

VE281 Midterm Distribution

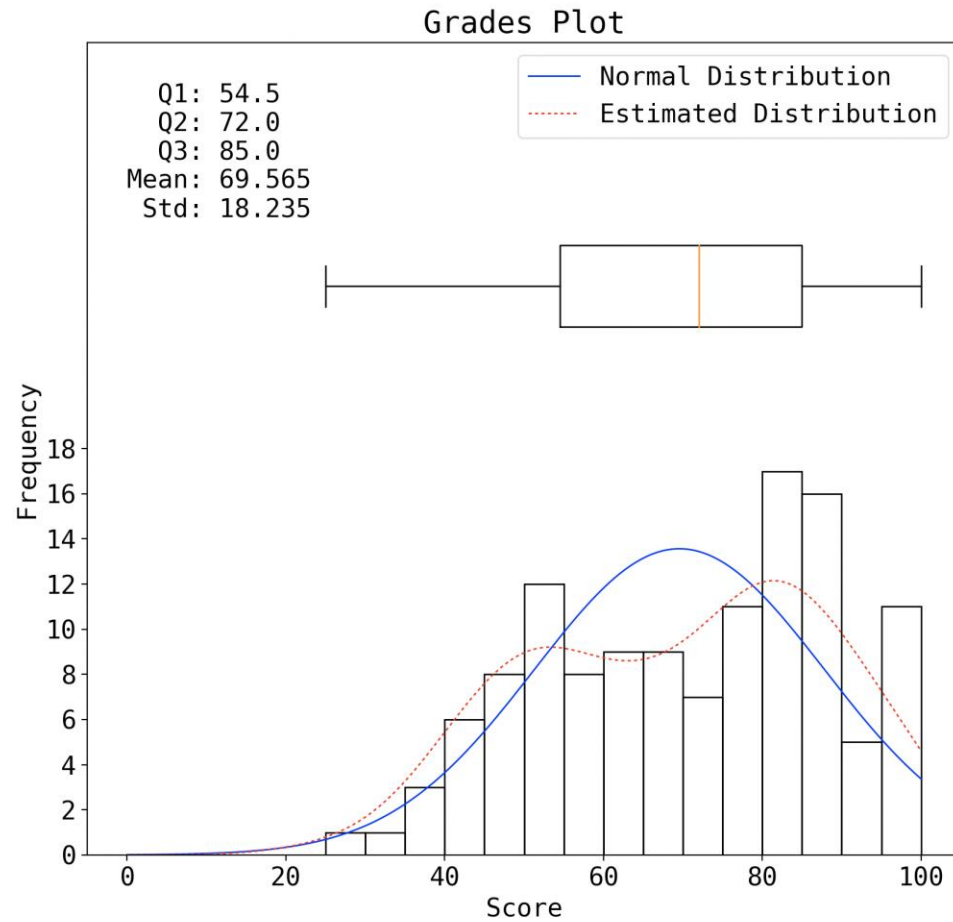
Biden Won Afterall

- How Similar to our Piazza Poll!
 - Trump was ahead but Biden had a comeback
- Don't give up too early!

