## Permeability of free space

 $\mu_0$  = permeability of free space

Units: Tm/A

$$\mu_0 = 4\pi \times 10^{-7}~\mathrm{Tm/A}$$

## Magnetic Field Produced by Moving Charges

$$\vec{\mathrm{B}}_{\mathrm{point\ charge}} = \left(\frac{\mu_0}{4\pi}\right) \left(\frac{q}{r^2}\right) (\vec{v} \times \hat{r})$$

## Magnetic Field Produced by Straight Currents

$$|\vec{\mathrm{B}}_{\mathrm{current}}| = rac{\mu_0 I}{2\pi r}$$

Direction: Point right thumb in direction of current flow, curl fingers around wire. Direction fingers curl represent direction of magnetic field around wire

## **Magnetic Force Between Parallel Currents**

$$|ec{F}_{
m mutual}| = rac{\mu_0 I_1 I_2 L}{2\pi r}$$

$$ec{F}_1 = I_1 ig(ec{L}_1 imes ec{B}_2ig)$$

Direction:

- Same Current Direction: Attracts
- Opposite Current Direction: Repels

## Mutual Magnetic Force on Parallel Charges

$$|\vec{F}_{\mathrm{mutual}}| = \frac{\mu_0 q_1 q_2 v_1 v_2}{4\pi r^2}$$

Direction:

- Same Direction, Same Charge: Attract
- Opposite Direction, Opposite Charge: Attract
- Anything Else: Repel

## Magnetic Field Produced by <u>Curved</u> Current Loops

#### **Single or Multiple Loops**

$${
m B_{center\ of\ loop}} = rac{{ ilde{\mu}_0 I}}{2R} N$$

Direction:

- Current curves: Fingers
- B is straight: Thumb

#### Solenoid (very long loop)

$$\mathbf{B} = \frac{\mu_0 I}{L} N = \mu_0 I n$$

$$let n = \frac{N}{L}$$

Total Length of Wire =  $(2\pi R)N$ 

## Magnetic Field by Toroidal Solenoids

$$\mathbf{B} = \frac{\mu_0 I}{2\pi r} N$$

r: distance from center

Direction: Same as Loops

 $\vec{\mathrm{B}}$  exists between  $R_{\mathrm{inner}}$  and  $R_{\mathrm{outer}},$  zero outside

### **Biot-Savart Law**

$$d\vec{B} = \frac{\mu_0}{4\pi} \frac{Id\vec{l} \times \hat{r}}{r^2}$$

# Magnetic Field by Finite Straight Line of Current $B = \frac{\mu_0 I}{4\pi x} \frac{2a}{\sqrt{x^2 + a^2}}$

$$B = \frac{\mu_0 I}{4\pi x} \frac{2a}{\sqrt{x^2 + a^2}}$$