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**VE320 – Summer 2021**

**Introduction to Semiconductor Devices**

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**Chapter 12 Bipolar Junction Transistor**

# Outline

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12.1 Review and example

12.2 Bipolar Junction transistor

12.3 Early Effect

12.4 Summary

12.5 Quantitative analysis of BJT gain

12.6 BJT symbols and planar device structure

# Outline

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## 12.1 Review and example

## 12.2 Bipolar Junction transistor

## 12.3 Early Effect

## 12.4 Summary

## 12.5 Quantitative analysis of BJT gain

## 12.6 BJT symbols and planar device structure

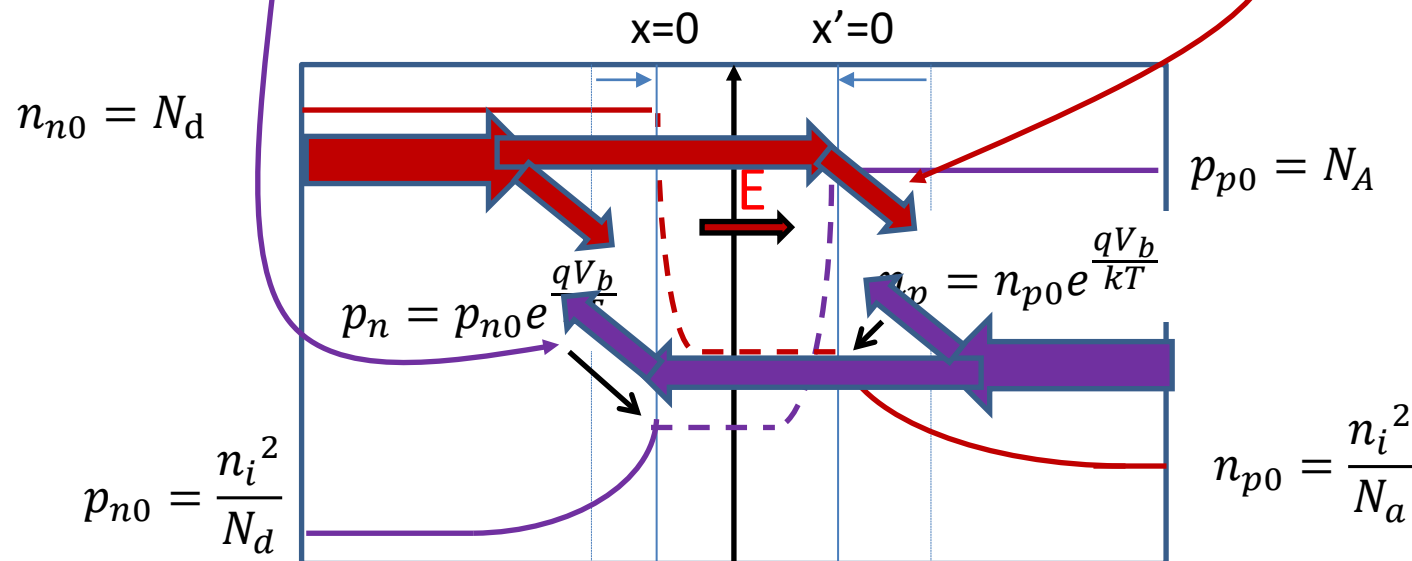
# 12.1 Previously: pn Junction Current

- charge carrier transport: forward bias: current ratio

$$J_n = -qD_n \frac{dn_p}{dx} = -\frac{qD_n n_{p0}}{L_n} (e^{\frac{qV_b}{kT}} - 1) e^{-x/L_n}$$

$$J_p = -qD_p \frac{dp_n}{dx} = -\frac{qD_p p_{n0}}{L_p} (e^{\frac{qV_b}{kT}} - 1) e^{x/L_p}$$

$$\frac{J_n}{J_p} = \frac{D_n N_d / L_n}{D_p N_a / L_p}$$



Assumption: No recombination-generation in depletion region.

# 12.1 Example: pn Junction Current

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Finding  $L_n, \tau_n$  in **p-type** region because electrons are minority carriers.

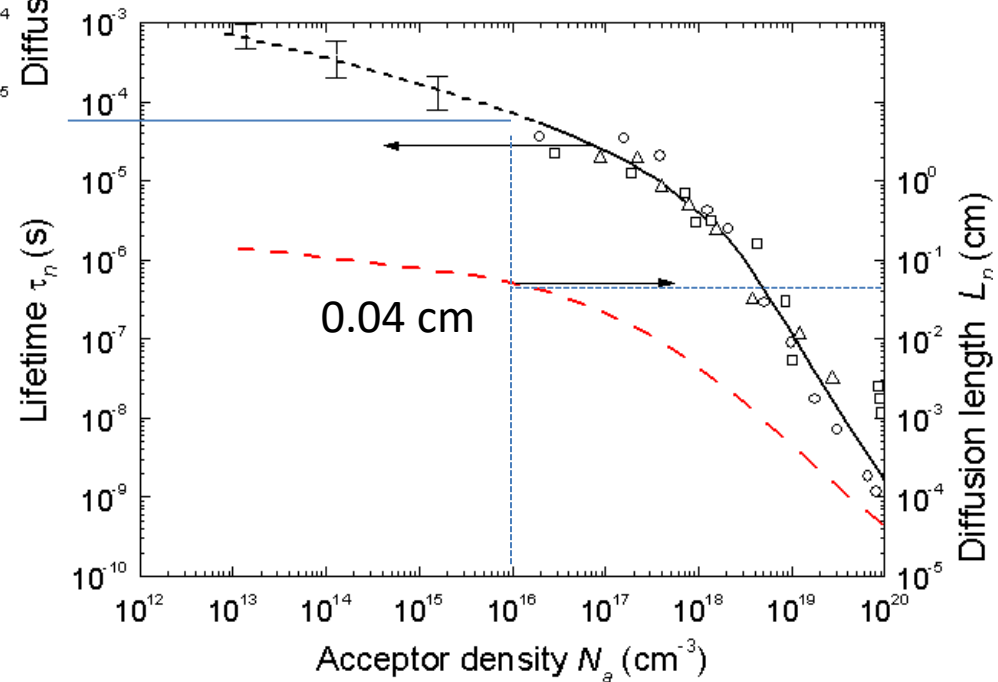
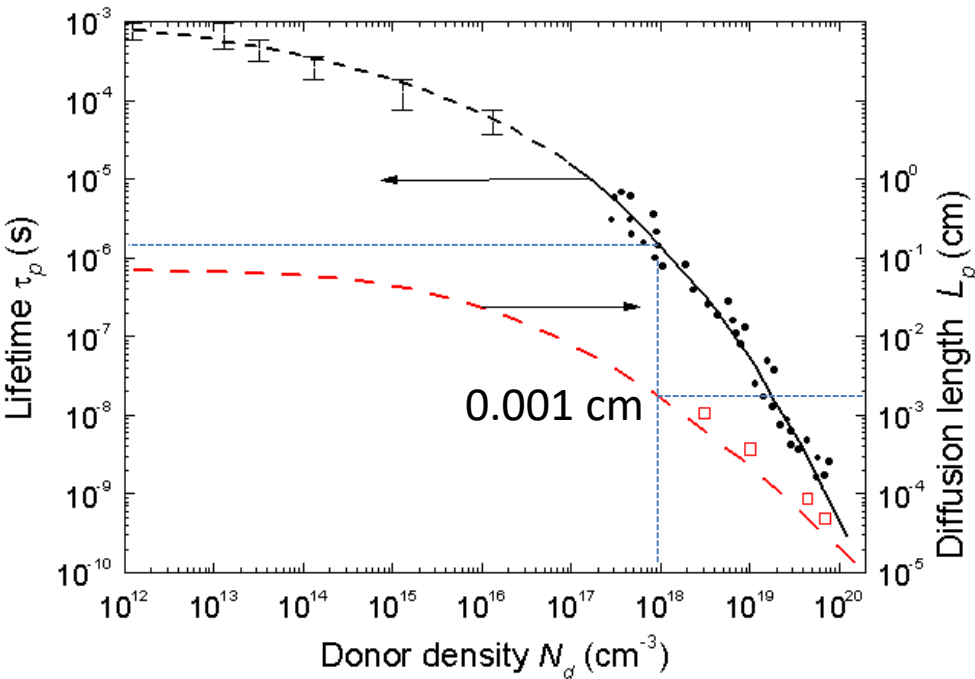
$$\text{For } N_a = 10^{16} \text{ cm}^{-3} \quad L_n = 0.04 \text{ cm} \quad \tau_n = 5 \times 10^{-5} \text{ s}$$

Finding  $L_p, \tau_p$  in **n-type** region because holes are minority carriers.

$$\text{For } N_d = 10^{18} \text{ cm}^{-3} \quad L_p = 0.0015 \text{ cm} \quad \tau_p = 1.5 \times 10^{-6} \text{ s}$$

$$\frac{J_n}{J_p} = \frac{D_n N_d / L_n}{D_p N_a / L_p} = \frac{L_n / \tau_n}{L_p / \tau_p} \frac{N_d}{N_a} \approx \frac{\frac{4 \times 10^{-2}}{5 \times 10^{-5}}}{\frac{1.5 \times 10^{-3}}{1.5 \times 10^{-6}}} \times \frac{10^{18}}{10^{16}} = 80$$

# 12.1 Example: pn Junction Current



<http://www.ioffe.ru/SVA/NSM/Semicond/Si/>

# Outline

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12.1 Review and example

**12.2 Bipolar Junction transistor**

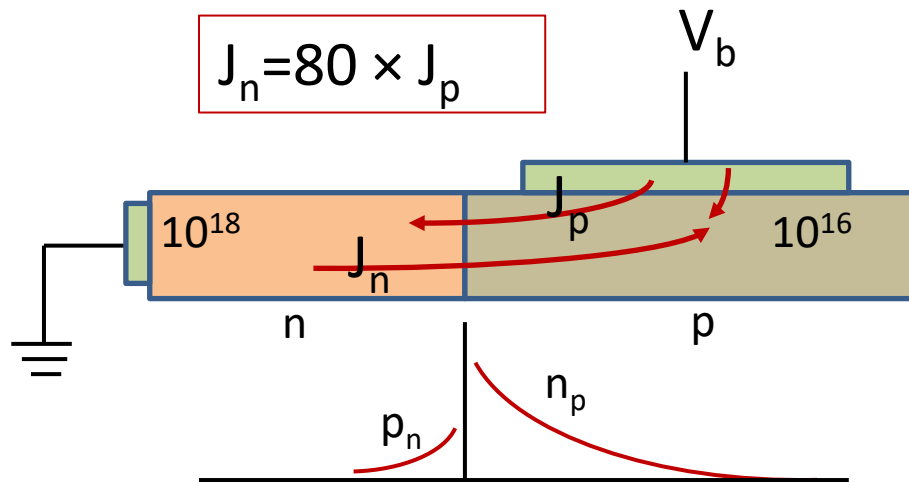
12.3 Early Effect

12.4 Summary

12.5 Quantitative analysis of BJT gain

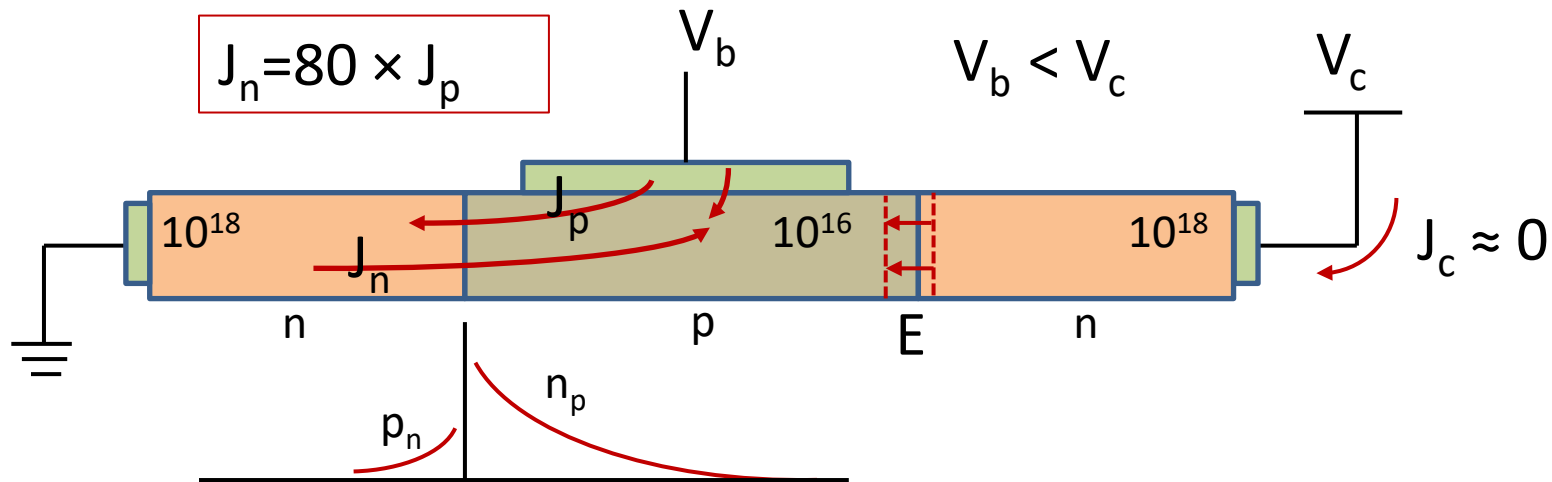
12.6 BJT symbols and planar device structure

