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DEPARTAMENTO DE INGENIERÍA DE SISTEMAS Y AUTOMÁTICA

**MASTER THESIS**

**BALANCE CONTROL OF HUMANOID ROBOT TEO  
USING FORCE/TORQUE SENSORS**

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*"The true knowledge is ..."*

*Daniel*



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# Acknowledgments

Thanks to all ...



# Resumen

Esta tesis desarrolla ...





# Abstract

This thesis develops ...



# Chapter 1

## Introduction

Industry was one of the first fields of application of robotics, where the environment is mainly static, the tasks to be performed are repetitive and automated, and the human interaction is quite low. For that reason, the idea of designing robots able to work in dynamic environments, with a high variety of tasks and interacting with humans and their environment, was fulfilled thanks to the evolution of new techniques related to robotics. Humanoid robots, physically similar to the human being, meet all that needs. Mainly, the possibility of moving, solves the problem of industrial robots that can only work in fixed areas. Moreover, the provision of artificial intelligence, allows the robot to interact with the surrounding environment in a more natural way, as the human being.

Nevertheless, the possibility of moving, brings the problem of stability. Maintaining the humanoid robot in an upright posture and walking is a complex task related to control. For humans, walking is so simple that we do almost unconsciously, so we are not aware of its complexity. At all the times, it had to be ensured that the robot is in an upright posture in order to not to fall over and simultaneously, it is performing a series of movements previously defined to walk. As well, in a unbalanced situation, humans, unconsciously, try to stabilize moving their own body or the other limbs and the same behaviour is expected for the humanoid robot.

First works about biped robots were carried out about 1970 by authors Kato [Kaj2005] and Vukobratović. The first anthropomorphic robot, WABOT-1, was exhibited by Kato in 1973 in Waseda University (Japan). Using a very simple control diagram, the robot was able to perform a few slow gaits, maintaining its balance all the times. This achievement, was the first one that encouraged researchers about humanoid robots and their locomotion.

At the same time, Vukobratović and his research team were studying stability in biped systems in the former Yugoslavia, basing on a new stability criterion, presented in 1972, as *Zero-Moment Point (ZMP)*. Taking into account the dynamic effects produced during a walking, from then until now, the ZMP stability criterion has been the most used in humanoid or biped robotics.

The rise of humanoid robotics started with the development of P2 robot by the company Honda in 1996 [Kaj2005]. The project began in secret ten years before, after the exhibition of WABOT-2 playing the piano. P2 (180 centimetres high and 210 kg weight), was the first humanoid able to walk in a stable enough way and carry its processor and battery on its back. After that, robots P3 and ASIMO were its advanced versions, reducing height and weight of the robot.

## 1.1 Objectives

This Master Thesis deals with the balance control of humanoid robot TEO (*Task Environment Operator*) using Force-Torque sensors. The design of the control system must include the sensors feedback in real time to maintain stability.

The main objectives of this work are:

- Data acquisition in real time from Force-Torque sensors assembled in the robot ankles, which are the main feedback of the control loop.
- Computation of the ZMP *Zero-Moment Point* stability parameter and definition of stability regions that determine the stability rate.

- Design of a feedback control system which allows the movement of the robot joints in order to maintain stability at all the times.



## Chapter 2

# Literature review

The control of humanoid robots which are supposed to interact with the surrounding environment including human presence is a complex task which has to be divided, e.g., controlling locomotion separately from manipulation. A principal aspect in locomotion is stability or balance control, which avoids the humanoid to fall over during a walk pretending to imitate the human walking.

This chapter will provide a brief introduction about humanoid stability control, the bases of biped walking and essential concepts such as *Zero-Moment Point (ZMP)* and its extensions.

### 2.1 Biped locomotion

Robot walking, as humans, is performed in a three phase cycle (Fig. 2.1). The cycle is divided in two, left and right steps. At the beginning, the humanoid is in a stable position with both feet on the ground (Fig. 2.1 (a)) and all the body weight is transferred from one foot to the other. Then the step generation starts when the right foot leaves the ground in the swinging phase (Figura 2.1 (b), (c) y (d)). After the right foot touches the ground, the next (right) step with the same basic phases is started, and the whole cycle ends. The single-support phase is the complex one in terms of balance, because all the weight remains in only one

support foot.

Swinging phase has also three sub-phases: acceleration, swinging and deceleration (Fig. 2.1 (b), (c) y (d), respectively). The acceleration phase takes its name due to the acceleration of the lifting leg that stops being supported in the ground and gives the impulse to the step. Once the support leg is overtaken, the lifting leg starts the swinging pahse in order to reach the ground with the consequent deceleration.

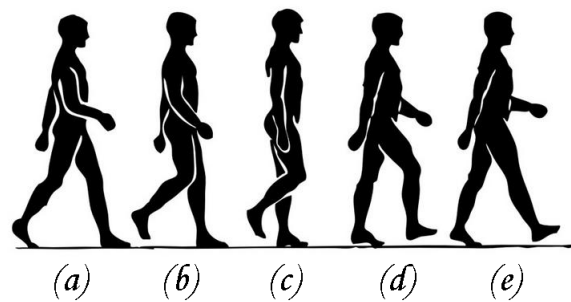


Figure 2.1: Phases of biped walking.

As in the case of the leg, the same occurs with the foot, what adds complexity to control the walking cycle. During a gait, a human foot has four different phases as one can see in Fig. 2.2. In (a) it is shown how the body weight is supported when the heel is touching the ground. In (b), the foot remains totally plane. In (c), the heel lifts and the weight goes to the front part of the foot. Finally, in (d) the foot is not in contact with the ground and it starts to swing.

Almost all humanoid robots do not have articulated feet, due to the high complexity. Mostly they use plane and rigid feet and the control is done in the ankle joint. Some of them, as the robot HRP-4 [Kan ], have a joint called "active toe joint" which allows the movement of the toes. The reason of this improvement is related to reach a more natural and fluent walking, as the human walk.



