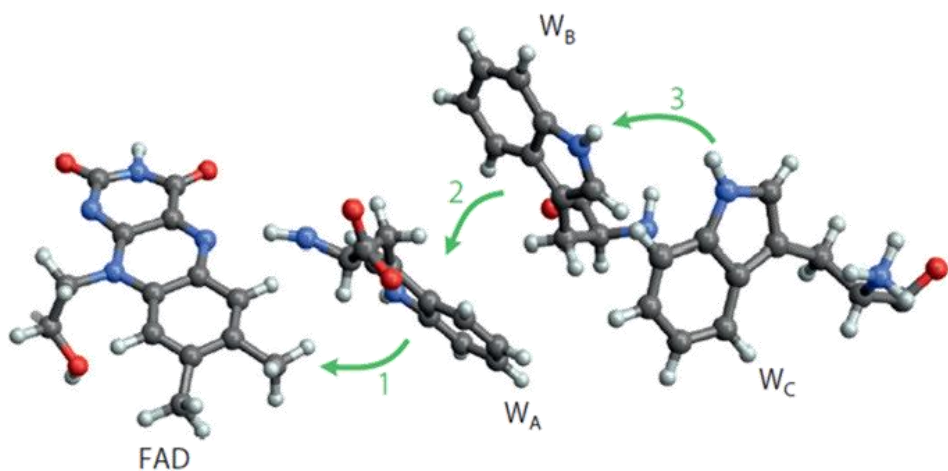


Cryptochrome, Radical pairs

# Principle of radical pair mechanism

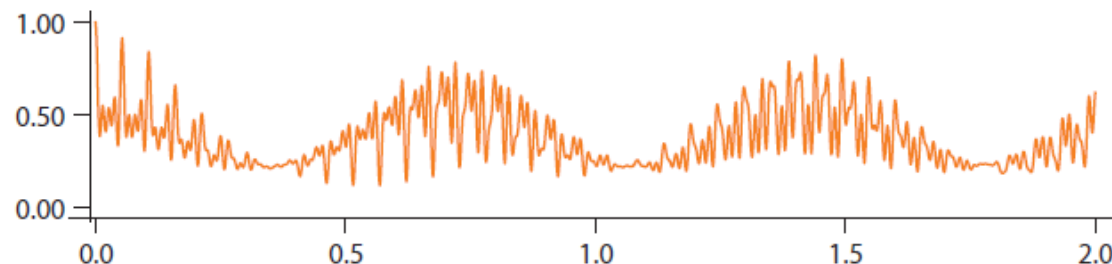


## Cryptochrome

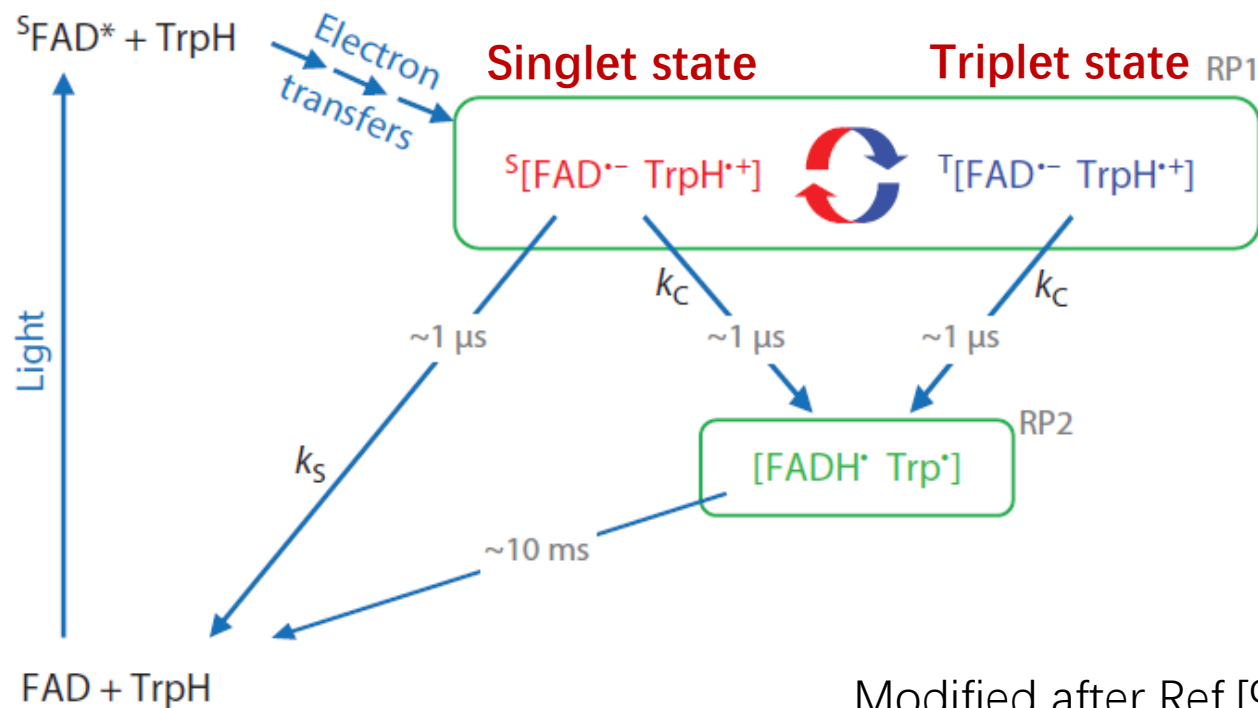


FAD - Flavin adenine dinucleotide  
Trp(W) - Tryptophan

Singlet Fraction

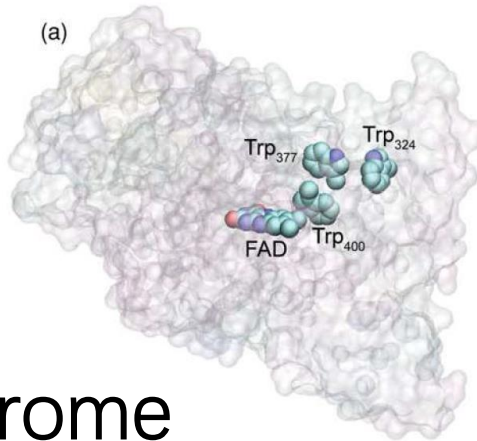


50  $\mu$ T



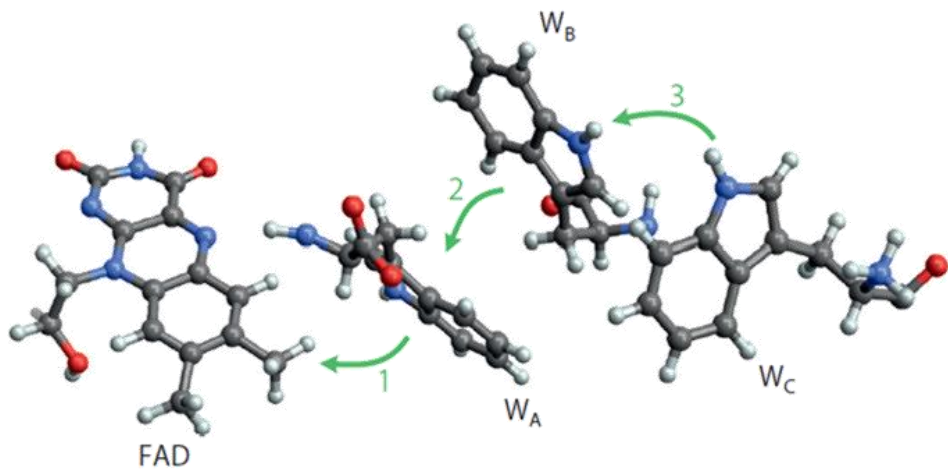
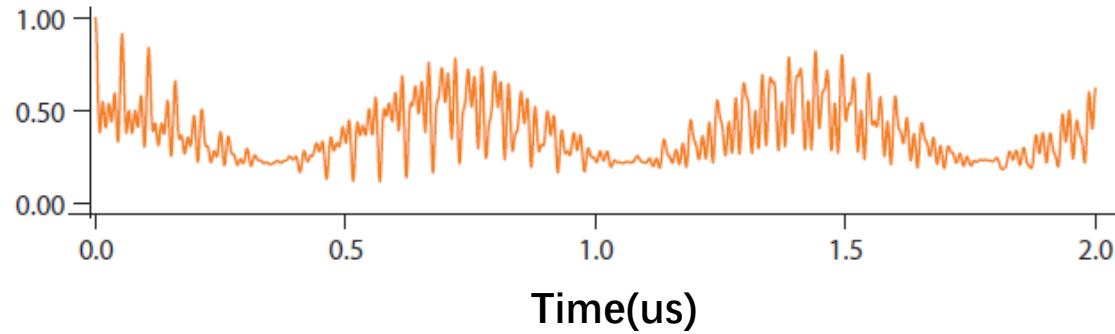
Modified after Ref.[9]