A total of **80** vote(s) in **167** hours

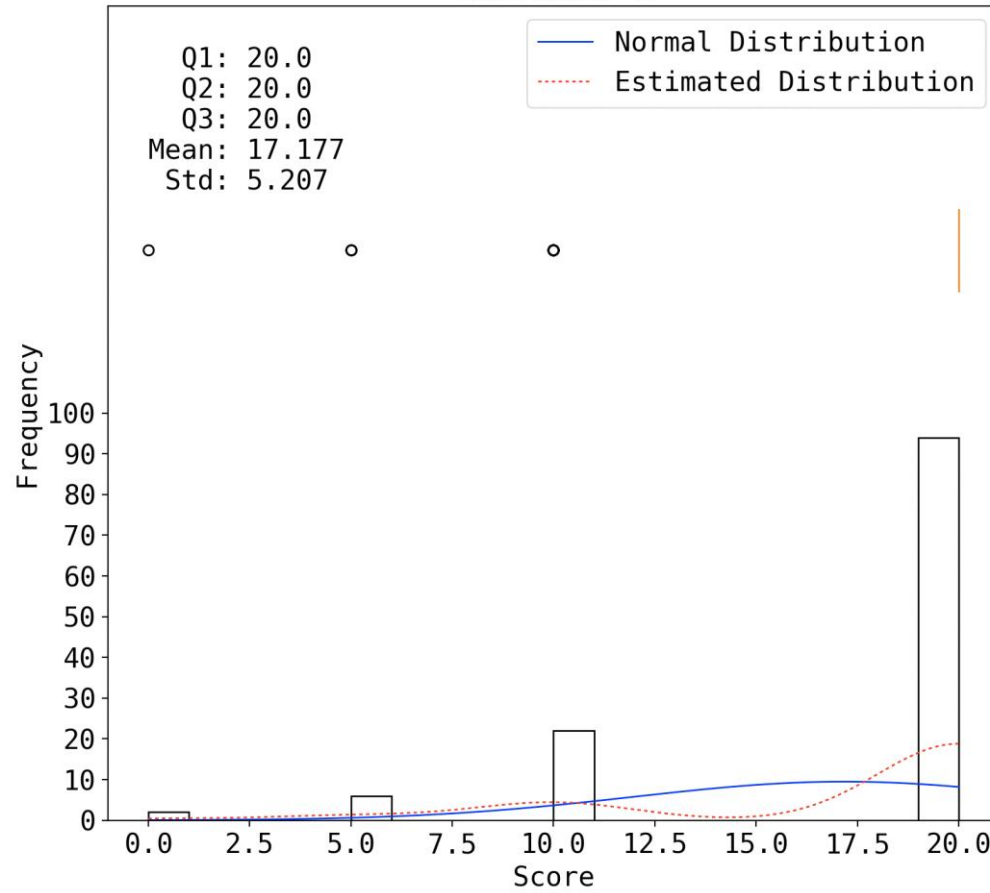


Overall Distribution



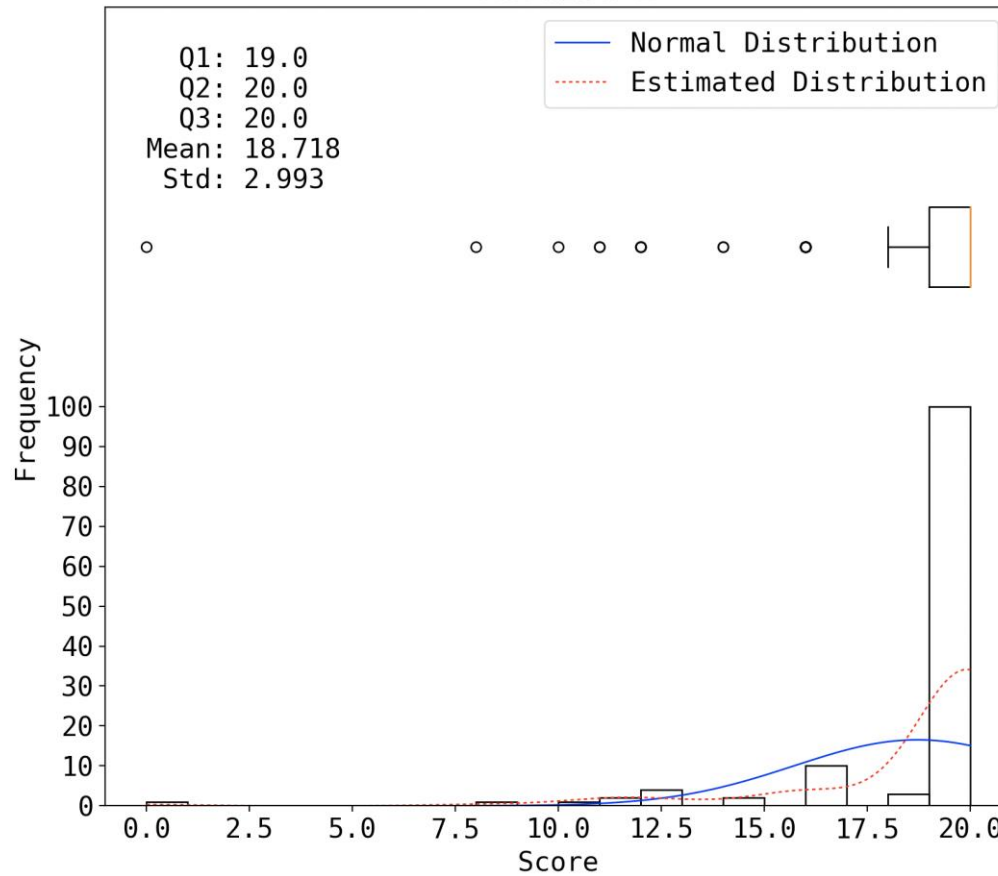
P1

Exercise 1



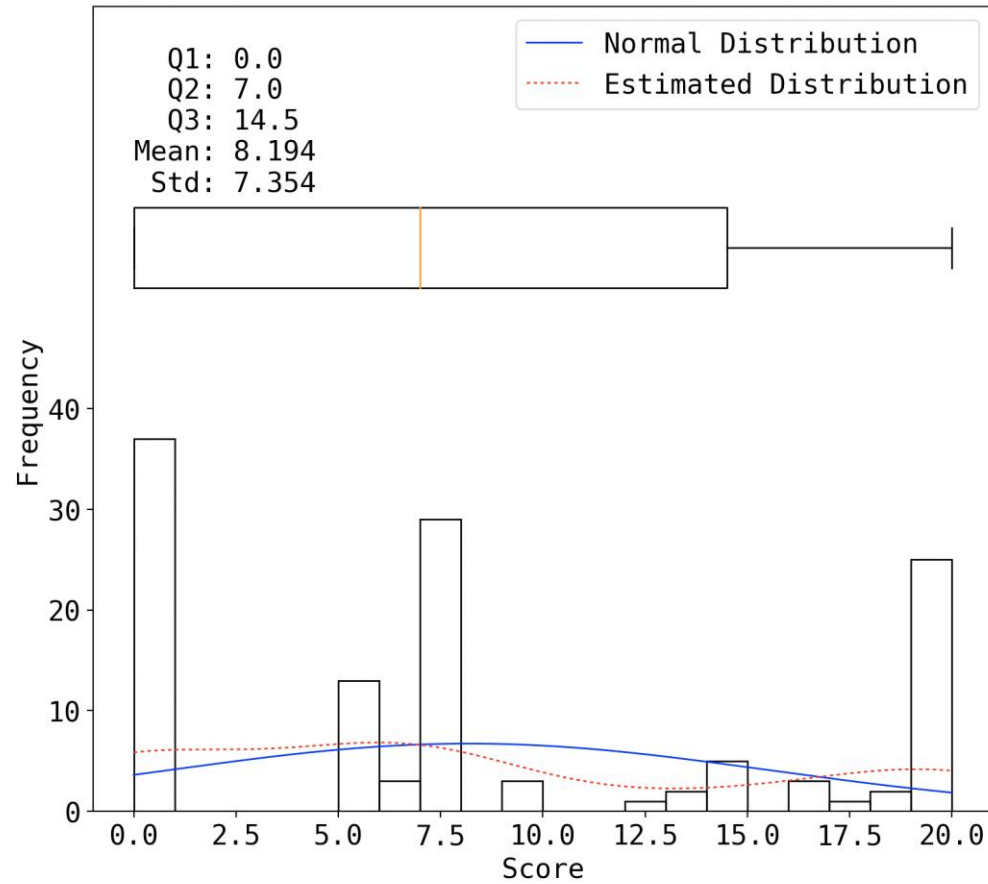
P2

Exercise 2



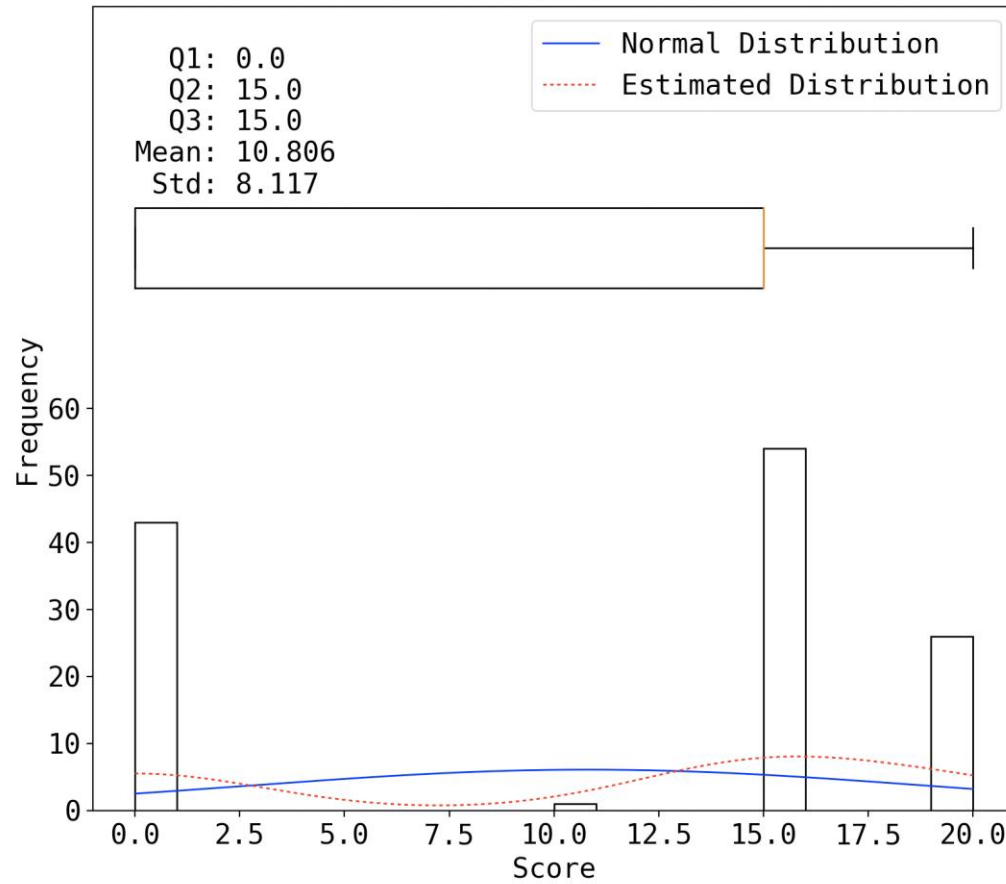
P3

Exercise 3



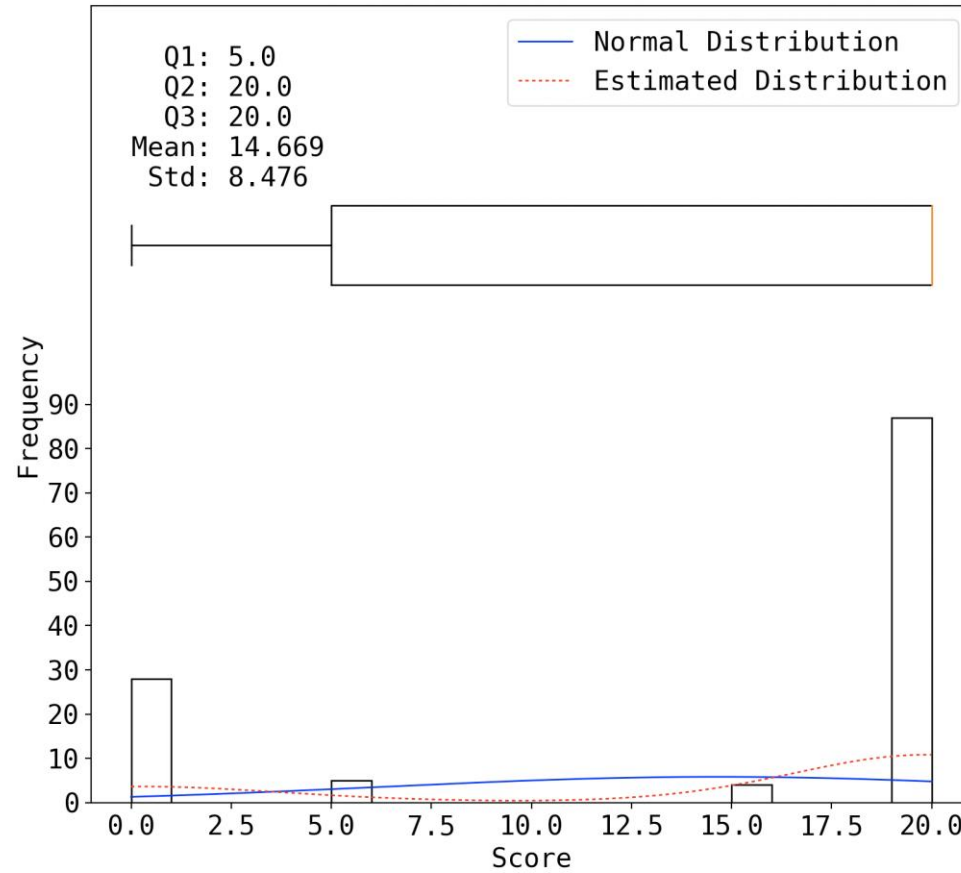
P4

Exercise 4



P5

Exercise 5

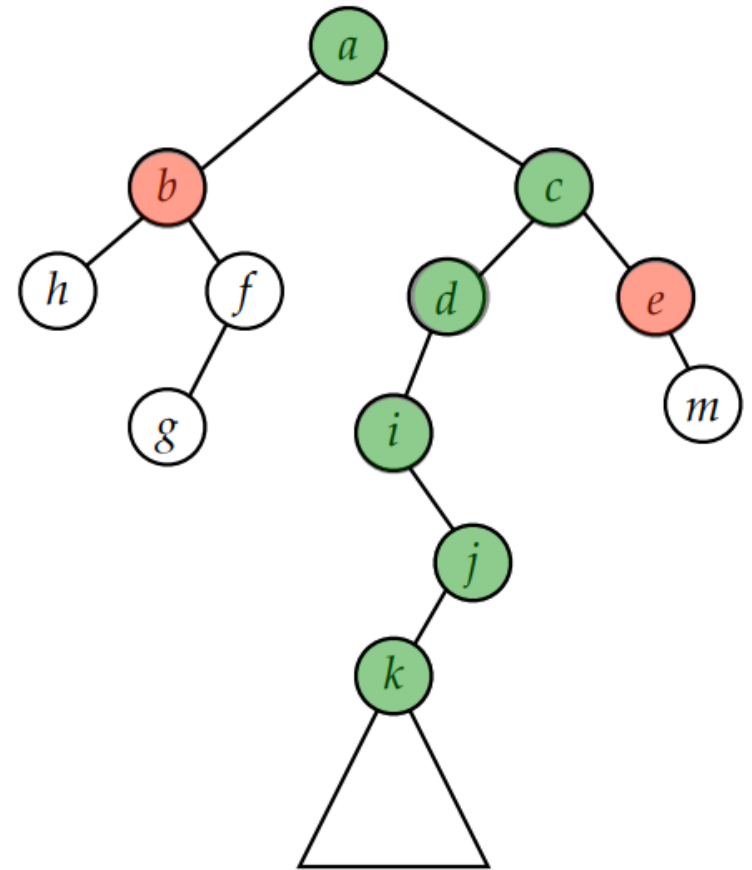
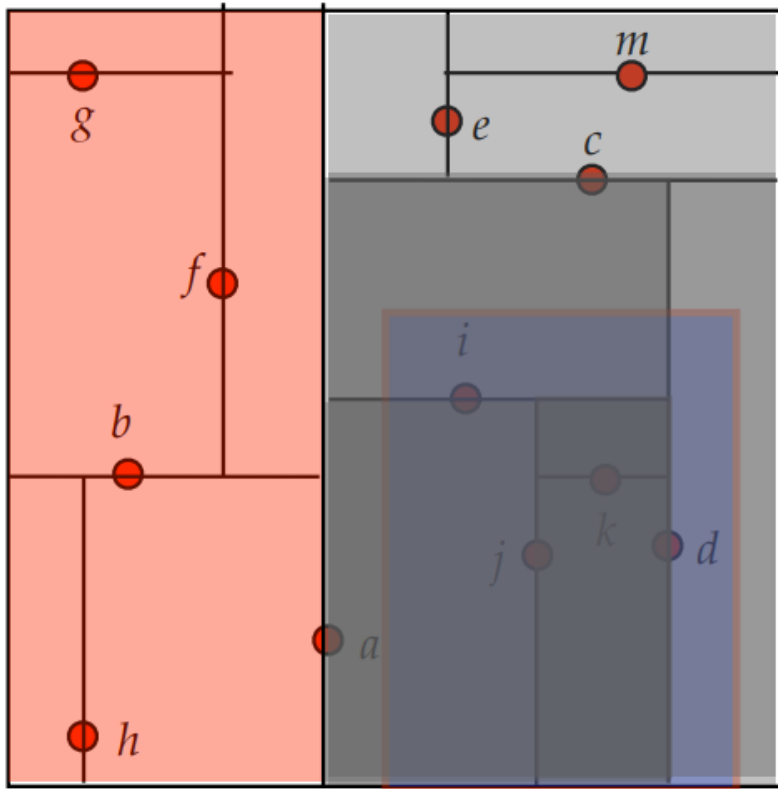


Regrading

- This Friday RC time
 - 8-10 PM
 - Location: JI Building, Room 326H

Ranged Search in K-d Tree

Range Searching Example



If query box doesn't overlap bounding box, stop recursion