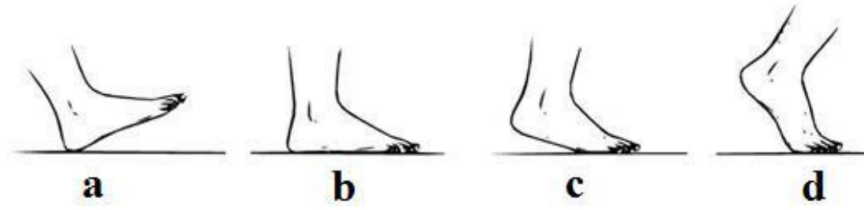


Figure 2.2: Phases of foot support during a walk.

However, in order to perform a stable walk, is not only necessary the lower body movement. The upper body is also involved in recovery movements. In an example, if a person stumbles. Unwittingly, he or she would move the opposite arm of the unbalanced leg, or even more, moving the torso in order to not to fall down. In the case of a biped robot, the same strategy is followed, what means an high increase of the complexity of the control of the robot stability.

## 2.2 Biped balance/equilibrium

One of the most important and complex tasks for humanoid locomotion is to avoid overturning during the walking or even to reach an upright position of its body. To prevent that, a necessary and sufficient condition is to ensure that there exists a contact area between the foot and the ground and not a line or a point [Vuk2007]. Given a rectangular-shaped foot, the support area of the robot will be the polygon. In the case that only one foot is touching the ground (single-support), the support area is the contact region between the sole and the ground, i.e., the footprint (Fig. 2.3(a)). On the contrary, when both feet are touching the ground (double-support), the support area will be determined by the footprints and the common tangents between them (Fig. 2.3(b)). It means that in the double-support phase of the walk, the stability area is bigger than in the single-support phase, so the complexity of balance control is lower.

In [Vuk2007], Vukobratović makes a distinction between the term “balance”

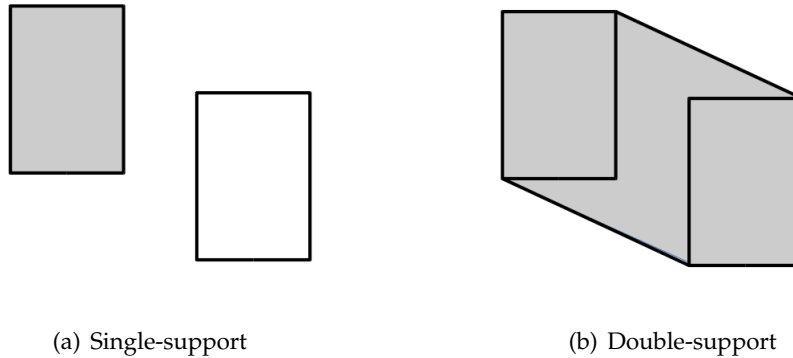


Figure 2.3: Support areas depending on the support type.

used in the sense of maintaining an upright posture, and “equilibrium”, taking into account the D’Alembert’s principle. The D’Alembert’s principle states that the resultant of the external forces and the kinetic reaction acting on a body equals zero (condition of kinetic equilibrium). When the humanoid is falling since it is rotating about one foot edge, the D’Alembert’s principle still holds for a point on the foot edge where the pressure force acts. Anyway, this case cannot be contemplated as balanced in the sense of the definition previously provided. This point is called as *Center of Pressure (CoP)* and it is known as the point, in a single-support phase, where the pressure forces (normal to the sole) are equivalent to a single resultant force exerted at the point where the resultant moment is zero.

## 2.3 Zero Moment Point (ZMP)

From the concept of the CoP, appears a new term known as *Zero-Moment Point (ZMP)*. When a human or a humanoid robot executes a gait during a walk, the ZMP is a point inside the support area where, always, the resulting dynamic reaction of the biped system is acting. In a more specific definition, the ZMP is a point inside the support area where the resultant of all forces and torques acting

on the full body, is equal to zero.

Vukobratović [Vuk2007] explains the difference between the CoP and ZMP: CoP and ZMP coincide only when both are inside the support area. When the ZMP goes to the edge of the support area, the humanoid body loses balance and it will fall down. In that case, the ZMP has no sense existing even the CoP.

Goswami [Gos] presented that, mathematically was possible that the point could be outside of the support area and continue satisfying the equilibrium conditions. This point, called *Foot Rotation Indicator (FRI)*, is defined as the point on the contact area between the ground and the foot, inside or outside the support area, where the resultant moment of the forces and torques applied on the foot are normal to the surface. Forces and torques applied mean the forces and torques at the ankle joint, and also other external forces, the foot weight and reaction forces between the foot and the ground.

However, Vukobratović, on the contrary, stills that the ZMP can only exist inside the support area of the robot. When the ZMP comes close to the edge, any force or moment applied to the system, will produce a rotation about the foot edge and the robot will fall down. In this case, the reaction force of the ground will be at the foot edge and, therefore, it can not be considered as ZMP because there is no stability ensured. That is why the author suggests to denote the point as *Fictitious ZMP* or *FZMP*, if it is outside the support area.

When the robot walking is enough slow to consider almost static, appears the term *pseudo-ZMP*, which is the projection over the ground of the *Center of Gravity (CoG)* of the system. In such case, lateral accelerations are so small and can be omitted and the *pseudo-ZMP* = ZMP. Although the *pseudo-ZMP* do not give precise information about the balance of the mechanism, it can be used in order to make a first approximation in control and design of a humanoid robot.

### 2.3.1 Equations of ZMP

Let us consider the locomotion mechanism in the single-support phase, with the whole foot being on the ground (Fig. 2.4). To facilitate the analysis we can neglect the part of the mechanism above the ankle of the support foot (point A) and replace its influence by the force  $F_A$  and moment  $M_A$ , whereby the weight of the foot itself acts at its gravity center (point G). The foot also experiences the ground reaction at point P, whose action keeps the whole mechanism in equilibrium.