## 12.2 Bipolar Junction transistor

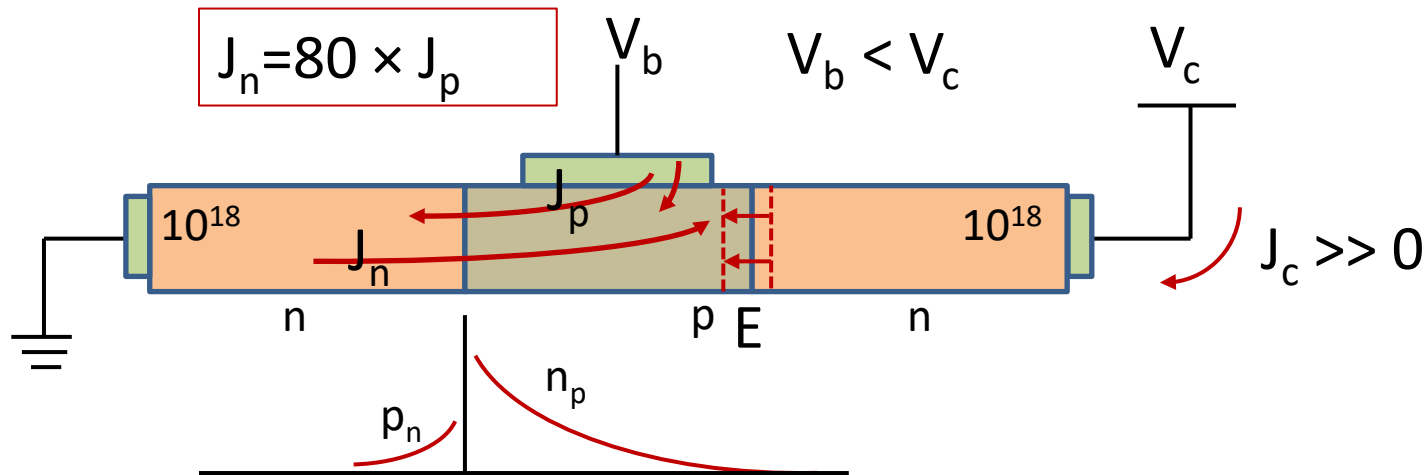




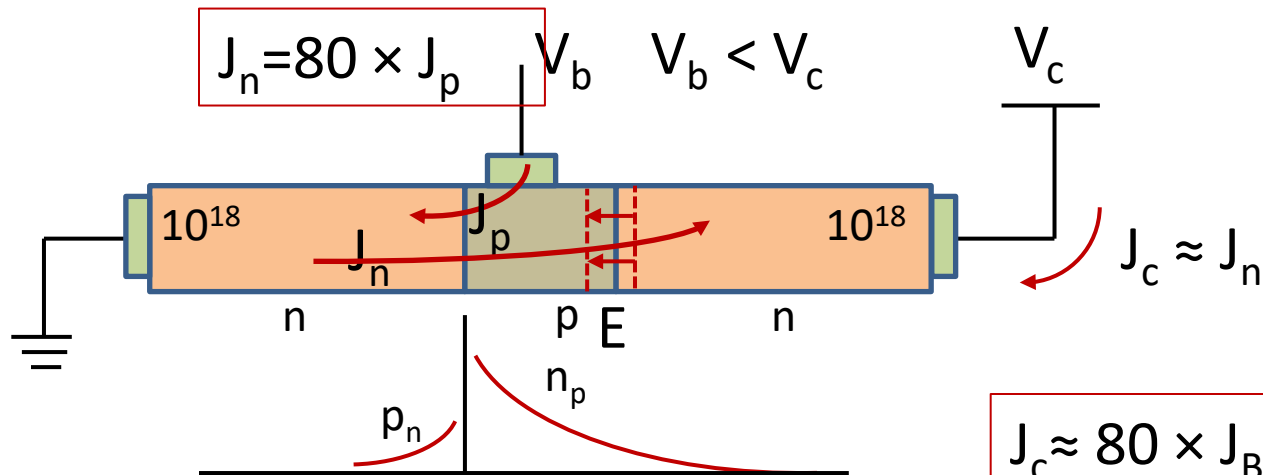
## 12.2 Bipolar Junction transistor



## 12.2 Bipolar Junction transistor

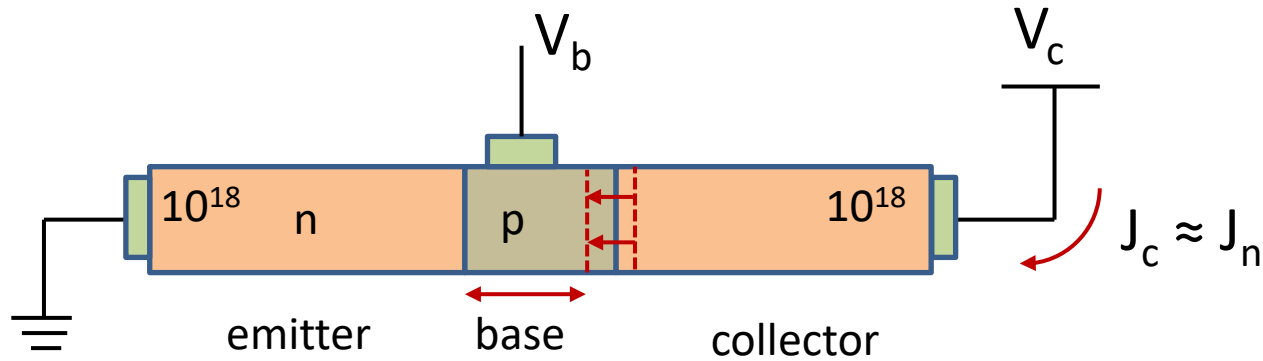


## 12.2 Bipolar Junction transistor



$$J_c \approx 80 \times J_B \rightarrow \text{Gain } \beta = 80$$

## 12.2 Bipolar Junction transistor

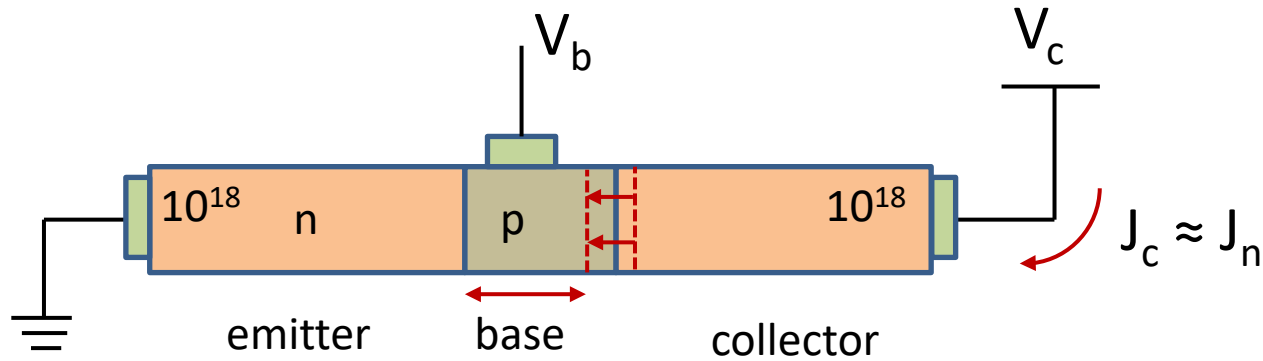


$$J_c \approx 80 \times J_B \rightarrow \text{Gain } \beta = 80$$

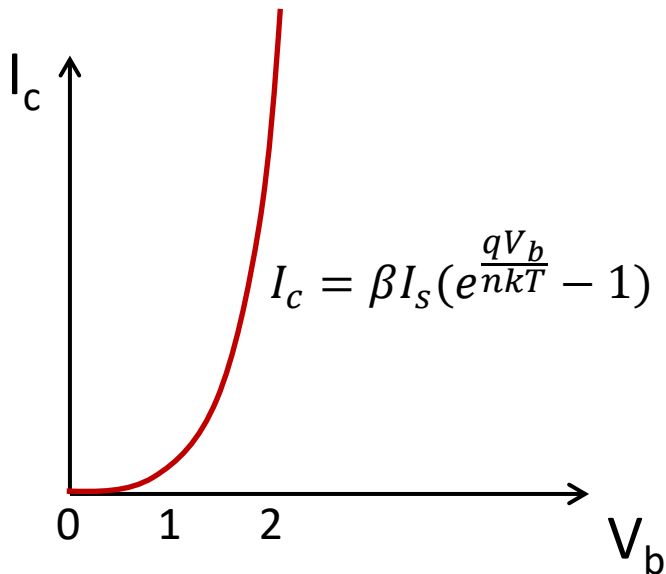
BJT Characteristics:

1. Base width smaller  $\rightarrow$  higher gain
2. Larger emitter-base concentration ratio  $\rightarrow$  higher gain

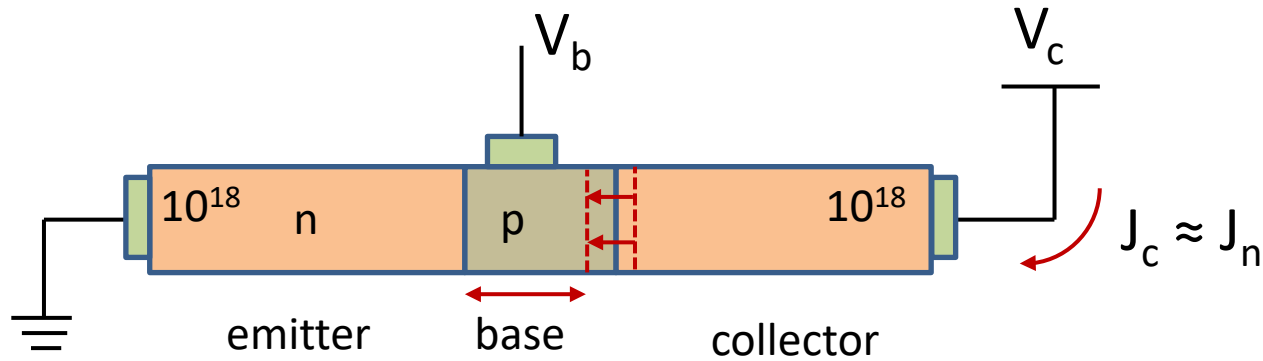
## 12.2 Bipolar Junction transistor: I-V



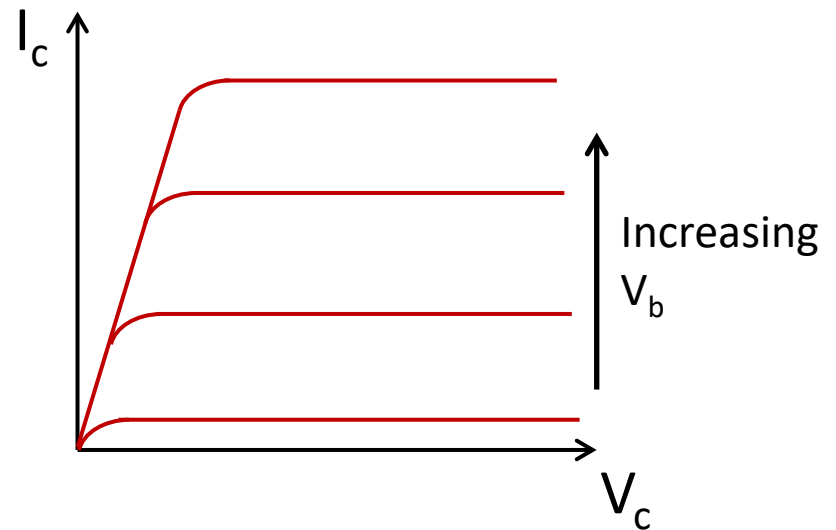
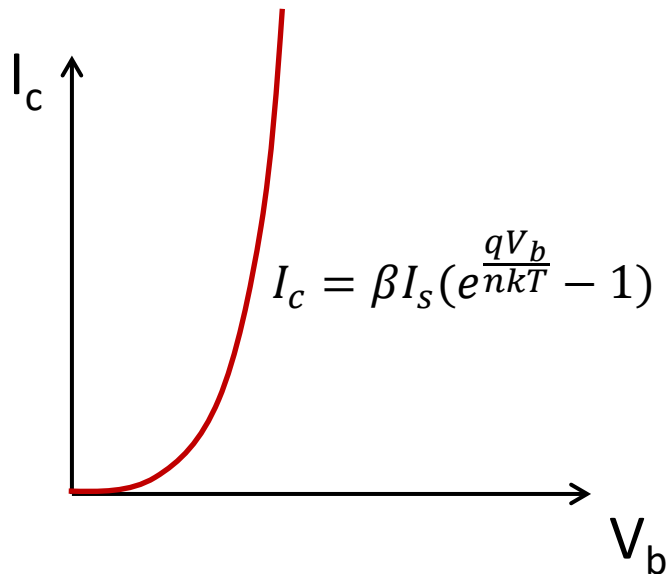
$$J_c \approx 80 \times J_B \rightarrow \text{Gain } \beta = 80$$



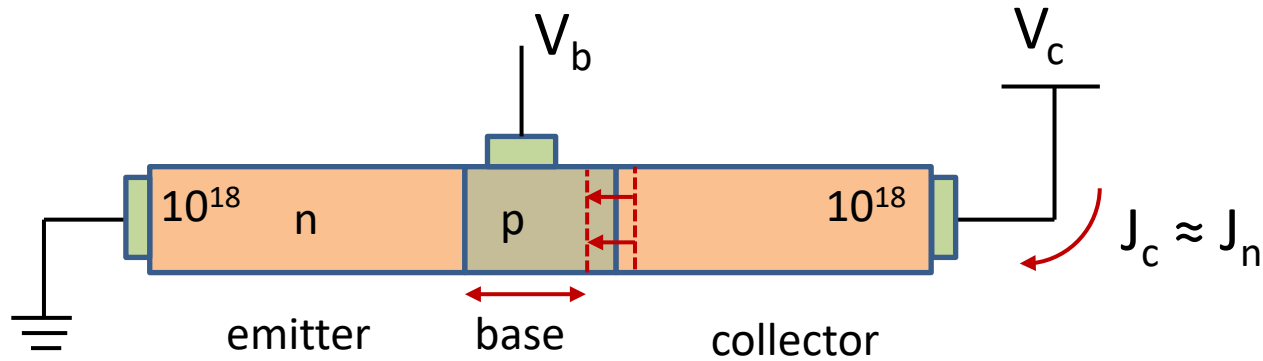
## 12.2 Bipolar Junction transistor: I-V



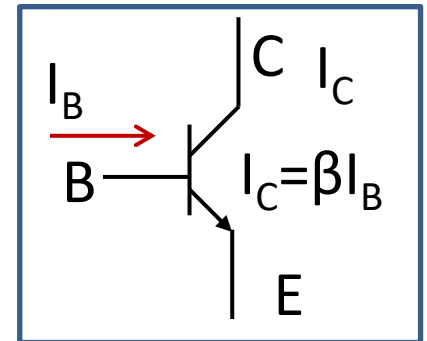
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## 12.2 Bipolar Junction transistor: I-V



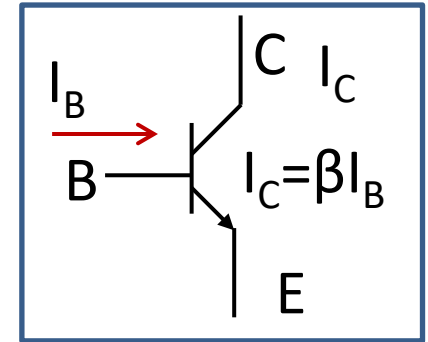
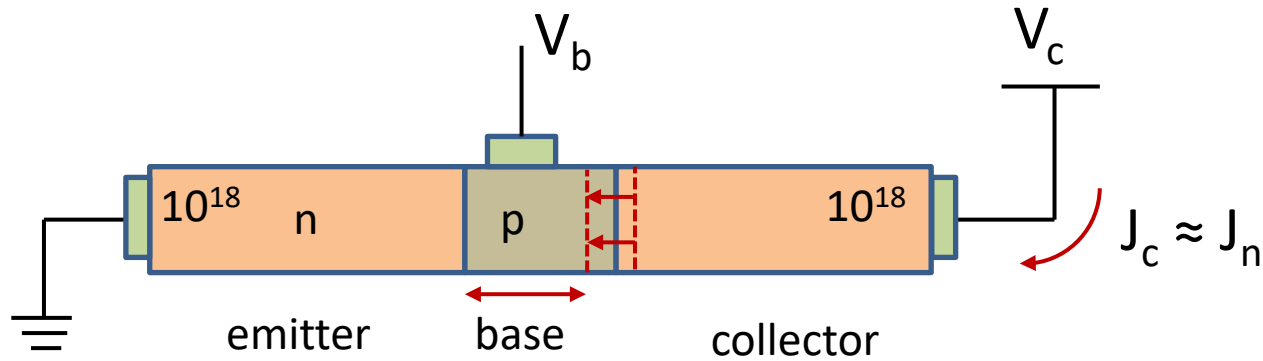
$$J_c \approx 80 \times J_B \rightarrow \text{Gain } \beta = 80$$