If bounding box is a subset of query box, report all the points in current subtree

If bounding box overlaps query box, recurse left and right.

Range Query PseudoCode

```
def RangeQuery(Q, T):  
    if T == NULL: return empty_set()  
    if BB(T) doesn't overlap Query: return 0  
    if Query subset of BB(T): return AllNodesUnder(T)  
  
    set = empty_set()  
    if T.data in Query: set.union({T.data})  
  
    set.union(RangeQuery(Q, T.left))  
    set.union(RangeQuery(Q, T.right))  
  
    return set
```

VE281

Data Structures and Algorithms

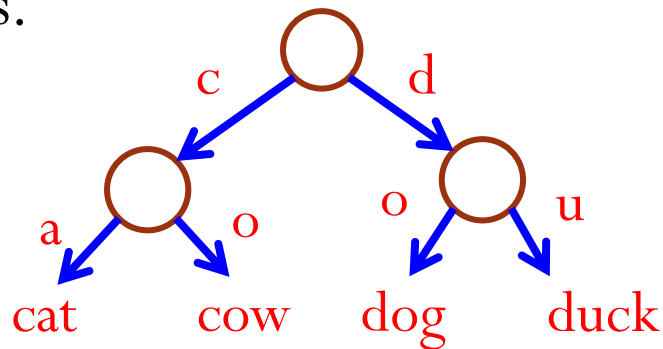