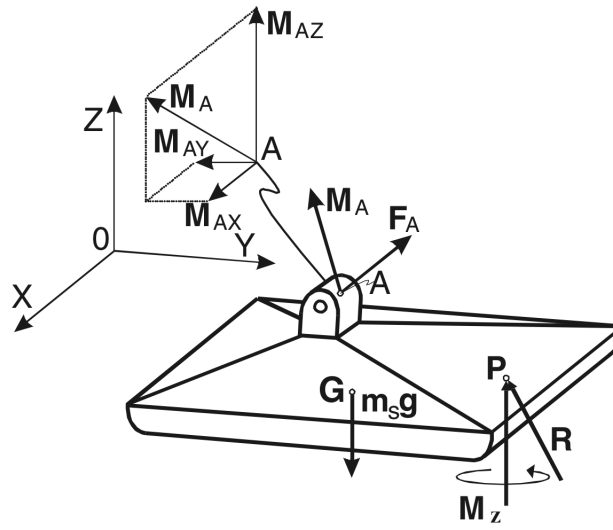


Figure 2.4: Forces acting on the foot of the bipedal mechanism [Vuk2004]

In general, the total ground reaction consists of three components of the force  $R(R_x, R_y, R_z)$  and moment  $M(M_x, M_y, M_z)$  exerted at the foot-ground contact point. During the support phase, it is assumed there is no shifting in the contact point, which means that horizontal reaction force  $R_x$  and  $R_y$  balances the horizontal component of the force  $F_A$ , whereas the vertical reaction moment  $M_z$  represents the moment of friction reaction forces that balances the vertical component of the moment  $M_A$  and the moment induced by the force  $F_A$ .

However, due to a unidirectional nature of the connection between the foot

and the ground (it is obvious that the ground reaction force induced by foot action is always oriented upwards) horizontal components of all active moments ( $M_A$ ) can be compensated for only by changing position of the reaction force  $R$  within the support polygon. This is illustrated in Fig. 2.5 where a planar case in  $y - z$  plane is represented.

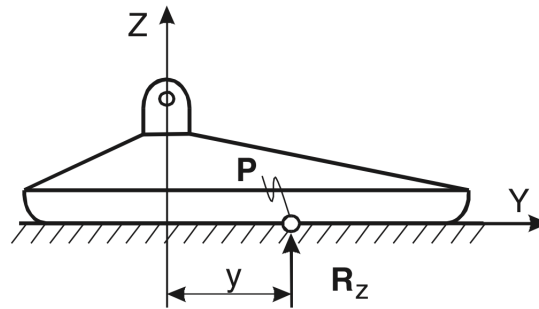


Figure 2.5: Compensación  $M_{Ax}$  [Vuk2004]

The moment  $M_{Ax}$  is balanced by shifting the acting point of the force  $R_z$ , whose intensity is determined from the equation of balance of all the forces acting on the foot, by the corresponding distance  $y$ . It is necessary to emphasize that all the time the reaction force is within the area covered by the foot, the increase in the ankle moment will be compensated for by changing the position of this force  $R_z$ , and no horizontal components of the moments  $M_x$  and  $M_z$  will exist. This is the reason why in Fig. 2.4 at point  $P$  only the  $M_z$  component exists.

However, if the real support polygon is not large enough to encompass the appropriate position of the force  $R$  to balance the action of external moments, the force  $R$  will act at the foot edge and the uncompensated part of the horizontal component of the reaction moment will cause the mechanism's rotation about the foot edge, which can result in the mechanism's overturning. Therefore, it can be said that the necessary and sufficient condition for the locomotion mechanism to be in dynamic equilibrium is that for the point  $P$  on the sole where the ground

reaction force is acting,

$$M_x = 0; M_y = 0. \quad (2.1)$$

That is why the *Zero-Moment Point* is called the contact point with the ground ( $P$ ) where there no exist shifting, i.e., moments  $M_x$  y  $M_y$  are zero.

From Fig. 2.4 static equilibrium equations for the supporting foot are obtained:

$$\sum \vec{F} = 0 \Rightarrow \vec{R} + \vec{F}_A + m_s g = 0 \quad (2.2)$$

$$\sum \vec{M}_O = 0 \Rightarrow \vec{OP} \times \vec{R} + \vec{OG} \times m_s g + M_A + M_z + \vec{OA} \times F_A = 0, \quad (2.3)$$

where  $\vec{OP}$ ,  $\vec{OG}$  and  $\vec{OA}$  are radius vectors from the origin of the coordinate system  $O_{xyz}$  to the ground reaction force acting point ( $P$ ), foot mass center ( $G$ ), and ankle joint ( $A$ ), respectively, while the foot mass is  $m_s$ . If we place the origin of the coordinate system at the point  $P$  and project Eq. 2.5 onto the z-axis, then the vertical component of the ground reaction momentc (actually, it is the ground friction moment) will be

$$M_z = M_{fr} = -M_A^Z + (\vec{OA} \times F_A)^Z \quad (2.4)$$

In a general case, this moment is different from zero and can be reduced to zero only by the appropriate dynamics of the overall mechanism. However, the projection of Eq. 2.5 onto the horizontal plane gives:

$$(\vec{OP} \times \vec{R})^H + \vec{OG} \times m_s g + (M_A)^H + (\vec{OA} \times F_A)^H = 0, \quad (2.5)$$

This equation is a basis for computing the position of the ground reaction force acting point ( $P$ ) which gives the ZMP position.

### 2.3.2 Relation between COG and ZMP

When a humanoid robot is in the single-support phase during a walking cycle, its dynamics can be represented by a single inverted pendulum where the

supporting foot is the point where all body mass is concentrated (COG) and a mass less telescopic leg [Kaj2001]. The pendulum can increase or decrease its length, thus simulating the functioning of the ankle joint.

Now, let us consider that the inverted pendulum instead of only one contact point considered above, has a contact polygon as the surface in contact with the ground (Fig. 2.6).