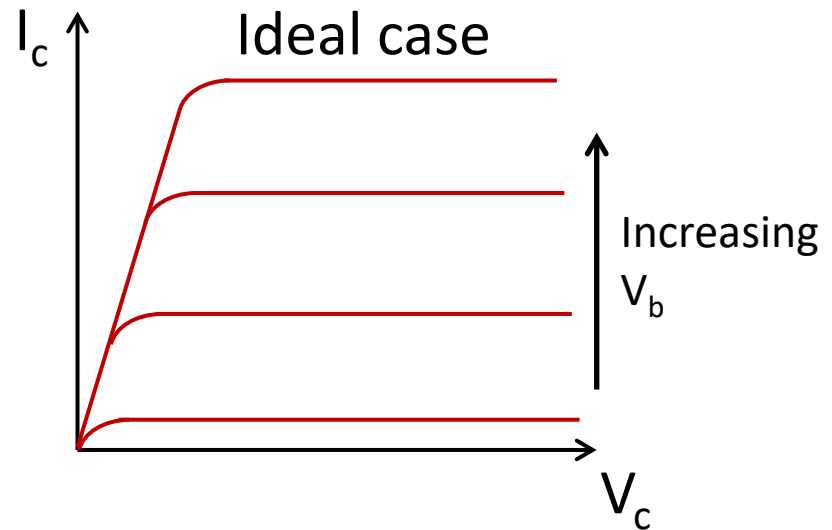
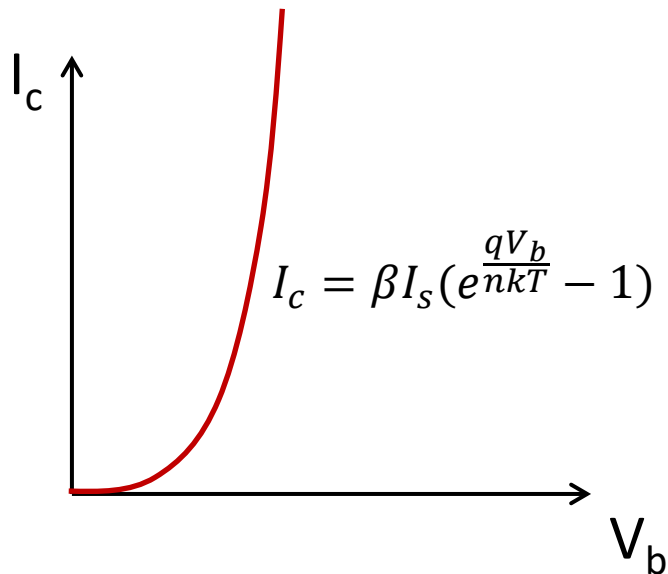
Basic facts:

1. Narrower base  $\rightarrow$  larger gain
2.  $\beta \approx N_D/N_A$ , higher emitter-to-base doping ratio  $\rightarrow$  higher gain

# 12.2 Bipolar Junction transistor: I-V



$$J_c \approx 80 \times J_B \rightarrow \text{Gain } \beta = 80$$





# Outline

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12.2 Bipolar Junction transistor

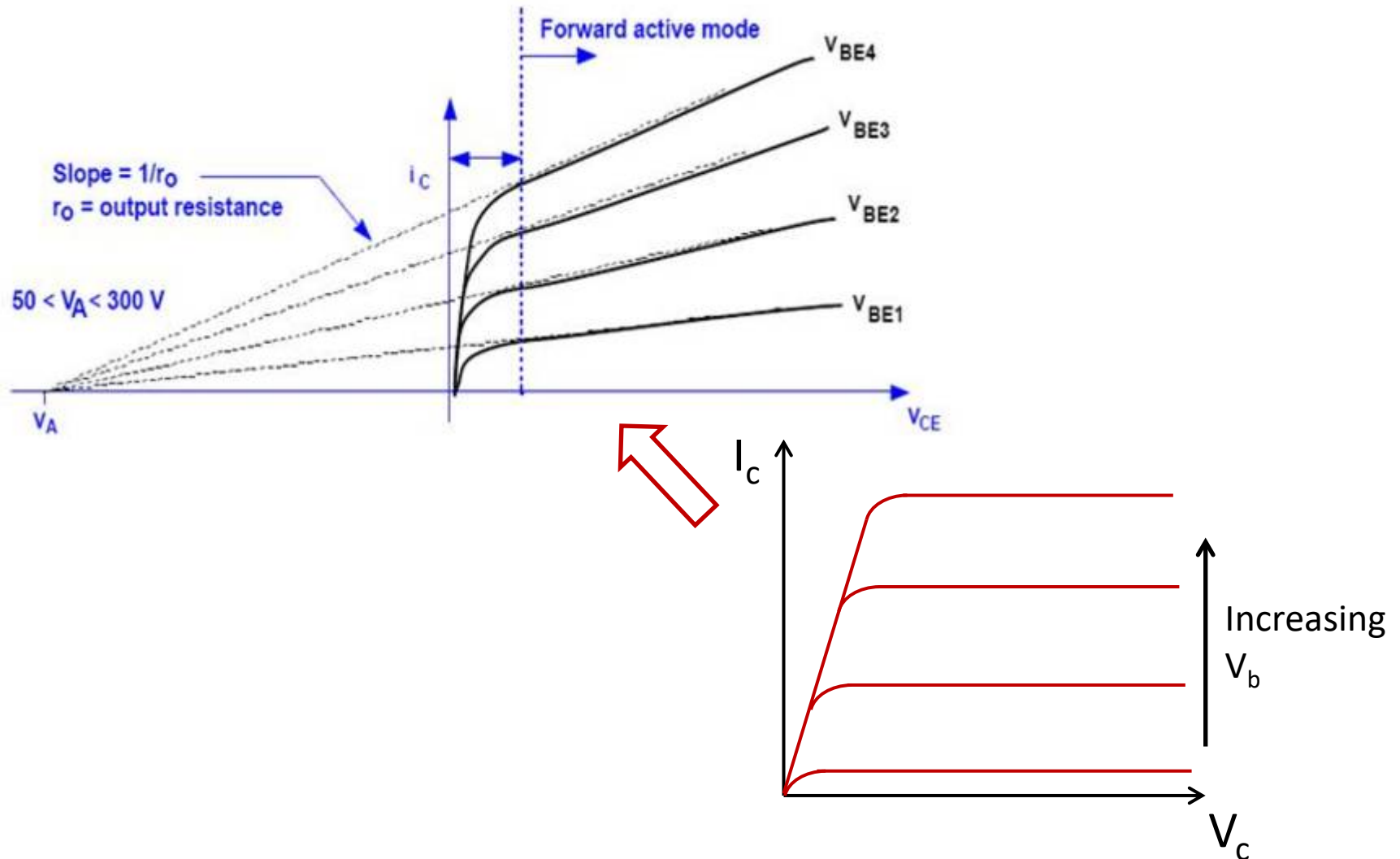
**12.3 Early Effect**

12.4 Summary

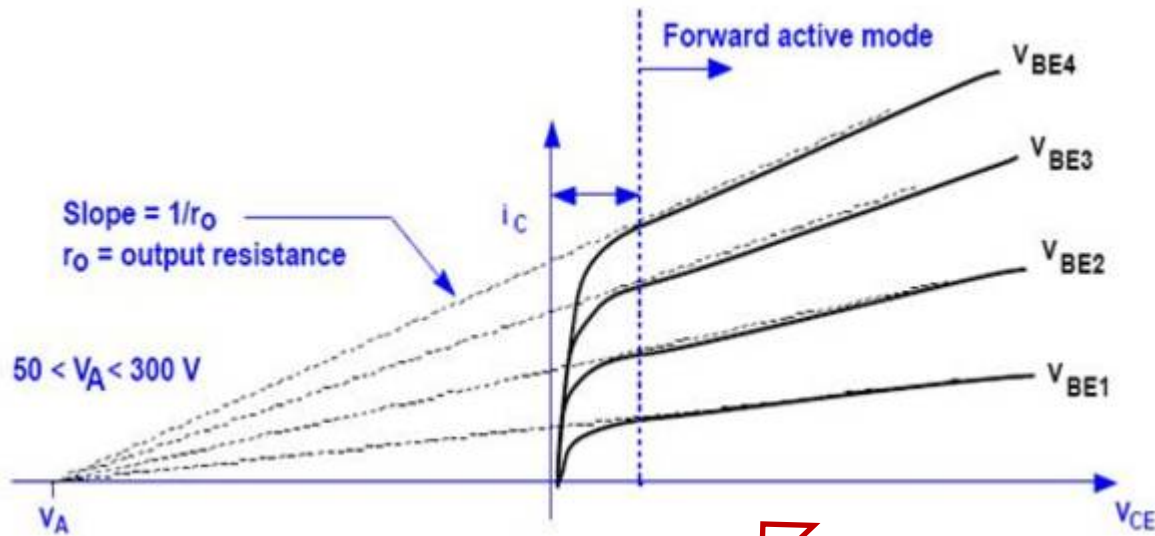
12.5 Quantitative analysis of BJT gain

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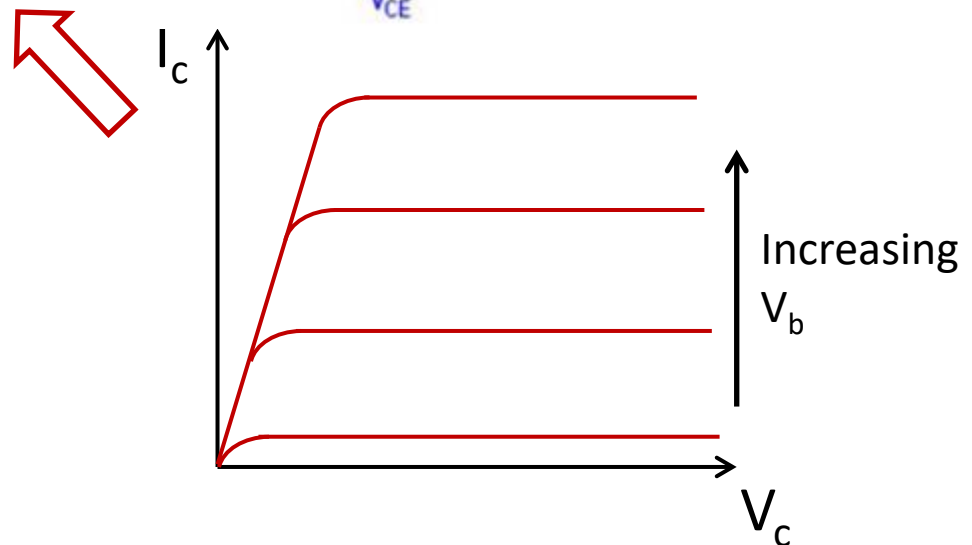
## 12.3 Early Effect



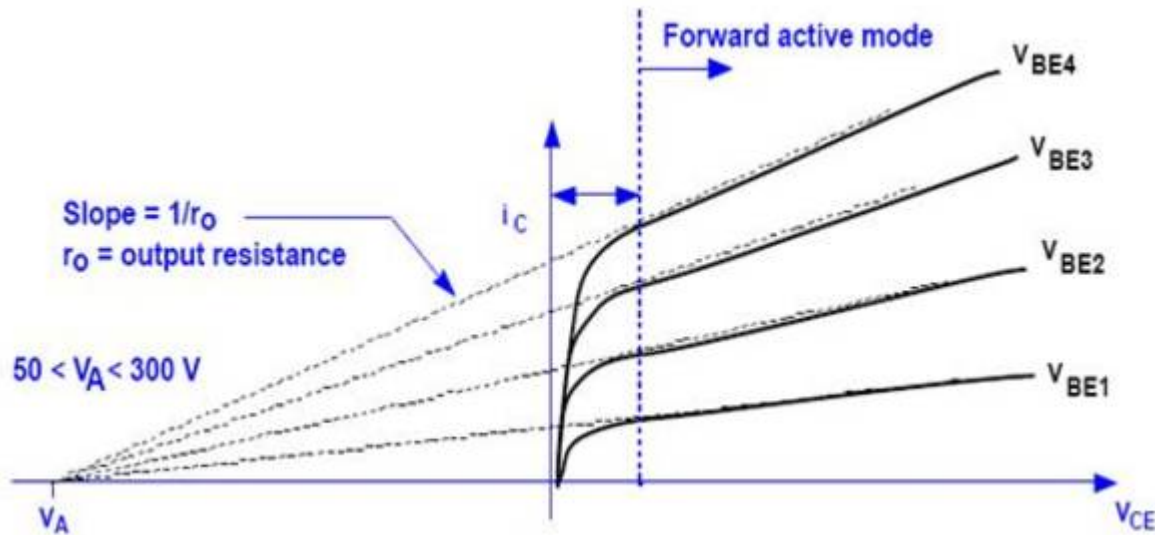
## 12.3 Early Effect



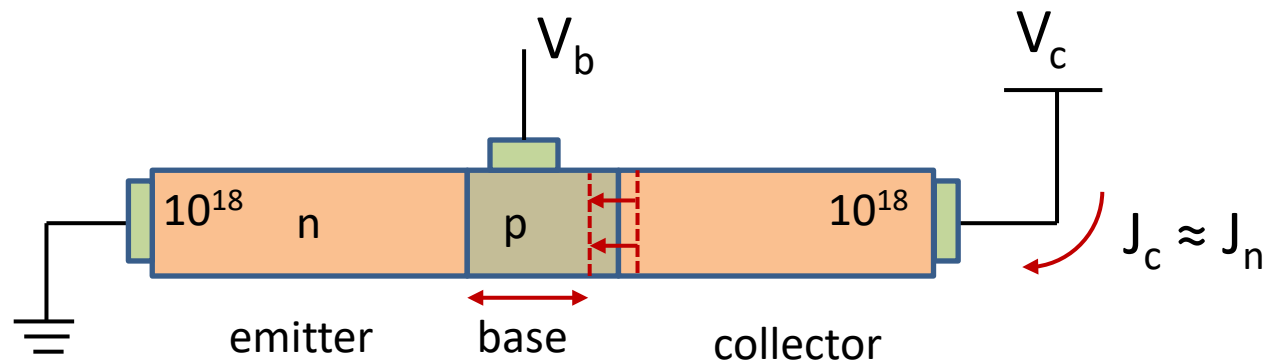
James M. Early



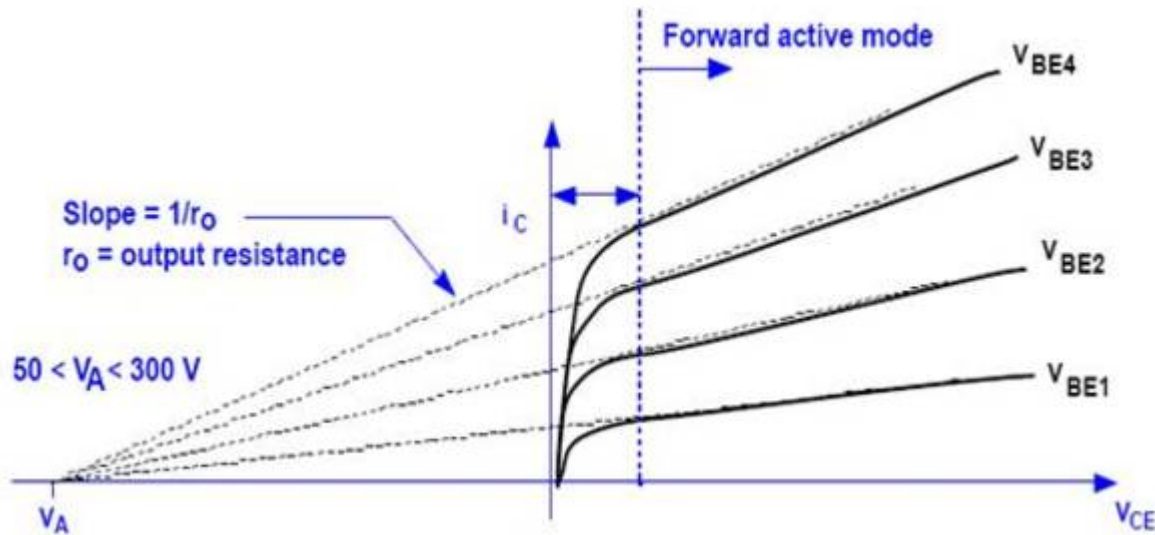
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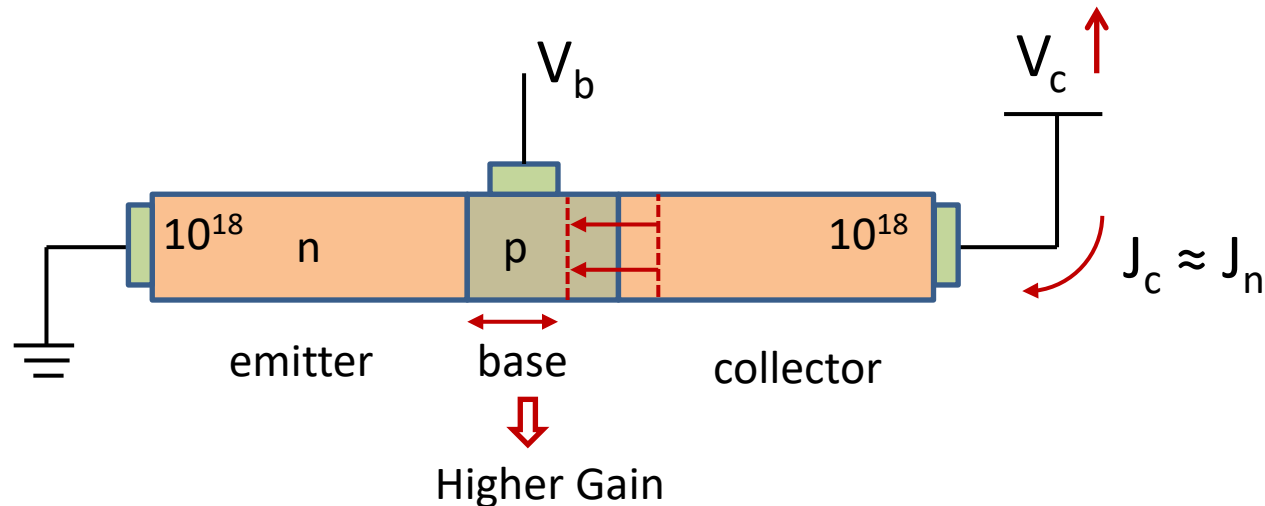
James M. Early