Tries

Learning Objectives:

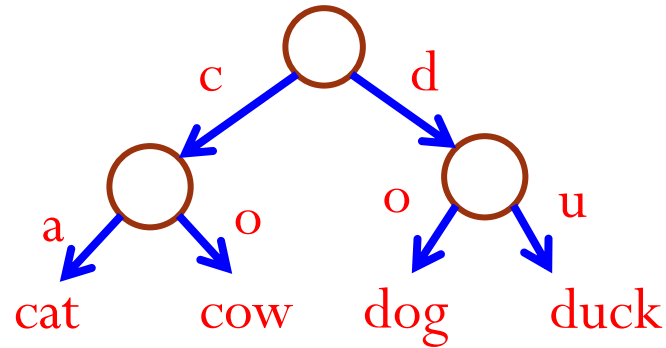
- Know what a trie is and understand its difference between binary search trees
- Know how to implement search, insertion, and removal for a trie

Trie

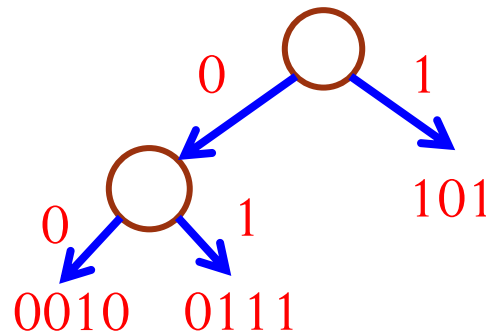
- The word “trie” comes from re**trie**val.
 - To distinguish with “tree”, it is pronounced as “try”.
- A trie is a tree that uses parts of the key, as opposed to the whole key, to perform search.
- Data records are only stored in **leaf** nodes. Internal nodes do not store records; they are “**branch**” points to direct the search process.