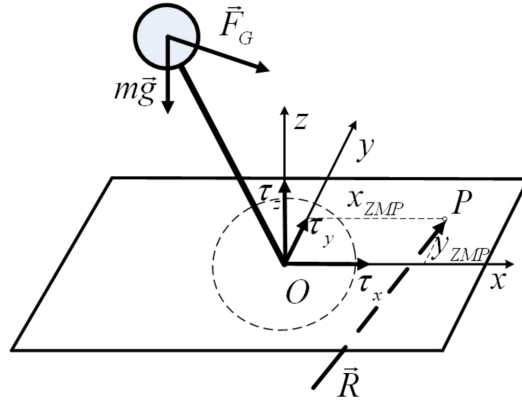


Figure 2.6: 3D Linear Inverted Pendulum with a contact polygon. CITA

Inertial  $\vec{F}_G$  and gravity  $m\vec{g}$  forces act on the point mass located in the COG of the humanoid robot. The contact of the pendulum with the ground produces a reaction force  $\vec{R}$  and reaction moment  $\vec{M}_P$  at point  $P$ . For any other point of the support polygon (taking point  $O$  as origin), the moment  $M_0 = [\tau_x, \tau_y, \tau_z]^T$  produced by the ground reaction force  $\vec{R}$  is represented:

$$M_0 = M_P + \vec{OP} \times \vec{R} \quad (2.6)$$

If it is considered point  $P$  to be the ZMP of the system, then from the interpretation of the ZMP presented above  $M_P = 0$ . In this case we can denote vector

$\vec{OP} = [x_{ZMP}, y_{ZMP}, z_{ZMP}]^T$  and eq. 2.6 gives the following equation:

$$\begin{pmatrix} \tau_x \\ \tau_y \\ \tau_z \end{pmatrix} = \begin{pmatrix} x_{ZMP} \\ y_{ZMP} \\ z_{ZMP} \end{pmatrix} \times \vec{R} \quad (2.7)$$

From the other side, applying Newton's law of mechanics to system in Fig. 2.6:

$$m\vec{a}_G = \vec{R} - m\vec{g} \quad (2.8)$$

where  $\vec{a}_G = [\ddot{x}, \ddot{y}, \ddot{z}]^T$  is the acceleration of the COG. From 2.8 it is obtained:

$$\vec{R} = m \begin{pmatrix} \ddot{x} \\ \ddot{y} \\ \ddot{z} + g \end{pmatrix} \quad (2.9)$$

Substituting equation 2.9 into the equation of balance of moments 2.7 it is obtained:

$$\begin{pmatrix} \tau_x \\ \tau_y \\ \tau_z \end{pmatrix} = m \begin{pmatrix} x_{ZMP} \\ y_{ZMP} \\ z_{ZMP} \end{pmatrix} \times \begin{pmatrix} \ddot{x} \\ \ddot{y} \\ \ddot{z} + g \end{pmatrix} \quad (2.10)$$

After a cross product and taking into account that  $z_{zmp} = 0$ , because the ZMP lies into the ground:

$$\begin{pmatrix} \tau_x \\ \tau_y \\ \tau_z \end{pmatrix} = m \begin{pmatrix} y_{ZMP}(\ddot{z} + g) \\ -x_{ZMP}(\ddot{z} + g) \\ x_{ZMP}\ddot{y} - y_{ZMP}\ddot{x} \end{pmatrix} \quad (2.11)$$

From (2.11), it can be stated the ZMP position of the system:

$$x_{ZMP} = -\frac{\tau_y}{m(\ddot{z} + g)} \quad (2.12)$$

$$y_{ZMP} = \frac{\tau_x}{m(\ddot{z} + g)} \quad (2.13)$$



If it is supposed that the COG always remains within the horizontal plain intersecting the  $z$  axis in the point  $z_c$  (one of the constraints of the 3D-LIPM model), then the vertical component of the COG acceleration  $\ddot{z} = 0$ . Then, finally, equations 2.12 and 2.13 take the form:

$$x_{ZMP} = -\frac{\tau_y + hF_x}{mg} \quad (2.14)$$

$$y_{ZMP} = \frac{\tau_x + hF_y}{mg} \quad (2.15)$$

where  $h$  is the distance between the ground and the measuring point, i.e, the height of the sole. These are the *ZMP equations*, without forgetting it was considered before that lateral accelerations of the COG  $\ddot{x} = 0$  and  $\ddot{y} = 0$ . One can see that moments  $\tau_x$  and  $\tau_y$  in  $x$  and  $y$  directions respectively affect the ZMP position of the mecanism and it can loose balance because of their change.

If we take into account these lateral accelerations of the COG, the ZMP can be expressed as a function of the acceleration of the COG as: **REFERENCIA?**

$$x_{ZMP} = x - \frac{z_c}{g} \ddot{x} \quad (2.16)$$

$$y_{ZMP} = y - \frac{z_c}{g} \ddot{y} \quad (2.17)$$

These equations can only be applied to compute ZMP in single-support phase. In the case of the double-support phase, it is necessary to calculate the weighted average of the sensor measurements form both feet as recommended in [Kaj2005]. Therefore, the resulting equations for ZMP in double-support phase are:

$$x_{ZMP} = -\frac{F_y^R \cdot x^R + F_y^L \cdot x^L}{F_z^R + F_z^L} \quad (2.18)$$

$$y_{ZMP} = \frac{F_x^R \cdot y^R + F_x^L \cdot y^L}{F_z^R + F_z^L} \quad (2.19)$$

where the upper index  $R$  represents the right foot and  $L$  the left one. **Revisar si el numerador es par o fuerza.**

### 2.3.3 ZMP areas.

As mentioned before, ZMP is a point in the sole which depends on the forces and moments applied to the robot. Therefore, depending on the magnitude of that forces, ZMP will change and it becomes a dynamic parameter. As suggested in [Vuk2007], three regions are defined depending on the position of the ZMP as one can see in Fig. 2.7. In the balanced area (safe region), the control action will not actuate. In the nearly critical region, the control action will actuate as a secondary solution. This may be the case of a walking task. As humans do, the robot may use its arms in order to reduce the zero-moment point position closer to the safe region. Finally, in the critical region, the stabilizer will actually disconnect the ongoing task and actuate on the full body. Even if this region is still stable, the balance may be easily lost.

