

# Project

Jordan Klein

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## Helper Functions

This functions will be used for preprocessing and analysis.

```
impute_lm <- function(feature, data, condition) {

  # Impute values in a numeric column using a linear model.
  # Rows where `condition` is FALSE are used to train the model.
  # For rows where `condition` is TRUE, the function predicts and replaces the value.
  # All other rows keep their original values.

  feature <- rlang::enquo(feature)
  condition <- rlang::enquo(condition)

  # Rows where condition is FALSE
  train_data <- data %>%
    dplyr::filter(!(!condition))

  # Fit LM
  formula <- as.formula(paste0(rlang::as_name(feature), " ~ ."))
  fit <- lm(formula, data = train_data)

  # Predict for rows needing imputation
  pred_data <- data %>% dplyr::filter(!(!condition))
  preds <- predict(fit, newdata = pred_data)

  # Original column
  out <- data[[rlang::as_name(feature)]]

  # Correctly evaluate logical condition within `data`
  cond_logical <- rlang::eval_tidy(condition, data)

  # Replace
  out[cond_logical] <- preds

  out
}

get_predictions <- function(
  formula,
  train,
  test,
```

```

model = c("lm", "rf"),
...
) {

# Train a linear model or random forest on `train` and generate predictions for `test`.
# Select model via `model = "lm"` or `"rf"`.
# Returns a vector of predictions.

# match the argument + enforce allowed values
model <- match.arg(model)

if (model == "lm") {
  # Linear Model
  fit <- lm(formula, data = train, ...)
  preds <- predict(fit, newdata = test)

} else if (model == "rf") {
  # Random Forest
  fit <- ranger::ranger(
    formula,
    data = train,
    num.threads = parallel::detectCores(),
    ...
  )
  preds <- predict(fit, test)$predictions
}

return(preds)
}

kfold_metrics <- function(
  formula,
  data,
  k = 10,
  model = c("lm", "rf"),
  ...
) {

# Perform k-fold cross-validation for a given formula and model type (lm or rf).
# Trains on k-1 folds and predicts the held-out fold, repeating for all k folds.
# Returns MAE and MAPE along with the model type and formula used.

model <- match.arg(model)

# Create folds
folds <- createFolds(1:nrow(data), k = k, list = TRUE)

preds <- numeric(nrow(data))
actual <- model.response(model.frame(formula, data))

# Perform CV
}

```

```

for (i in seq_along(folds)) {
  test_idx <- folds[[i]]
  train_idx <- setdiff(seq_len(nrow(data)), test_idx)

  train <- data[train_idx, ]
  test <- data[test_idx, ]

  # use your helper
  preds[test_idx] <- get_predictions(
    formula = formula,
    train    = train,
    test     = test,
    model    = model,
    ...
  )
}

# Metrics
mae <- mean(abs(preds - actual))
mape <- mean(abs((actual - preds) / actual)) * 100

data.frame(
  model    = model,
  formula = paste(deparse(formula), collapse = ""),
  mae      = mae,
  mape     = mape
)
}

eval_circuit <- function(
  formulas,
  data,
  k = 10,
  excel_path = NULL,
  ...
) {

  # -----
  # Eval Circuit
  # Runs model evaluation across all provided formulas.
  #
  # Given:
  #   - formulas: a named list of formulas
  #   - data: dataset
  #   - k: number of folds for k-fold CV
  #   - excel_path: optional path to save results as an Excel file
  #
  # Process:
  #   • For each formula:
  #     - Run k-fold CV using Linear Regression
  #     - Run k-fold CV using Random Forest
  #     - Store MAE, MAPE, model type, and the formula name
}

```

```

#   • Combine results for all formulas and models
#   • Sort final table by MAE (ascending)
#   • Optionally export the results to Excel
#
# Returns:
#   A data frame with:
#     formula_name, model type, mae, mape, and other metrics
# -----
results <- Map(function(name, form) {

  lm_res <- kfold_metrics(
    formula = form,
    data    = data,
    k       = k,
    model   = "lm",
    ...
  )
  lm_res$formula_name <- name      # <--- save the name

  rf_res <- kfold_metrics(
    formula = form,
    data    = data,
    k       = k,
    model   = "rf",
    ...
  )
  rf_res$formula_name <- name      # <--- same

  rbind(lm_res, rf_res)

}, names(formulas), formulas)

# Combine all
results_df <- do.call(rbind, results)

# Order by MAE
results_df <- results_df[order(results_df$mae), ]
rownames(results_df) <- NULL

# Save Excel if needed
if (!is.null(excel_path)) {
  write_xlsx(results_df, excel_path)
  message("Results written to: ", excel_path)
}

return(results_df)
}

