Inductive Proof

$$a(0) = 1$$
, $d = 2$

$$a(1) = 1 + 2 = 3 = a(0) + 2$$

$$a(2) = 3 + 2 = 5 = a(1) + 2 = ((a(0) + 2) + 2) + 2$$

$$a(n) = a(0) + 2n$$

Prove:

$$a(n) = a(n-1) + 2 = a(0) + 2n$$

Base Case (usually the recursive

$$a(0) = a(0) + 2(0)$$

$$a(0) = a(0)$$

Hypothesis:

$$a(k) = a(k-1) + 2 = a(0) + 2k$$
 is TRUE

$$a(0) = 1$$

for
$$k \geq 0$$

Proof:

$$a(k+1) = a(k+1-1) + 2 = a(0) + 2(k+1)$$

$$a(k+1) = a(k) + 2 = a(0) + 2k + 2$$

$$a(0) + 2k + 2 = a(0) + 2k + 2$$

Second Proof

Prove:

$$a(n) = a(n-1) \cdot r = a(0) \cdot r^n$$

Base Case:

$$n = 0$$

$$a(0) = a(0) \cdot r^0$$

Hypothesis:

$$a(k) = a(k-1) \cdot r = a(0) \cdot r^k$$
 is TRUE

for
$$k \ge 0$$

Proof:

$$a(k+1) = a(k+1-1) \cdot r = a(0) \cdot r^{k+1}$$

$$a(k+1) = a(k) \cdot r = a(0) \cdot r^{k+1}$$

$$a(k+1) = a(0) \cdot r^k \cdot r = a(0) \cdot r^{k+1}$$

$$a(k+1) = a(0) \cdot r^{k+1} = a(0) \cdot r^{k+1}$$