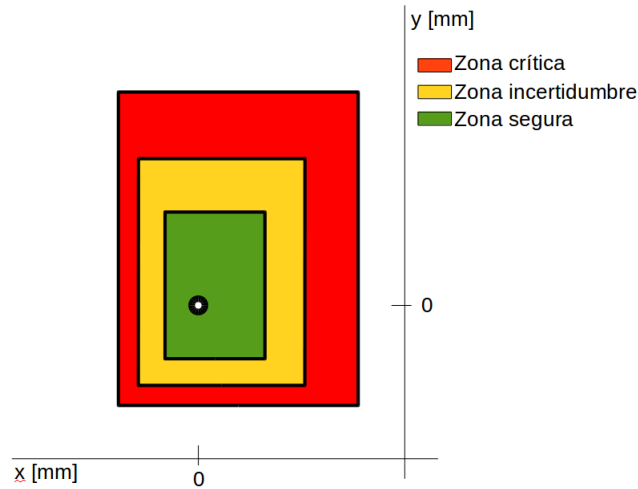


Figure 2.7: ZMP stability regions in single-support.

## 2.4 Biped modeling

Humanoid robots have a very complex dynamics because of their complex mechanical configuration and they require a high computational cost. Figure ??? represents a simplified mechanical configuration of a typical humanoid robot. As one can see, the high number of DOFs due to the precise knowledge of robot dynamics including, mass, location of the centre of mass and moments of inertia of each link, make stable biped locomotion very complex. Thus, different simplified models of the mechanics have been developed. These methods use limited knowledge of the dynamics and the humanoid is usually represented by a planar inverted pendulum with the base representing the ankle joint and, in case of 3D locomotion, the Three-Dimensional Inverted Pendulum Mode (3D-LIPM) [Kaj2001 ].



## Chapter 3

# Platform description

### 3.1 Humanoid robot TEO

Humanoid robot RH-2, also known as TEO (Task Environment Operator), from University Carlos III of Madrid, is an advanced version of humanoid robots RH-0 and RH-1. TEO is 165 cm high overtaking 150 cm of RH-1 and 120 cm of RH-0. It weighs about 60 kg and it can carry about 2 kg of payload. It has 24 DOFs (26 DOFs taking into account head motors), 3 more DOFs than in previous RH versions. In Figure ?? one can see the robot DOFs, besides their movements, being 6 DOFs for each leg, 6 DOFs for each arm, 2 DOFs for the torso and 2 DOFs for the head.

The robot has 4 microprocessors: locomotion, manipulation, artificial vision tasks and last, the main processor which manages the others. The locomotion processor, that controls the legs and the torso, will be responsible for getting the sensors information and maintain the robot in a balance and upright position, being static or in a walking cycle. The manipulation processor controls the movement of the arms and the head. The processor responsible for the computer vision uses a camera with infrared sensor ASUS located in the head.

The communication system is based on the CAN-bus protocol. Making a sagittal and transversal division, there are 4 CAN-bus lines: 1 line per each arm

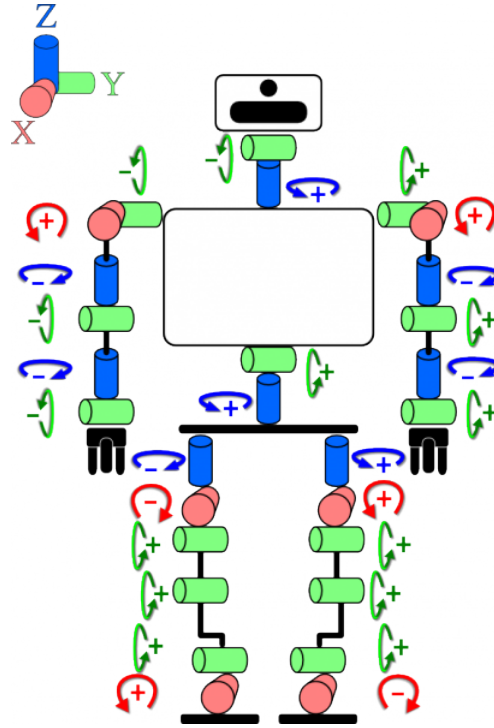


Figure 3.1: Distribución de grados de libertad del robot TEO.

and neck, and 1 line per each leg and torso.

For data acquisition, the robot has Force-Torque sensors located at the robot ankles and wrists, used locomotion and manipulation, respectively. These sensors are plugged into real time data acquisition PCI cards. Including F/T sensors is an important difference and advantage respect RH-2 predecessors. They allow to close the control loop and then, to obtain a kind of feedback which is necessary to accomplish tasks successfully.

### 3.2 Force/Torque sensors

Force-Torque (F-T) sensors are based on strain gauge sensors arranged in such a way that allows to obtain force and moment measures in all axes of the 3D space.

The sensors used in the platform, are the commercial JR3 F-T sensors described in Table 3.1. Look at the full scales difference between the sensors used in the wrists joints and the ones used in the ankle joints. Ankle sensors must be able to support greater forces and moments including the ones exerted by the own robot.

Joint	Model	$F_{x,y}$	$F_z$	$M_{x,y,z}$
Wrist	50M31A	100N	200N	5 Nm
Ankle	85M35A	250N	500N	212Nm

Table 3.1: F-T sensor models and characteristics. [JR3 Inc.]

According to the manufacturer, the two first digits of the model show the sensor diameter, followed by the serie, and the next two digits, the thickness. As mentioned before, the ankle sensors are bigger and they support greater forces and moments. The sensors used in this Master Thesis are the ones mentioned in Table 3.1 for ankle joints.