# Principle of radical pair mechanism

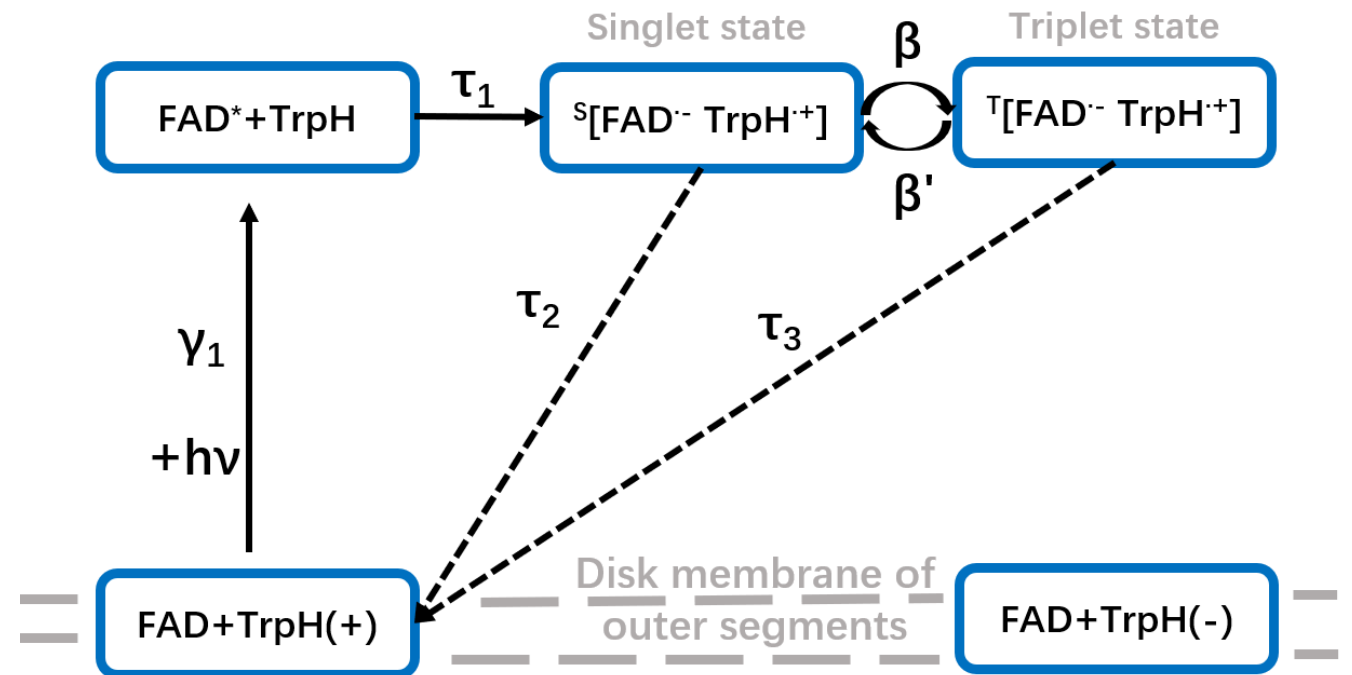


Cryptochrome

Singlet Fraction

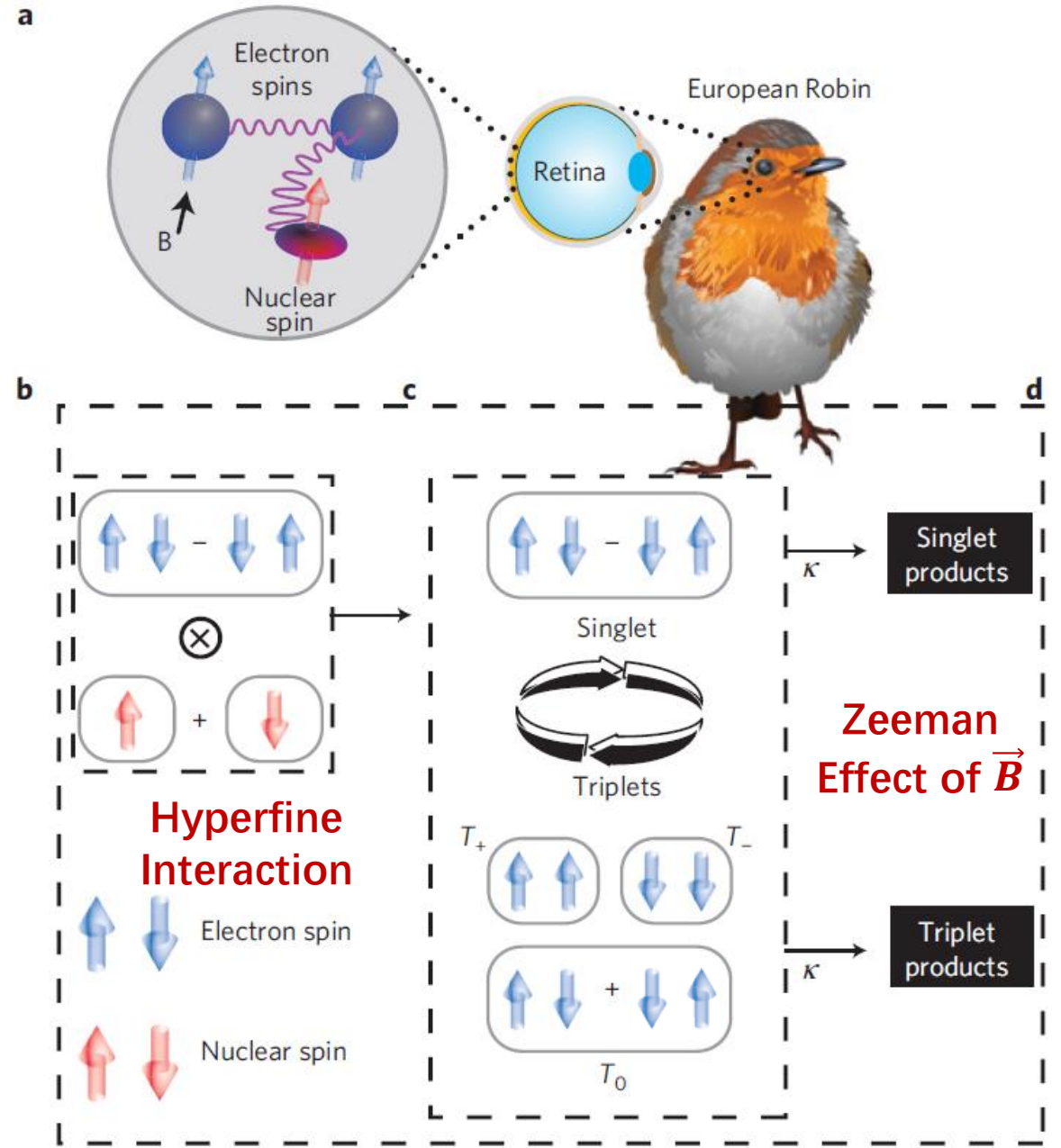
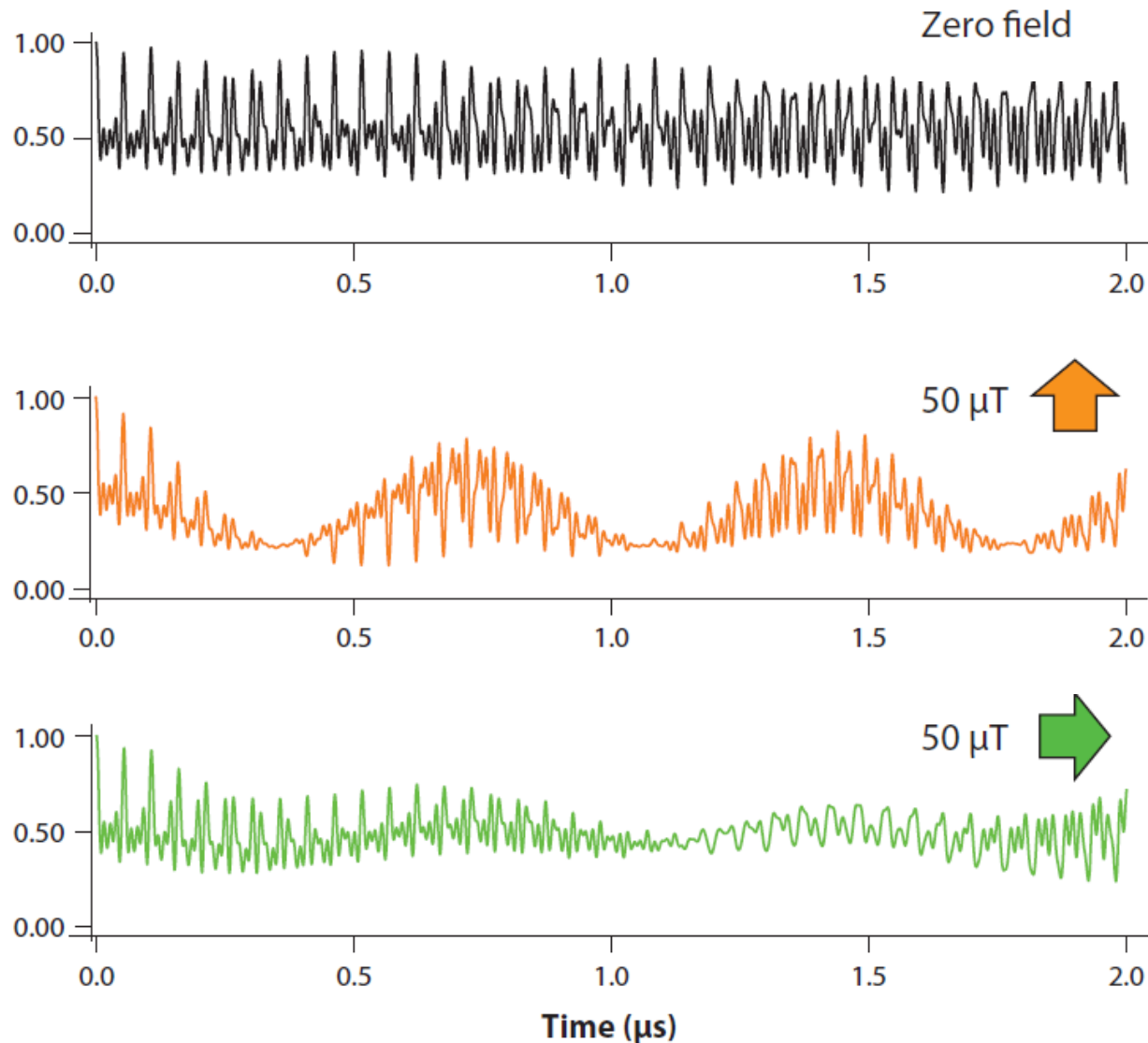


FAD - Flavin adenine dinucleotide  
Trp(W) - Tryptophan

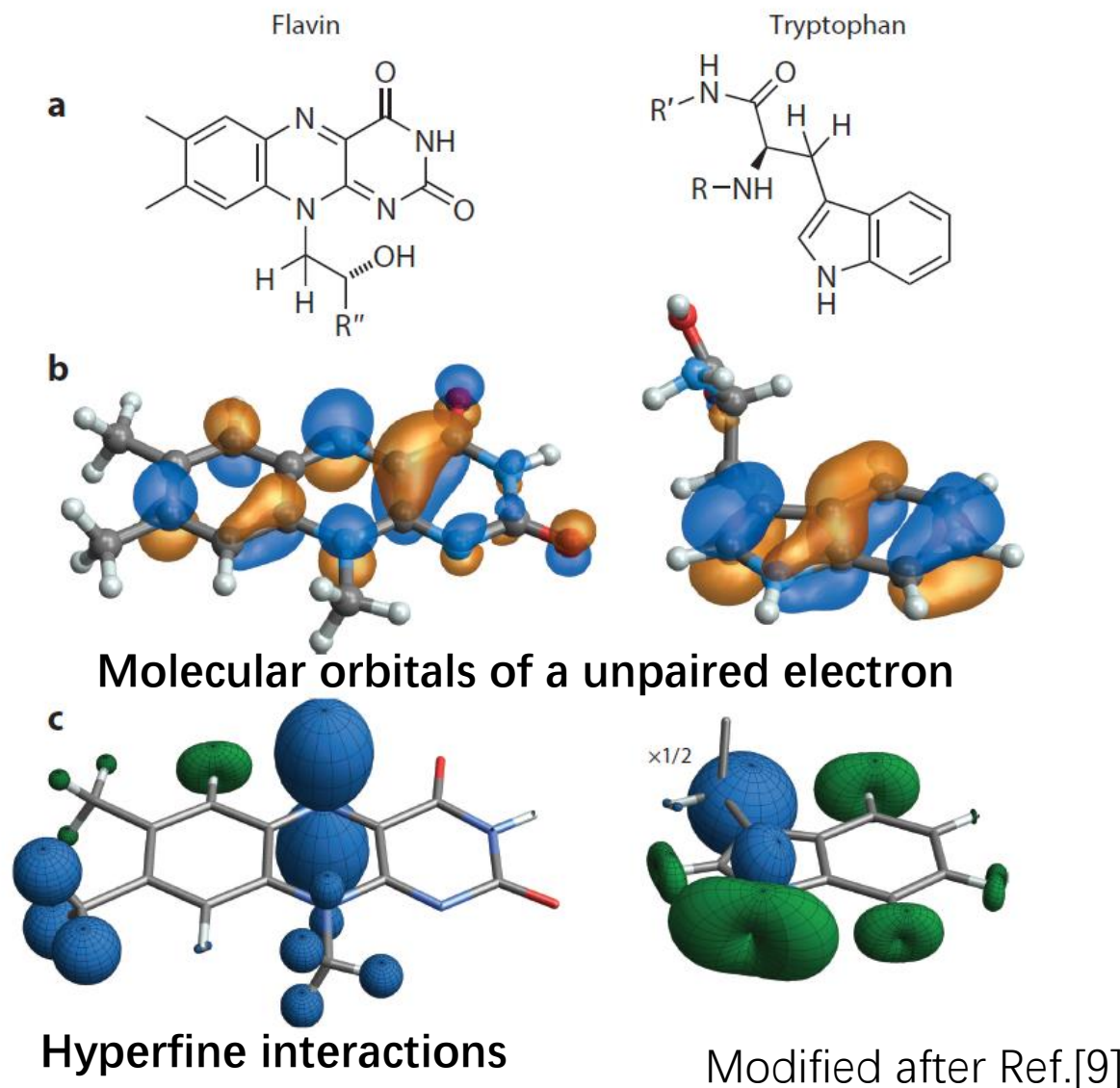




# Spin dynamics



# Quantum effect



The fractional yield of singlet and triplet state product is  $\phi_S = 1 - \phi_T$  is an integral of the real part of  $T(t)$  which is the singlet fraction at arbitrary time  $t$ .

$$\phi_T = k_T \int_0^\infty T(t) dt$$

$$T(t) = \text{Tr}[Q^T \rho(t)]$$

$Q^T$  is the projection operator of triplet state while  $\rho(t)$  is the density matrix of the radical pair at arbitrary time. The triplet state fraction is a trace operation of the density matrix projected on the triplet state product.

$$\rho(t) = \frac{1}{N} e^{-\frac{iHt}{\hbar}} \rho(0) e^{\frac{iHt}{\hbar}}$$

Assume there is only singlet product at time 0, where  $\rho(0) = Q^S e^{-kt}$ , here to make it simple, we let  $k = k_S = k_T$ .  $N$  is the number of nuclear spin.

The hamiltonian for two electron spins are  $H_1$  and  $H_2$  respectively.  $\vec{B}$  is the magnetic field vector with a specific direction.