Trie

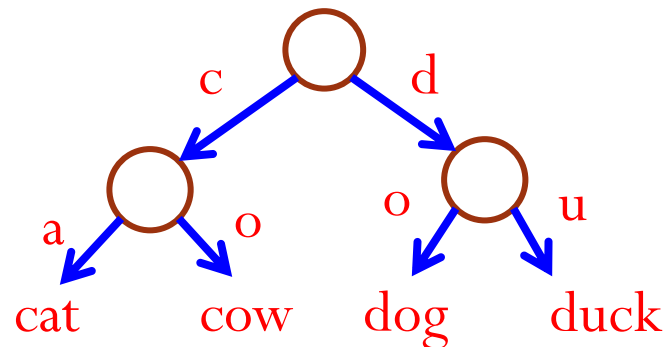


- Trie usually is used to store a set of strings from an **alphabet**.
 - The alphabet is in the general sense, not necessarily the English alphabet.
- For example, $\{0, 1\}$ is an alphabet for binary codes $\{0010, 0111, 101\}$. We can store these three codes using a trie.



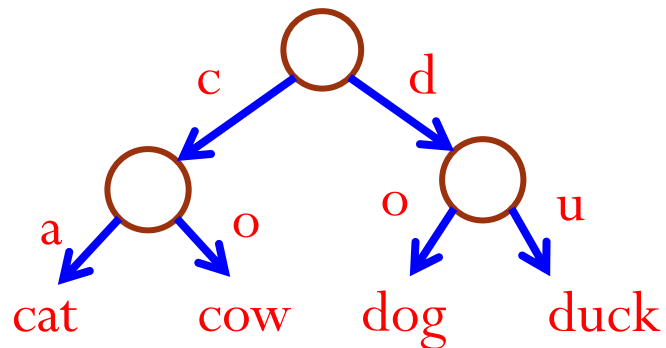
Trie

- Each edge of the trie is labeled with symbols from the alphabet.
- Labels of edges on the path from the root to any leaf in the trie forms a **prefix** of a string in that leaf.
 - Trie is also called **prefix-tree**.



Trie

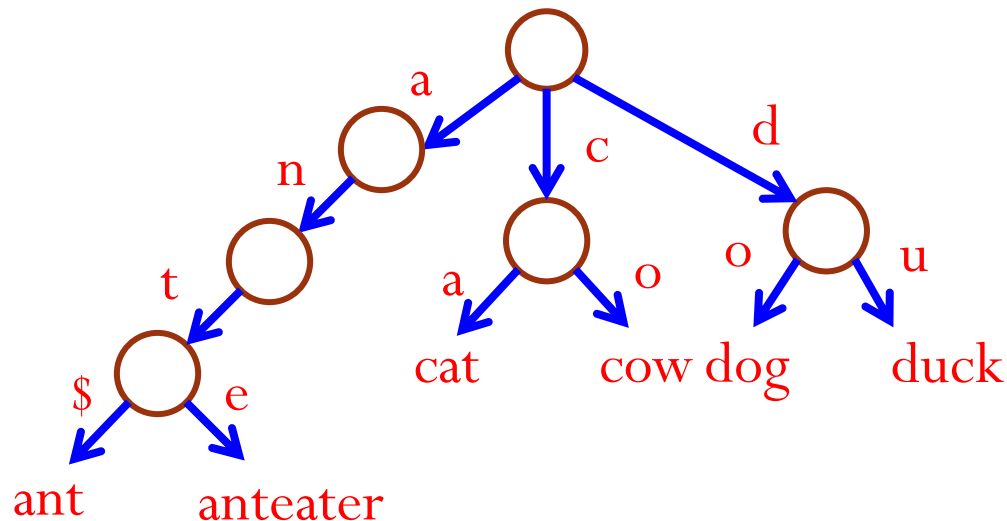
- The most significant symbol in a string determines the branch direction at the root.
- Each internal node is a “**branch**” point.
- As long as there is only one key in a branch, we do not need any further internal node below that branch; we can put the word directly as the leaf of that branch.



Trie

Implementation Issue

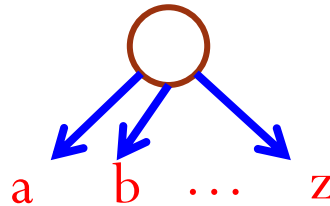
- Sometimes, a string in the set is exactly a **prefix** of another string.
 - For example, “ant” is a prefix of “anteater”.
 - How can we make “ant” as a leaf in the trie?
- We add a symbol to the alphabet to indicate the end of a string. For example, use “\$” to indicate the end.



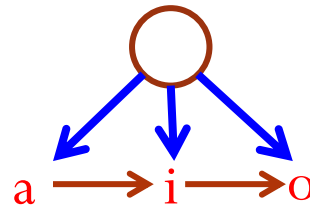
Trie

Implementation Issue

- We can keep an array of pointers in a node, which corresponds to **all** possible symbols in the alphabet.