## 12.3 Early Effect



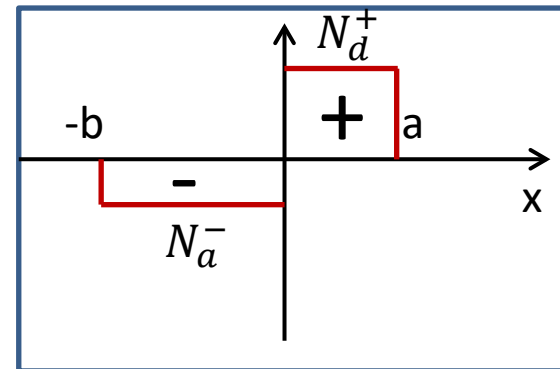
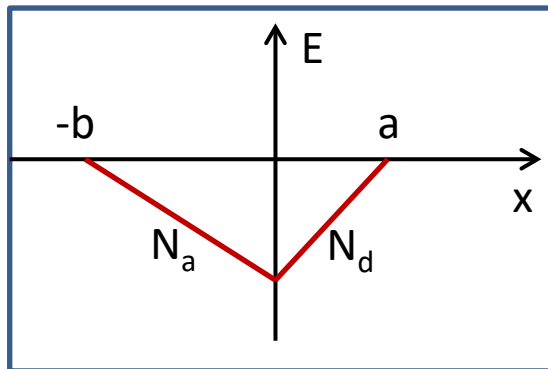
James M. Early



# Previously...

$$a = \sqrt{\frac{2\epsilon(V_{bi}-V_R)}{q} \frac{N_a}{N_d} \frac{1}{N_a + N_d}}$$

$$N_A^- b = N_D^+ a \Rightarrow b = \sqrt{\frac{2\epsilon(V_{bi}-V_R)}{q} \frac{N_d}{N_a} \frac{1}{N_a + N_d}}$$



# Previously...

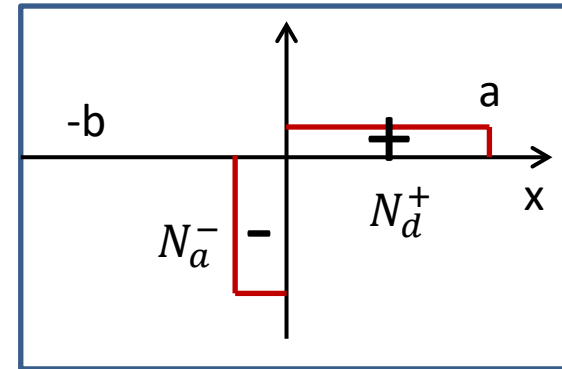
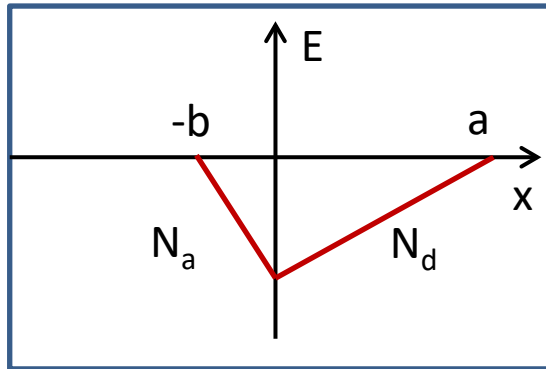
$$a = \sqrt{\frac{2\varepsilon(V_{bi}-V_R)}{q} \frac{N_a}{N_d} \frac{1}{N_a + N_d}}$$

$$N_A^- b = N_D^+ a \Rightarrow b = \sqrt{\frac{2\varepsilon(V_{bi}-V_R)}{q} \frac{N_d}{N_a} \frac{1}{N_a + N_d}}$$

$$N_a = 100 N_d$$

$$a = \sqrt{\frac{2\varepsilon(V_{bi}-V_R)}{q} \frac{100\cancel{N_a}}{N_d} \frac{1}{100\cancel{N_a}}}$$

$$b = \sqrt{\frac{2\varepsilon(V_{bi}-V_R)}{q} \frac{\cancel{N_a}}{100\cancel{N_a}} \frac{1}{100N_d}}$$



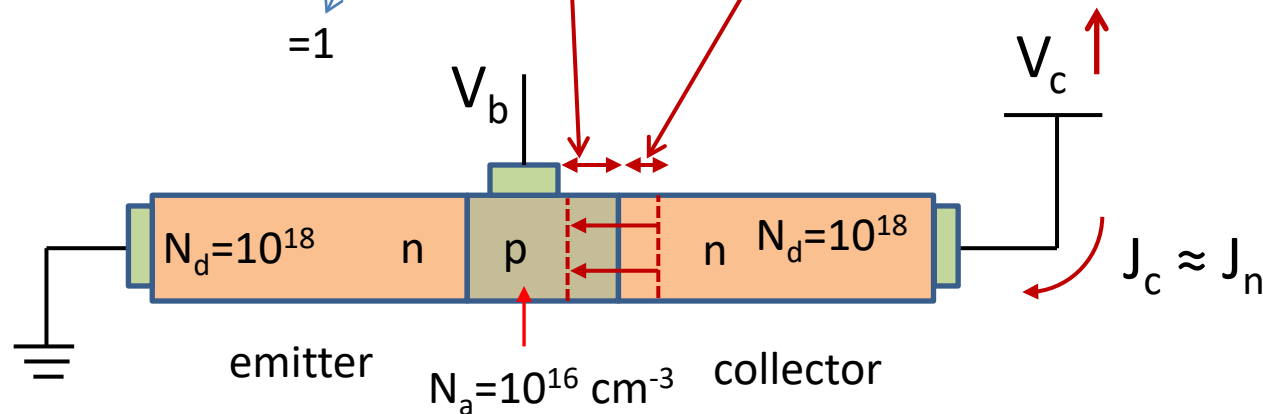
# 12.3 Early Effect

$$a = \sqrt{\frac{2\epsilon(V_{bi}-V_R)}{q} \frac{10^{16}}{10^{18}} \frac{1}{10^{16} + 10^{18}}} = 1/10000$$

$$b = \sqrt{\frac{2\epsilon(V_{bi}-V_R)}{q} \frac{10^{18}}{10^{16}} \frac{1}{10^{16} + 10^{18}}} = 1$$



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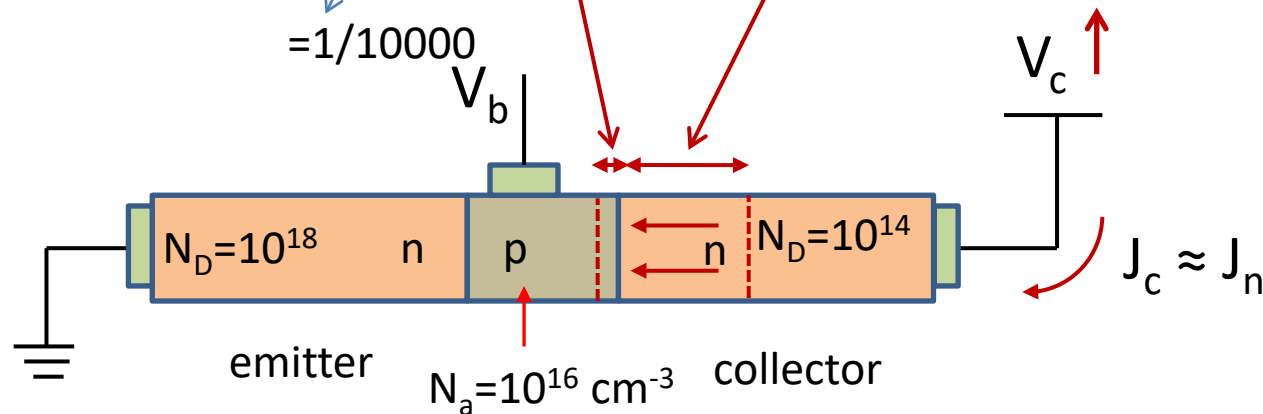
# 12.3 Early Effect

$$a = \sqrt{\frac{2\epsilon(V_{bi}-V_R)}{q} \frac{10^{16}}{10^{14}} \frac{1}{10^{16} + 10^{14}}} \quad \text{=1}$$

$$b = \sqrt{\frac{2\epsilon(V_{bi}-V_R)}{q} \frac{10^{14}}{10^{16}} \frac{1}{10^{16} + 10^{14}}}$$



James M. Early



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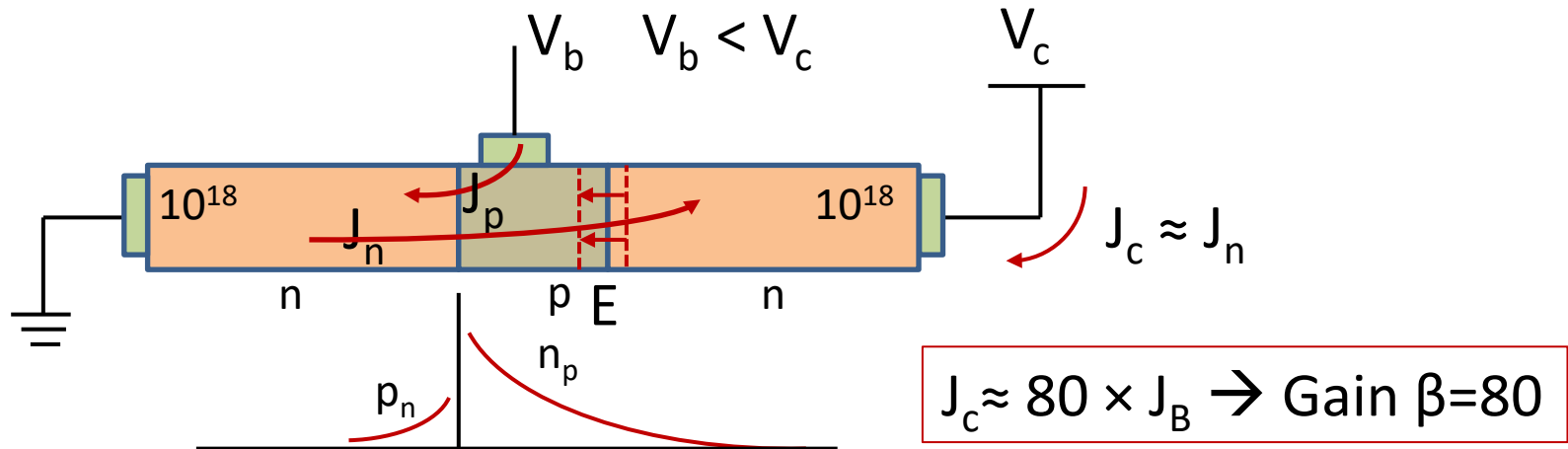
12.3 Early Effect

**12.4 Summary**

12.5 Quantitative analysis of BJT gain

12.6 BJT symbols and planar device structure

## 12.4 Summary



1. highest doping concentration is limited by solubility ( $<10^{20}$ )
2. Lowest doping concentration is limited by  $n_i$  and fabrication process

Basic facts:

1. Narrower base  $\rightarrow$  larger gain
2.  $\beta \approx N_D/N_A$ , higher emitter-to-base doping ratio  $\rightarrow$  higher gain
3. Trade-off for base doping concentration (gain and Early effect)

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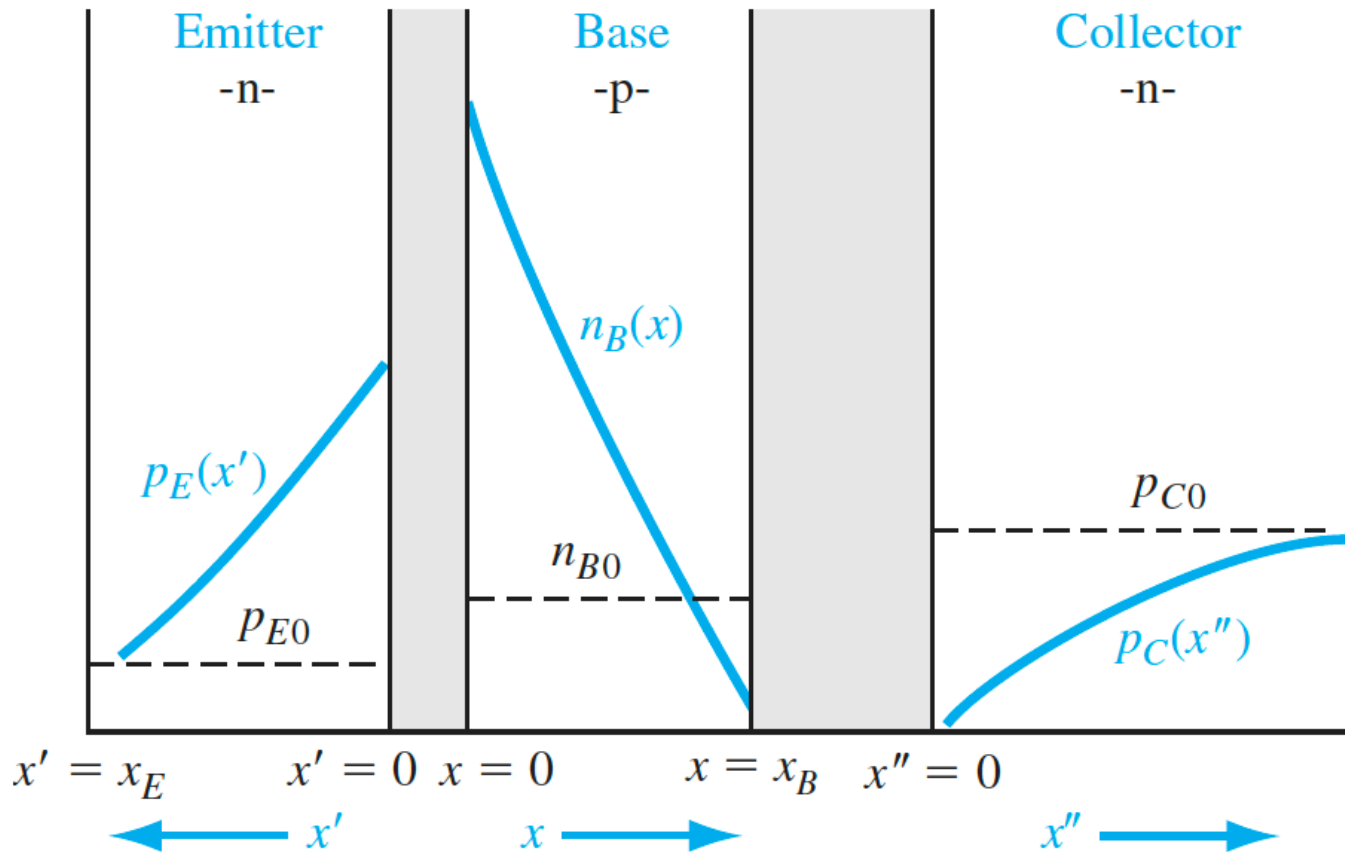
12.3 Early Effect