Serie M sensors include inner electronics in order to filter noise, digital output to use a data acquisition PCI card from the same manufacturer and an analogical output option. The nominal precision of all sensors of serie M is 1% of full scale, and a 1/4000 full scale resolution.

The sensors used in this work, provide the option of acquiring data in International System Units or Imperial System Units, according to Figure **FIGURA**.

### 3.3 Data Acquisition

The PCI cards used for data acquisition are PCI 1592D from JR3 Inc, which has 4 ports (named as in Figure ???). The sensors are plugged through a 6 or 8 pinout cables (RJ-11 and RJ-45, respectively). In the case of RJ-45, two pinouts are not used. The PCI card uses these cables to receive high speed data and provide power supply to the sensors. About the PCI supply, it is provided by

the PCI slot from the computer where it is installed.

In order to access to received data from the sensors, it is necessary to access to card memory, specifying the memory address for each available data. These addresses can be found at [ANEXO. DATOS DEL FABRICANTE].

It is important to take into account that the forces and torques obtained from the sensors and processed by the card, are in the International System Units. Forces are given in Newton [N] and torques are given in tenths of a newton per meter [dN·m].



## Chapter 4

# Control Architecture

### 4.1 Introduction

Vukobratovic [Vuk1970] was one of the first researchers involved in the stability of bipedal robots, followed by [Kaj2001] and [Kim2004]. In all their studies, the biped robot was usually represented by a planar inverted pendulum with the base representing the foot and the ankle joint. And in the latest control strategies, researchers divide robot balance control into the hip strategy and the ankle strategy **REFERENCIA Y EXTENDER MÁS**. The basis of both strategies are close to the ZMP areas explained in previous sections. When the robot is in a stable posture and a disturbance is applied, depending the magnitude or the application point of that disturbance, the robot will react different. If the change of the ZMP position remains in a stable area, the control will react by the motion of the ankle joints to recover the robot balance. Nevertheless, if the ZMP position reaches an uncertain-stability area, it will be also necessary to move the hip joints to recover balance. Even a gait will be necessary if the loss of stability is unavoidable.

A humanoid is an electromechanical system, so it should have all type of errors: structure flexion, small backlash between motion parts, etc. Also it will operate in a co-existing environment with humans, so the disturbances are un-

expected at any time. Therefore, the Stabilizer is an essential element to provide stable human-like walking of a humanoid robot. The Stabilizer should perform two basic operations: 1. When the humanoid robot walks, it should correct the robot's walking trajectory in order to provide the secure position at any time of its motion. 2. When the humanoid robot has stopped, it should control its posture.

Thus, the Stabilizer can be decoupled into ZMP and Attitude controllers. This Master Thesis will deal with the issue of maintaining an upright posture while the robot is in a static position, without following a motion pattern.

## 4.2 Single Inverted Pendulum Model

The simple inverted pendulum is the most basic model used to simplify humanoids' body. The basis of the pendulum are a mass  $m$  linked to a pivot point 0 by means of a massless link of longitude  $l$  as in Figure 4.1.

The mass  $m$  represents the total mass of the modelled system, a humanoid robot in this case, located at its Centre of Mass (CoM), and the longitude  $l$  is the distance between the pivot point to the CoM. Its dynamical model in a planar, for example XZ case, is expressed by the equation 4.1, if gravitational force is considered the only force acting in the system.

$$\tau_0 = ml^2\ddot{\theta} - mgl \sin \theta \quad (4.1)$$

where  $\tau_0$  is the torque generated by the ankle joint,  $\theta$  its angular position and  $l$ , the distance between the joint and the CoM. It is assumed that angles are small enough and  $\sin \theta = \theta$ . Then, equation 4.1 changes to equation 4.2

$$\tau_0 = ml^2\ddot{\theta} - mgl\theta \quad (4.2)$$

The main complexity of this model is the fact that equation 4.2 does not give the possibility of controlling the ZMP by angular position of the ankle joint. To

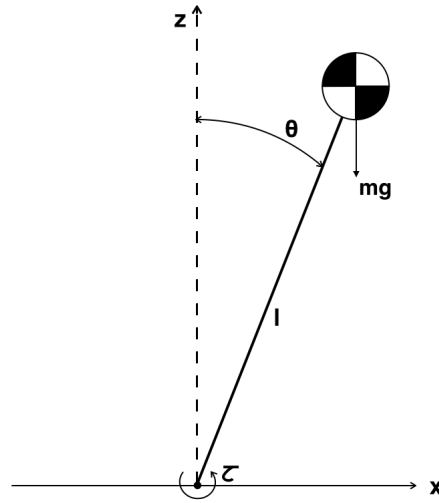


Figure 4.1: Single inverted pendulum.

overcome this problem, the inverted pendulum model can be slightly modified. The link of the pendulum which connects the ankle joint to the concentrated mass (CoM) is generally assumed to be rigid. However, in the real humanoid mechanism it is flexible because the leg length is relatively long and the mechanical structure suffers from flexibility and small backlashes. Because of this compliance, the humanoid robot exhibits the characteristics of a lightly damped structure [Kim2004]. For example, in a static case when the ankle joint is under position control, a pushing external force can easily excite an oscillation. This oscillation exists even when the position error in every joint is zero. This phenomenon is prevalent in the fast dynamical gait; therefore it is very important to implement a control mechanism allowing ZMP fast correction considering the stiffness of the humanoid robot links. The most suitable model in this case will be a single mass inverted pendulum with compliant joint as shown in Figure 4.2, where  $u$  denotes the ankle joint reference angle and  $\theta$  denotes the actual inclined angle produced by the compliance of the mechanical structure of the humanoid,  $k$  denotes the stiffness of the leg and  $\tau_0$  is the torque produced by the motor of the ankle joint to place the inverted pendulum into the desired angular position.