$$H = H_1(\vec{B}) + H_2(\vec{B})$$

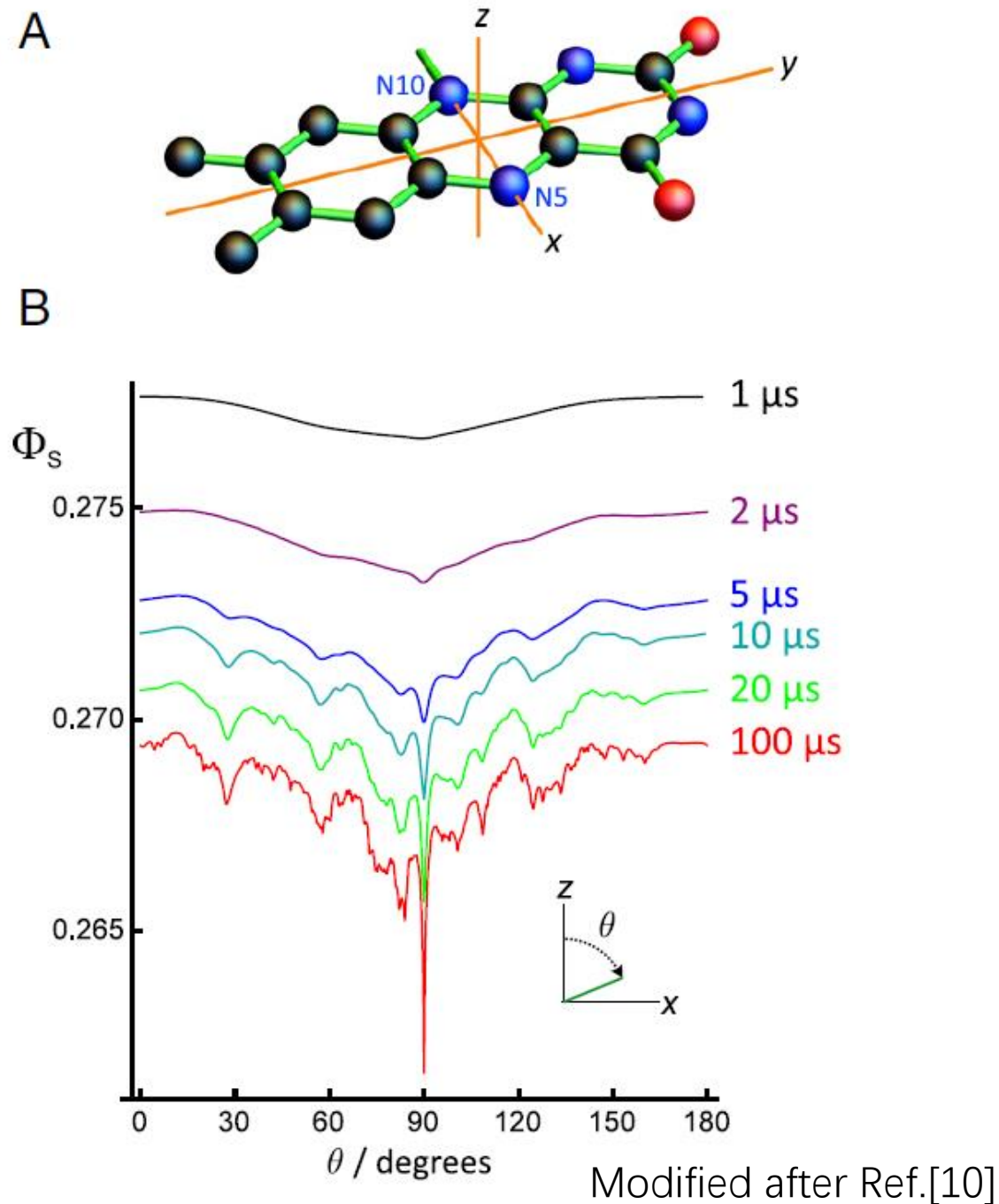
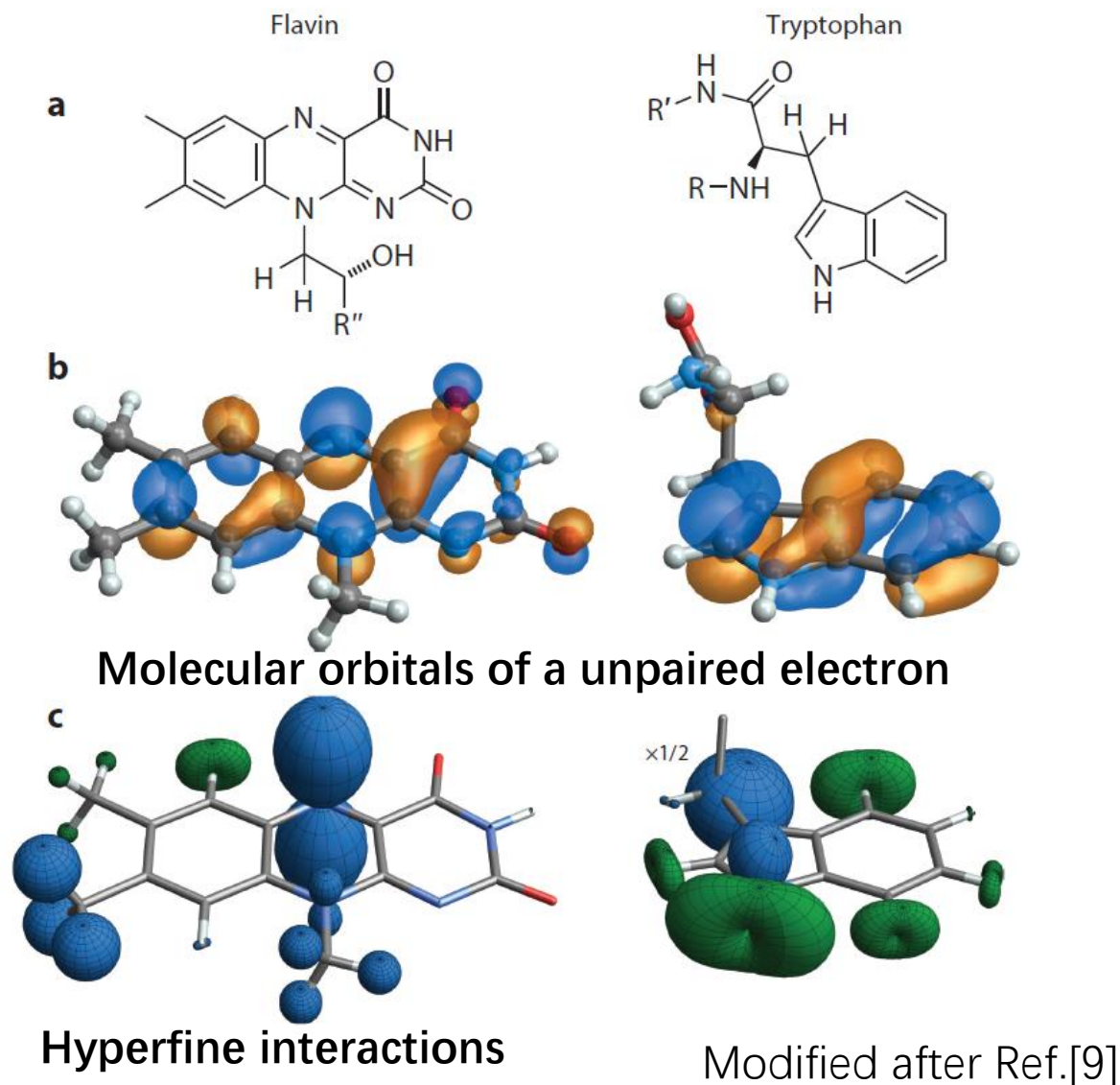
$$H_j = g\mu_B \vec{S}_j \cdot (\vec{B} + A_j \vec{I}_j)$$

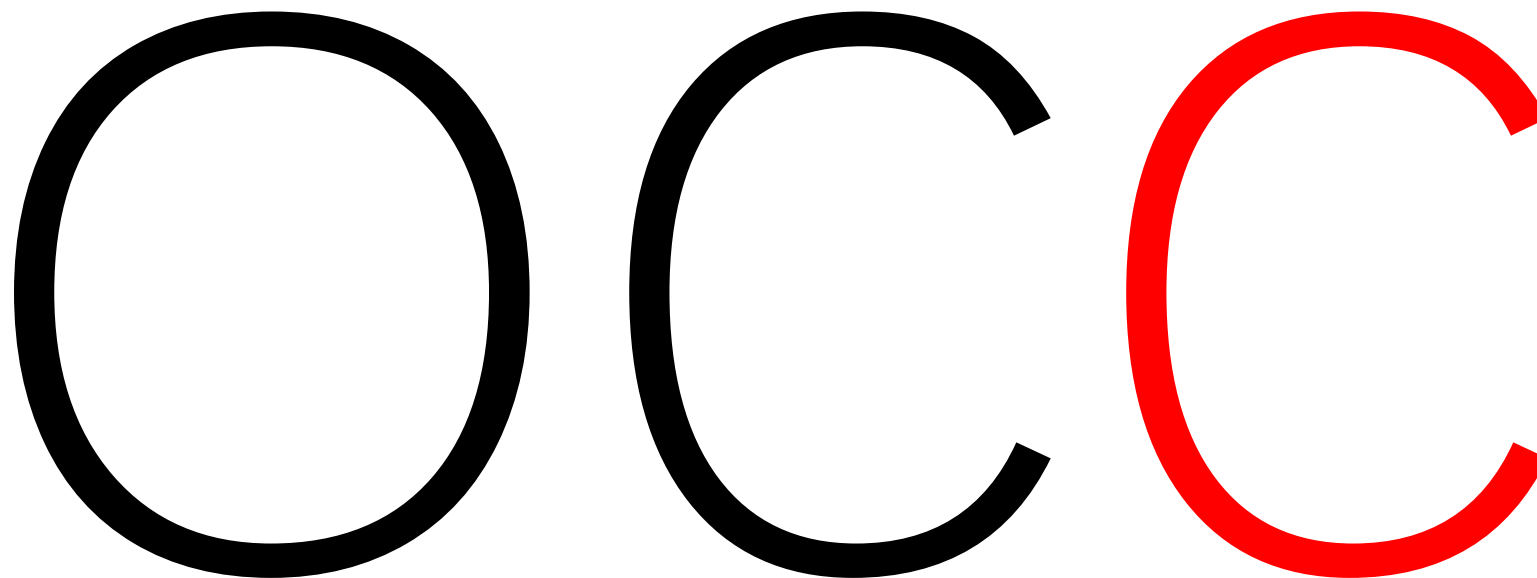
$\vec{S}_j$  is the electron spin operator whereas  $\vec{I}_j$  is the nuclear spin operator correlated with the nuclear spin in vicinity.  $A_j$  is the anisotropic coefficient of the nuclear spin.

$$T(t) = \phi_S = 1 - \text{Tr}[Q^T \frac{1}{N} e^{-\frac{iHt}{\hbar}} Q^S e^{-kt} e^{\frac{iHt}{\hbar}}]$$

$$\phi_S = 1 - \frac{1}{N} \sum_{mn} Q_{mn}^T Q_{nm}^S \frac{k^2}{k^2 + (\omega_m - \omega_n)^2}$$

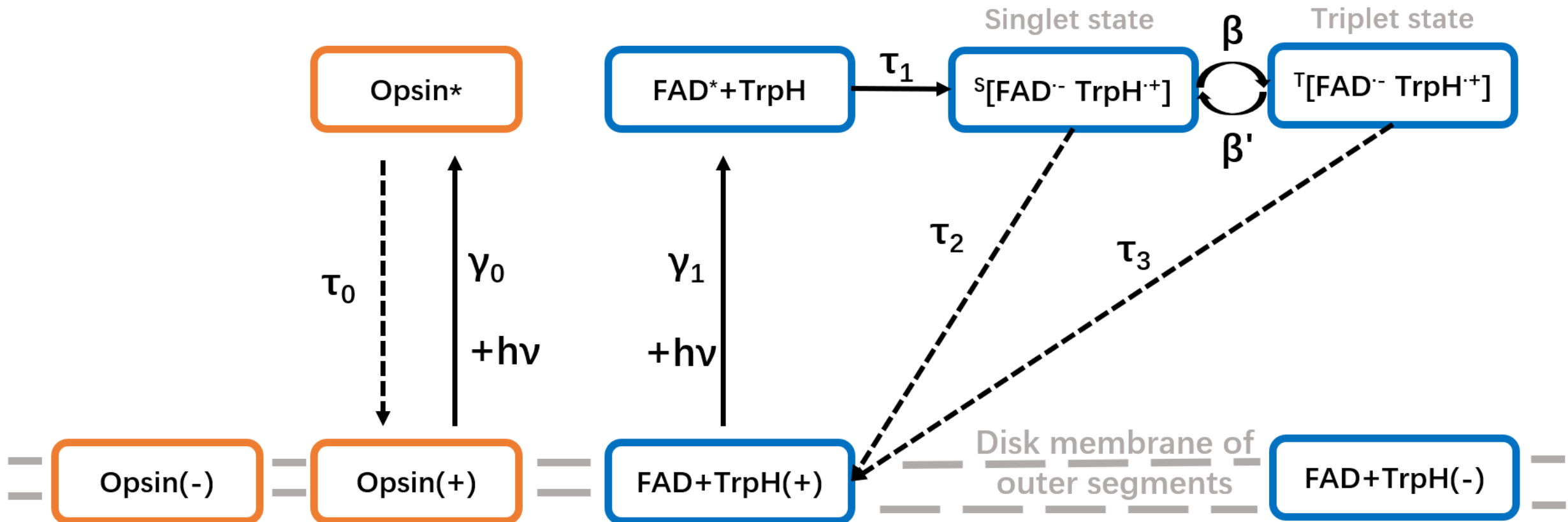
# Quantum effect





Photon Competition

# Opsin-Cryptochrome Competition model



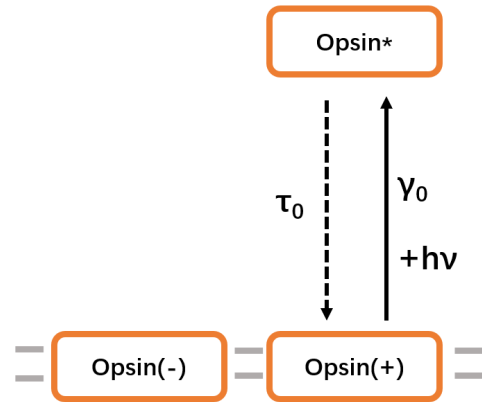
(+) represents the ground state of a molecule absorbed by one photon; (\*) represents the excitation state of a molecule after photon absorption; (s) and (t) represent the singlet and triplet state of a molecule.



# Model formulation

$$N_{op}^{(+)} + N_{FAD}^{(+)} = N_{photon} \quad (9)$$

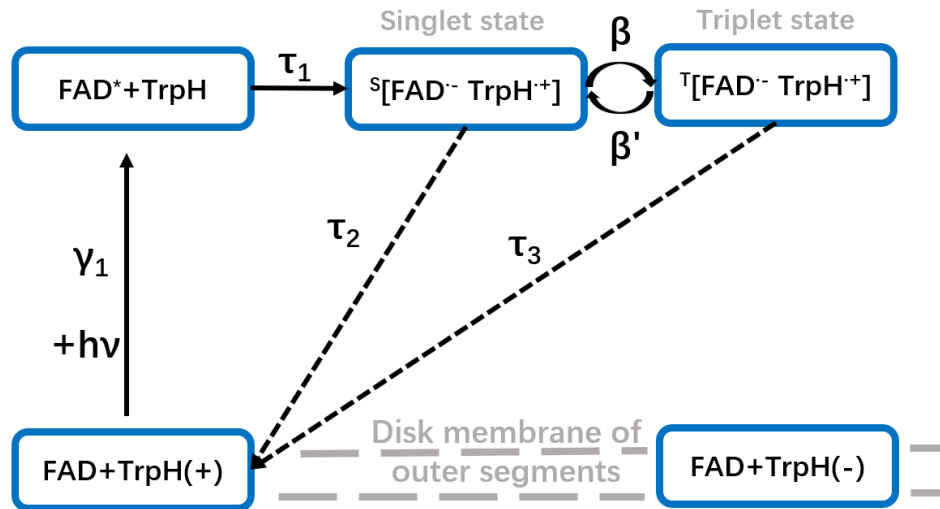
$$R_{opsin} = \frac{N_{op}^{(+)}}{N_{photon}} \quad (10)$$



$$N_{op}^{(+)} + N_{op}^* + N_{op}^{(-)} = C_1 \quad (1)$$

$$\frac{d(N_{op}^{(+)} + N_{op}^{(-)})}{dt} = -\gamma_0 N_{op}^{(+)} + \frac{1}{\tau_0} N_{op}^* \quad (2)$$

$$\frac{dN_{op}^*}{dt} = \gamma_0 N_{op}^{(+)} - \frac{1}{\tau_0} N_{op}^* \quad (3)$$



$$N_{FAD}^{(+)} + N_{FAD}^* + N_{FAD}^{Singlet} + N_{FAD}^{Triplet} + N_{FAD}^{(-)} = C_2 \quad (4)$$

$$\frac{d(N_{FAD}^{(+)} + N_{FAD}^{(-)})}{dt} = -\gamma_1 N_{FAD}^{(+)} + \frac{1}{\tau_2} N_{FAD}^{Singlet} + \frac{1}{\tau_3} N_{FAD}^{Triplet} \quad (5)$$

$$\frac{dN_{FAD}^*}{dt} = \gamma_1 N_{FAD}^{(+)} - \frac{1}{\tau_1} N_{FAD}^* \quad (6)$$

$$\frac{dN_{FAD}^{Singlet}}{dt} = \frac{1}{\tau_1} N_{FAD}^* - \frac{1}{\tau_2} N_{FAD}^{Singlet} - \beta N_{FAD}^{Singlet} + \beta' N_{FAD}^{Triplet} \quad (7)$$

$$\frac{dN_{FAD}^{Triplet}}{dt} = \beta N_{FAD}^{Singlet} - \beta' N_{FAD}^{Triplet} - \frac{1}{\tau_3} N_{FAD}^{Triplet} \quad (8)$$



