

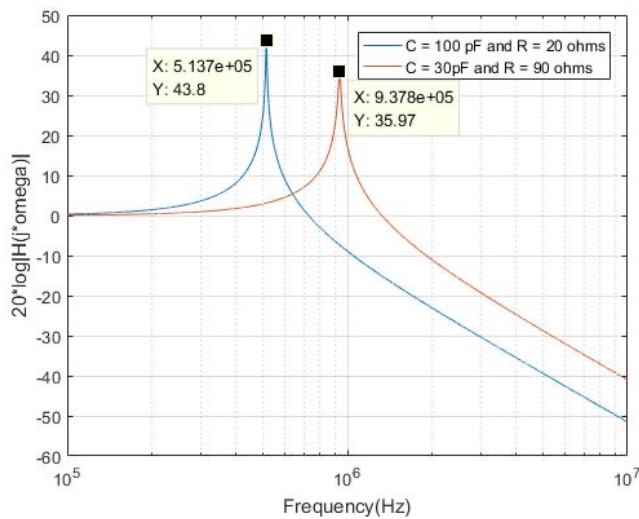
$$1. (a). H(j\omega) = \frac{V_{out}(j\omega)}{V_{in}(j\omega)} = \frac{\frac{1}{j\omega C}}{R_{int} + \frac{1}{j\omega C} + j\omega L} = \frac{\frac{1}{sC}}{R + \frac{1}{sC} + sL} = \frac{1}{LCs^2 + RCs + 1}$$

(b). Values from plot:

|            | Peak freq. (kHz) | 3dB BW (kHz) | Quality Factor |
|------------|------------------|--------------|----------------|
| C = 100 pF | 513.7            | 3.3          | 155.7          |
| C = 30 pF  | 937.8            | 14.9         | 62.9           |

Values from equations:

|            | Peak freq. (kHz) | 3dB BW (kHz) | Quality Factor |
|------------|------------------|--------------|----------------|
| C = 100 pF | 513.67           | 3.32         | 154.92         |
| C = 30 pF  | 937.83           | 14.92        | 62.85          |



$$2. (a). \begin{cases} \frac{V_A - V_i}{R_1} + \frac{V_A}{R_2} + \frac{V_A - V_o}{\frac{1}{j\omega C}} + \frac{V_A - 0}{\frac{1}{j\omega C}} = 0 \\ \frac{0 - V_A}{\frac{1}{j\omega C}} + \frac{0 - V_o}{R_3} = 0 \end{cases}$$

$$H(j\omega) = \frac{V_o}{V_i} = \frac{-\frac{R_2 R_3 C}{R_1 + R_2} j\omega}{\frac{R_1 R_2 R_3}{R_1 + R_2} C^2 (j\omega)^2 + \frac{2R_1 R_2}{R_1 + R_2} C j\omega + 1} = \frac{-\frac{R_2 R_3 C}{R_1 + R_2} s}{\frac{R_1 R_2 R_3 C^2}{R_1 + R_2} s^2 + \frac{2R_1 R_2 C}{R_1 + R_2} s + 1}$$

$$\text{Therefore } \begin{cases} a_2 = \frac{R_1 R_2 R_3 C^2}{R_1 + R_2} \\ a_3 = \frac{2R_1 R_2 C}{R_1 + R_2} \end{cases}$$

With the specified resistors and capacitors, we have

$$\begin{cases} a_1 = -1.61 \times 10^{-6} \\ a_2 = 2.41 \times 10^{-12} \\ a_3 = 3.21 \times 10^{-7} \end{cases}$$

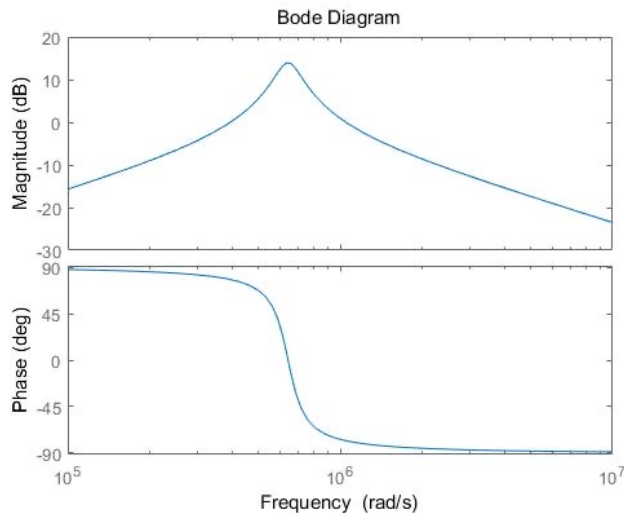
$$(b). H(j\omega) = \frac{a_1 s}{a_2 s^2 + a_3 s + a_4} = \frac{\frac{a_1}{a_2} s}{s^2 + \frac{a_3}{a_2} s + \frac{a_4}{a_2}}$$

$$\omega_o = \sqrt{\frac{a_4}{a_2}} = \sqrt{\frac{R_1 + R_2}{R_1 R_2 R_3 C^2}} = 6.44 \times 10^5 \text{ rad/s} \Rightarrow 102.5 \text{ kHz}$$

$$\beta = \frac{a_3}{a_1} = \frac{2}{R_3 C} = 1.33 \times 10^5 \text{ rad/s} \Rightarrow 21.2 \text{ kHz}$$

$$H_o = \frac{a_1}{a_3} = -\frac{R_2}{2R_1} = 5 = 13.98 \text{ dB}$$

(C).



From plot, we have

$$a_3 = 3.21 \times 10^7$$

$$\omega_o = 6.37 \times 10^5 \text{ rad/s}$$

$$\Rightarrow 101.4 \text{ kHz}$$

$$H_o = 13.9 \text{ dB}$$

Therefore, the approximation is quite good.

3.

| $f_c$ (kHz) | $f_{LO1}$ (kHz) | $f_{LO2}$ (kHz) | $f_{image1}$ (kHz) | $f_{image2}$ (kHz) |
|-------------|-----------------|-----------------|--------------------|--------------------|
| 1600        | 1500            | 1700            | 1400               | 1800               |
| 530         | 430             | 630             | 330                | 730                |

4.

