The hat imphis a

I grantum mechanical

operator, the operator

can be a vector as well, having 3 component

Consider impaired electrons non-interacting electrons. Each of them has spin 1/2, and an associated magnetic

moment:  $\frac{\Lambda}{M} = -\frac{9}{MB} \frac{3}{4}$ 

 $M_B = \frac{e \pi}{2m} = 5.79 \times 10^4 \text{ eVT}^{-1} \left( \frac{B \delta h r}{magneton} \right)$ 

 $\hat{\vec{S}} = \frac{1}{2} \hat{\vec{\sigma}}$  where  $\hat{\vec{\sigma}} = (\hat{\sigma}_{x}, \hat{\sigma}_{y}, \hat{\sigma}_{z})$ 

g; Landi g-factor

wide If the particles were nuclean, then the corresponding in is called muchar magneton, and 3 would be replaced by nuclear isospin. The corresponding phenomenon is: Nuclear magnetic resonance (NMR)

Gutting back to the electronic system, the Hamiltonian for such system in a magnetic field is given by:

 $\hat{\chi} = -\vec{M}.\vec{B} = -g M_B + \vec{S}.\vec{B}$ 

i.e., the interaction between the magnetic moments in the magnetic field gives rise to an energy!

 $U = -M.B = (g_{MB} m_s B), m_s = \pm 1/2 \text{ for oheten's spin a$ 

elictron's spin gtm.

So far we considered only the spin to contribute to electron's angular momentum. In general, electron can have orbital angular momentum as well, so that, the total angular

momentum is:  $\hat{J} = \hat{1} + \hat{3}$ , with eigenvalues

"I" that goes from (l-5) to (l+5)
(consult qtm. mech. book.)

expression for Landé g-Jactor is: The general  $+\frac{j(j+1)+s(s+1)-l(l+1)}{2j(j+1)}$ a ratue 2 for l=0 (so that j=8). magnetic field is Let us assume, for now, that the pointing to 2-direction, so that: H = - 9 MB 1 S 2 B Consider, an atom that carries such impaired, non-interactly "spins" as electrons. Let this have let the Ground State be identified by m= 1/2 and sok excited state by m=3/2. Then, only a single transition can be induced by absorbtion of can be induced by absorption of m=3/2 and the absence M=3/2 and M=3/2 a El M=1/2 TESR Because the energy of the electronic

State does not depend on the spin

angular momentum, the GS is doubly

GS. degenerate, corresponding to ms = ± 1/2 of & Sz, and the excited state is quadruply degenerate corresponding to ms = +3/2,+1/2,-1/2,-3/2 & 52. The magnetic field breaks such digeneracy by sphittily the GES in 2-sublevels & the ES to 4-sublevels, called Zeeman Sphity Now, instead of a single transition with freq. W= (E2-E1)/t, several transitions with frequency close to w are possible (See Fig.). This is Beenan Effect.

Because ESR involves transitions only between sublevels of one (original) electronic level, we do not need to consider the detailed Hamiltonian for the atom / molecule, or even the pasts that gives rise to the electronic levels, but consider only the terms of the Hamiltonian that general the sublevels and transitions between them.

Because our real system & (DPPH) has just on impaired electron,  $\mathcal{H}_0 = -g \, \mu_B \, \frac{B}{\hbar} \, \hat{S}_z$ 

We then turn on an additional AC magnetic field of frequency w, in a direction perpendicular to B. (here Bz). Hence this new AC field lies in xy-plane.  $\hat{\mathcal{H}} = \hat{\mathcal{H}}_0 + \hat{\mathcal{D}} \hat{\mathcal{V}} \cos \omega t = 0$ 