A stationary solution: let all derivatives=0

$$N_{op}^{(+)} + N_{FAD}^{(+)} = N_{photon} \quad (9)$$

$$R_{opsin} = \frac{N_{op}^{(+)}}{N_{photon}} \quad (10)$$

$$N_{op}^{(-)} + B * N_{op}^{(+)} = C_1 \quad (11)$$

$$N_{FAD}^{(-)} + A * N_{FAD}^{(+)} = C_2 \quad (12)$$

$$(A - B)N_{op}^{(+)^2} + (C_1 + C_2 - N_{photon}(A - B))N_{op}^{(+)} - N_{photon}C_1 = 0 \quad (15)$$

$$R_{opsin} = \frac{-(C_1 + C_2 - N_{photon}(A - B)) + \sqrt{(C_1 + C_2 - N_{photon}(A - B))^2 + 4N_{photon}C_1(A - B)}}{2N_{photon}(A - B)} \quad (16)$$

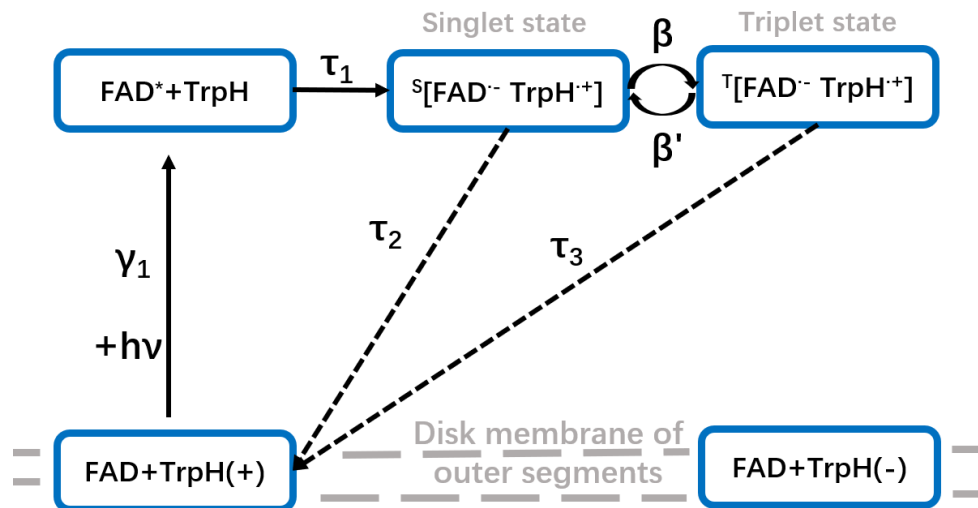
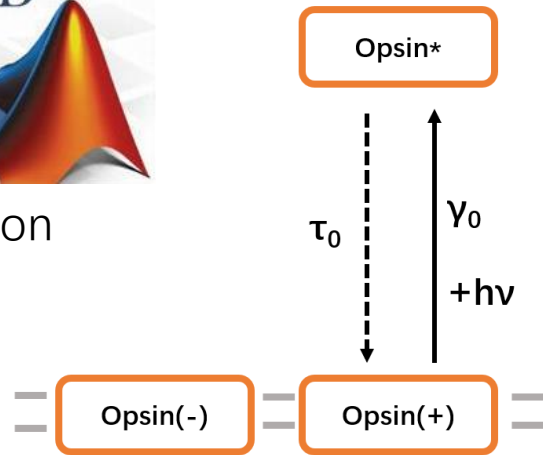
$$A = 1 + \gamma_1 \left( \tau_1 + \frac{1}{\frac{\beta'}{\tau_2\beta} + \frac{1}{\tau_2\tau_3\beta} + \frac{1}{\tau_3}} + \frac{1}{\frac{1}{\tau_2} + \frac{\beta}{\tau_3\beta' + 1}} \right) \quad B = \tau_0\gamma_0 + 1$$

# Simulation

# Parameter initiation



Simulation



- **Singlet-triplet oscillation  $\beta$  coefficient:**

$$\beta' = 0; \beta = \frac{\Delta(\Phi T)}{\Delta(\tau_2)} \text{ in terms of angle}$$

- **Reciprocal of rate constant(lifetime):**

$$\tau_0 = 4.2\text{ms}; \tau_1 = 1\text{ns};$$

$$\tau_2 = 1\mu\text{s}; \tau_3 = 10\text{ms};$$

- **Rate constant of light absorption:**

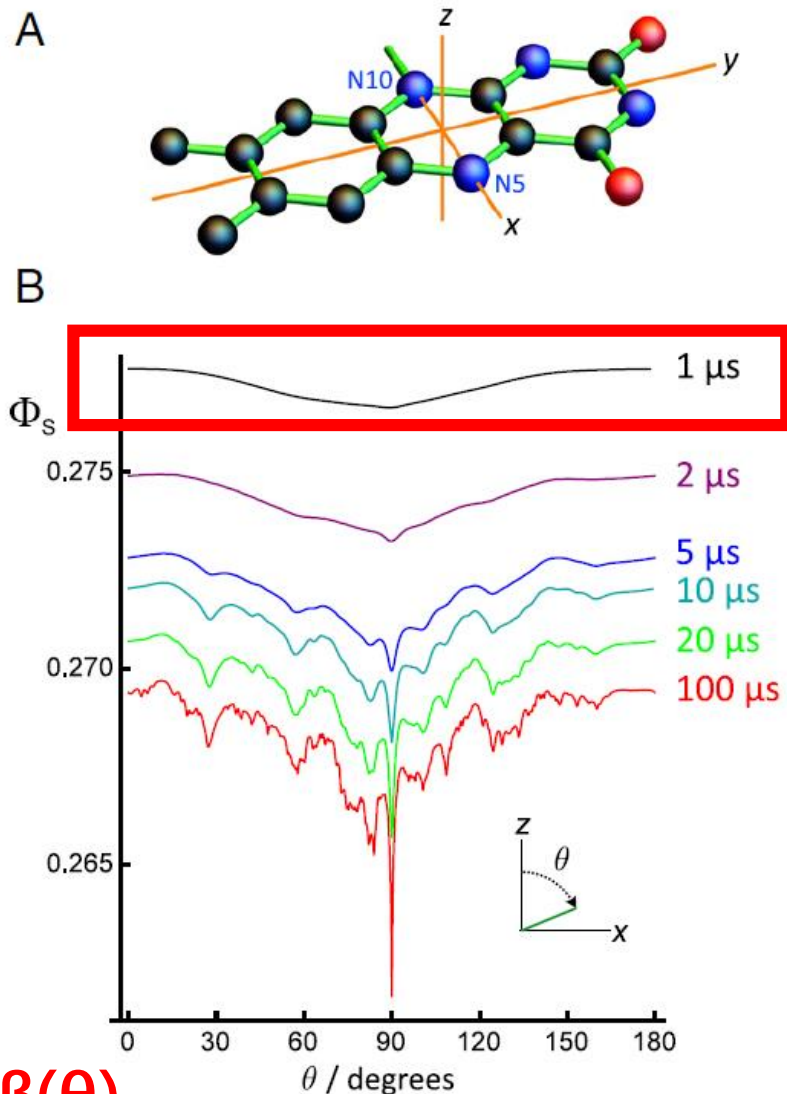
$$\gamma_0 = \gamma_1 = 10^9/\text{s};$$

- Assume the **protein number** of opsin and cryptochrome is the same:  $C_1 = C_2$

- **Incident photon number  $N_{\text{photon}}$**

$$\text{where } N_{\text{photon}} : C_1 = 10^{-3}$$

# Parameter initiation

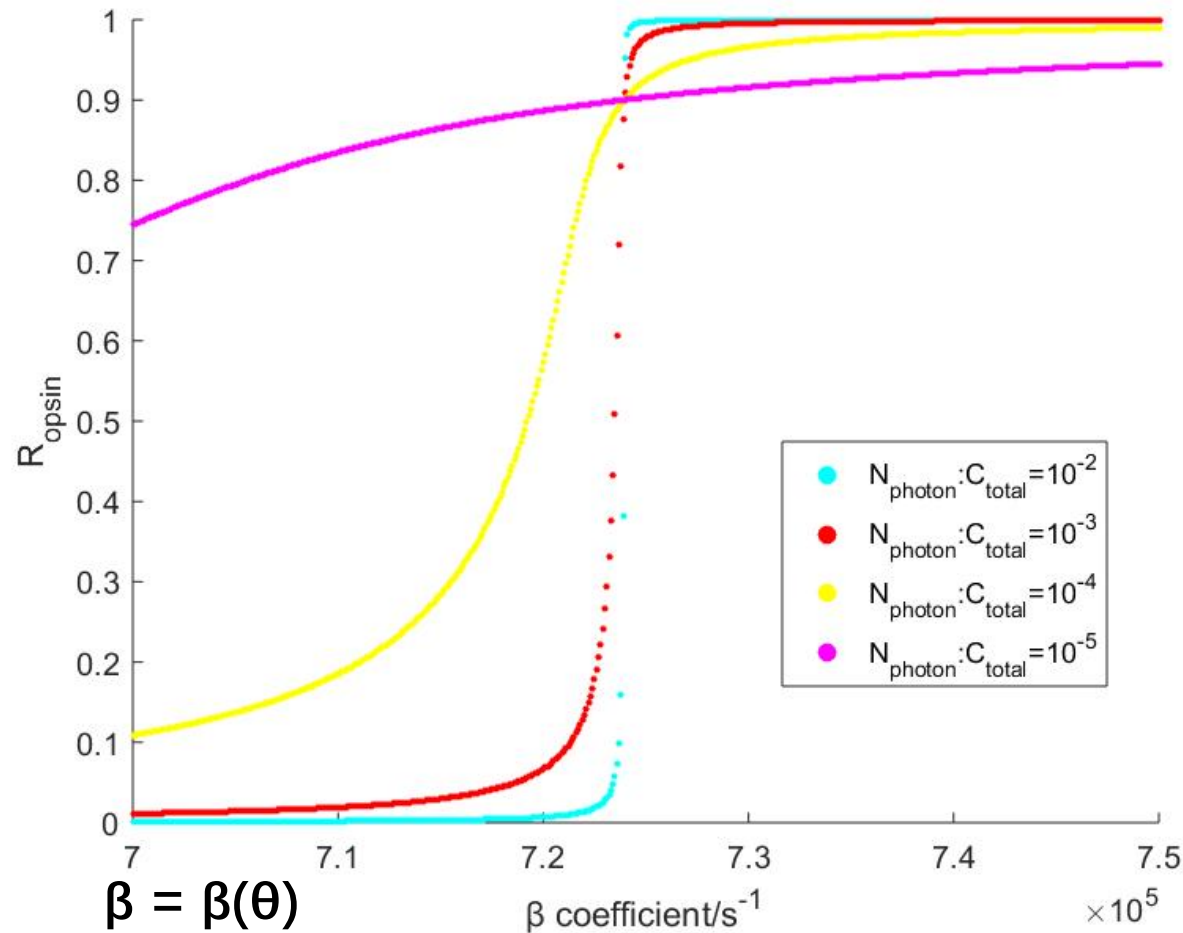


$$\beta = \beta(\theta)$$

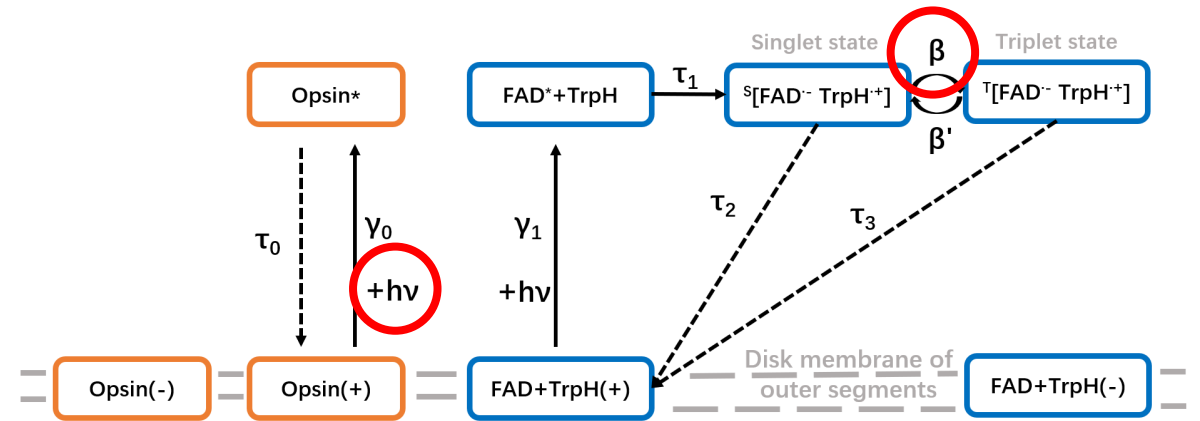
- Singlet-triplet oscillation  $\beta$  coefficient:  
 $\beta' = 0$ ;  $\beta = \frac{\Delta(\Phi T)}{\Delta(\tau_2)}$  in terms of angle
- Reciprocal of rate constant(lifetime):  
 $\tau_0 = 4.2\text{ms}$ ;  $\tau_1 = 1\text{ns}$ ;  
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- Assume the protein number of opsin and cryptochrome is the same:  $C_1 = C_2$
- Incident photon number  $N_{\text{photon}}$   
 where  $N_{\text{photon}}:C_1 = 10^{-3}$