```

## Load and Preprocess

Impute missing values, engineer features of EDA and modeling

```

data <- read.csv("train2.csv")

Features <- list(
  Target = "Age",
  Size = c("Length", "Height", "Diameter"),
  Mass = c("Weight", "Shucked.Weight", "Viscera.Weight", "Shell.Weight")
)
Features$All <- c(Features$Size, Features$Mass)

abalone <- data %>%
  mutate(
    Volume = 4/3 * pi * Length/2 * Height/2 * Diameter/2,
    IsAdult = factor(if_else(Sex == "I", "Infant", "Adult"),
                     ordered = TRUE, levels = c("Infant", "Adult")),
    Sex = factor(case_when(
      Sex == "I" ~ "Infant",
      Sex == "F" ~ "Female",
      Sex == "M" ~ "Male"
    )),
    Height = impute_lm(
      feature = Height,
      data = cur_data(),
      condition = Height == 0
    ),
    Diameter = impute_lm(
      feature = Diameter,
      data = cur_data(),
      condition = Diameter == 0
    ),
    Shucked.Weight = impute_lm(
      feature = Shucked.Weight,
      data = cur_data(),
      condition = Shucked.Weight > Weight
    ),
    Weight.Mean1 = (Shucked.Weight*Viscera.Weight*Shell.Weight)**(1/3),
    Weight.Mean2 = (Weight*Shucked.Weight*Viscera.Weight*Shell.Weight)**(1/4),
    Weight.Norm1 = sqrt(Shucked.Weight**2 + Viscera.Weight**2 + Shell.Weight**2),
    Weight.Norm2 = sqrt(Shucked.Weight**2 + Viscera.Weight**2 + Shell.Weight**2 + Weight **2),
    Size.Norm = sqrt(Length**2 + Diameter**2 + Height**2),
    Size.Mean = (Length + Diameter + Height)**(1/3),
    Shell.Ratio = Shell.Weight / Weight,
    Meat.Ratio = Shucked.Weight / Weight,
    Viscera.Ratio = Viscera.Weight / Weight,
    Soft.Ratio = (Shucked.Weight + Viscera.Weight) /Weight,
    Elongation = Length / Diameter,
    Flatness = Height / sqrt(Length*Diameter),
    SurfaceArea = (Length * Diameter + Length * Height + Diameter * Height),
    Roundness = Diameter / Length,
    Density = Volume / Weight
  )
## Warning: There was 1 warning in `mutate()` .
## i In argument: `Height = impute_lm(...)` .

```

```

## Caused by warning:
## ! 'cur_data()' was deprecated in dplyr 1.1.0.
## i Please use 'pick()' instead.

summary(abaalone)

##      id          Sex        Diameter       Length
## Min.   : 1 Female:4576   Min.   :0.2000   Min.   :0.200
## 1st Qu.: 3751 Infant:4967   1st Qu.:0.8875   1st Qu.:1.150
## Median : 7500 Male  :5457    Median :1.0750   Median :1.375
## Mean   : 7500                   Mean   :1.0221   Mean   :1.315
## 3rd Qu.:11250                  3rd Qu.:1.2000   3rd Qu.:1.538
## Max.   :15000                  Max.   :1.5750   Max.   :2.038
##      Height        Weight     Shucked.Weight  Viscera.Weight
## Min.   :0.0250   Min.   :0.2268   Min.   : 0.0245   Min.   : 0.01417
## 1st Qu.:0.2875  1st Qu.:13.1967  1st Qu.: 5.6557   1st Qu.: 2.80660
## Median :0.3625  Median :23.5584   Median : 9.8585   Median : 4.89029
## Mean   :0.3468  Mean   :23.2434   Mean   :10.0330   Mean   : 5.01447
## 3rd Qu.:0.4125  3rd Qu.:32.1625   3rd Qu.:13.9763   3rd Qu.: 6.98815
## Max.   :0.6000  Max.   :75.3246   Max.   :42.1841   Max.   :20.12814
##      Shell.Weight      Age         Volume      IsAdult
## Min.   :0.09922  Min.   : 1.000   Min.   :0.0000   Infant: 4967
## 1st Qu.: 3.82718 1st Qu.: 8.000   1st Qu.:0.1548   Adult  :10033
## Median : 6.80388 Median :10.000   Median :0.2829
## Mean   : 6.67329 Mean   : 9.985   Mean   :0.2813
## 3rd Qu.: 9.07184 3rd Qu.:11.000   3rd Qu.:0.3953
## Max.   :29.10076 Max.   :29.000   Max.   :0.8821
##      Weight.Mean1     Weight.Mean2     Weight.Norm1     Weight.Norm2
## Min.   : 0.06579  Min.   :0.09683  Min.   : 0.1671   Min.   : 0.3414
## 1st Qu.: 3.96474  1st Qu.: 5.35190  1st Qu.: 7.5146   1st Qu.:15.2543
## Median : 6.97497  Median : 9.47937  Median :13.1642   Median :27.0724
## Mean   : 6.91257  Mean   : 9.35784  Mean   :13.1161   Mean   :26.6984
## 3rd Qu.: 9.61440  3rd Qu.:13.01581  3rd Qu.:18.2722   3rd Qu.:37.0408
## Max.   :22.89460  Max.   :30.53401  Max.   :48.2741   Max.   :89.4661
##      Size.Norm      Size.Mean     Shell.Ratio     Meat.Ratio
## Min.   :0.3562   Min.   :0.8298   Min.   :0.1383   Min.   :0.08231
## 1st Qu.: 1.4808  1st Qu.: 1.3248  1st Qu.: 0.2679   1st Qu.:0.39884
## Median : 1.7897  Median : 1.4136  Median : 0.2887   Median :0.43269
## Mean   : 1.7014  Mean   : 1.3800  Mean   : 0.2924   Mean   :0.43054
## 3rd Qu.: 1.9899  3rd Qu.: 1.4659  3rd Qu.: 0.3137   3rd Qu.:0.46344
## Max.   : 2.6282  Max.   : 1.6054  Max.   : 1.0000   Max.   :0.82876
##      Viscera.Ratio    Soft.Ratio     Elongation     Flatness
## Min.   : 0.01587  Min.   :0.1746   Min.   :0.6667   Min.   :0.0603
## 1st Qu.: 0.19867  1st Qu.: 0.6116  1st Qu.: 1.2632   1st Qu.:0.2790
## Median : 0.21463  Median : 0.6494   Median : 1.2885   Median :0.2964
## Mean   : 0.21600  Mean   : 0.6465   Mean   : 1.2925   Mean   :0.2975
## 3rd Qu.: 0.23270  3rd Qu.: 0.6841   3rd Qu.: 1.3165   3rd Qu.:0.3146
## Max.   : 0.76190  Max.   : 1.2381   Max.   : 2.2500   Max.   :0.5653
##      SurfaceArea     Roundness      Density
## Min.   :0.09977  Min.   :0.4444   Min.   :0.00000
## 1st Qu.: 1.60988 1st Qu.: 0.7596  1st Qu.: 0.01110
## Median : 2.38016 Median : 0.7761   Median : 0.01196
## Mean   : 2.26747 Mean   : 0.7748   Mean   : 0.01196
## 3rd Qu.: 2.96352 3rd Qu.: 0.7917   3rd Qu.: 0.01284