When the new AC magnetic fld is weak (i.e. N is small compared to Ho [00 pl. understand the meaning of an sperator being smaller than another!]), we can treat it as perfurbable and obviously we have to use time-dependent pert. theory. The unperturbed states are  $|m_2\rangle$ , s.t.  $\hat{3}_2/m_2\rangle = \hbar m_s/m_2$ ,  $m_5 = \pm 1/2$  here, whose energies are:

g/B = 3 = 2 m = = Em |m2 | 1 8m = g/B = ms

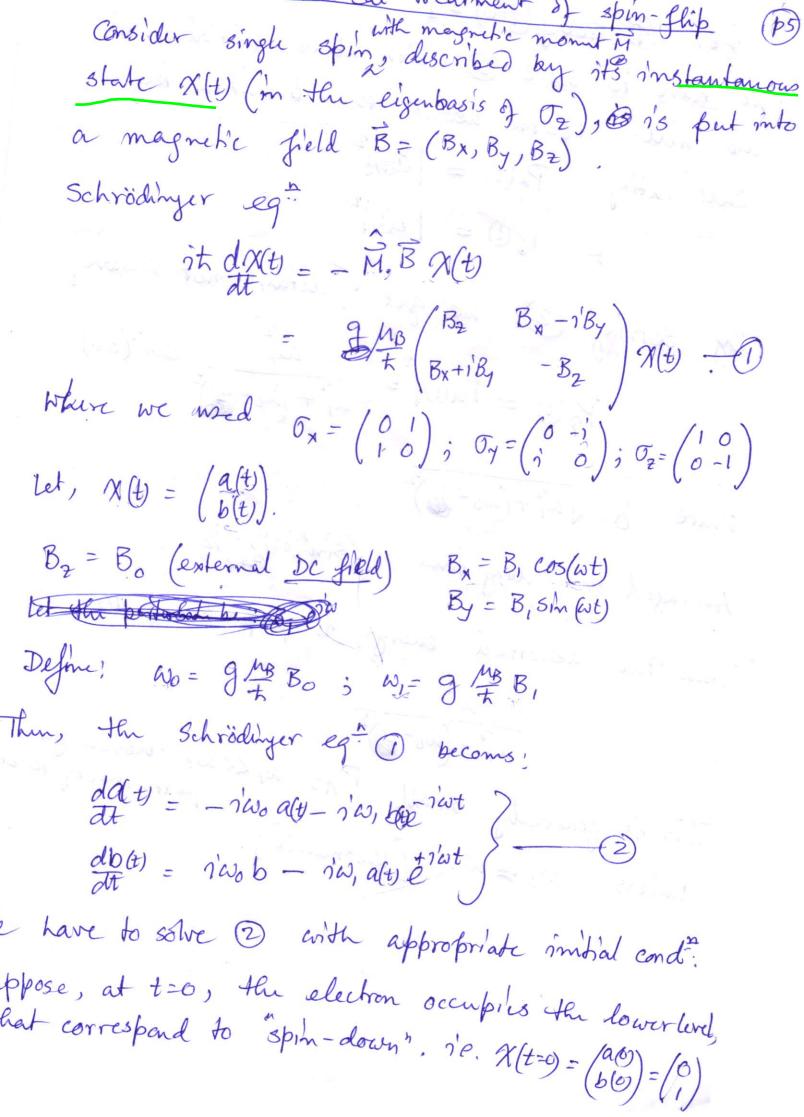
Note that VX Tx + or Ty rie. V Not or o

Which raises or lowers the spin of the unperturbed states and thereby causes

The transition rates are given by Fermi Golden W1+2 = 21 (2 | V | 1) 28 (82-8, - tw)

assumed &> E1

Also, the selection rule (that comes from the principle of conservation of angular momentue) ensures that the toams it an only occurs when Ams = #1 [This is of course guarranteed for our case, where only two two Zeeman levels are m'th  $m_s = \pm 1/2$ 



ie. P Prob. (t=0) = 1 We have to solve @ with above mittal condis and will learn about the trans. Hen by calculating Pr(t) = [alt] 2 P(t) = 16(t) 12 By solving 2 we get [details not shown]  $P_{\uparrow}(t) = |a(t)|^2 = \frac{\omega_1^2}{\omega_1^2 + (\omega_0 - \omega_0)^2} \sin^2(8t)$ where 8 =  $\sqrt{\omega_1^2 + (\omega_0 - \omega_0)^2}$ Averaged over long time (Sim (8t)) = 1/2 Thus the absorbed energy is proportional to  $\frac{\omega_1^2}{\omega_1^2 + (\omega_0 - \omega_0)^2}$ This is generally small [As w, << wo chosen for pert, theory to be value unless  $\omega_0 \approx \omega$ . [Resonance].

> Please verify the algebra! It might centain missed jactors)