# Secondary amplification effect

$$R_{opsin} = \frac{-(C_1 + C_2 - N_{photon}(A - B)) + \sqrt{(C_1 + C_2 - N_{photon}(A - B))^2 + 4N_{photon}C_1(A - B)}}{2N_{photon}(A - B)}$$

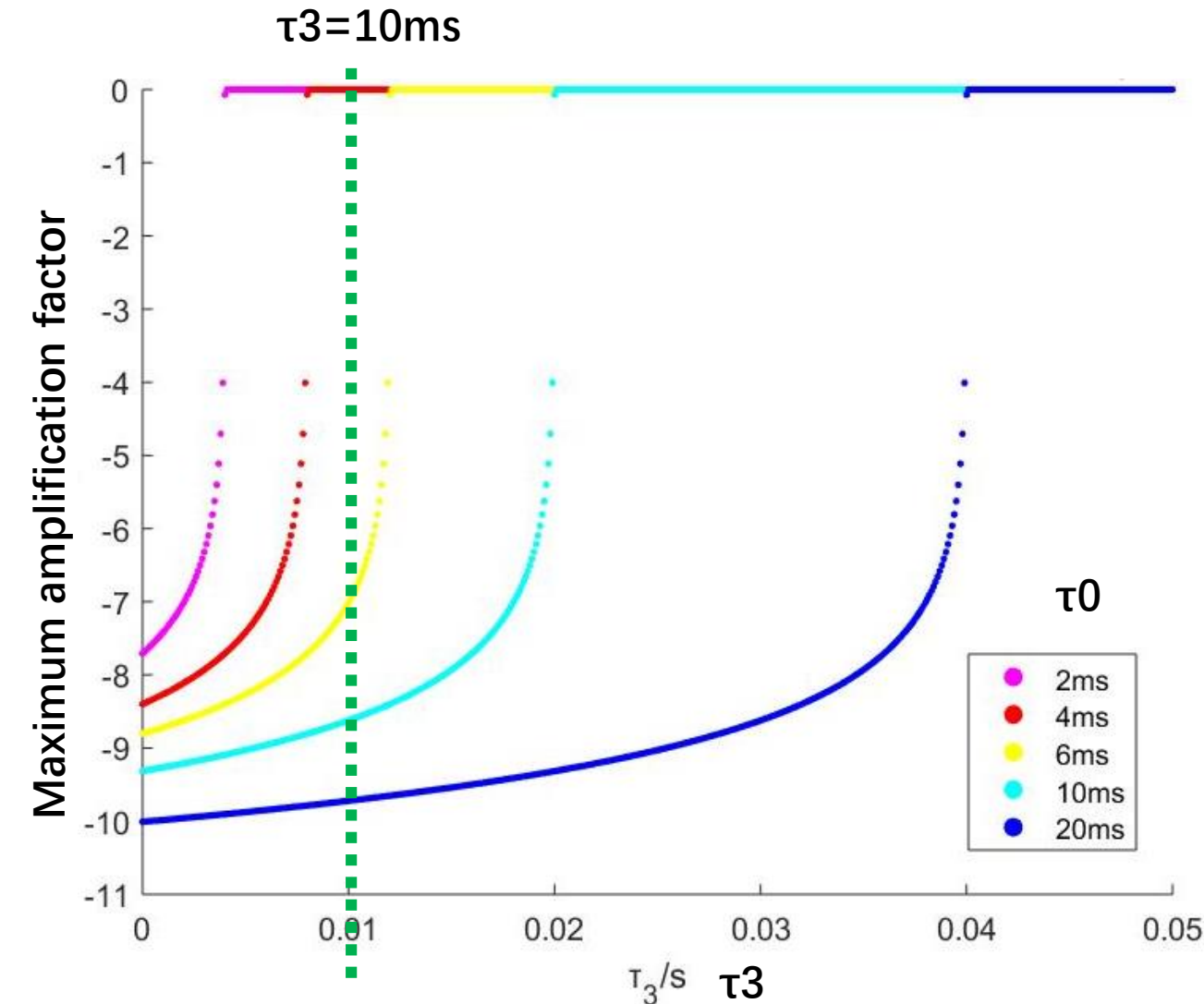


$R_{opsin} \in (0, 1)$  representing the percentage of incident photons that are absorbed by rhodopsin.

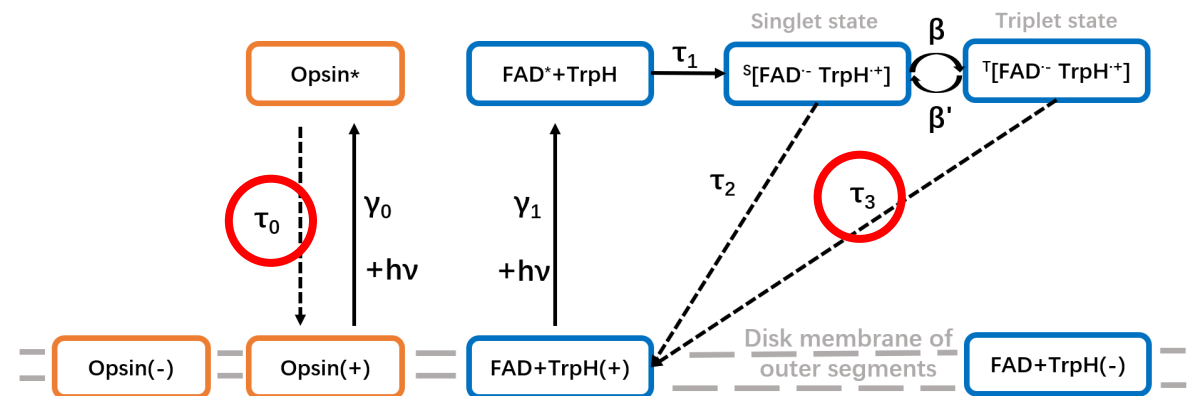


- Ratio of incident photons and protein numbers are critical for amplification **indicating a photon threshold** for magnetoreception.

# Secondary amplification effect

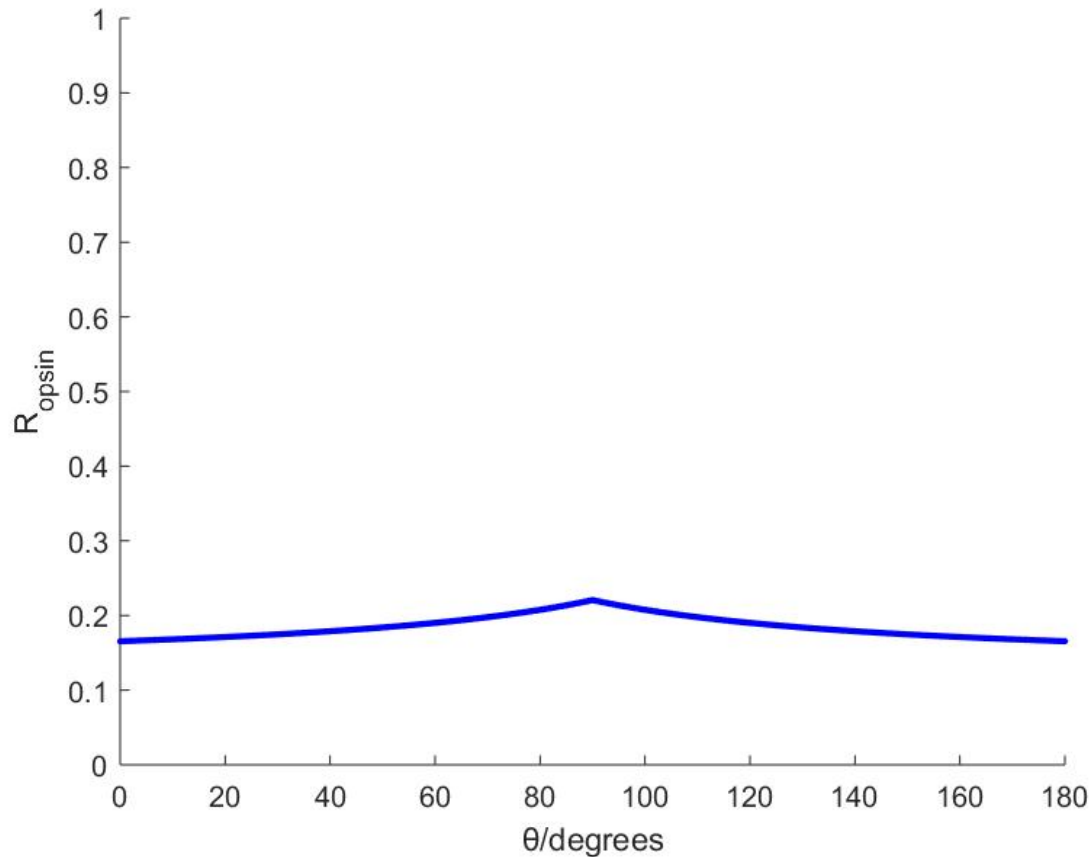


- The quantity of  $\tau_0$  is critical for the amplification effect.
- The secondary amplification effect is a key step to **convert a physical cause into biological consequence**.