12.4 Summary

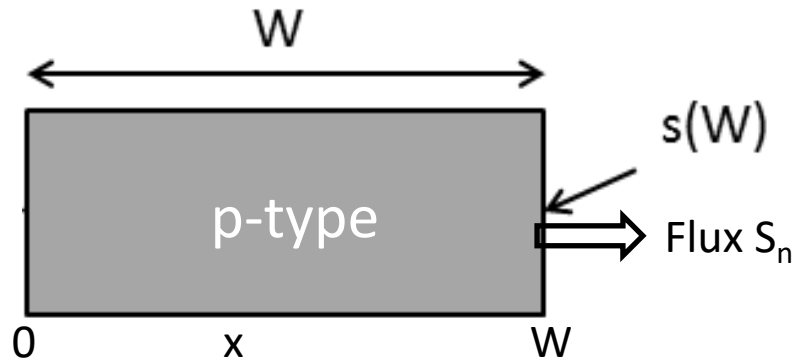
**12.5 Quantitative analysis of BJT gain**

12.6 BJT symbols and planar device structure

## 12.5 Quantitative analysis of BJT gain



## 12.5 Quantitative analysis of BJT gain

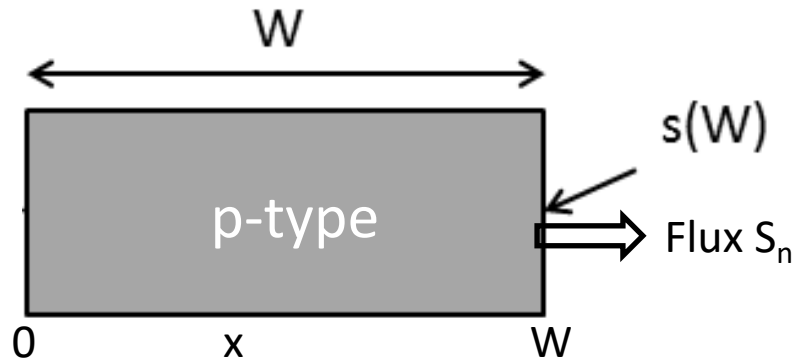


$$N_a = 10^{17} \text{ cm}^{-3}, D_n = 10 \text{ cm}^2/\text{s}, \tau_n = 10^{-7} \text{ s}, \text{SRV } s(x=W) = \infty$$
$$\Delta n(x=0) = 10^{14} \text{ cm}^{-3}$$

Find the electron flux  $S_n$  at  $x=0$  and  $W$ , if

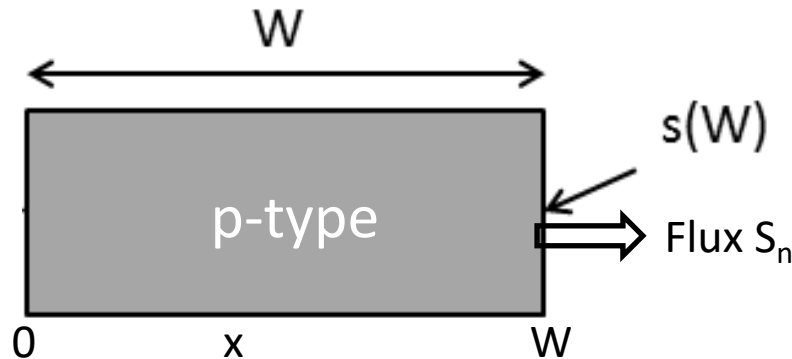
- 1)  $W=20\mu\text{m}$
- 2)  $W=2\mu\text{m}$

## 12.5 Quantitative analysis of BJT gain



$$0 = D_n \frac{\partial^2 \Delta n}{\partial x^2} - \frac{\Delta n}{\tau} \quad \Rightarrow \Delta n = A \exp\left(-\frac{x}{L_n}\right) + B \exp\left(\frac{x}{L_n}\right)$$

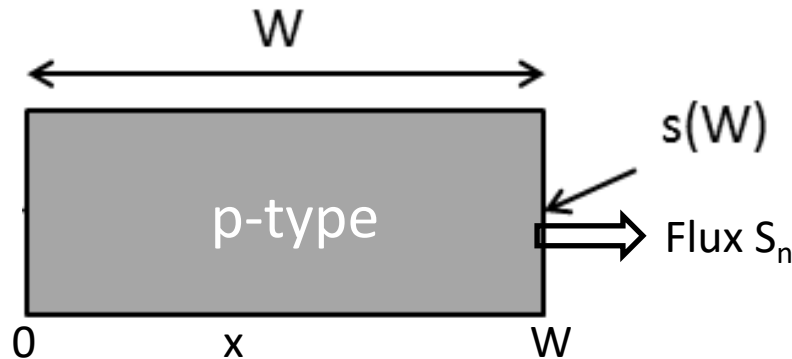
## 12.5 Quantitative analysis of BJT gain



$$\boxed{0 = D_n \frac{\partial^2 \Delta n}{\partial x^2} - \frac{\Delta n}{\tau}} \quad \Rightarrow \Delta n = A \exp\left(-\frac{x}{L_n}\right) + B \exp\left(\frac{x}{L_n}\right)$$
$$\begin{cases} x = 0 \Rightarrow \Delta n_0 = \Delta n(x = 0) = A + B \\ x = W \Rightarrow \Delta n = A \exp\left(-\frac{W}{L_n}\right) + B \exp\left(\frac{W}{L_n}\right) = 0 \end{cases}$$



## 12.5 Quantitative analysis of BJT gain

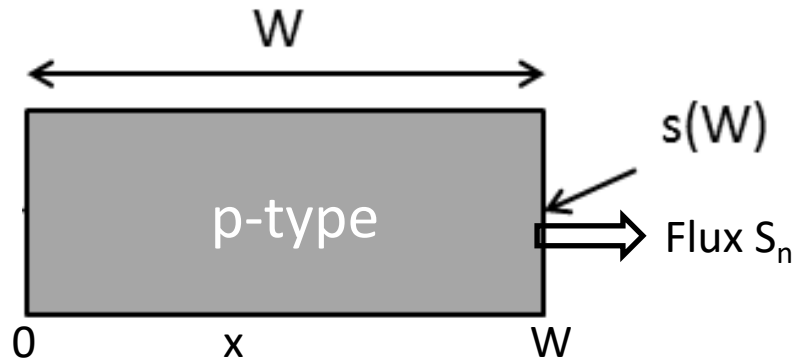


$$0 = D_n \frac{\partial^2 \Delta n}{\partial x^2} - \frac{\Delta n}{\tau} \quad \Rightarrow \Delta n = A \exp\left(-\frac{x}{L_n}\right) + B \exp\left(\frac{x}{L_n}\right)$$

$$A = (\Delta n)_0 \frac{\exp\left(\frac{W}{L_n}\right)}{\exp\left(\frac{W}{L_n}\right) - \exp\left(-\frac{W}{L_n}\right)}$$

$$B = (\Delta n)_0 \frac{\exp\left(-\frac{W}{L_n}\right)}{\exp\left(\frac{W}{L_n}\right) - \exp\left(-\frac{W}{L_n}\right)}$$

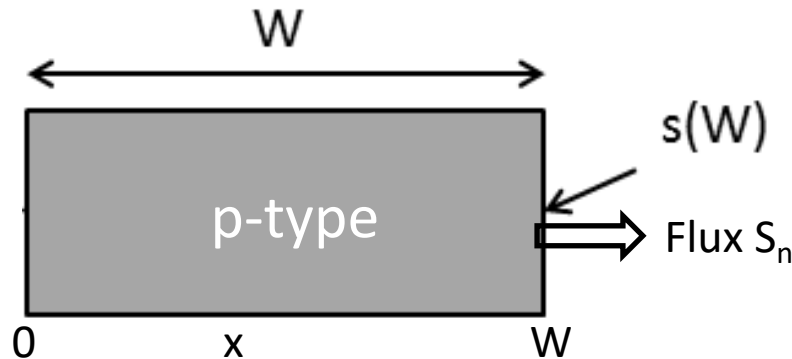
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$$0 = D_n \frac{\partial^2 \Delta n}{\partial x^2} - \frac{\Delta n}{\tau} \quad \Rightarrow \Delta n = A \exp\left(-\frac{x}{L_n}\right) + B \exp\left(\frac{x}{L_n}\right)$$

$$\Delta n(x) = (\Delta n)_0 \frac{\text{sh}\left(\frac{W-x}{L_n}\right)}{\text{sh}\left(\frac{W}{L_n}\right)}$$

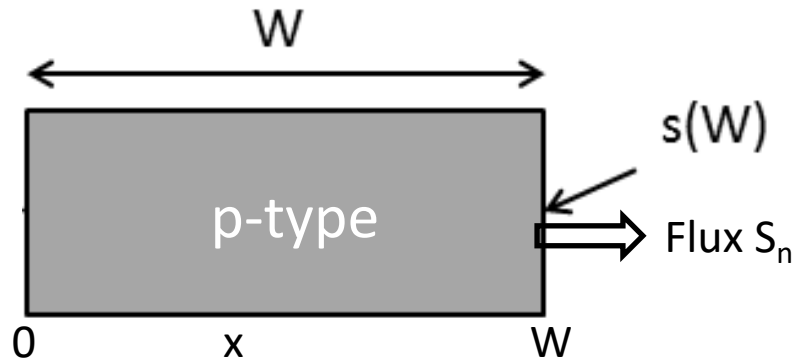
## 12.5 Quantitative analysis of BJT gain



$$0 = D_n \frac{\partial^2 \Delta n}{\partial x^2} - \frac{\Delta n}{\tau} \Rightarrow \Delta n = A \exp\left(-\frac{x}{L_n}\right) + B \exp\left(\frac{x}{L_n}\right)$$

$$\Delta n(x) = (\Delta n)_0 \frac{\text{sh}\left(\frac{W-x}{L_n}\right)}{\text{sh}\left(\frac{W}{L_n}\right)} \quad S_n = -D_n \frac{d\Delta n(x)}{dx} = \frac{D_n (\Delta n)_0}{L_n} \frac{\text{ch}\left(\frac{W-x}{L_n}\right)}{\text{sh}\left(\frac{W}{L_n}\right)}$$

## 12.5 Quantitative analysis of BJT gain

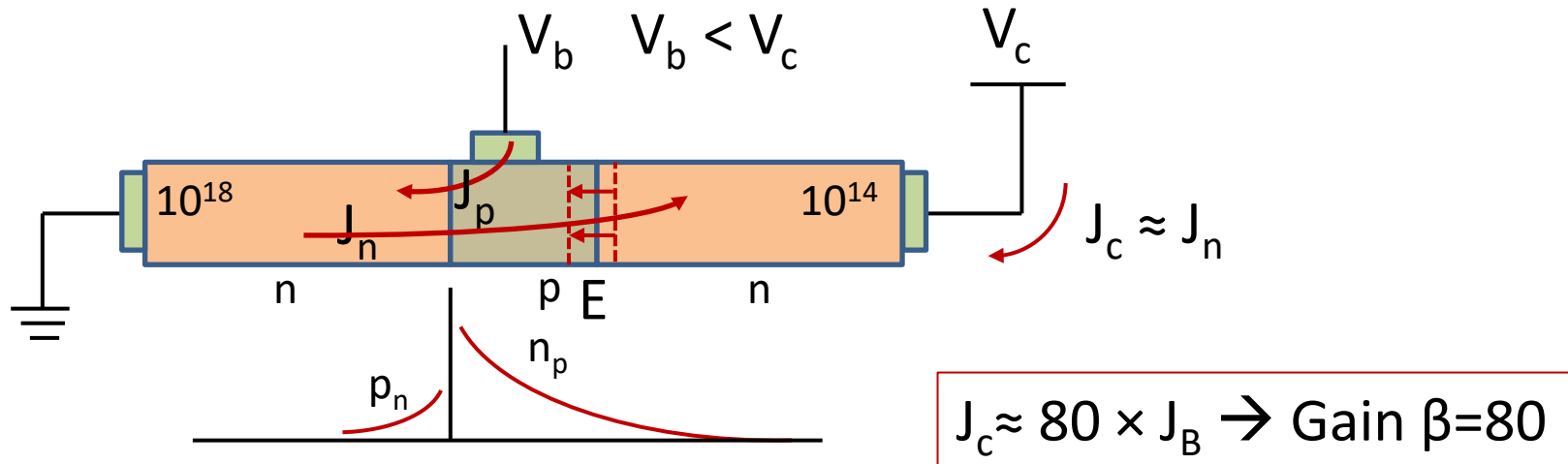


$$S_n = -D_n \frac{d\Delta n(x)}{dx} = \frac{D_n(\Delta n)_{B0}}{L_n} \frac{ch(\frac{W-x}{L_p})}{sh(\frac{W}{L_p})}$$

$$S_n(0) = \frac{D_n(\Delta n)_0}{L_n} \frac{ch(\frac{W}{L_p})}{sh(\frac{W}{L_p})}$$

$$S_n(W) = \frac{D_n(\Delta n)_0}{L_n} \frac{1}{sh(\frac{W}{L_p})}$$

## 12.5 Quantitative analysis of BJT gain

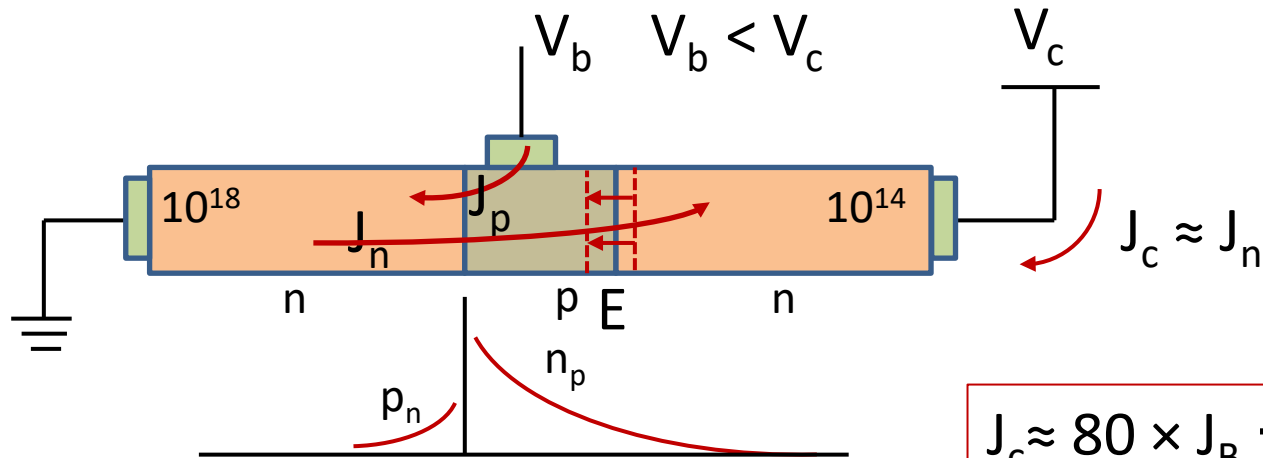


$$S_n(0) = \frac{D_B \cdot (\Delta n)_{B0}}{L_B} \frac{ch(\frac{W}{L_B})}{sh(\frac{W}{L_B})} \quad S_n(W_b) = \frac{D_B \cdot (\Delta n)_{B0}}{L_B} \frac{1}{sh(\frac{W}{L_B})}$$