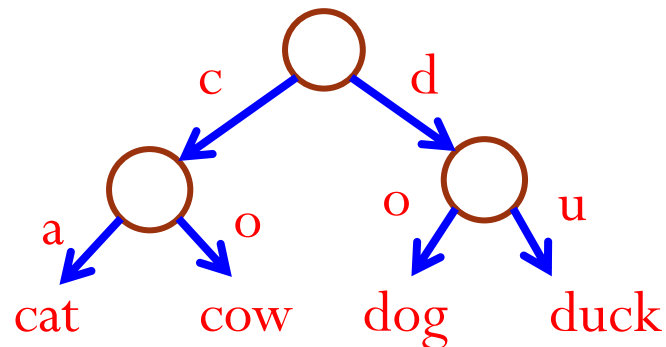
- However, most internal nodes have branches to only a small fraction of the possible symbols in the alphabet.
 - An alternate implementation is to store a linked list of pointers to the child nodes.



Trie

Search

- Follow the search path, starting from the root.
- When there is no branch, return false.
- When the search leads to a leaf, further compare with the key at the leaf.



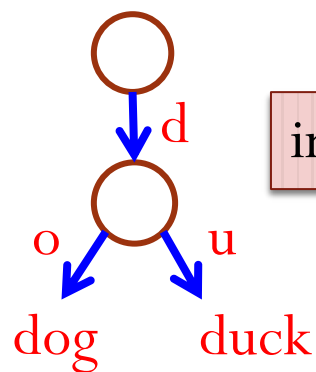
search “monkey”

search “cat”

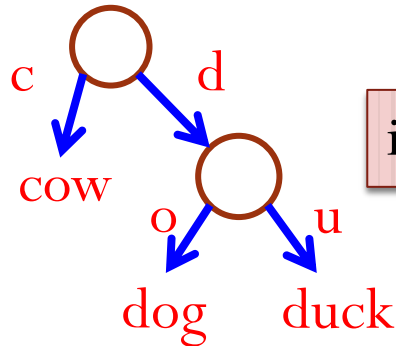
Trie

Insertion

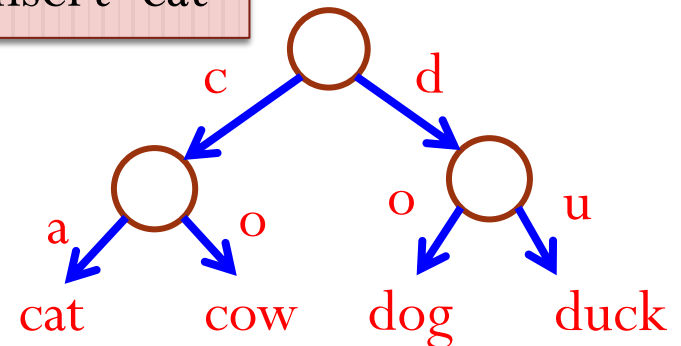
- Follow the search path, starting from the root.
- If a new branch is needed, add it.
- When the search leads to a leaf, a conflict occurs. We need to branch.
 - Use the next symbol in the key
 - The originally-unique word must be moved to lower level



insert "cow"



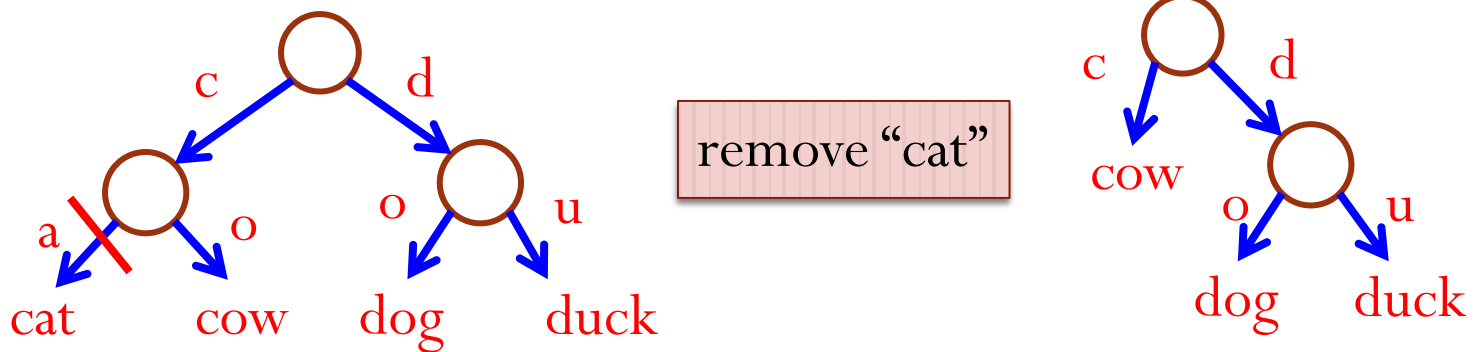
insert "cat"



Trie

Removal

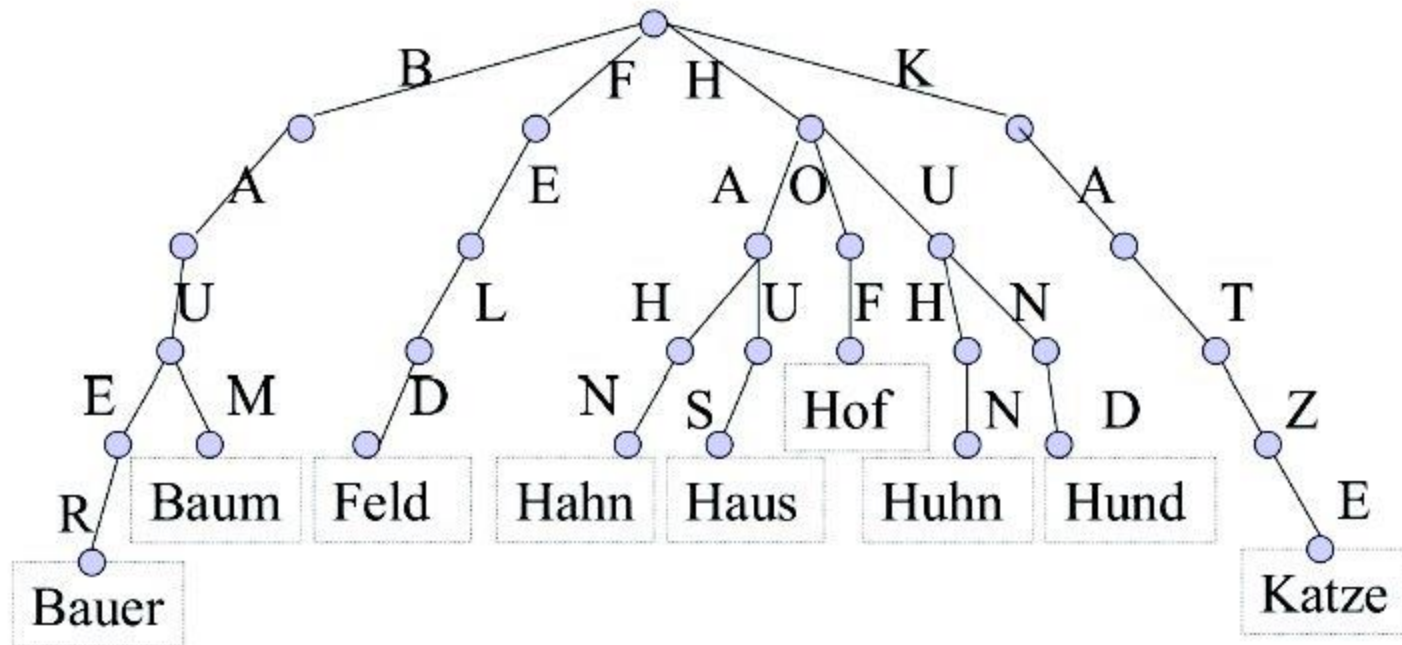
- The key to be removed is always at the leaf.
- After deleting the key, if the parent of that key now has only one child C , remove the parent node and move key C one level up.
- If key C is the only child of its new parent, repeat the above procedure again.