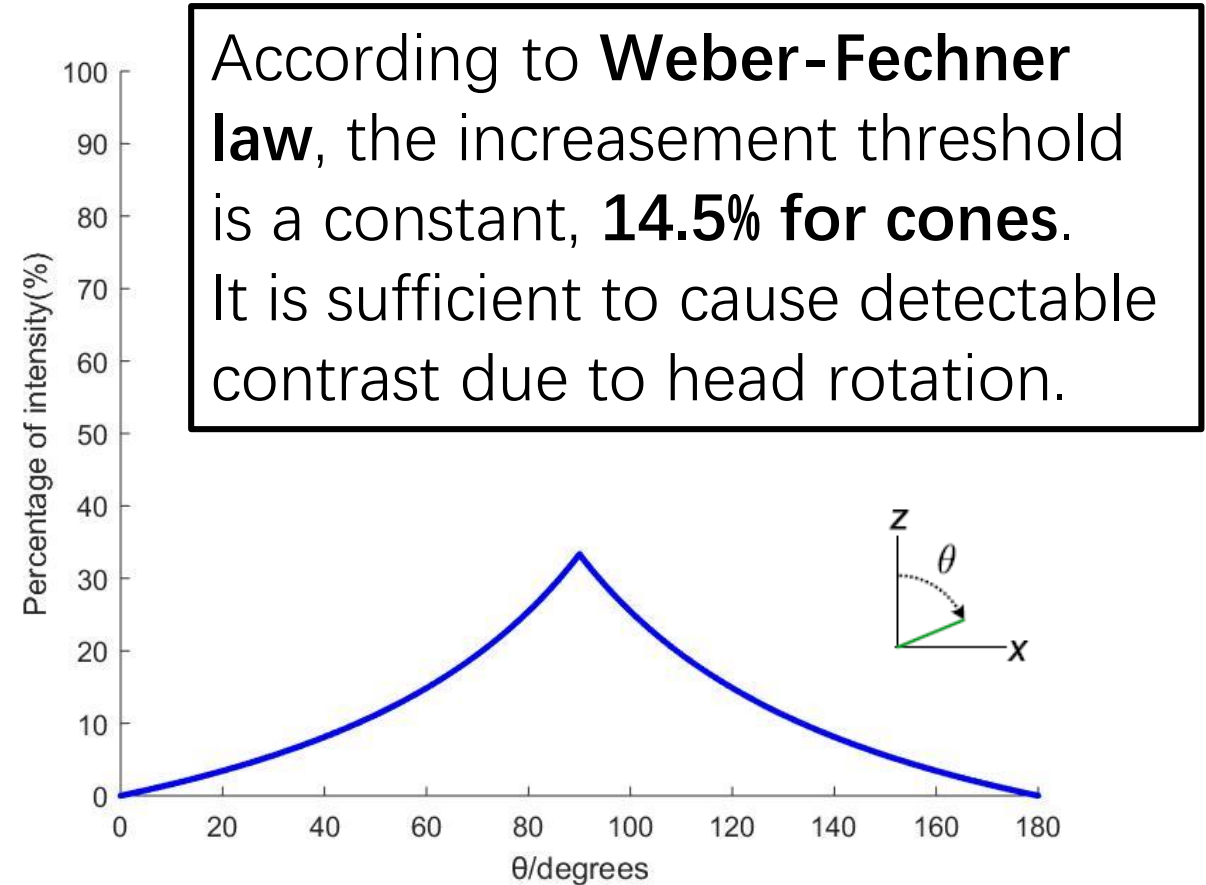




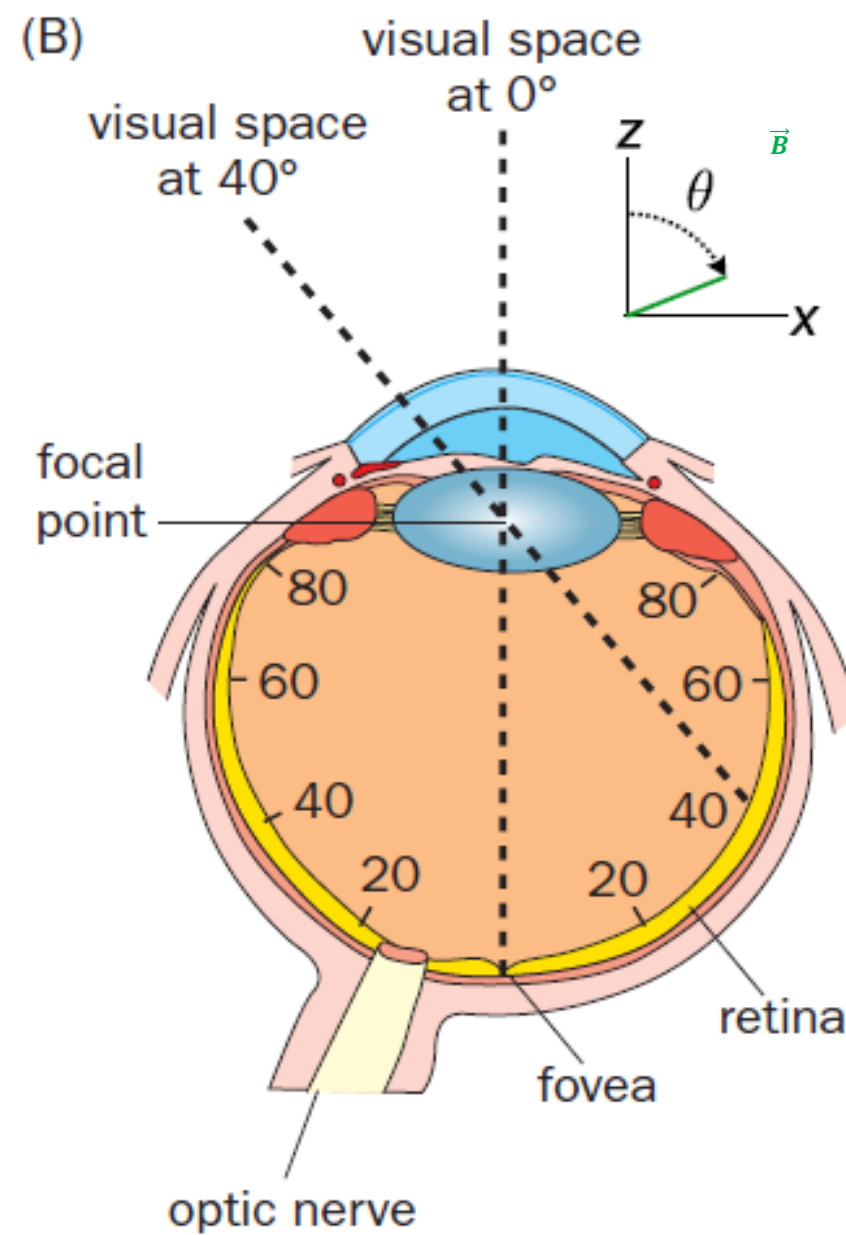
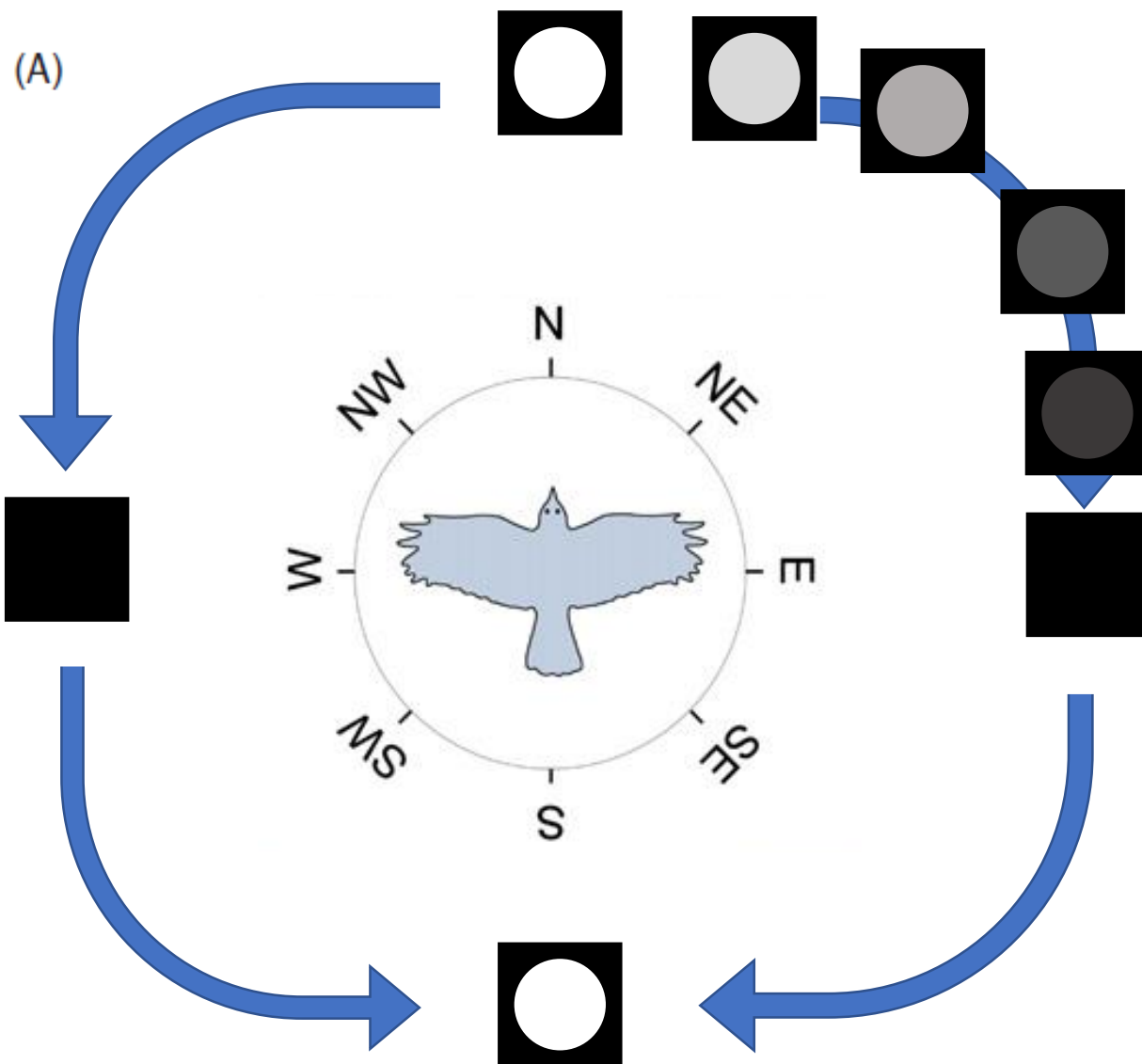
# Photon competition simulation result



$$R_{\text{opsin}} = R_{\text{opsin}}(\beta) \text{ and } \beta = \beta(\theta)$$



$$\text{Incresement threshold} = \frac{\Delta I}{I}$$

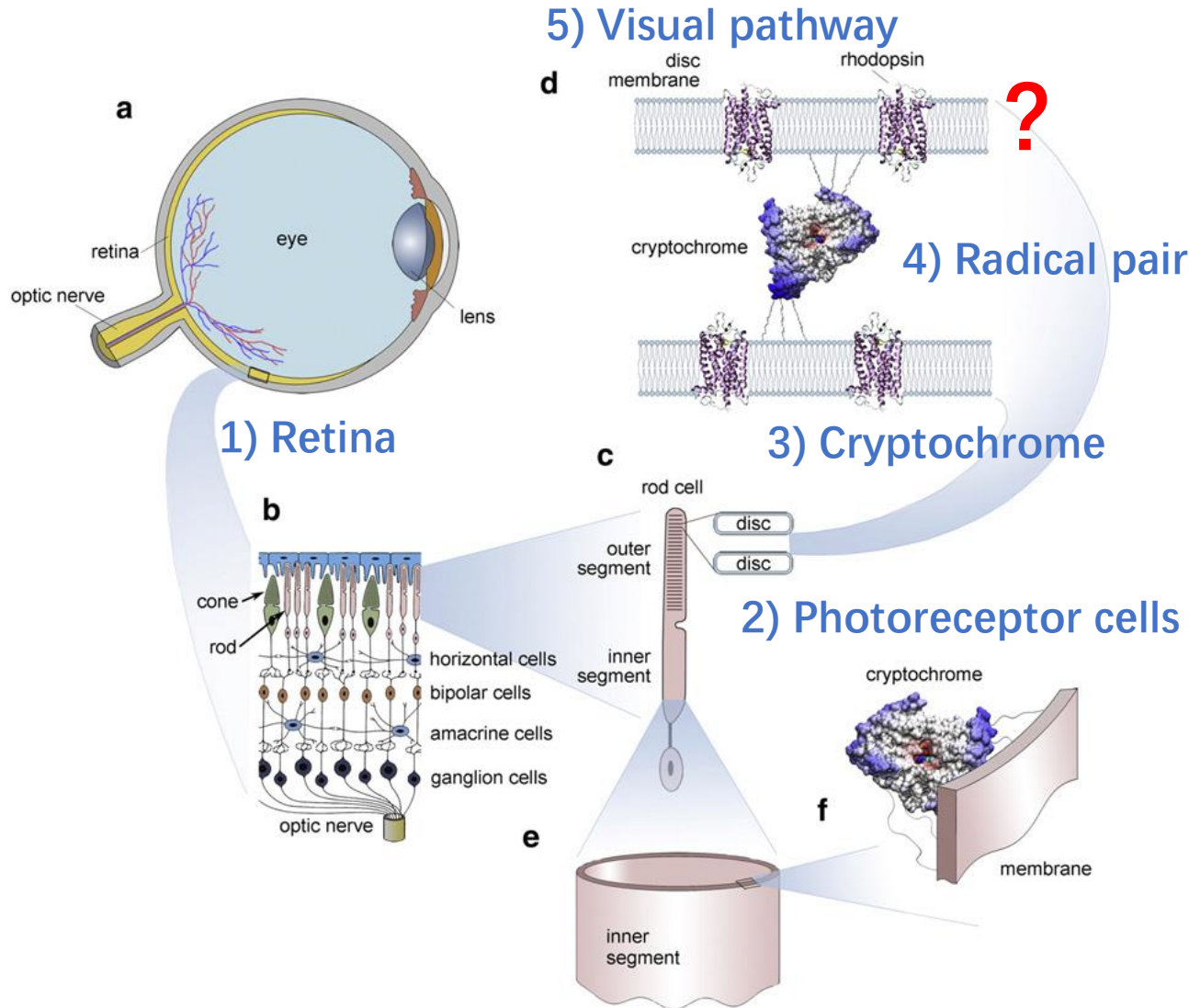


# Experimental predictions

- Our model give a prediction that **cone cells are magnetic sensors** with two properties:
  - (1) **Incident photon threshold** for magnetic sensing.
    - There are lower and upper photon thresholds for competition of opsin and cryptochrome. Controlled light intensity of background can be a on-off effect for magnetoreception.
  - (2) **Disruption/Analogy** of the magnetic sensing.
    - Under zero magnetic field, generate an artificial light pattern resembling the earth magnetic field effect.
    - Use changing spatial intensity of incident light on the retina to disrupt the existing light pattern caused by earth magnetic field .

# Summary

? ➡ OCC?



- A popular hypothesis of (4)-(5) is an noncanonical biological pathway of visual system that can modulate night vision. **No such signaling pathway** is found till now.
  - We propose that no downstream signaling involved and instead a photon competition plays a key role.
- A novel biophysical model:

**Opsin-Cryptochrome competition model(OCC model).**

Experiments to verify this model are proposed.

# Discussion

- Our model only works under **the radical-based magnetoreception** in **migratory birds** under **total overcast and under dim light**.
- European robin, pigeon and turtle seems use a inclination magnetic compass whereas other animals use intensity or polarity compass.

Parameter setting:

- Recovery time of retinal:  $\tau_0$
  - Singlet-triplet oscillation  $\beta$
  - Singlet product  $\tau_2$
  - Triplet products  $\tau_3$
1. Decoherence time – molecular motion
  2. Photon threshold and visual pattern
  3. Protein distribution
  4. Number ratio of cry4 and opsin protein
  5. Intensity perception of rods and cones

# References

- [1] Keeton W T . Magnets Interfere with Pigeon Homing[J]. Proceedings of the National Academy of Sciences of the United States of America, 1971, 68(1):102-106.
- [2] Henrik M . Long-distance navigation and magnetoreception in migratory animals[J]. Nature, 2018, 558(7708):50-59.
- [3] Johnsen S, Lohmann K J . The physics and neurobiology of magnetoreception[J]. Nature Reviews Neuroscience, 2005, 6(9):703-712.
- [4] Johnsen S, Lohmann K J . Magnetoreception in animals[J]. Physics Today, 2008, 61(3):29-35.
- [5] Chen L, Bazylnski D A, Lower B H . Bacteria That Synthesize Nano-sized Compasses to Navigate Using Earth's Geomagnetic Field[J]. Nature Education Knowledge, 2010.
- [6] Solov'yov I A, Mouritsen H, Schulten K. Acuity of a cryptochrome and vision-based magnetoreception system in birds.[J]. Biophysical Journal, 2010, 99(1):40-49.
- [7] Liqun Luo. Principles of Neurobiology[M]. UK: Taylor & Francis Group, 2016: 121-129.
- [8] Saari, John C . Vitamin A Metabolism in Rod and Cone Visual Cycles[J]. Annual Review of Nutrition, 2012, 32(1):125-145.
- [9] Hore P J, Mouritsen H. The Radical-Pair Mechanism of Magnetoreception[J]. Annual Review of Biophysics, 2016, 45(1):299-344.
- [10] Hiscock H G, Worster S, Kattnig D R, et al. The quantum needle of the avian magnetic compass.[J]. Proc Natl Acad Sci U S A, 2016, 113(17):4534-4639.
- [11] Lambert N, Chen Y N, Cheng Y C, et al. Quantum biology[J]. Nature Physics, 2012, 9(1):10-18.