Electron flux from emitter to base:  $S_n(0)$

Electron flux from base to collector:  $S_n(W_b)$

# 12.5 Quantitative analysis of BJT gain



$$S_n(0) = \frac{D_B(\Delta n)_{B0}}{L_B} \frac{ch(\frac{W}{L_B})}{sh(\frac{W}{L_B})}$$

$$S_n(W_b) = \frac{D_B(\Delta n)_{B0}}{L_B} \frac{1}{sh(\frac{W}{L_B})}$$

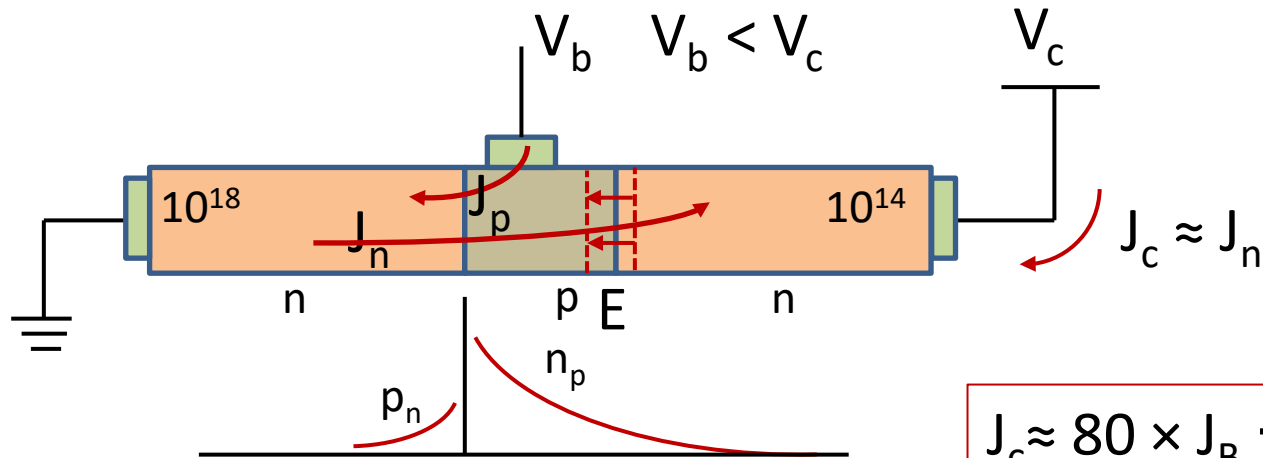
Electron flux from emitter to base:  $S_n(0)$

Electron flux from base to collector:  $S_n(W_b)$

Hole flux from base to emitter:  $S_p$

$$S_p = D_E \frac{dp_E}{dx} = \frac{D_E p_{E0}}{L_E}$$

# 12.5 Quantitative analysis of BJT gain



$$J_c \approx 80 \times J_B \rightarrow \text{Gain } \beta = 80$$

$$S_n(0) = \frac{D_B(\Delta n)_{B0}}{L_B} \frac{ch(\frac{W}{L_B})}{sh(\frac{W}{L_B})}$$

$$S_n(W_b) = \frac{D_B(\Delta n)_{B0}}{L_B} \frac{1}{sh(\frac{W}{L_B})}$$

Electron flux from emitter to base:  $S_n(0)$

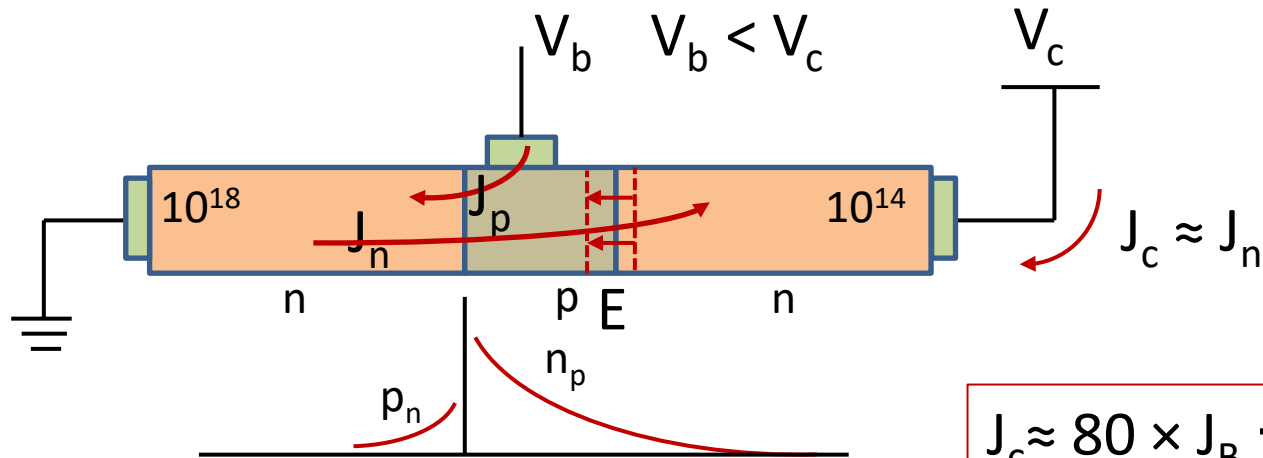
Electron flux from base to collector:  $S_n(W_b)$

Hole flux from base to emitter:  $S_p$

Base electrode flux:  $S_p + S_n(0) - S_n(W_b)$

$$S_p = D_E \frac{dp_E}{dx} = \frac{D_E p_{E0}}{L_E}$$

# 12.5 Quantitative analysis of BJT gain



$$J_c \approx 80 \times J_B \rightarrow \text{Gain } \beta = 80$$

$$S_n(0) = \frac{D_B(\Delta n)_{B0}}{L_B} \frac{ch(\frac{W}{L_B})}{sh(\frac{W}{L_B})} \quad S_n(W_b) = \frac{D_B(\Delta n)_{B0}}{L_B} \frac{1}{sh(\frac{W}{L_B})}$$

Electron flux from emitter to base:  $S_n(0)$

Electron flux from base to collector:  $S_n(W_b)$

Hole flux from base to emitter:  $S_p$

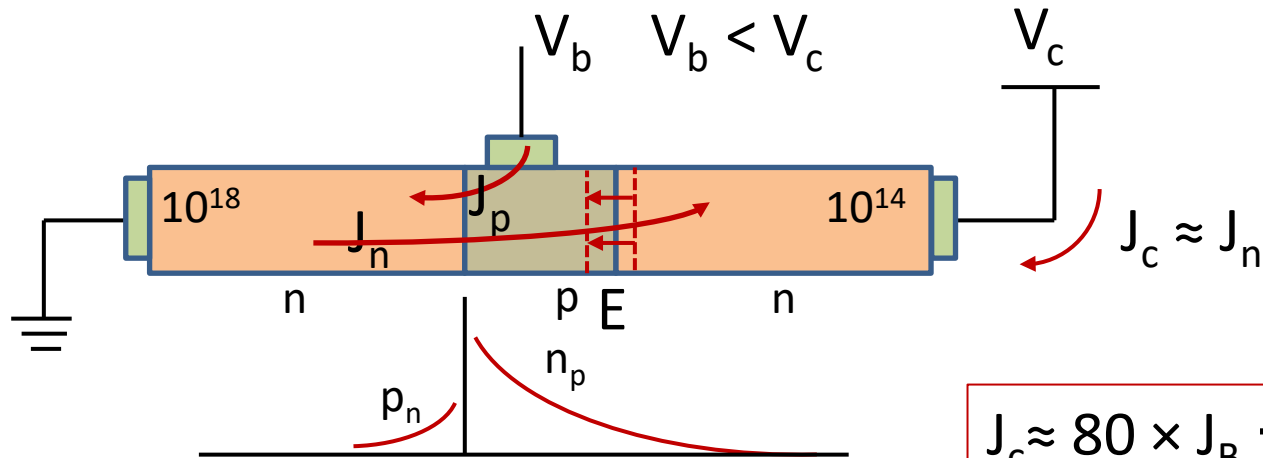
Base electrode flux:  $S_p + S_n(0) - S_n(W_b)$

Gain  $\beta$  = collector flux / base electrode flux =  $S_n(W_b) / (S_p + S_n(0) - S_n(W_b))$

$$S_p = D_E \frac{dp_E}{dx} = \frac{D_E p_{E0}}{L_E}$$



# 12.5 Quantitative analysis of BJT gain

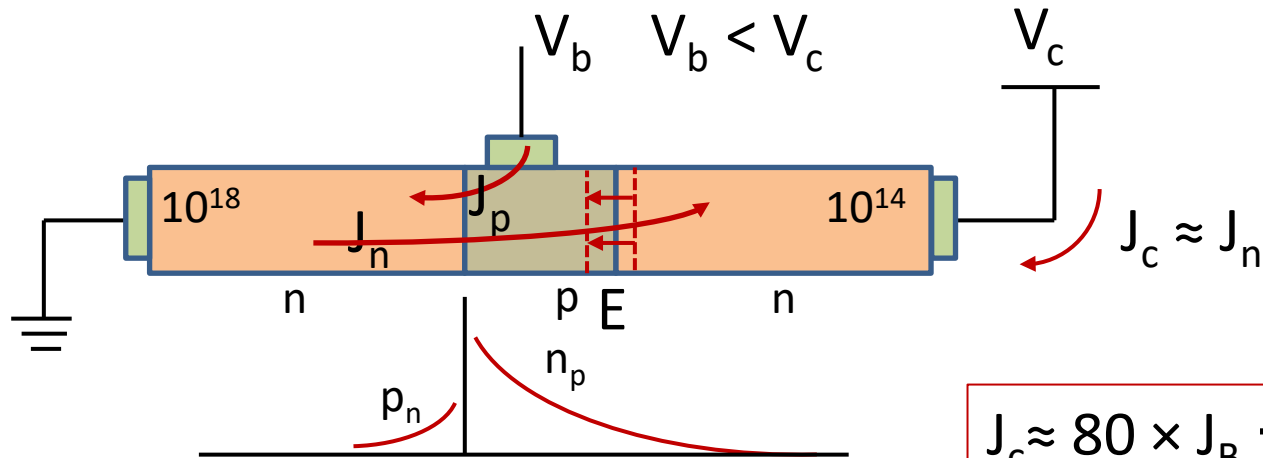


$$J_c \approx 80 \times J_B \rightarrow \text{Gain } \beta = 80$$

$$S_n(0) = \frac{D_B(\Delta n)_{B0}}{L_B} \frac{ch(\frac{W}{L_B})}{sh(\frac{W}{L_B})} \quad S_n(W_b) = \frac{D_B(\Delta n)_{B0}}{L_B} \frac{1}{sh(\frac{W}{L_B})}$$

$$\beta = \frac{\frac{D_B(\Delta n)_{B0}}{L_B} \frac{1}{sh(\frac{W}{L_B})}}{\frac{D_E(\Delta p)_{E0}}{L_E} + \frac{D_B(\Delta n)_{B0}}{L_B} \frac{ch(\frac{W}{L_B})}{sh(\frac{W}{L_B})} - \frac{D_B(\Delta n)_{B0}}{L_B} \frac{1}{sh(\frac{W}{L_B})}}$$

# 12.5 Quantitative analysis of BJT gain



$$J_c \approx 80 \times J_B \rightarrow \text{Gain } \beta = 80$$

$$S_n(0) = \frac{D_B(\Delta n)_{B0}}{L_B} \frac{ch(\frac{W}{L_p})}{sh(\frac{W}{L_p})} \quad S_n(W_b) = \frac{D_B(\Delta n)_{B0}}{L_B} \frac{1}{sh(\frac{W}{L_p})}$$

$$\beta = \frac{\frac{D_B(\Delta n)_{B0}}{L_B}}{\frac{D_E(\Delta p)_{E0}}{L_E} sh(\frac{W}{L_B}) + \frac{D_B(\Delta n)_{B0}}{L_B} [ch(\frac{W}{L_p}) - 1]}$$

## 12.5 Quantitative analysis of BJT gain

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$$\operatorname{sh}\left(\frac{W}{L_B}\right) = \frac{1}{2} \left[ \exp\left(\frac{W}{L_B}\right) - \exp\left(-\frac{W}{L_B}\right) \right]$$

$$\exp\left(\frac{W}{L_B}\right) = 1 + \frac{W}{L_B} + \frac{1}{2} \left(\frac{W}{L_B}\right)^2 + \dots$$

$$\exp\left(-\frac{W}{L_B}\right) = 1 - \frac{W}{L_B} + \frac{1}{2} \left(\frac{W}{L_B}\right)^2 - \dots$$

$$\beta = \frac{\frac{D_B(\Delta n)_{B0}}{L_B}}{\frac{D_E(\Delta p)_{E0}}{L_E} \operatorname{sh}\left(\frac{W}{L_B}\right) + \frac{D_B(\Delta n)_{B0}}{L_B} \left[ \operatorname{ch}\left(\frac{W}{L_p}\right) - 1 \right]}$$

## 12.5 Quantitative analysis of BJT gain

$$\operatorname{sh}\left(\frac{W}{L_B}\right) = \frac{1}{2} \left[ \exp\left(\frac{W}{L_B}\right) - \exp\left(-\frac{W}{L_B}\right) \right] = \frac{W}{L_B}$$

$$\begin{aligned} \exp\left(\frac{W}{L_B}\right) &= 1 + \frac{W}{L_B} + \frac{1}{2} \left(\frac{W}{L_B}\right)^2 + \dots \\ \exp\left(-\frac{W}{L_B}\right) &= 1 - \frac{W}{L_B} + \frac{1}{2} \left(\frac{W}{L_B}\right)^2 - \dots \end{aligned} \quad \begin{array}{l} \nearrow \\ \nearrow \end{array} \quad \text{if } \frac{W}{L_p} < 1$$

$$\beta = \frac{\frac{D_B(\Delta n)_{B0}}{L_B}}{\frac{D_E(\Delta p)_{E0}}{L_E} \operatorname{sh}\left(\frac{W}{L_B}\right) + \frac{D_B(\Delta n)_{B0}}{L_B} \left[ \operatorname{ch}\left(\frac{W}{L_p}\right) - 1 \right]}$$

## 12.5 Quantitative analysis of BJT gain

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$$\cosh\left(\frac{W}{L_B}\right) - 1 = \frac{1}{2} \left[ \exp\left(\frac{W}{L_B}\right) + \exp\left(-\frac{W}{L_B}\right) \right] - 1$$

$$\exp\left(\frac{W}{L_B}\right) = 1 + \frac{W}{L_B} + \frac{1}{2} \left(\frac{W}{L_B}\right)^2 + \dots$$

$$\exp\left(-\frac{W}{L_B}\right) = 1 - \frac{W}{L_B} + \frac{1}{2} \left(\frac{W}{L_B}\right)^2 - \dots$$

$$\beta = \frac{\frac{D_B(\Delta n)_{B0}}{L_B}}{\frac{D_E(\Delta p)_{E0}}{L_E} \frac{W}{L_B} + \frac{D_B(\Delta n)_{B0}}{L_B} \left[ \cosh\left(\frac{W}{L_B}\right) - 1 \right]}$$