```

```
##  Max.    :5.10562  Max.    :1.5000  Max.    :0.02557
```

## EVALUATE DATA QUALITY

Some features have missing data. Diameter and Height have 0 values. Some rows have Shucked Weight which are higher than the total weight.

This values are impossible, and will be replaced using a predictive model that considers all other features.

```
data <- read.csv("train2.csv")

p1<- data %>%
  select(Weight, Shucked.Weight) %>%
  mutate(
    Suspect = Shucked.Weight > Weight
  ) %>%
  ggplot(aes(x = Weight, y = Shucked.Weight)) +
  # Shade area below y = x
  geom_ribbon(aes(ymin = Weight, ymax = Inf), fill = "red", alpha = 0.1) +
  # Points
  geom_point(aes(color = Suspect, size = Suspect)) +
  scale_color_manual(values = c("FALSE" = "gray60", "TRUE" = "firebrick")) +
  scale_size_manual(values = c("FALSE" = 1, "TRUE" = 3)) +
  # Optional: draw y = x line for reference
  geom_abline(slope = 1, intercept = 0, linetype = "dashed") +
  annotate(
    "text",
    x = 0,
    y = 20,
    label = "Suspect Zone: Shucked Weight > Total Weight",
    hjust = -.1,           # left-align text at x = 0
    vjust = 1,             # anchor at top of plot
    size = 6,
    color = "firebrick"
  ) +
  scale_y_continuous(limits = c(0,20)) +
  scale_x_continuous(limits = c(0,20)) +
  theme_excel_new() +
  labs(title = "Analysis of Data Quality: Total vs. Shucked Weight",
       x = "Total Weight (g)",
       y = "Shucked Weight (g)") +
  theme(
    plot.title = element_text(size = 20),
    axis.title = element_text(size = 16),
    axis.text = element_text(size = 12),
    legend.position = "none",
    plot.background = element_rect(fill = "aliceblue", color = NA),
    panel.background = element_rect(fill = "aliceblue", color = NA)
  )
```

```
## Warning: The 'size' argument of 'element_line()' is deprecated as of ggplot2 3.4.0.
## i Please use the 'linewidth' argument instead.
## i The deprecated feature was likely used in the ggthemes package.
```

```

## Please report the issue at <https://github.com/jrnold/ggthemes/issues>.
## This warning is displayed once every 8 hours.
## Call `lifecycle::last_lifecycle_warnings()` to see where this warning was
## generated.

```

```

p2 <- data %>%
  select(Diameter, Height) %>%
  mutate(
    Suspect = Diameter == 0 | Height == 0
  ) %>%
  ggplot(aes(x = Height, y = Diameter)) +
  # Points
  geom_point(aes(color = Suspect, size = Suspect)) +
  scale_color_manual(values = c("FALSE" = "gray60", "TRUE" = "firebrick")) +
  scale_size_manual(values = c("FALSE" = 1, "TRUE" = 3)) +
  # Labels
  labs(
    title = "Analysis of Data Quality: Height & Diameter",
    x = "Height (mm)",
    y = "Diameter (mm)"
  ) +
  annotate(
    "text",
    x = 0.01, y = 0.8,
    label = "Suspect Entries:\nZero Height or Zero Diameter",
    color = "firebrick",
    size = 6,
    hjust = 0
  ) +
  theme_excel_new() +
  theme(
    legend.position = "none",
    plot.background = element_rect(fill = "aliceblue", color = NA),
    panel.background = element_rect(fill = "aliceblue", color = NA)
  )

