```
Prove:
```

 $n! > 2^n$ for $n \ge 4$

Base Case:

n = 4

 $4! > 2^4$

24 > 16

Hypothesis:

 $k! > 2^k$ is TRUE for $k \ge 4$

Proof:

$$(k+1)! > 2^{k+1}$$

$$(k+1)k! > 2(2^k)$$

$$(k+1)2^k > 2(2^k)$$

$$k \ge 4 :: k+1 > 2$$

$$(k+1)! > k!(k+1) > 2^k(k+1) > 2\big(2^k\big) > 2^k$$

Prove:

 $2^{2n} - 1$ is divisible by 3

Base Case:

$$n = 1$$

$$2^{2(1)}-1$$

$$4-1=\frac{3}{3}=1$$

Hypothesis:

 $2^{2k}-1$ is divisible by 3 is TRUE for $k\geq 1$

Proof:

$$2^{2(k+1)} - 1$$

$$2^{2k+2}-1$$

$$2^2(2^k)-1$$

$$4(2^k)-1$$

$$(3+1)2^k-1$$

$$3(2^k) + 2^k - 1$$

Prove

```
fact(n)
   if n == 0:
      return 1
   else:
```

Base case

$$n = 0$$

```
fact(0)
    if 0 == 0:
        return 1

Hypothesis:
fact(k) is TRUE for k ≥ 0

Proof:
fact(k + 1):
    if k + 1 == 0 false
    else:
```