## 12.5 Quantitative analysis of BJT gain

$$\cosh\left(\frac{W}{L_B}\right) - 1 = \frac{1}{2} \left[ \exp\left(\frac{W}{L_B}\right) + \exp\left(-\frac{W}{L_B}\right) \right] - 1 = \frac{1}{2} \left(\frac{W}{L_B}\right)^2$$

$$\exp\left(\frac{W}{L_B}\right) = 1 + \frac{W}{L_B} + \frac{1}{2} \left(\frac{W}{L_B}\right)^2 + \dots$$

$$\exp\left(-\frac{W}{L_B}\right) = 1 - \frac{W}{L_B} + \frac{1}{2} \left(\frac{W}{L_B}\right)^2 - \dots$$

if  $\frac{W}{L_B} < 1$

$$\beta = \frac{\frac{D_B(\Delta n)_{B0}}{L_B}}{\frac{D_E(\Delta p)_{E0}}{L_E} \frac{W}{L_B} + \frac{D_B(\Delta n)_{B0}}{L_B} \left[ \frac{1}{2} \left(\frac{W}{L_B}\right)^2 \right]}$$

## 12.5 Quantitative analysis of BJT gain

$$\cosh\left(\frac{W}{L_B}\right) - 1 = \frac{1}{2} \left[ \exp\left(\frac{W}{L_B}\right) + \exp\left(-\frac{W}{L_B}\right) \right] - 1 = \frac{1}{2} \left(\frac{W}{L_B}\right)^2$$

$$\exp\left(\frac{W}{L_B}\right) = 1 + \frac{W}{L_B} + \frac{1}{2} \left(\frac{W}{L_B}\right)^2 + \dots$$

$$\exp\left(-\frac{W}{L_B}\right) = 1 - \frac{W}{L_B} + \frac{1}{2} \left(\frac{W}{L_B}\right)^2 - \dots$$

if  $\frac{W}{L_B} < 1$

$$\beta = \frac{\frac{D_B(\Delta n)_{B0}}{L_B}}{\frac{D_E(\Delta p)_{E0}}{L_E} \frac{W}{L_B} + \frac{D_B(\Delta n)_{B0}}{L_B} \left[ \frac{1}{2} \left(\frac{W}{L_B}\right)^2 \right]} = \frac{1}{\frac{D_E(\Delta p)_{E0} W}{D_B(\Delta n)_{B0} L_E} + \frac{1}{2} \left(\frac{W}{L_B}\right)^2}$$

## 12.5 Quantitative analysis of BJT gain

$$\cosh\left(\frac{W}{L_B}\right) - 1 = \frac{1}{2} \left[ \exp\left(\frac{W}{L_B}\right) + \exp\left(-\frac{W}{L_B}\right) \right] - 1 = \frac{1}{2} \left(\frac{W}{L_B}\right)^2$$

$$\exp\left(\frac{W}{L_B}\right) = 1 + \frac{W}{L_B} + \frac{1}{2} \left(\frac{W}{L_B}\right)^2 + \dots$$

$$\exp\left(-\frac{W}{L_B}\right) = 1 - \frac{W}{L_B} + \frac{1}{2} \left(\frac{W}{L_B}\right)^2 - \dots$$

if  $\frac{W}{L_B} < 1$

$$\beta = \frac{1}{\frac{N_B D_E W}{N_E D_B L_E} + \frac{1}{2} \left(\frac{W}{L_B}\right)^2}$$



## 12.5 Quantitative analysis of BJT gain

$$\cosh\left(\frac{W}{L_B}\right) - 1 = \frac{1}{2} \left[ \exp\left(\frac{W}{L_B}\right) + \exp\left(-\frac{W}{L_B}\right) \right] - 1 = \frac{1}{2} \left(\frac{W}{L_B}\right)^2$$

$$\exp\left(\frac{W}{L_B}\right) = 1 + \frac{W}{L_B} + \frac{1}{2} \left(\frac{W}{L_B}\right)^2 + \dots$$

$$\exp\left(-\frac{W}{L_B}\right) = 1 - \frac{W}{L_B} + \frac{1}{2} \left(\frac{W}{L_B}\right)^2 - \dots$$

if  $\frac{W}{L_B} < 1$

$$\beta = \frac{1}{\frac{N_B D_E W}{N_E D_B L_E} + \frac{1}{2} \left(\frac{W}{L_B}\right)^2}$$

$$\beta = S_n(W_b) / (S_p + S_n(0) - S_n(W_b))$$

# Outline

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12.1 Review and example

12.2 Bipolar Junction transistor

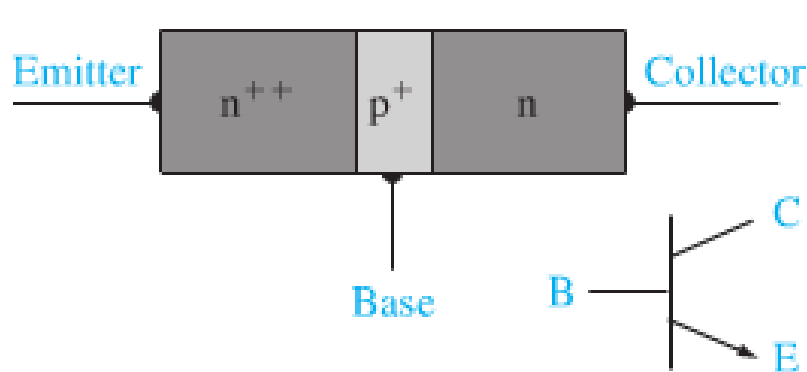
12.3 Early Effect

12.4 Summary

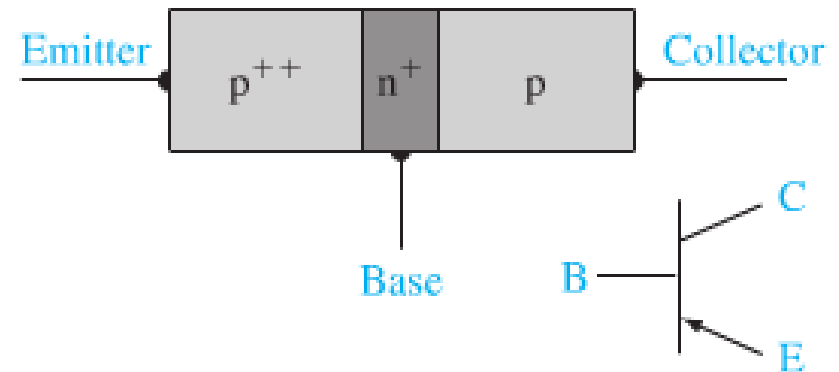
12.5 Quantitative analysis of BJT gain

**12.6 BJT symbols and planar device structure**

## 12.6 BJT symbols and planar device structure

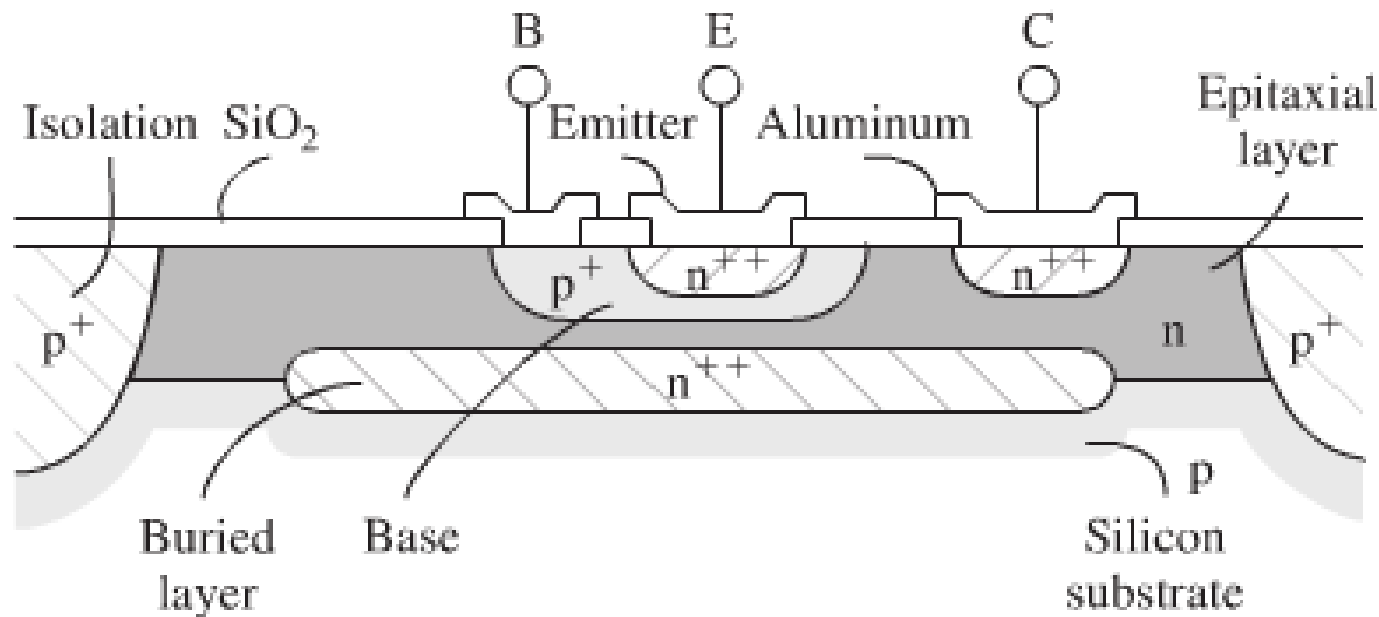


(a)



(b)

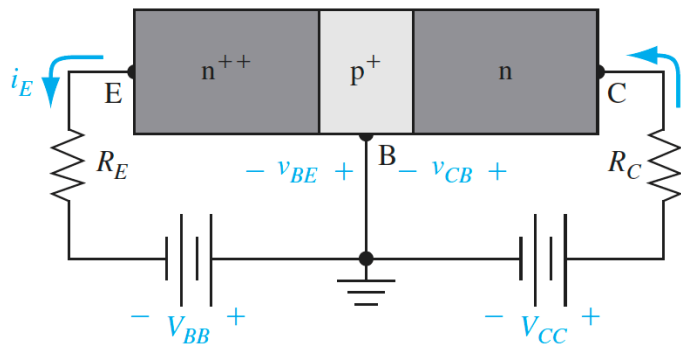
## 12.6 BJT symbols and planar device structure



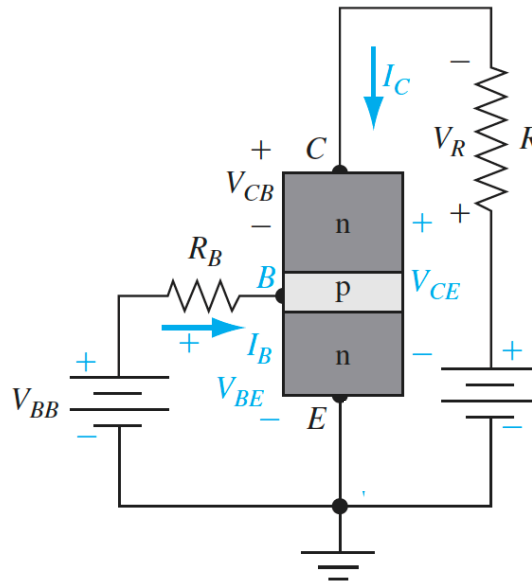
Conventional npn transistor

# 12.7 BJT symbols and planar device structure

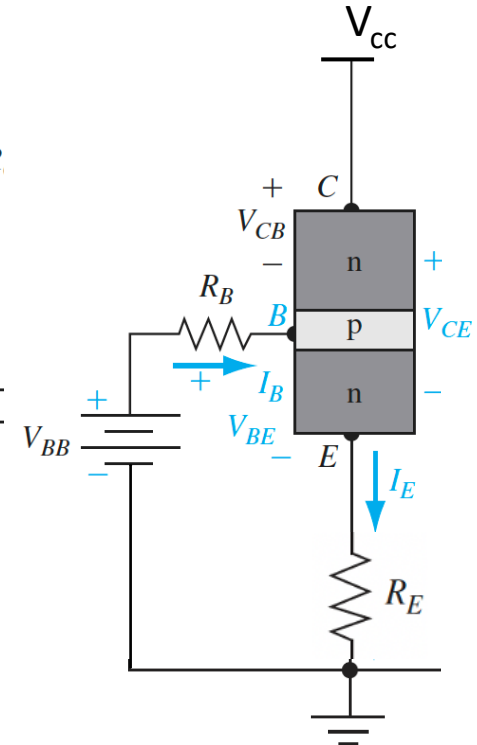
The basic principle of operation



Common base



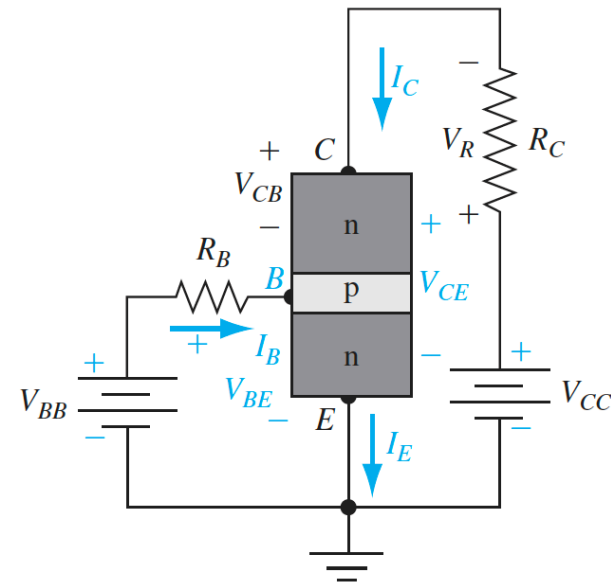
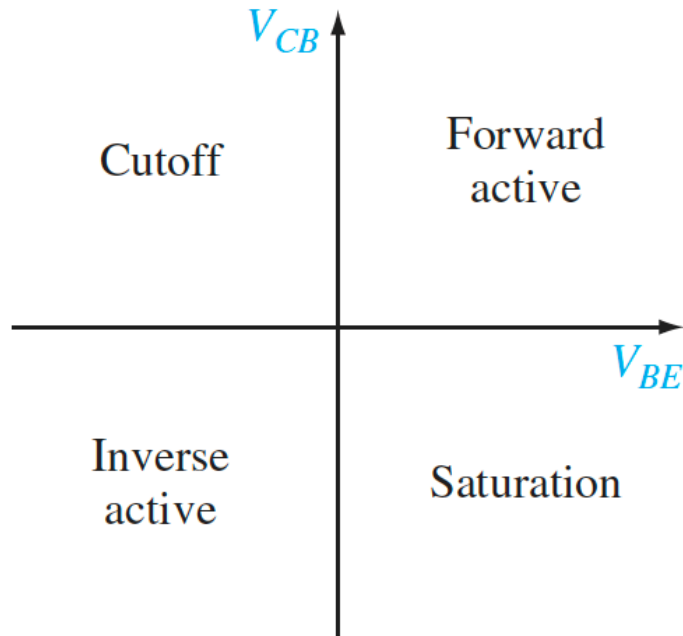
Common emitter