```

p1/p2

```

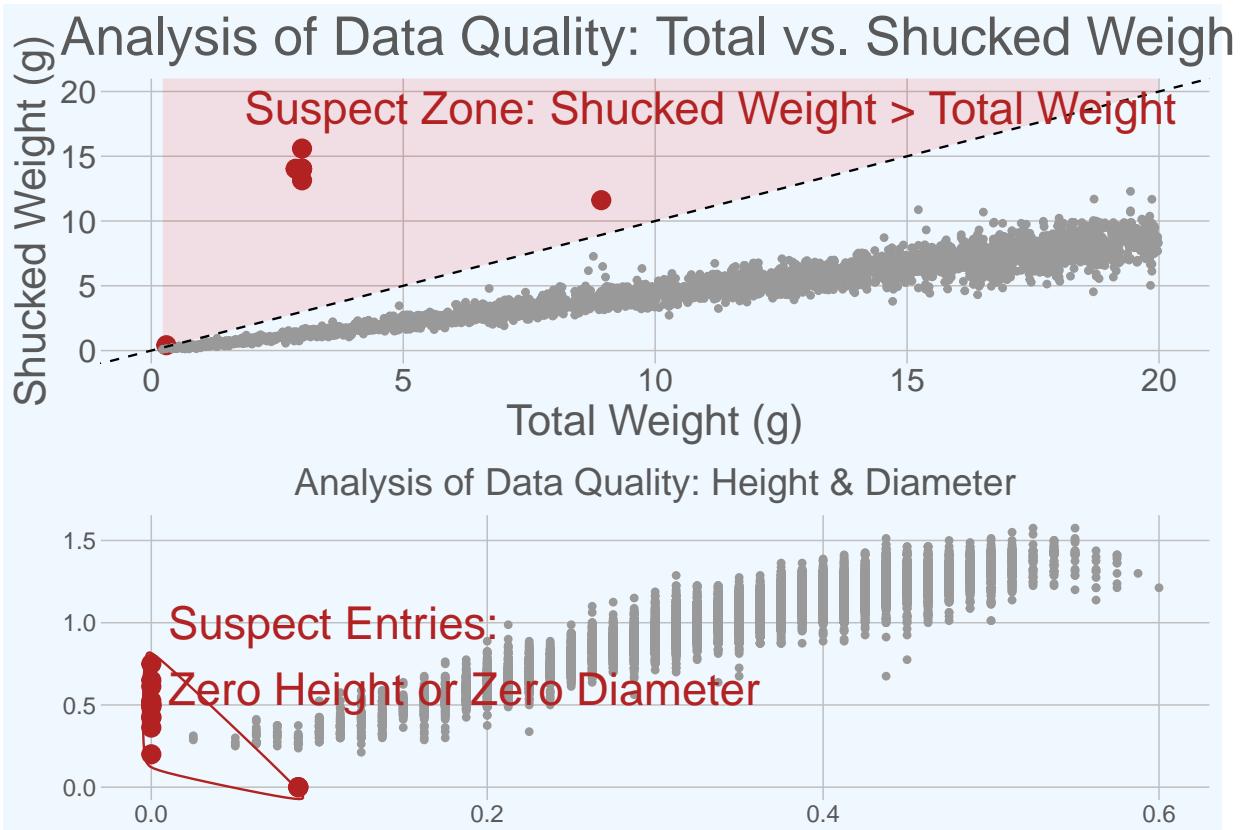
## Warning: Removed 8718 rows containing missing values or values outside the scale range
## (`geom_ribbon()`).

```

```

## Warning: Removed 8718 rows containing missing values or values outside the scale range
## (`geom_point()`).

```



## CHECK FOR CORRELATIONS

This code yields a correlogram for all numeric features.

All features are strongly correlated with one another, and only moderately correlated with Age. This signals difficulties in producing an accurate predictive model.

```
abalone.corr <- round(
  cor(abalone[,c(Features$Size, Features$Mass, Features$Target)]),
  1
)

abalone.corr %>%
  ggcorrplot(
    type = "lower",
    hc.order = TRUE,
    lab = TRUE,
    lab_size = 6,
    method = "circle",
    colors = c("tomato2", "white", "springgreen3"),
    title = "Correlogram of Abalone Features",
    ggtheme = theme_excel_new
  ) +
  scale_size(range = c(0, 20)) + # << enlarge circles
  theme(
```

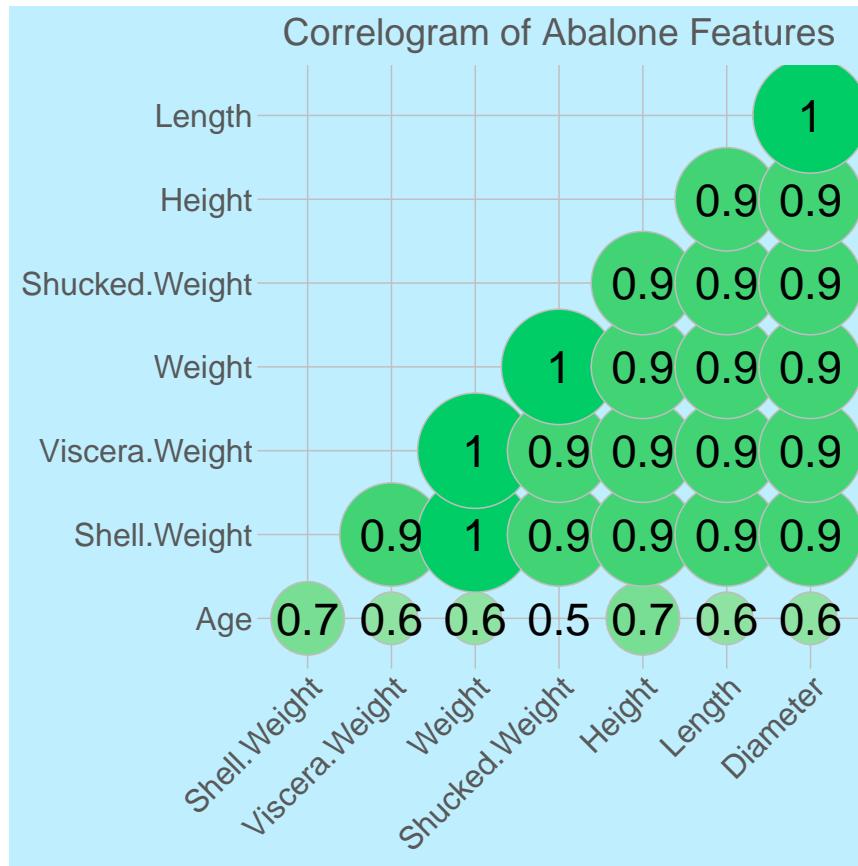
```

    legend.position = "none",
    plot.background  = element_rect(fill = "lightblue1", color = NA),
    panel.background = element_rect(fill = "lightblue1", color = NA)
  )

## Warning: `aes_string()`' was deprecated in ggplot2 3.0.0.
## i Please use tidy evaluation idioms with `aes()`'.
## i See also `vignette("ggplot2-in-packages")`' for more information.
## i The deprecated feature was likely used in the ggcrrplot package.
##   Please report the issue at <https://github.com/kassambara/ggcrrplot/issues>.
## This warning is displayed once every 8 hours.
## Call `lifecycle::last_lifecycle_warnings()` to see where this warning was
## generated.

## Scale for size is already present.
## Adding another scale for size, which will replace the existing scale.

