```
sit315-001@sit315-001-VirtualBox:~$ time mpirun -np 4 --hostfile ~/hostfile ./mpi_matrix_multiply
Authorization required, but no authorization protocol specified
Result matrix (sample):
328350 323400 318450 313500 308550
333300 328250 323200 318150 313100
338250 333100 327950 322800 317650
343200 337950 332700 327450 322200
348150 342800 337450 332100 326750
real
        0m0.825s
        0m0.098s
user
        0m0.141s
```

Time

1. Sequential Version (sequential_matrix_multiply):

real: 0m0.007s user: 0m0.005s sys: 0m0.002s

2. MPI Version (mpi_matrix_multiply):

real: 0m0.825s user: 0m0.098s sys: 0m0.141s

Conclusion

Sequential Program: The sequential method is fast for small-scale operations due to minimal overhead. However, this method only uses a single CPU core and will not scale efficiently for larger matrices or more complex operations. Its real-time execution is the shortest, but it's limited to small data sizes and lacks scalability.

MPI Programs: MPI introduces parallelization by distributing tasks across multiple processes, but this comes at the cost of inter-process communication overhead. While it makes sense for distributed systems with large data sizes, the observed real-time execution is much higher than the sequential approach due to this overhead.

2.

```
sit315-001@sit315-001-VirtualBox:-$ time mpirun -np 4 --hostfile -/hostfile ./mpi_openmp_matrix_multiply
Authorization required, but no authorization protocol specified
Result matrix (sample):
328350 323400 318450 313500 308550
333300 328250 323200 318150 313100
338250 333100 327950 322800 317650
343200 337950 332700 327450 322200
348150 342800 337450 332100 326750
real
       0m0.817s
       0m0.124s
user
       0m0.136s
```

Time

3. MPI + OpenMP Version (mpi_openmp_matrix_multiply):

real: 0m0.817s user: 0m0.124s sys: 0m0.136s

Conclusion

MPI + OpenMP Program: Adds multi-threading but provides minimal additional benefit for small-scale tasks. The overhead from both MPI communication and thread management limits its effectiveness at small sizes, making it no better than MPI alone for smaller problems.

3.

Time

real: 0m0.101s user: 0m0.051s sys: 0m0.046s

Conclusion

OpenCL Program: OpenCL shows a dramatic reduction in execution time compared to the other methods. Leveraging GPU acceleration for parallel computation of matrix elements results in a significant performance gain. The real-time execution is the lowest of all methods, highlighting OpenCL's suitability for matrix operations where the workload can be parallelized efficiently across a large number of GPU threads.