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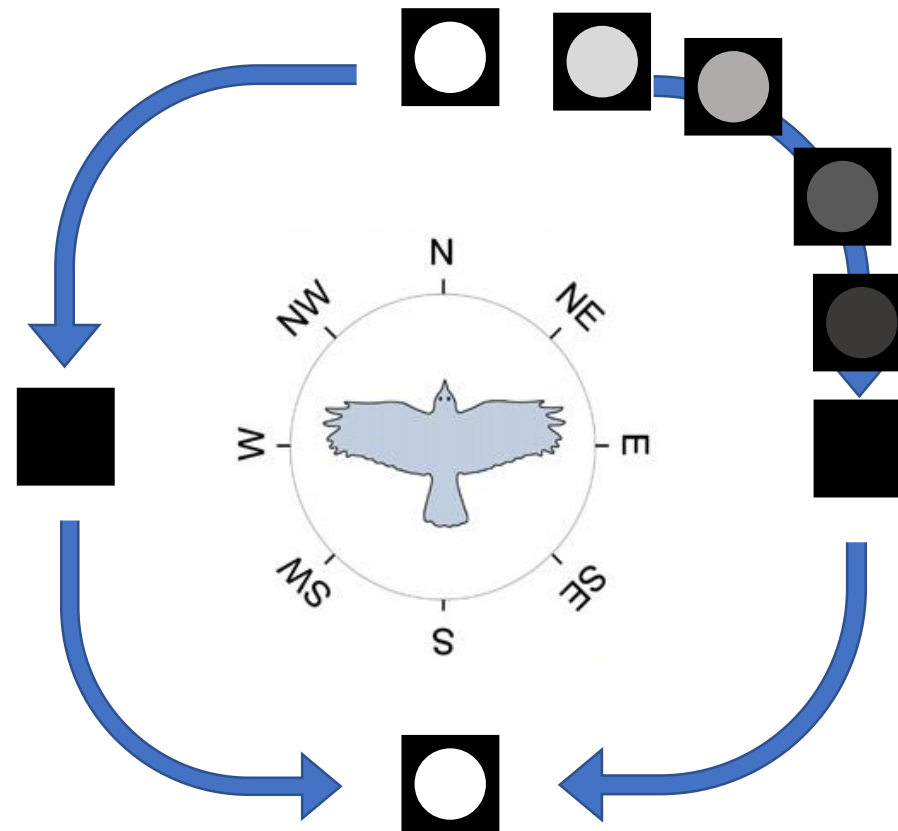
Jiansheng Wu,  
Assistance professor  
Department of Physics  
SUSTech



<https://github.com/LokyWei/Biophysical-model>



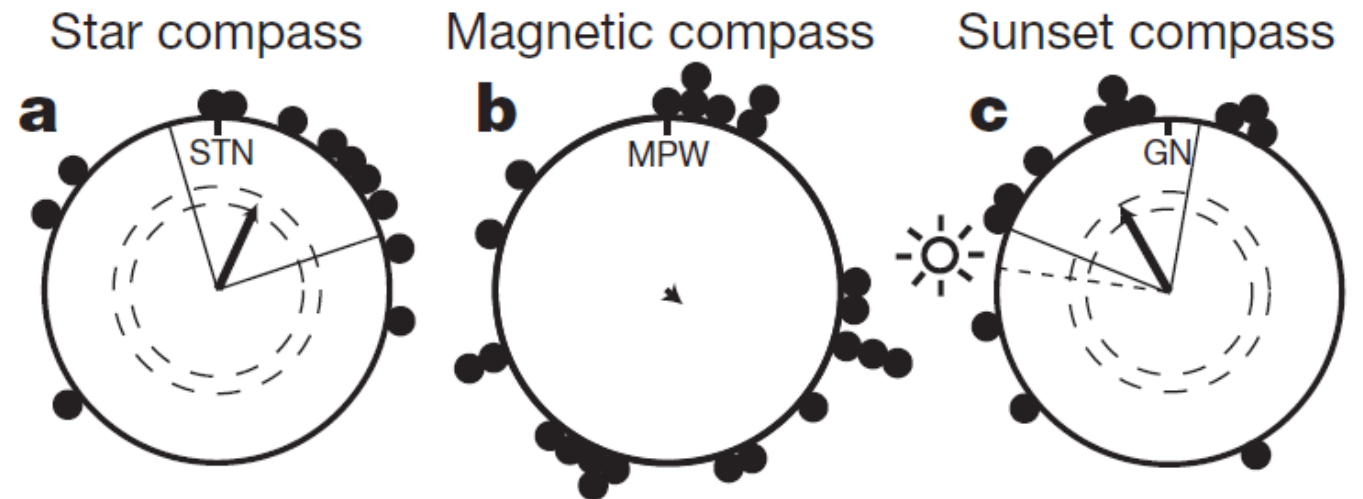
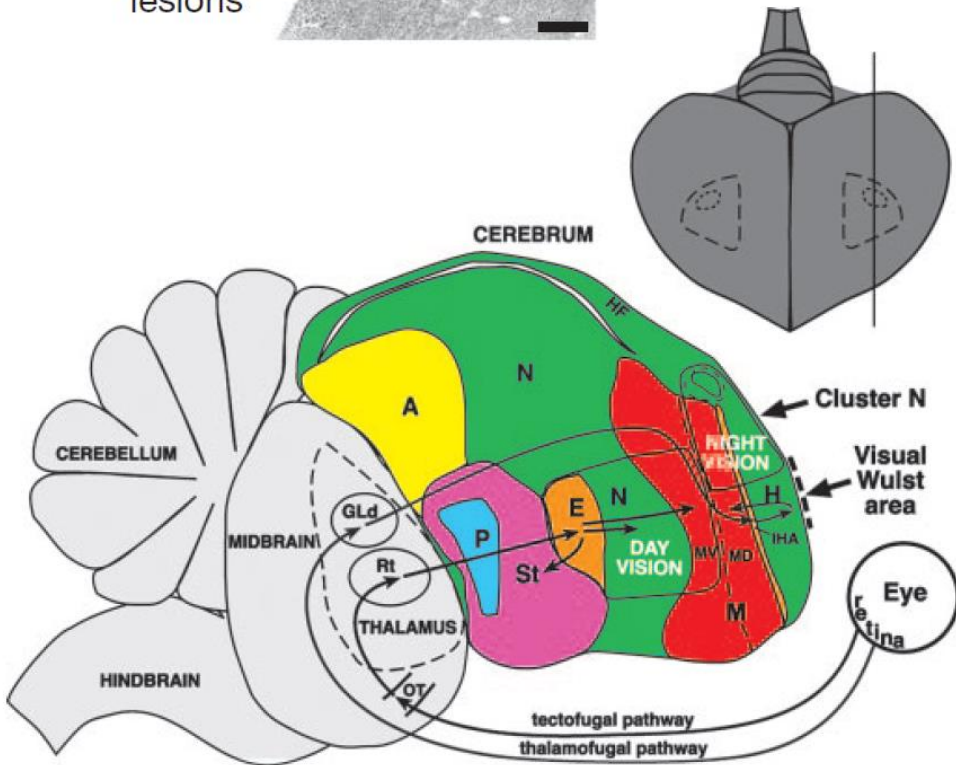
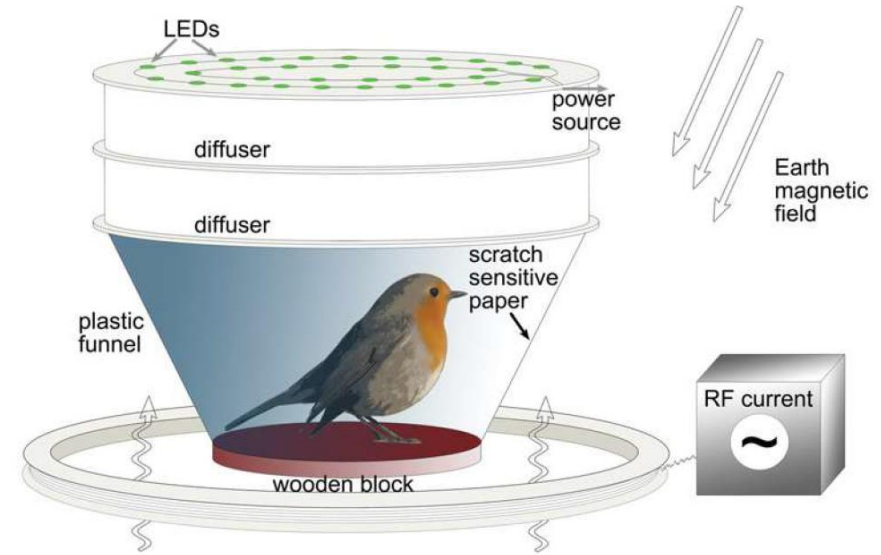
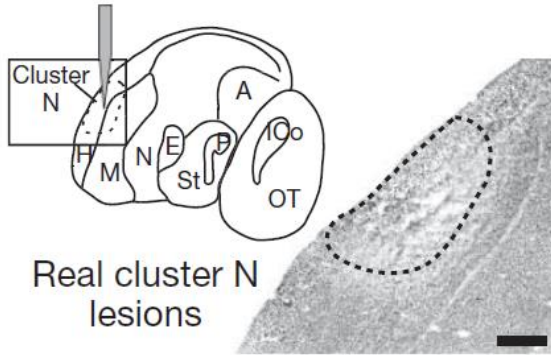
# Thank you



# Appendix

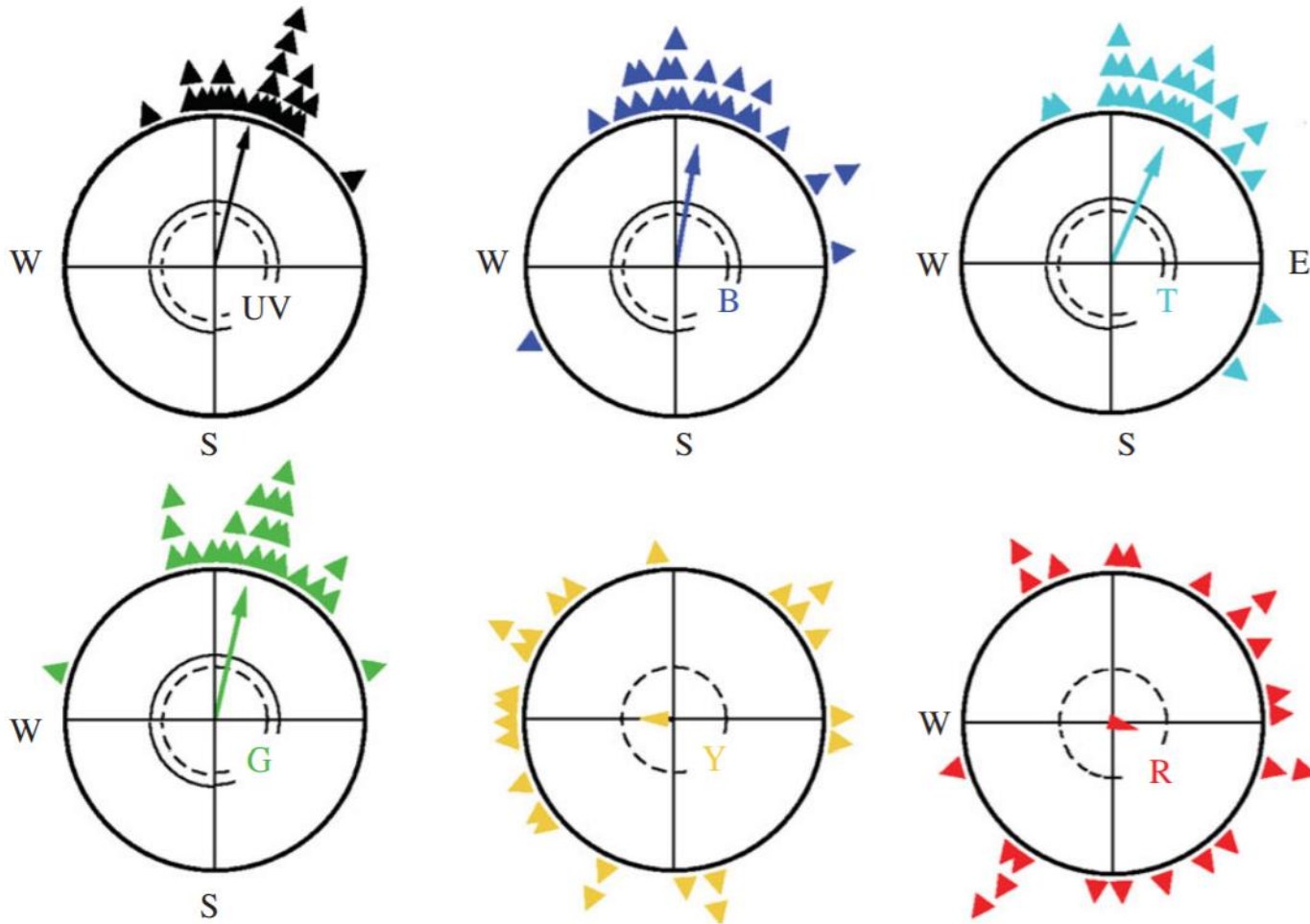
- [12] Zapka M, Heyers D, Hein C M, et al. Visual but not trigeminal mediation of magnetic compass information in a migratory bird [J]. NATURE, 2009, 461(7268):1274-1277.
- [13] Ritz T, Thalau P, Phillips J B, et al. Resonance effects indicate a radical-pair mechanism for avian magnetic compass[J]. Nature (London), 2004, 429(6988):177-180.
- [14] Wiltschko R, Stapput K, Thalau P, et al. Directional orientation of birds by the magnetic field under different light conditions[J]. Journal of The Royal Society Interface, 2010, 7(Suppl\_2):S163-S177.
- [15] Wiltschko W, Wiltschko R. Magnetic Compass of European Robins[J]. Science, 1972, 176(4030):62-64.
- [16] Lefeldt N, Dreyer D, Schneider N, et al. Migratory blackcaps tested in Emlen funnels can orient at 85 but not at 88 degrees magnetic inclination[J]. Journal of Experimental Biology, 2015, 218(2):206-11.
- [17] Günther A, Einwich A, Sjulstok E, et al. Double-Cone Localization and Seasonal Expression Pattern Suggest a Role in Magnetoreception for European Robin Cryptochrome 4[J]. Current Biology Cb, 2018, 28(2):211-223.