```



## CHECK SIZE AND WEIGHT DISTRIBUTION

Looking at size, the lowest value is high, indicating flatness. Diameter and Length are closer, with most abalone being slightly elongated.

Looking at weight, the the highest mass part is the meat, followed by the shell, and then the viscera.

```

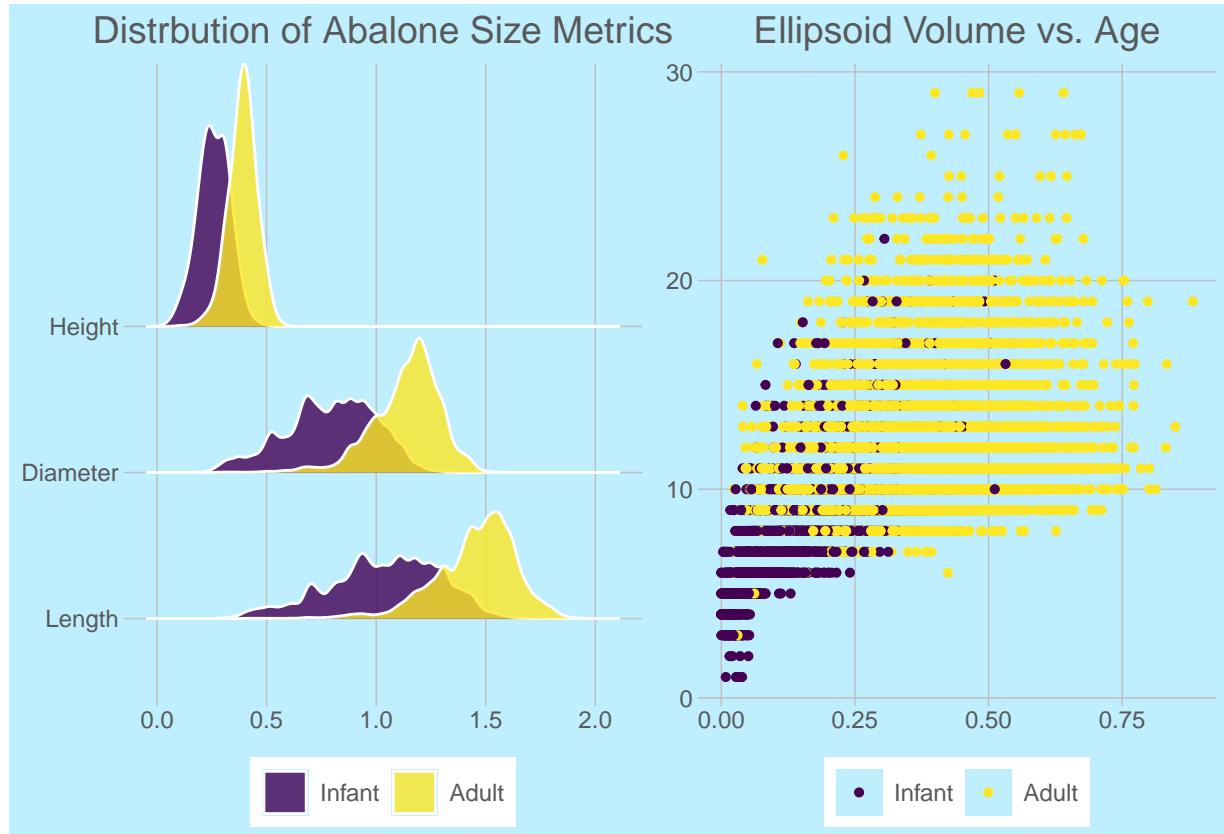
p1 <- abalone %>%
  ggplot(aes(x = Volume, y = Age, color = IsAdult)) +
  geom_point() +
  labs(
    title = "Ellipsoid Volume vs. Age",
    x = expression("Ellipsoid Volume (cm"^{3*})"),
    color = NULL
  ) +
  theme_excel_new() +
  theme(
    plot.background = element_rect(fill = "lightblue1", color = NA),
    panel.background = element_rect(fill = "lightblue1", color = NA)
  )

p2 <- abalone %>%
  pivot_longer(
    cols = c(Height, Diameter, Length),
    names_to = "Measure",
    values_to = "Value"
  ) %>%
  mutate(
    Measure = factor(Measure, levels = c("Length", "Diameter", "Height"))
  ) %>%
  ggplot(aes(x = Value, y = Measure, fill = IsAdult)) +
  geom_density_ridges(alpha = 0.8, color = "white") +
  theme_excel_new() +
  labs (
    title = "Distribution of Abalone Size Metrics",
    y = "Metric",
    x = "Size (cm)",
    color = NULL
  ) +
  theme(
    plot.background = element_rect(fill = "lightblue1", color = NA),
    panel.background = element_rect(fill = "lightblue1", color = NA)
  )

p2 + p1

## Picking joint bandwidth of 0.0232