Common collector

# 12.7 BJT symbols and planar device structure

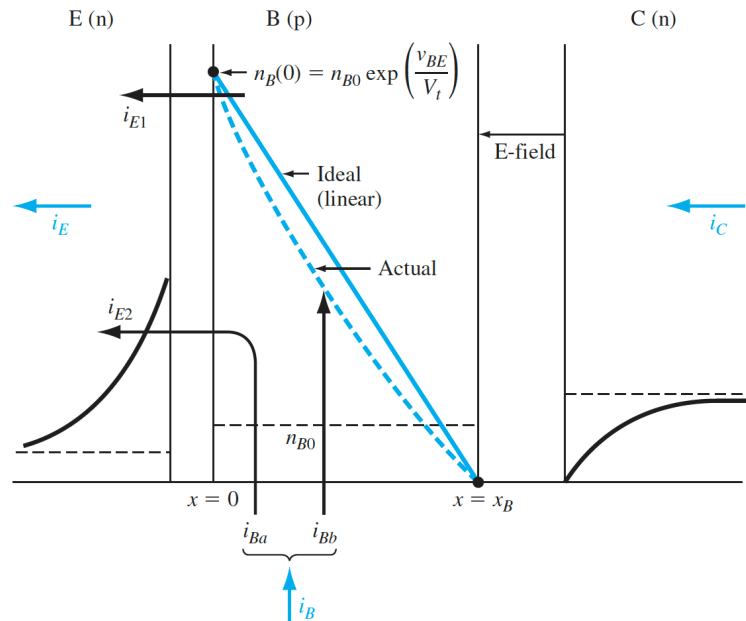
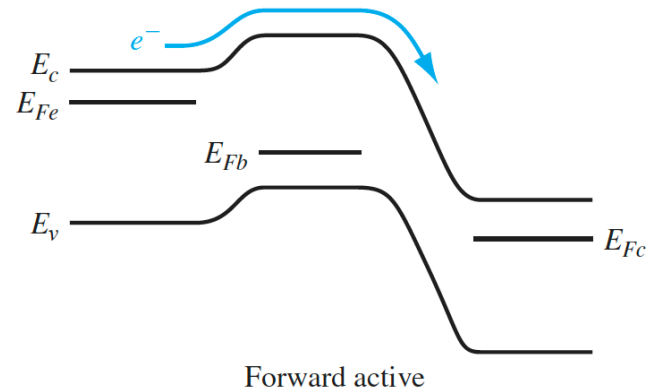
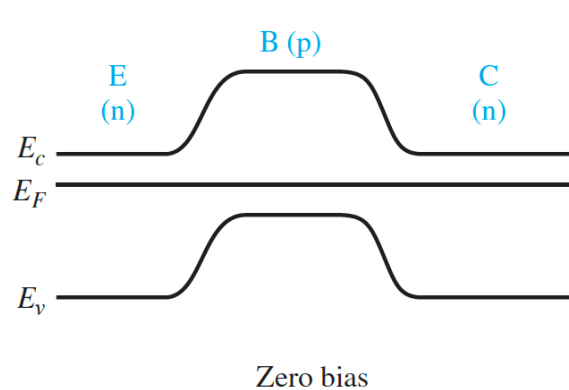
The basic principle of operation



Common emitter

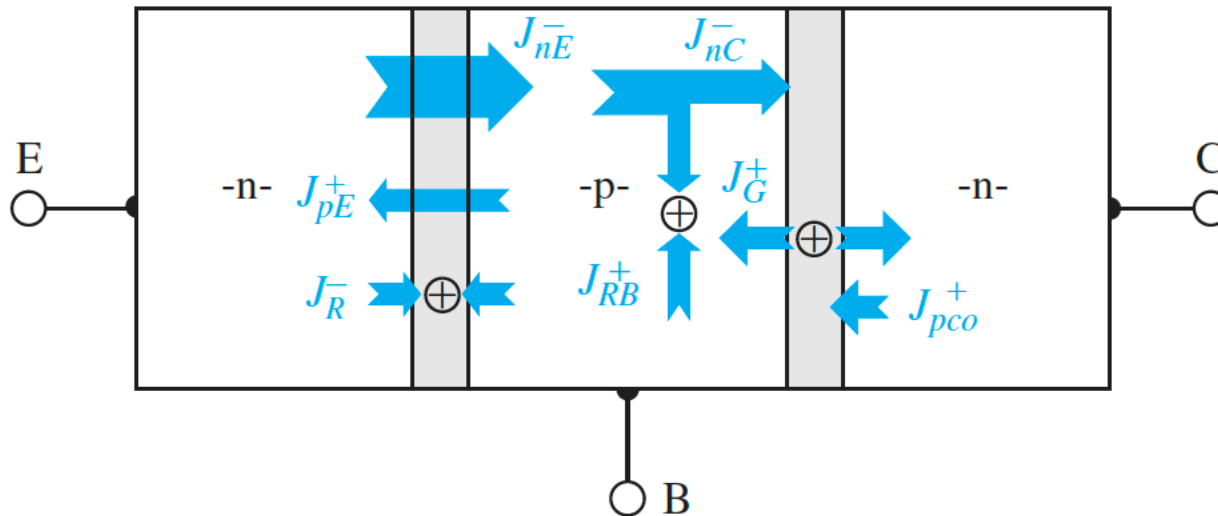
## 12.7 BJT symbols and planar device structure

## The basic principle of operation



## 12.7 BJT symbols and planar device structure

The basic principle of operation



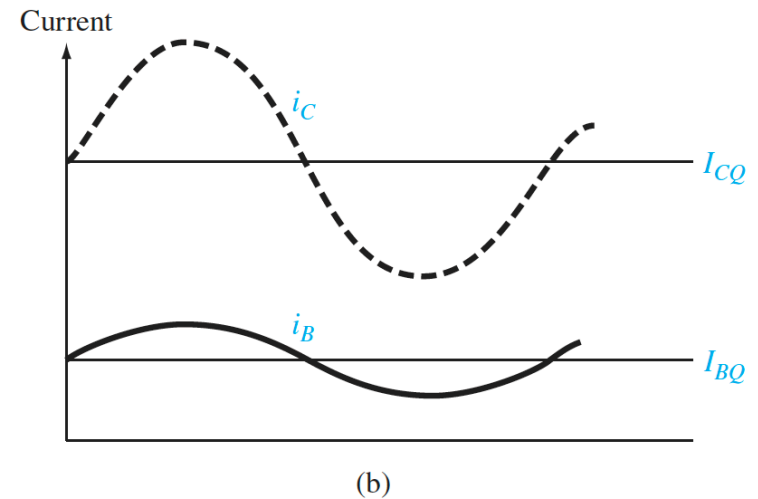
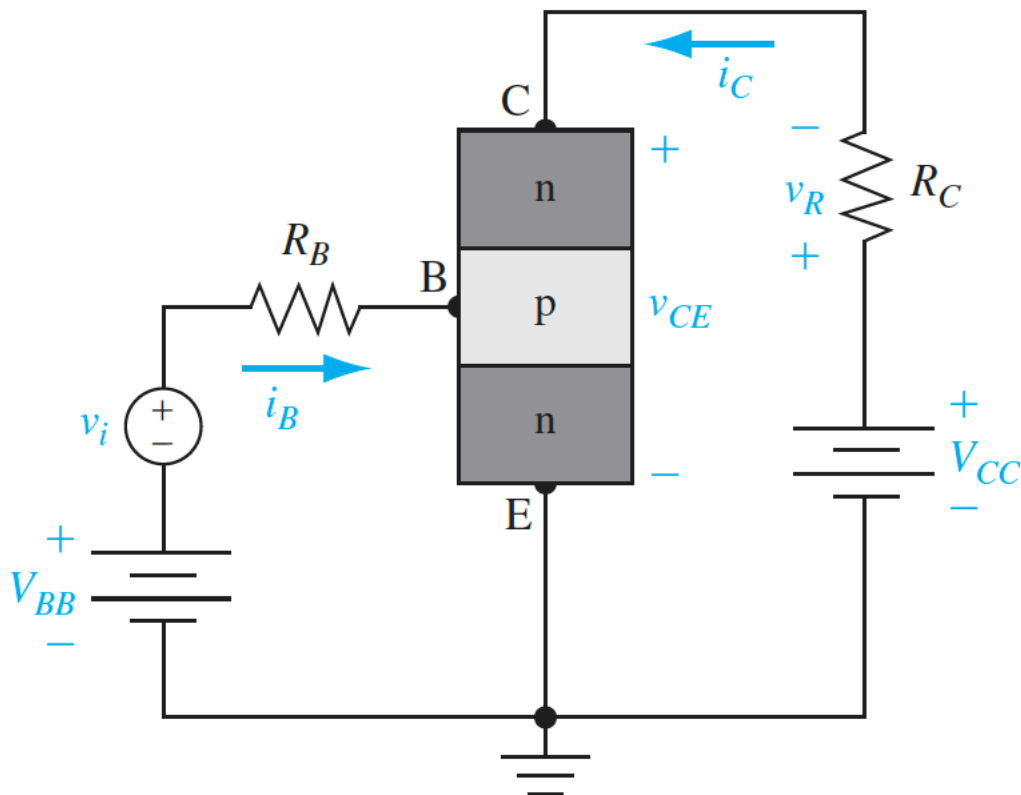
$$\alpha_0 = \frac{I_C}{I_E}$$

$$\alpha_0 = \frac{J_C}{J_E} = \frac{J_{nC} + J_G + J_{pC0}}{J_{nE} + J_R + J_{pE}}$$



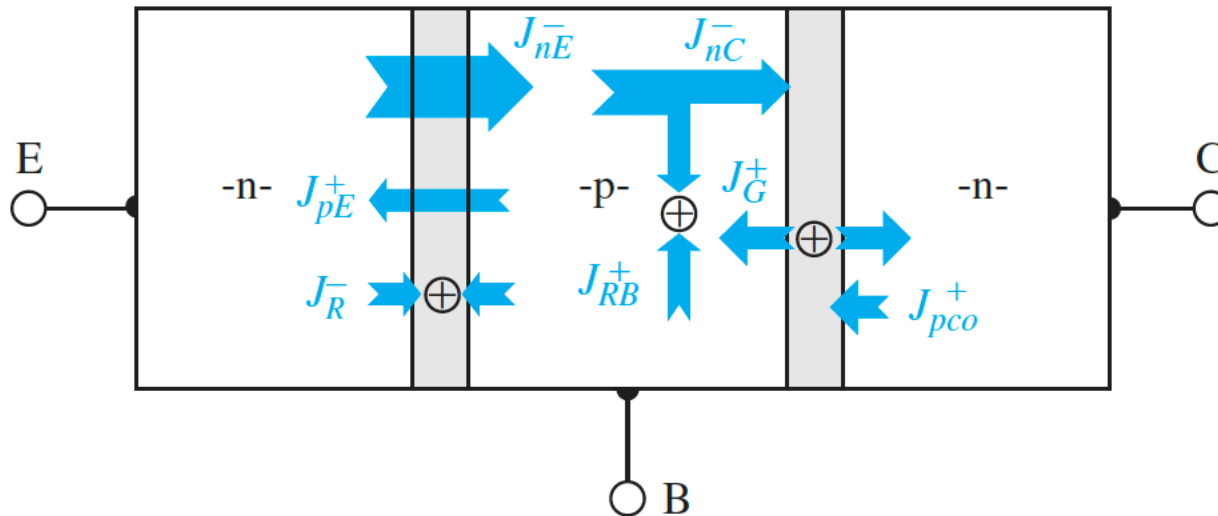
# 12.7 BJT symbols and planar device structure

The basic principle of operation



# 12.7 BJT symbols and planar device structure

The basic principle of operation



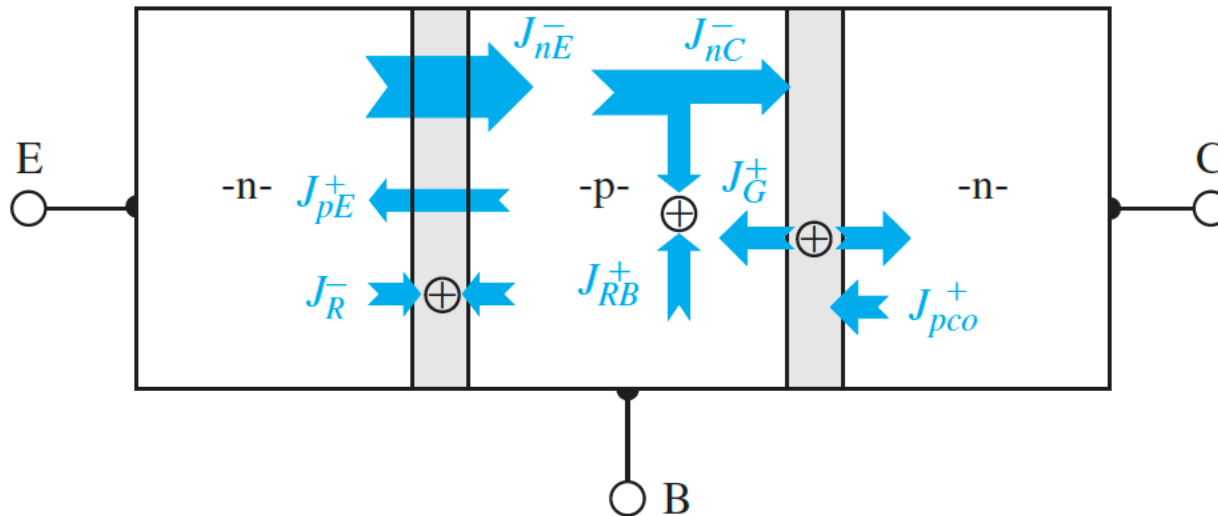
$$\alpha_0 = \frac{I_C}{I_E}$$

$$\alpha_0 = \frac{J_C}{J_E} = \frac{J_{nC} + J_G + J_{pc0}}{J_{nE} + J_R + J_{pE}}$$

$$\alpha = \frac{\partial J_C}{\partial J_E} = \frac{J_{nC}}{J_{nE} + J_R + J_{pE}}$$

# 12.7 BJT symbols and planar device structure

The basic principle of operation

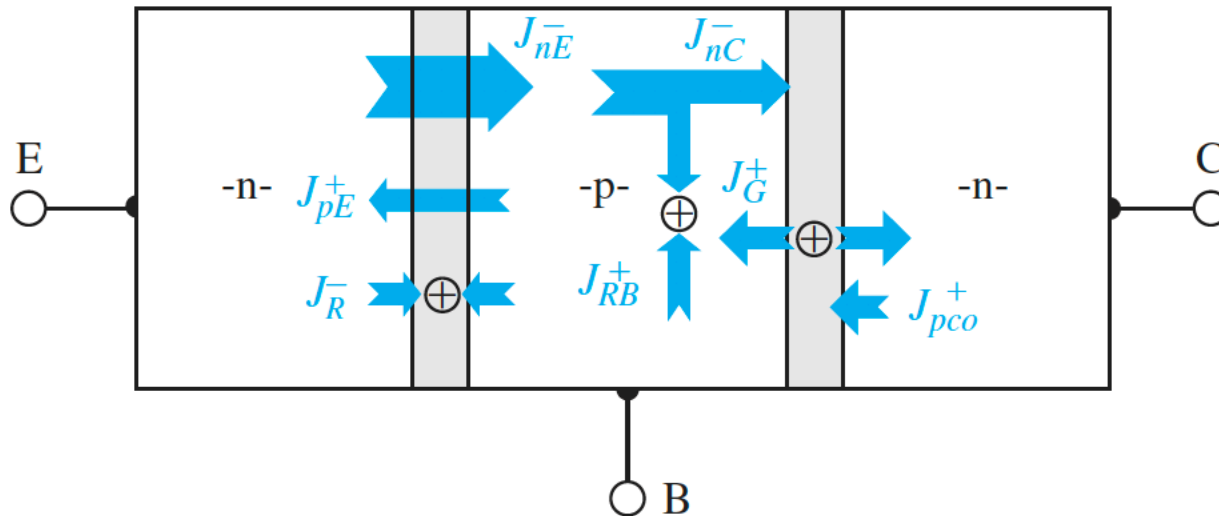


$$\alpha = \frac{\partial J_C}{\partial J_E} = \frac{J_{nC}}{J_{nE} + J_R + J_{pE}}$$

$$\alpha = \left( \frac{J_{nE}}{J_{nE} + J_{pE}} \right) \left( \frac{J_{nC}}{J_{nE}} \right) \left( \frac{J_{nE} + J_{pE}}{J_{nE} + J_R + J_{pE}} \right)$$

# 12.7 BJT symbols and planar device structure

The basic principle of operation



$$\gamma = \left( \frac{J_{nE}}{J_{nE} + J_{pE}} \right) \equiv \text{emitter injection efficiency factor}$$

$$\alpha_T = \left( \frac{J_{nC}}{J_{nE}} \right) \equiv \text{base transport factor}$$

$$\delta = \frac{J_{nE} + J_{pE}}{J_{nE} + J_R + J_{pE}} \equiv \text{recombination factor}$$