- 1) A neural connection between night vision and magnetic sensing in European robin.

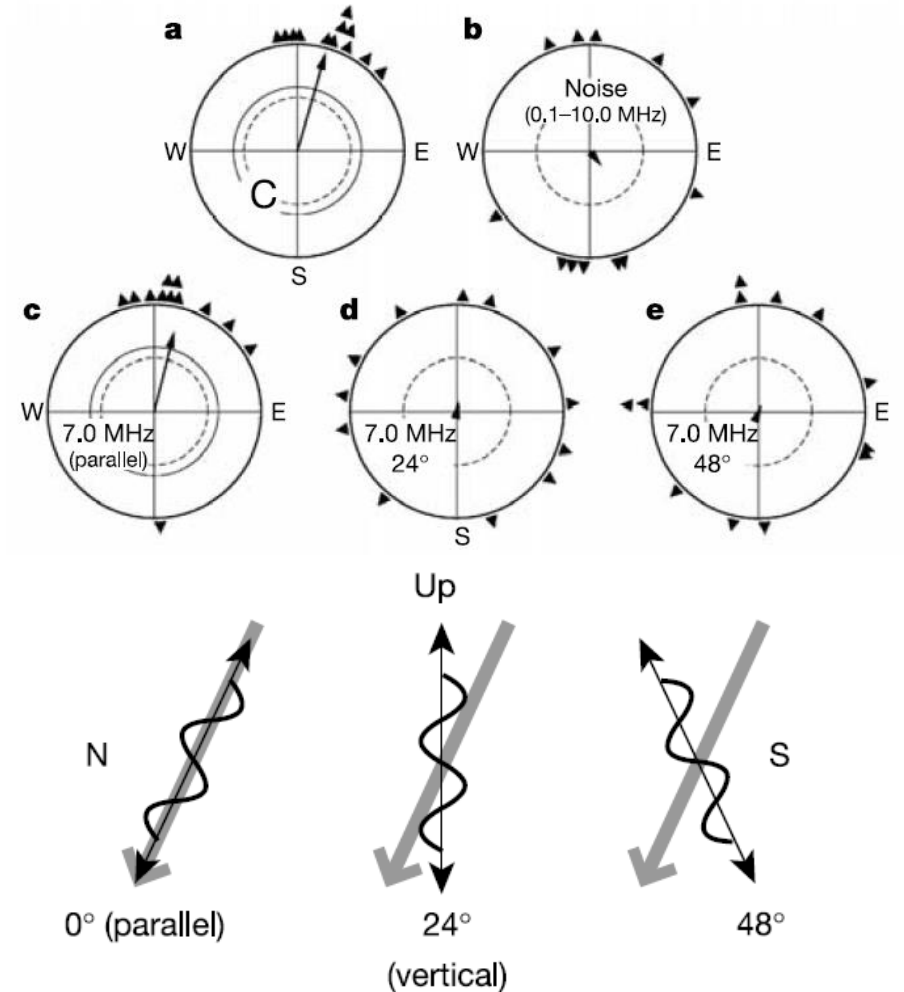




- 2) Different wavelength of incident light can disrupt magnetic orientation of European robin.

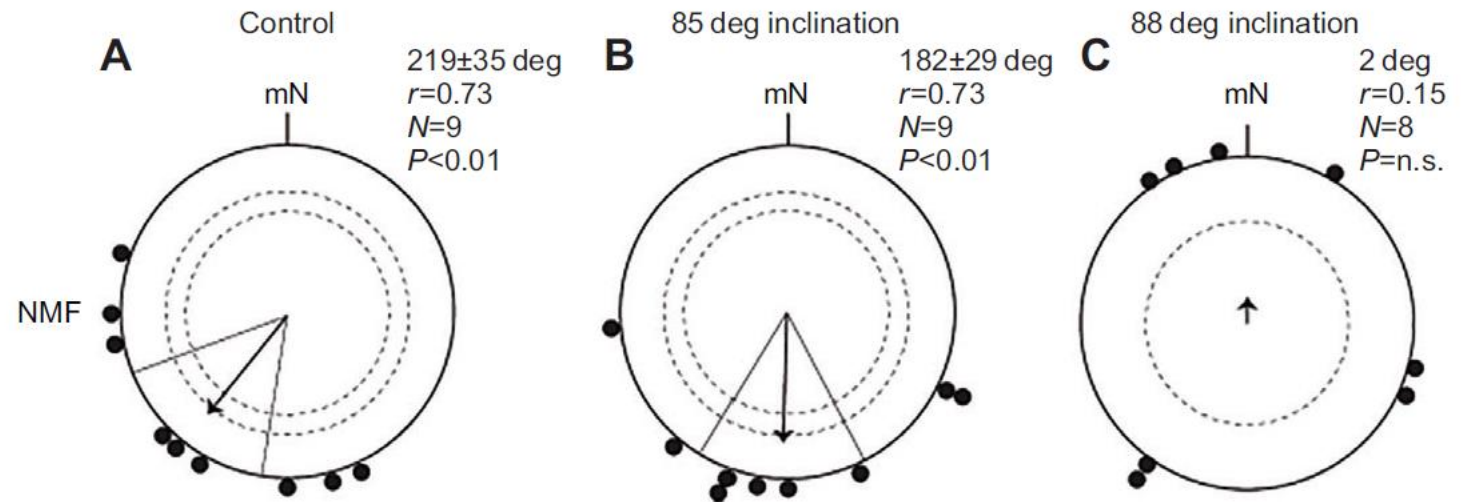
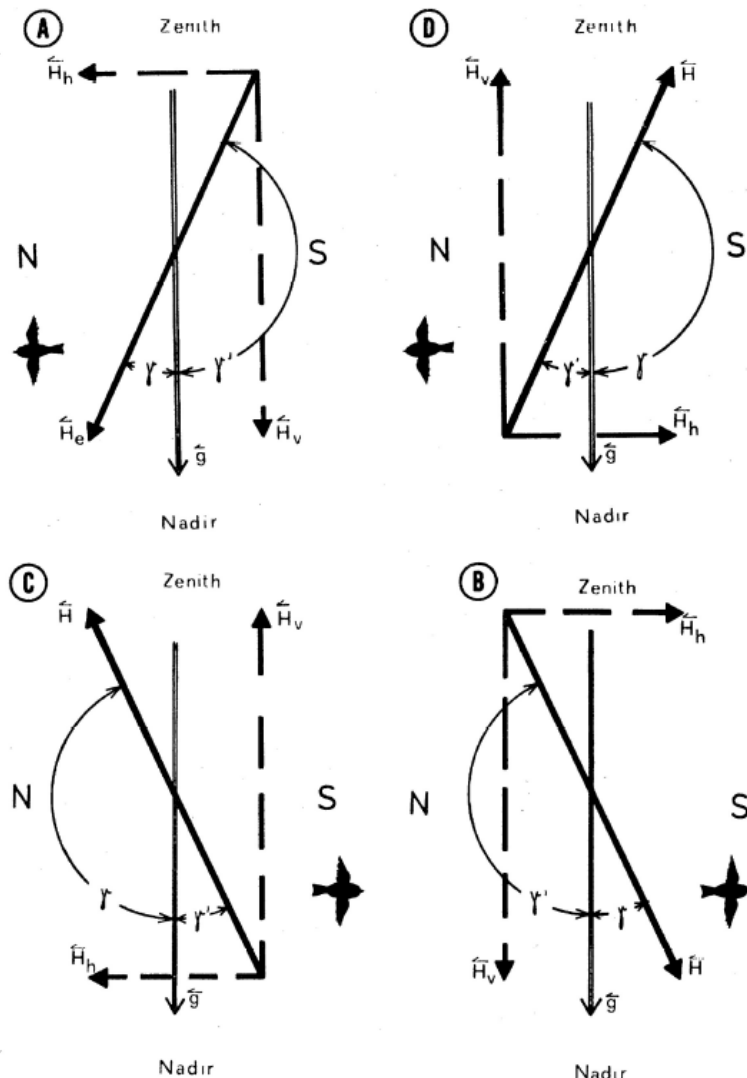


Orientation of European robin under monochromatic light of different wavelengths



Robins were disoriented when exposed to a vertically aligned broadband (0.1–10 MHz) or a single-frequency (7-MHz) field in addition to the geomagnetic field.

- 3) The magnetic compass of European robin is a inclination compass with  $<5^\circ$  precision, which can be explained by radical pair mechanism instead of any other hypothesis.



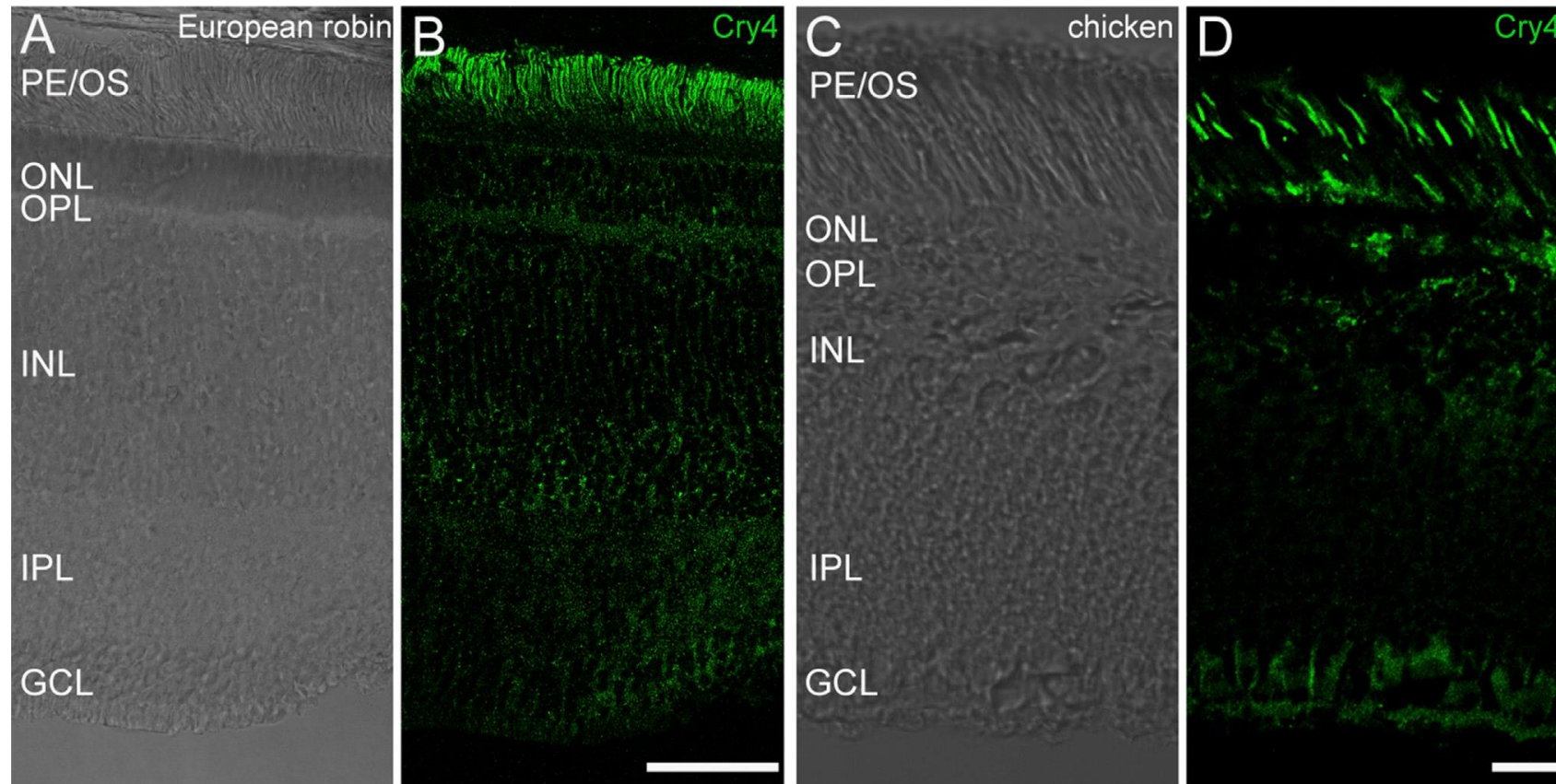
The orientation of individual blackcaps was tested in magnetic fields with 67, 85 or 88 degree inclination

The magnetic compass of European robins **does not use the polarity of magnetic field** for detecting the north direction.

The birds derive their north direction from interpreting the **inclination of the axial direction** of the magnetic field lines in space, where **field lines and gravity vector form the smaller angle**.



- 4) Cry4 protein, a member of cryptochrome family, is found recently located on the outer segment in cones in birds' retina.



**Cry4 Is Expressed in the Outer Segments of Specific Photoreceptor Cells in the Retina of European Robin and Chicken**