

Dielectrics

- insert an insulator between plates
- increases capacitance
- allows for more charge to be stored at a given charging voltage
- weakens E-fields

Constant Charge Q

- no battery connected
- $Q = C \uparrow V \downarrow$, V decreases
- $U = \frac{1}{2} \frac{Q^2}{C \uparrow}$, U decreases
- $u = \frac{1}{2} \epsilon_0 (E \downarrow)^2$, u decreases

Constant Voltage V

- inserted when batter still connected
- $C \uparrow = \frac{Q \uparrow}{V}$, Q increases
- $U = \frac{1}{2} C \uparrow V^2$, U increases
- $u = \frac{1}{2} \epsilon_0 (E \downarrow)^2$, u decreases

κ = dielectric constant, a measure of how well an insulator reduces V

$$\kappa = \frac{V_0}{V}$$

$$\kappa \geq 1$$

Different materials have different κ values

\vec{E}_d = displacement field

$$\vec{E}_{\text{total}} = \vec{E}_0 - \vec{E}_d$$

$$\sigma_d = \sigma \left(\frac{k-1}{k} \right)$$

ϵ = permittivity of the dielectric

$$\epsilon = \kappa \epsilon_0$$

$$C = \kappa C_0$$

$$E = \frac{E_0}{\kappa}$$

$$C = \kappa \epsilon_0 \frac{A}{d}$$

$$V_{\text{max}} = E_{\text{max}} d$$

Dielectric Strength

- maximum \vec{E} -field that a dielectric can tolerate before breaking down
- Dry air: $E_{\text{max}} = 3.0 \times 10^6 \text{ V/m}$

Energy Density

$$u = \text{energy density} = \frac{U}{\text{volume between plates}}$$

$$u = \frac{1}{2} \epsilon_0 E^2$$