```



```
p1 <- abalone %>%
  ggplot(aes(x = Weight, y = Age, color = IsAdult)) +
  geom_point() +
  labs(
    title = "Total Weight vs. Age",
    x = "Weight (grams)",
    color = NULL
  ) +
  theme_excel_new() +
  theme(
    plot.background = element_rect(fill = "lightblue1", color = NA),
    panel.background = element_rect(fill = "lightblue1", color = NA)
  )

p2 <- abalone %>%
  pivot_longer(
    cols = c(Shucked.Weight, Shell.Weight, Viscera.Weight),
    names_to = "Part",
    values_to = "Value"
  ) %>%
  mutate(
    Part = factor(
      case_when(
        Part == "Shucked.Weight" ~ "Meat",
        Part == "Shell.Weight" ~ "Shell",
        Part == "Viscera.Weight" ~ "Viscera"
      )
    )
  )
```

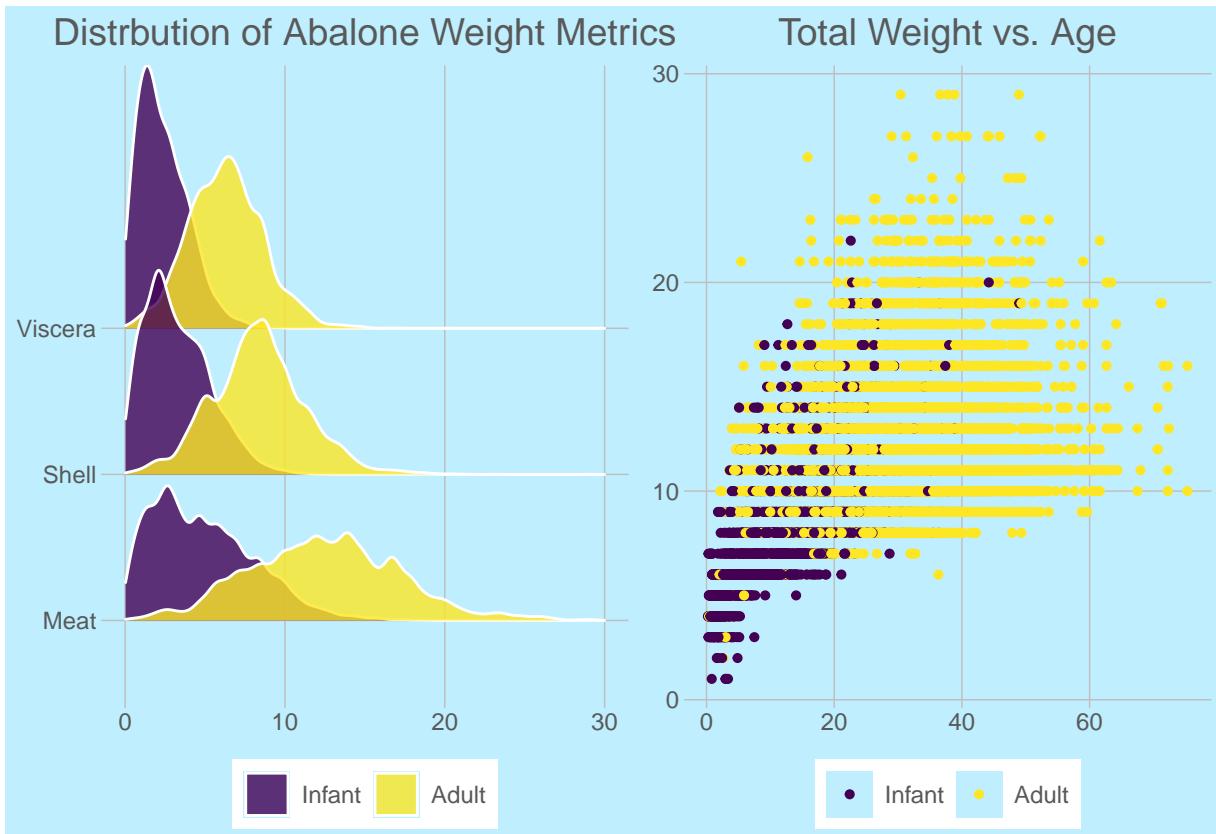
```

    ), levels = c("Meat", "Shell", "Viscera"))
) %>%
ggplot(aes(x = Value, y = Part, fill = IsAdult)) +
geom_density_ridges(alpha = 0.8, color = "white") +
theme_excel_new() +
labs (
  title = "Distrbution of Abalone Weight Metrics",
  x = "Weight (grams)",
  color = NULL
) +
scale_x_continuous(limits = c(0, 30)) +
theme(
  plot.background = element_rect(fill = "lightblue1", color = NA),
  panel.background = element_rect(fill = "lightblue1", color = NA)
)
p2 + p1

## Picking joint bandwidth of 0.416

## Warning: Removed 36 rows containing non-finite outside the scale range
## ('stat_density_ridges()').

```



## ANALYSIS OF RESIDUALS

Use residuals to probe the interaction between different variables and Age.