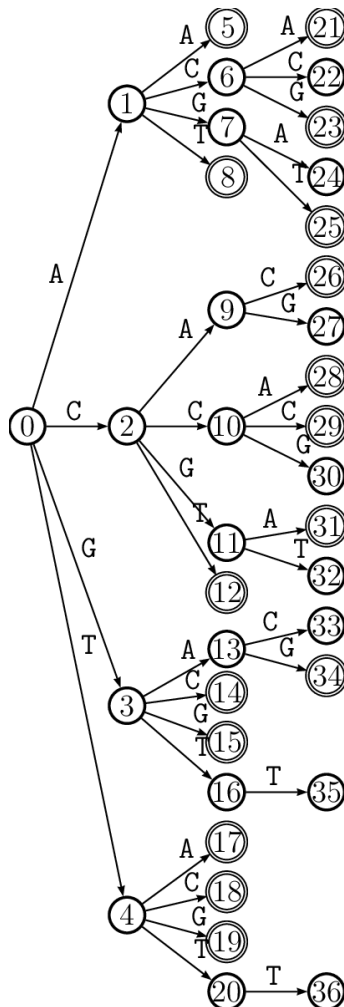
Time Complexity of Trie

- In the worst case, inserting or finding a key that consists of k symbols is $O(k)$.
 - This does not depend on the number of keys N .
 - Comparison: storing 32 integers in the range $[0, 127]$ using a trie versus using a BST. What are heights in the **worst case**?
 - BST: 32; Trie: 7
- Sometimes we can access records even faster.
 - A key is stored at the depth which is enough to distinguish it with others.
 - For example, in the previous example, we can find the word “duck” with just “du”.

Use Case – Spell Checking



Use Case – Human Genome



Example: Context Aware Seeds (My Research)

- Published in Algorithms in Molecular Biology 2020

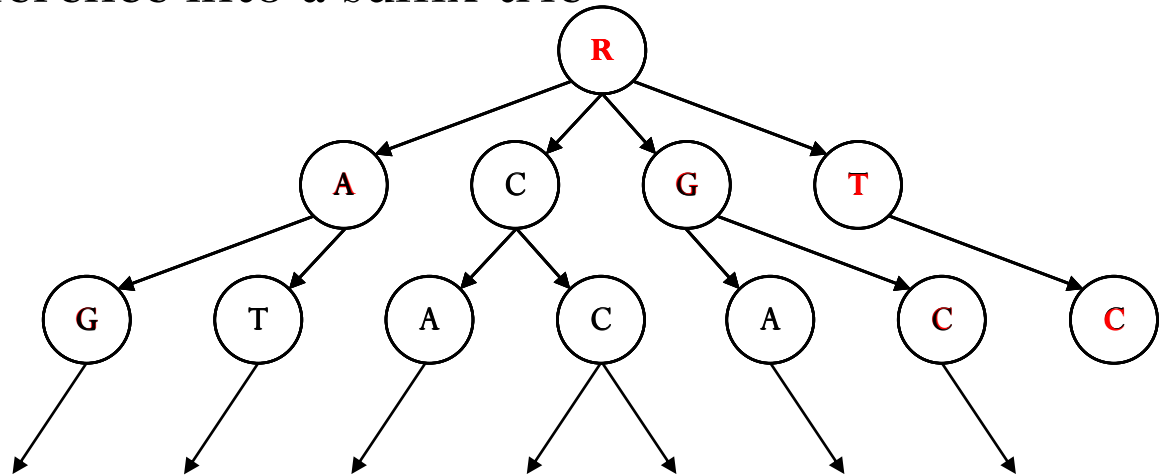
Compute the **Confidence Radii**

- **Confident radius**: **min** edit-distance (ED) to **non-immediate** neighbors
- Find all **neighbors**
- Find **non-immediate** neighbors
- Get the minimum ED

Suffix Trie

- Convert the reference into a suffix trie

Ref: **G**CCC**A**G**A****T****C**



Dynamic Programming

- A recurrence relationship
- a, b can be neighbors only if $\mathcal{P}(a), \mathcal{P}(b)$ are neighbors

a GCCCAGC
 $\mathcal{P}(a)$ GCCCAG

a GCCCAGC
 b GCCCACC

a GCCCAGC
 b GCCCAAC
 $\mathcal{P}(a)$ GCCCAG
 $\mathcal{P}(b)$ GCCCAAC

Neighbors

Neighbors

a GCCCAGC
 b' GCCCACT

Not Neighbors

\underline{a} GCCCAGC
 \underline{b} GCCCACC
 $\mathcal{P}(\underline{a})$ GCCCAG
 $\mathcal{P}(\underline{b})$ GCCCACC

