

```
In [11]: def bisection(f, a, b):  
  
    tolerance = 1e-10  
    max_iteration = 100000  
  
    if f(a) * f(b) > 0:  
        return None  
    iter_count = 0  
    while (b - a) / 2.0 > tolerance and iter_count < max_iteration:  
        midpoint = (a + b) / 2.0  
        if f(midpoint) == 0:  
            return midpoint  
        elif f(a) * f(midpoint) < 0:  
            b = midpoint  
        else:  
            a = midpoint  
        iter_count += 1  
    return (a + b) / 2.0
```

```
import math
```

```
# Test Case 1:  
f1 = lambda x: math.exp(x) + math.log(x)  
root1 = bisection(f1, 0.01, 1)  
print(f"Root of f1 in [0,1]: {root1}")
```

```
# Test Case 2:  
f2 = lambda x: math.atan(x) - x**2  
root2 = bisection(f2, 0, 2)  
print(f"Root of f2 in [0,2]: {root2}")
```

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# Test Case 3:  
f3 = lambda x: math.sin(x)  
root3 = bisection(f3, 3, 4)  
print(f"Root of f3 in [3,4]: {root3}")
```

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# Test Case 4:  
f4 = lambda x: math.log(math.cos(x))  
root4 = bisection(f4, 5, 7)  
print(f"Root of f4 in [5,7]: {root4}")
```

```
Root of f1 in [0,1]: 0.2698741375870304  
Root of f2 in [0,2]: 1.9999999999417923  
Root of f3 in [3,4]: 3.141592653642874  
Root of f4 in [5,7]: None
```