This pair of plots show that as abalone age past 10 years olds, the relative proportion of meat weight tends to decrease, and shell tends to increase.

```

analyze_residuals <- function(formula, data, ... ){

  fit <- lm(formula, data = data)
  data <- data %>%
    mutate(
      residual = resid(fit)
    )

  # get x-range for shading
  x_range <- range(data$Age, na.rm = TRUE)
  y_range <- range(data$residual, na.rm = TRUE)

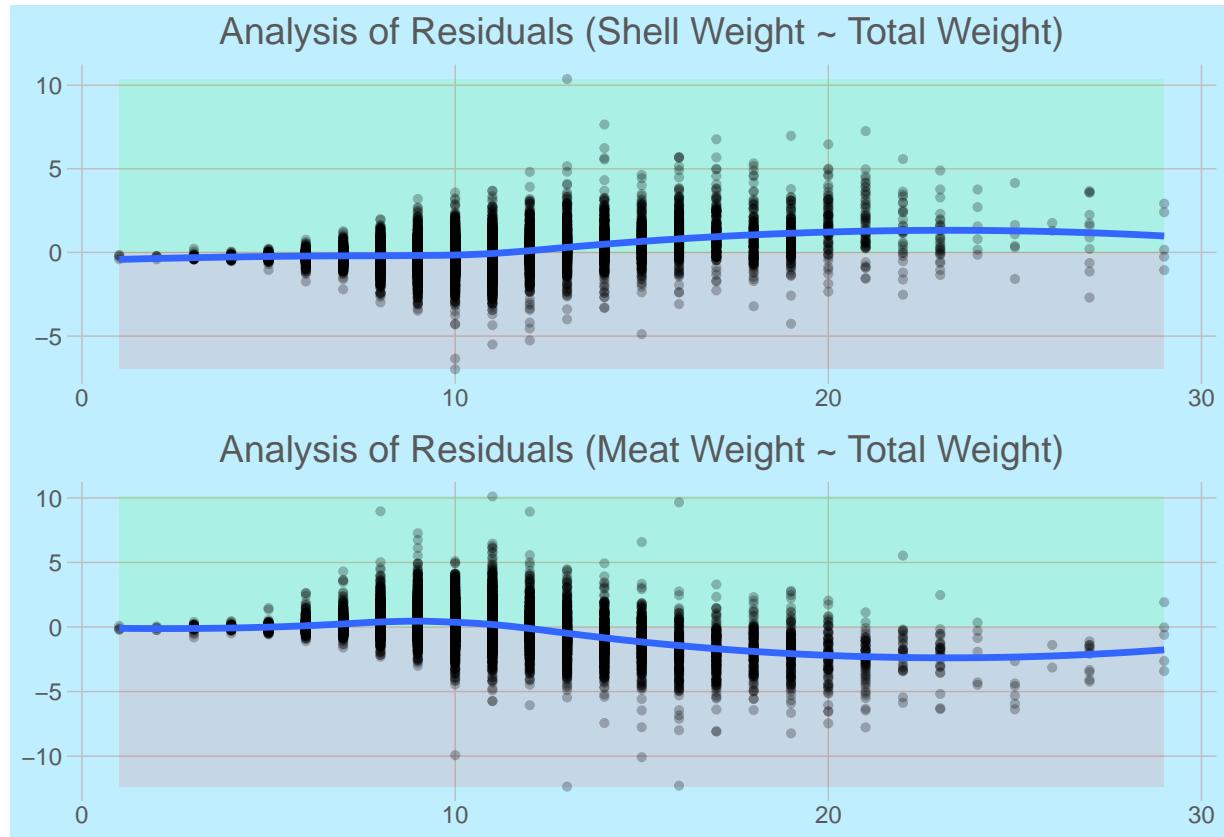
  ggplot(data, aes(x = Age, y = residual)) +
    # === background shading ===
    annotate("rect",
      xmin = x_range[1], xmax = x_range[2],
      ymin = 0, ymax = y_range[2],
      fill = "green", alpha = 0.1) +
    annotate("rect",
      xmin = x_range[1], xmax = x_range[2],
      ymin = y_range[1], ymax = 0,
      fill = "red", alpha = 0.1) +
    # points + smooth
    geom_point(alpha = 0.25) +
    geom_smooth(method = "loess", se = FALSE, linewidth = 1.2) +
    labs(...) +
    theme_excel_new() +
    theme(
      plot.background = element_rect(fill = "lightblue1", color = NA),
      panel.background = element_rect(fill = "lightblue1", color = NA)
    )
}

p1 <- analyze_residuals(
  Shell.Weight ~ Weight,
  abalone,
  title = "Analysis of Residuals (Shell Weight ~ Total Weight)",
  x = NULL,
  y = "Residual"
)

p2 <- analyze_residuals(
  Shucked.Weight ~ Weight,
  abalone,
  title = "Analysis of Residuals (Meat Weight ~ Total Weight)",
  x = "Age",
  y = "Residual"
)
```

p1/p2

```
## `geom_smooth()` using formula = 'y ~ x'  
## `geom_smooth()` using formula = 'y ~ x'
```