Not Neighbors

Not Neighbors

$c_{max} = 1$

Find Neighbors

- Initialization: find all neighbors of the root node
- Iterate the suffix trie: top-to-bottom
 - Find neighbors for children nodes
- Invariant: all neighbors of current node is found

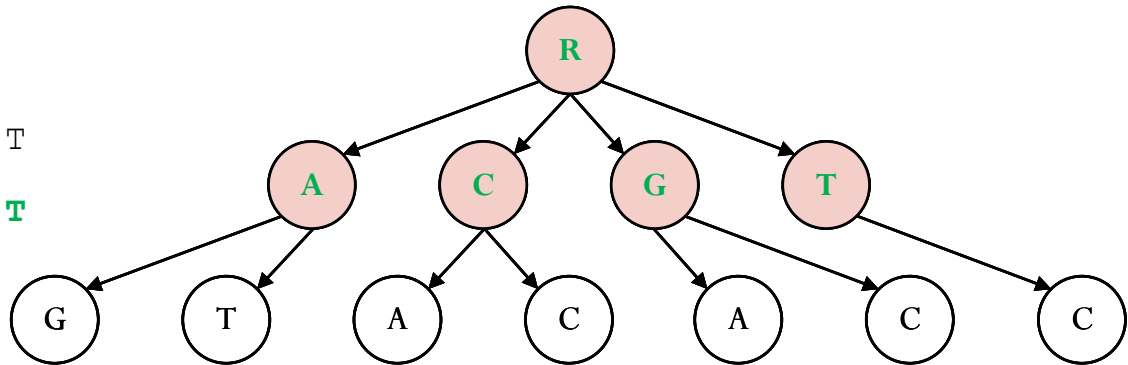
Initialize Root

$$c_{max} = 1$$

Ref: GCCCAGATC

Children of R : R, A, C, G, T

Neighbors of R : **R, A, C, G, T**



Iterate Trie—Build Neighbor List

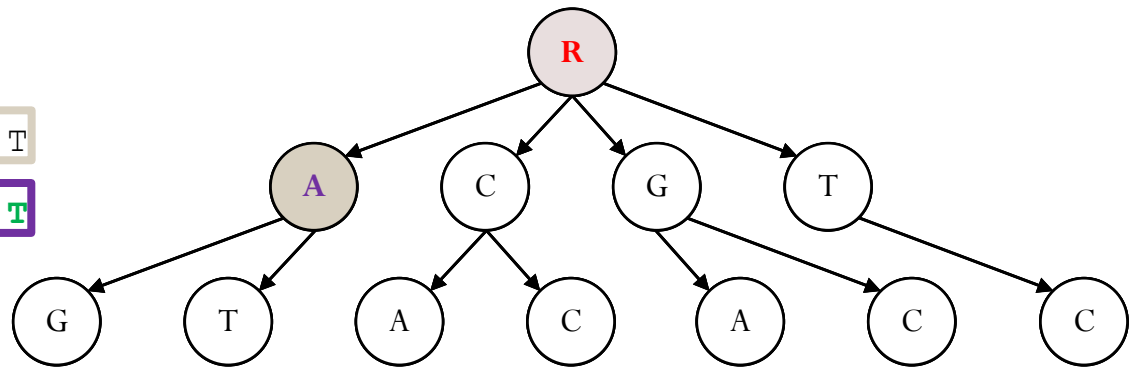
$$c_{max} = 1$$

Ref: GCCCAGATC

Children of R : R, A, C, G, T

Neighbors of R : R, A, C, G, T

Neighbors of A : Children of



χ is a neighbor of A $\rightarrow p(\chi)$ must be neighbor of $p(A)$
 $p(\chi)$ must be neighbor of R

Neighbors of A must be children of neighbors of R

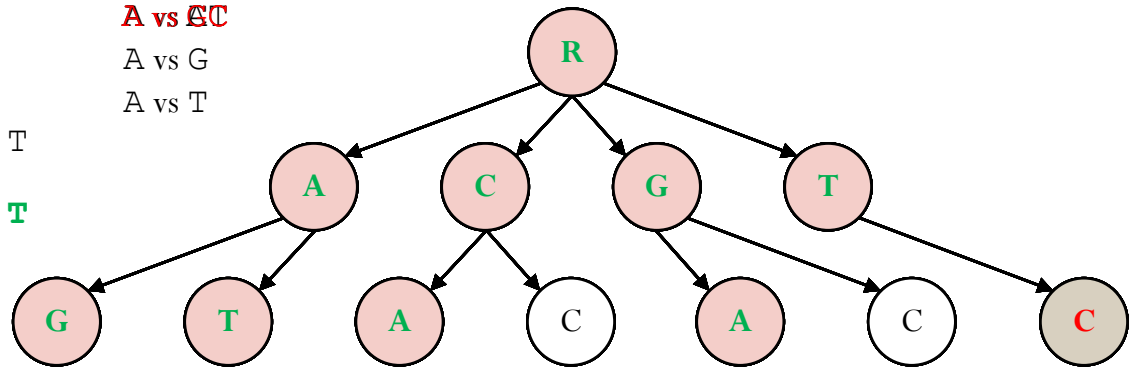
Neighbors of A

$$c_{max} = 1$$

A vs R
~~A~~ vs ~~AA~~
~~A~~ vs ~~AT~~
 A vs G
 A vs T

Children of R: ~~AA~~, ~~AT~~, C, G, T

Neighbors of R: R A, C, G, T



Neighbors of A:

All neighbors of A is found!



Neighbors of A must be children of neighbors of R

Complexity: $O(\mathcal{M})$
 \mathcal{M} : No. pairs of neighbors

Compute the **Confidence Radii**

- **Confident radius**: **min** edit-distance (ED) to **non-immediate** neighbors
- Find all **neighbors**
- Find **non-immediate** neighbors
 - Remove **immediate** neighbors
- Get the minimum ED

Does not increase complexity
Complexity: $O(\mathcal{M})$