Homework #3

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Course: Data Structures and Algorithms (VE 281)

Question 1

Determine whether the following propositions are true or false.

- (a) A complete tee is a tree where every node has either 0 or 2 children. True False
- (b) A complete tree is a tree where every level except the last is necessarily filled, and in the last level, nodes are filled in from left to right.

 True False
- (c) A complete tree is a tree where every node in the left subtree must be of lower priority than that of the root, and every node in the right subtree must be of greater priority than that of the root.

 True False
- (d) Heapsort has worst-case $\Theta(nlogn)$ time complexity. **True**
- (e) Percolate-up has an average-case time complexity of $\Theta(logn)$. True False
- (f) Dequeue is done by simply removing the root. True False
- (g) Enqueue in a min-heap is done by inserting the element at the end, and then calling percolate-up.

 True False
- (h) [2,13,8,16,13,10,40,25,17] is a representation of a min-heap. True False
- (*i*) [3,5,6,7,12,15,14,9,10,11] is a representation of a min-heap. True False
- (*j*) Proceeding from the bottom of the heap to the top, while repeatedly calling percolateDown() can initialize a min-heap.

 True False
- (k) Proceeding from the top of the heap to the bottom, while repeatedly calling percolateUp() can not initialize a min-heap.

 True False

For the tree in Figure 1, show the order in which the nodes are visited during the following tree traversals (The nodes in the tree are from A to I):

(a) Pre-order depth-first traversal.

Answer: ABCDEFGHI

(b) Post-order depth-first traversal.

Answer: DCFGEBIHA

(c) In-order depth-first traversal.

Answer: CDBFEGAIH

(*d*) Level-order traversal.

Answer: A B H C E I D F G

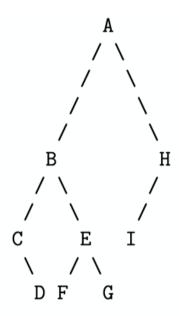


Figure 1: tree

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Suppose the node of a binary search tree is defined as follows.
struct node {
  Key key;
  node * left;
  node * right;
};
Implement the following function which gets the predecessor of a given key in
the tree:
node* getPred(node* root, Key key);
// REQUIRES: The tree rooted at "root" is non-empty.
      "kev" is in the tree rooted at "root".
// EFFECTS: Return the predecessor of "key" in the tree rooted at "root".
       Return NULL if there is no predecessor
You can assume the following function is availabe:
node* findMax(node* root);
// REQUIRES: The tree rooted at "root" is non-empty.
// EFFECTS: Return the node with the maximal key in the tree rooted at "root".
Complete the getPred() function below:
node* getPred(node* root, Key key)
  node * leftAncestor = NULL;
  while (root->key != key) {
    if (root->key < key) {
       leftAncestor = root;
       root = root >right;
    } else {
       root = root > left:
  if (root-> left == NULL) {
       return leftAncestor;
  } else {
      return findMax (root > left);
```

Given a key set $\{1,4,5,10,16,17,21\}$, please draw **ONE** BST of height 2, 3, 4, 5, and 6, respectively.

Answer.

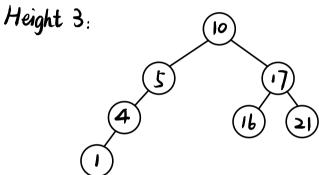
Height 2:

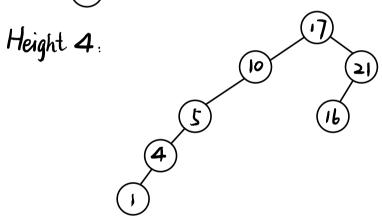
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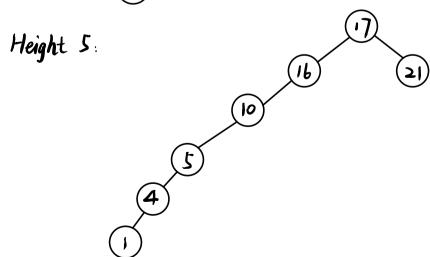
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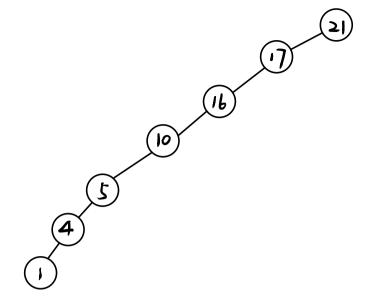
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Height b:



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Use DFS to complete the quest below:
0s and 1s are placed into an m \times n matrix. Adjacent 1s in the matrix are connected
(here adjacent means that one 1 is on the right, left, above or below of another 1),
which forms components (an isolated 1 is also a component). Goal: count the num-
ber of components in the matrix. Below are 2 examples.
       10000
       \frac{01000}{00011}: three components(red, blue, and yellow).
Matrix
       00011
       11011
       001100 \atop 00110: two components(blue and red).
Matrix
       00011
Finish the code below:
    // Your code is allowed to modify the matrix, X.
    void dfs(int** X, int i, int j, int m, int n){
         if (i<0 || i>m || j<0 || j>n || x[i][j]==0
                                                                     ) {
              return;
         X[i][j] = 0;
         // Hint: Recur here
         dfs (x, i-1, n, m, n);
         dfs (x, i+1, n, m, n);
         dfs (x, i, n-1, m, n);
         dfs (x, i, n+1, m,n);
    int numIslands(int** X, int m, int n){
         int count = 0;
         for(int i = 0; i < m; i++){
              for (int j = 0; j < n; j++){
                   if (X[i][j] == 1){
                       dfs(X, i, j, m, n);
                       count ++;
         return count;
```