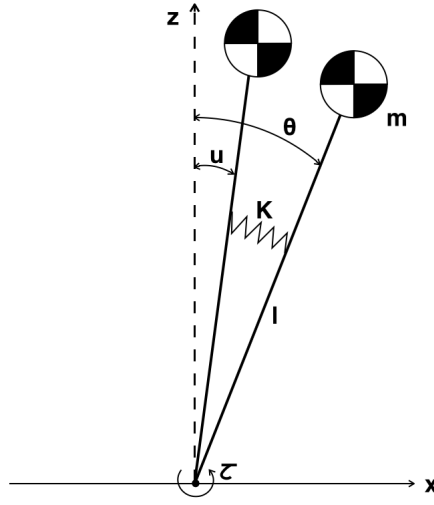


Figure 4.2: Single inverted pendulum with compliant joint.

Then, the torque  $\tau_0$  should be expressed as:

$$\tau_0 = k(\theta - u) \quad (4.3)$$

Taking the Laplace transform of equation 4.2, it is obtained:

$$T(s) = mgl\theta(s) - ml^2 s^2 \theta(s) \quad (4.4)$$

The Laplace transform of equation 4.3 is:

$$T(s) = k(\theta(s) - U(s)) \quad (4.5)$$

Reflecting  $\theta(s)$  from equation 4.5 and placing it into the equation 4.4 and simplifying, the transfer function is obtained:

$$\frac{T(s)}{U(s)} = k \frac{-s^2 + (\beta - \alpha)}{s^2 + \alpha} \quad (4.6)$$

where:

$$\alpha = \frac{k - mgl}{ml^2} \quad (4.7)$$

$$\beta = \frac{k}{ml^2} \quad (4.8)$$

On the other hand, from equation [REF ECUACION zmp] relating the moment produced by the ground reaction force around  $y$  axis with  $x$  ZMP direction (the planar XZ case of the inverted pendulum is considered) we can get:

$$\tau_y = -mgx_{ZMP} = -F_z x_{ZMP} \quad (4.9)$$

and then the Laplace transform of the equation 4.9 is:

$$\tau_y(s) = -F_z x_{ZMP}(s) \quad (4.10)$$

For the static equilibrium of the system, the moment generated by the motor of the ankle joint should compensate the moment produced by the ground reaction force:

$$\tau_0 = \tau_y \quad (4.11)$$

The relation between  $\tau_y$  and  $x_{ZMP}$  is lineal, therefore, placing 4.10 into 4.6 we get the following transfer function relating ZMP to ankle joint position:

$$\frac{x_{ZMP}(s)}{U(s)} = -k_1 \frac{-s^2 + (\beta - \alpha)}{s^2 + \alpha} \quad (4.12)$$

where  $k_1 = \frac{k}{mg}$ .

In the equation 4.6  $x_{ZMP}(s)$  is the output and  $U(s)$  is the input of the system. It allows for the ZMP of the humanoid robot to be controlled by the position of its ankle joint. From transfer function equation, we can obtain the space state model equations:

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -\alpha & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u \quad (4.13)$$

$$y = \begin{bmatrix} -k_1\beta & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} k_1 \end{bmatrix} u \quad (4.14)$$

where  $x_1$  and  $x_2$  are state variables and  $y$  is the output of the system, then the  $x_{ZMP}$

### 4.3 Feedback in state space. The Linear Quadratic Regulator

The quadratic optimal control method is one of the control methods applied in state space systems and it provides a systematic way of computing the state feedback control gain matrix [Ogata]. Given the state space system equation

$$\dot{x} = Ax + Bu, \quad (4.15)$$

the LQR determines the matrix  $K$  of the optima control vector

$$u(t) = -Kx(t) \quad (4.16)$$

so as to minimize the performance index

$$J = \int_0^\infty (x^T Q x + u^T R u) dt \quad (4.17)$$

where  $Q$  is a positive-definite (or positive-semidefinite) Hermitian or real symmetric matrix and  $R$  is a positive-definite Hermitian or real symmetric matrix. Note that the matrices  $Q$  and  $R$  determine the relative importance of the error and the expenditure of the energy of the control signals. The linear control law given by equation 4.16 is the optimal control law. Therefore, if the unknown elements of the matrix  $K = [K_1 \ K_2]$  are determined so as to minimize the performance index, then  $u(t) = -Kx$  is optimal for any initial state  $x(0)$ . The block diagram showing the optimal configuration for the single inverted pendulum system is presented in Figure 4.3. The controller maintain desired ( $x_{ZMP}$ ) position of the single pendulum close to zero. Thus, the reference input of the control system in Figure [REF] is not zero.?????

The state space representation 4.13, 4.14 is a controllable canonical form that is important for the LQR controller design. It is desired to keep the actual ZMP, measured and computed by force-torque sensors located in the feet of the humanoid robot, close to its stable reference position as was discussed in previous sections. As the system is a type 0 plant, it is necessary to insert an integrator in

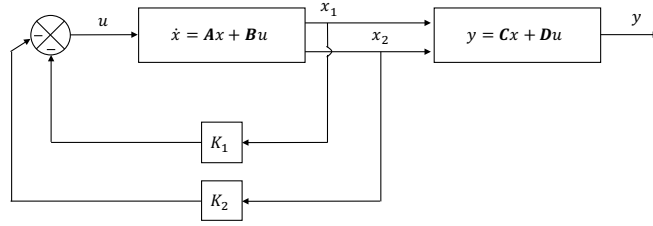


Figure 4.3: Block diagram

order to design a ZMP servo control system (type 1) and remove the steady state error. Therefore, we feed the output signal  $y$  (which indicates the real ZMP) back to the input and an integrator in the feedforward path as is shown in Figure 4.4.