## MODEL ZOO

We prepare a series of models using all baseline features and various engineered features. The final results are saved to are displayed.

```
str(abalone)
```

```
## 'data.frame': 15000 obs. of 27 variables:  
## $ id : int 1 2 3 4 5 6 7 8 9 10 ...  
## $ Sex : Factor w/ 3 levels "Female","Infant",...: 3 3 1 3 2 3 3 2 2 1 ...  
## $ Diameter : num 1.025 0.975 1.375 1.062 0.887 ...  
## $ Length : num 1.31 1.23 1.74 1.38 1.16 ...  
## $ Height : num 0.312 0.338 0.5 0.338 0.3 ...  
## $ Weight : num 21 18.7 54.1 22.7 14 ...  
## $ Shucked.Weight: num 9.89 9.61 19.45 10.9 6.1 ...  
## $ Viscera.Weight: num 4.41 3.77 14.93 5.56 2.61 ...  
## $ Shell.Weight : num 5.06 4.69 14.22 6.42 3.97 ...  
## $ Age : int 8 8 11 9 8 14 11 6 5 20 ...  
## $ Volume : num 0.22 0.211 0.625 0.258 0.162 ...  
## $ IsAdult : Ord.factor w/ 2 levels "Infant"><"Adult": 2 2 2 2 1 2 2 1 1 2 ...
```

```

## $ Weight.Mean1 : num 6.04 5.54 16.04 7.3 3.98 ...
## $ Weight.Mean2 : num 8.25 7.51 21.73 9.69 5.46 ...
## $ Weight.Norm1 : num 11.96 11.34 28.34 13.82 7.73 ...
## $ Weight.Norm2 : num 24.1 21.9 61 26.5 16 ...
## $ Size.Norm : num 1.69 1.6 2.27 1.77 1.49 ...
## $ Size.Mean : num 1.38 1.36 1.53 1.41 1.33 ...
## $ Shell.Ratio : num 0.241 0.251 0.263 0.283 0.283 ...
## $ Meat.Ratio : num 0.472 0.514 0.36 0.481 0.434 ...
## $ Viscera.Ratio : num 0.21 0.202 0.276 0.245 0.186 ...
## $ Soft.Ratio : num 0.682 0.715 0.636 0.726 0.62 ...
## $ Elongation : num 1.28 1.26 1.26 1.29 1.31 ...
## $ Flatness : num 0.269 0.309 0.323 0.279 0.295 ...
## $ SurfaceArea : num 2.08 1.94 3.95 2.28 1.65 ...
## $ Roundness : num 0.781 0.796 0.791 0.773 0.763 ...
## $ Density : num 0.0105 0.0113 0.0116 0.0114 0.0115 ...

formulas <- list(
  baseline = Age ~ Sex + Diameter + Length + Height + Weight + Shucked.Weight + Viscera.Weight + Shell.
)

formulas$Weight.Mean1 <- update(formulas$baseline, . ~ . + Weight.Mean1)
formulas$Weight.Mean2 <- update(formulas$baseline, . ~ . + Weight.Mean2)
formulas$Weight.Norm1 <- update(formulas$baseline, . ~ . + Weight.Norm1)
formulas$Weight.Norm2 <- update(formulas$baseline, . ~ . + Weight.Norm2)
formulas$Size.Norm <- update(formulas$baseline, . ~ . + Size.Norm)
formulas$Size.Mean <- update(formulas$baseline, . ~ . + Size.Mean)
formulas$Volume <- update(formulas$baseline, . ~ . + Volume)
formulas$Shell.Ratio <- update(formulas$baseline, . ~ . + Shell.Ratio)
formulas$Meat.Ratio <- update(formulas$baseline, . ~ . + Meat.Ratio)
formulas$Viscera.Ratio <- update(formulas$baseline, . ~ . + Viscera.Ratio)
formulas$Soft.Ratio <- update(formulas$baseline, . ~ . + Soft.Ratio)
formulas$Elongation <- update(formulas$baseline, . ~ . + Elongation)
formulas$Flatness <- update(formulas$baseline, . ~ . + Flatness)
formulas$SurfaceArea <- update(formulas$baseline, . ~ . + SurfaceArea)
formulas$Roundness <- update(formulas$baseline, . ~ . + Roundness)
formulas$Density <- update(formulas$baseline, . ~ . + Density)
formulas$Final1 <- update(formulas$baseline, . ~ . + Soft.Ratio + Weight.Norm1 + Size.Norm)
formulas$Final2 <- update(formulas$baseline, . ~ . + Weight.Norm2 + Volume + SurfaceArea)

results <- eval_circuit(formulas, abalone, excel_path = "results.xlsx")

```

```
## Results written to: results.xlsx
```

```
results %>% select(formula_name, model, mae)
```

```

##   formula_name model      mae
## 1      Soft.Ratio rf 1.389615
## 2      Final1    rf 1.391122
## 3      Meat.Ratio rf 1.394211

```

```
## 4  Weight.Norm2    rf 1.397993
## 5      Density     rf 1.398905
## 6      Final2      lm 1.398992
## 7      baseline    rf 1.401185
## 8      Roundness   rf 1.401832
## 9  Weight.Norm1   rf 1.402184
## 10     Size.Norm   rf 1.402738
## 11  Weight.Mean1  rf 1.403388
## 12     Elongation  rf 1.403637
## 13  Weight.Mean2  rf 1.404464
## 14     Size.Mean   rf 1.404672
## 15     Final2      rf 1.404745
## 16 Viscera.Ratio  rf 1.404828
## 17     Volume      rf 1.405200
## 18 SurfaceArea    rf 1.406294
## 19  Weight.Norm2  lm 1.406612
## 20     Flatness    rf 1.407100
## 21  Shell.Ratio   rf 1.408511
## 22  Weight.Mean2  lm 1.412326
## 23  Weight.Mean1  lm 1.412638
## 24  Weight.Norm1  lm 1.412816
## 25     Final1     lm 1.416033
## 26     Volume      lm 1.426365
## 27 SurfaceArea    lm 1.427834
## 28     Density     lm 1.432653
## 29     Size.Mean   lm 1.433627
## 30     Roundness   lm 1.438515
## 31     Size.Norm   lm 1.438854
## 32     Elongation  lm 1.439078
## 33 Viscera.Ratio  lm 1.439547
## 34     baseline    lm 1.439702
## 35  Shell.Ratio   lm 1.440525
## 36     Flatness    lm 1.440973
## 37  Soft.Ratio    lm 1.441989
## 38  Meat.Ratio    lm 1.443234
```