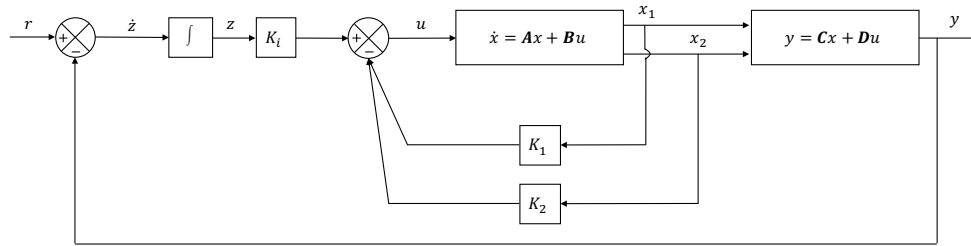


Figure 4.4: ZMP LQR control system.

Thus, referring equations 4.13 and 4.14 and Figure 4.4 and considering the actual ZMP position as the output of the system and  $r$  as the reference input signal we obtain the equations for the closed loop system as follows:

$$\dot{x} = \mathbf{A}x + \mathbf{B}u \quad (4.18)$$

$$y = \mathbf{C}\mathbf{x} + \mathbf{D}u \quad (4.19)$$

$$u = -\mathbf{K}\mathbf{x} + K_i z \quad (4.20)$$

$$\dot{z} = r - y = r - (\mathbf{C}\mathbf{x} + \mathbf{D}u) \quad (4.21)$$

For the type 1 servo system, the state error equation is given by:

$$\begin{bmatrix} \dot{\mathbf{x}} \\ \dot{z} \end{bmatrix} = \begin{bmatrix} \mathbf{A} & \mathbf{0} \\ -\mathbf{C} & 0 \end{bmatrix} \begin{bmatrix} \mathbf{x} \\ z \end{bmatrix} + \begin{bmatrix} \mathbf{B} \\ 0 \end{bmatrix} u \quad (4.22)$$

and the control signal  $u$  is given by:

$$u = \begin{bmatrix} -\mathbf{K} & K_i \end{bmatrix} \begin{bmatrix} \mathbf{x} \\ z \end{bmatrix} \quad (4.23)$$

The optimum  $K$  matrix is obtained from equations 4.24 and 4.25.

$$K = R^{-1}B^T P \quad (\text{continuous case}) \quad (4.24)$$

$$K = (R + B^T P B)^{-1} B^T P A \quad (\text{discrete case}) \quad (4.25)$$

where  $P$  is a positive-definite Hermitian or real symmetric matrix and it is necessary to compute the algebraic Ricatti Equation

$$P \rightarrow A^T P + P A - P B R^{-1} B^T P + Q = 0 \quad (\text{continuous case}) \quad (4.26)$$

$$P \rightarrow A^T P A + P - A^T P B (R + B^T P B)^{-1} B^T P A + Q = 0 \quad (\text{discrete case}) \quad (4.27)$$

In order to obtain the controller design for further simulations and experiments, the following mechanical parameters of the inverted pendulum (corresponding to Rh-2 humanoid robot) were taken:  $m = 62.416$  kg,  $l = 1.03$  m,  $k = 0.1$ .



Valor y unidades de stiffness???. For the optimum response of the control system, it is suggested to take  $Q = C^T C = \begin{bmatrix} 5.037 \cdot 10^{-8} & 0 \\ 0 & 0 \end{bmatrix}$  and  $R = 1$ . After the LQR controller was designed, the control gains matrix  $K = [18.89 \quad 6.14]$  was obtained using a sample time  $T = 0.001$  s.

## 4.4 Stabilizer

Previously it was shown that the dynamics of a humanoid robot can be a single inverted pendulum and how the pendulum maintains a desired position thanks to the controller designed. Now, let us introduce the detailed stabilizer structure (Figure 4.5).

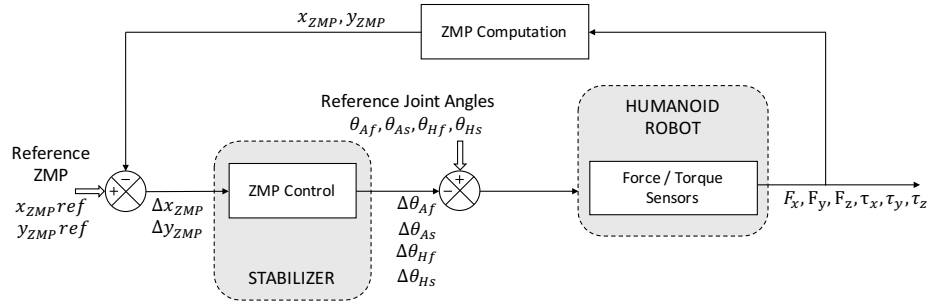


Figure 4.5: Stabilizer architecture.

The sensorial system of the robot consisting of two six-axis force-torques located at the robot ankles, provides the controller the real distribution of the forces and torques  $F_x, F_y, F_z, \tau_x, \tau_y, \tau_z$  at the contact point of the foot with the ground. After the actual ZMP position  $x_{ZMP}, y_{ZMP}$  is computed, the ZMP  $\Delta x_{ZMP}, \Delta y_{ZMP}$  errors can be estimated. These errors are the input data for the Stabilizer and it controls the error in ZMP positioning of the humanoid robot by

the motion of the ankle and hip joints.

## 4.5 Control strategy

As previously mentioned, the human body can be divided in three basic planes: sagittal, transversal and frontal. Frontal and sagittal planes are useful to simplify the controller and it can be decoupled into two 2D linear pendulums instead of one 3D pendulum.

In the frontal control, the pendulum will rotate around the X axis. Sagittal joint ankles and sagittal hip will move. In the sagittal control, the pendulum will rotate around the Y axis. Frontal joint ankles will move.

The phenomenon of locomotion can be understood more easily if we study the motion of a human in three basic planes: sagittal, transversal and frontal (Fig. 5.1). It is important to mention that the most important motions occur in the sagittal plane because it coincides with the main walking direction. Motions in transversal and frontal planes are not so radical. The joints responsible for motion in these two plains (for the most part in the frontal plane) help significantly in the stabilization of the locomotion cycle.