

Midterm 2 Review

Teaching Assistant
Xie Jinglei



DC circuits

DC circuits

Kirchhoff's Rules

Kirchhoff's junction rule
(valid at any junction):

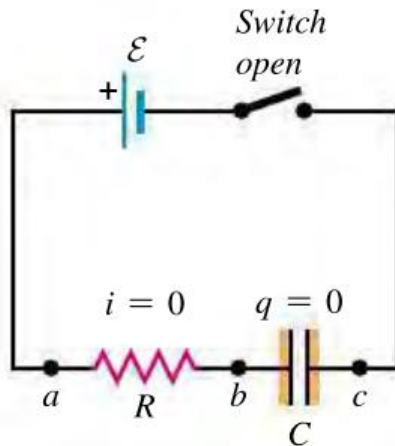
The sum of the currents into any junction ...
 $\sum I = 0$... equals zero.

Kirchhoff's loop rule
(valid for any closed loop):

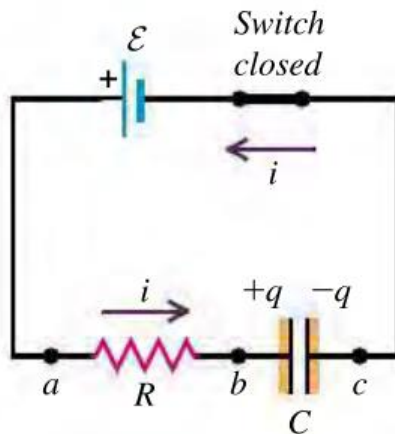
The sum of the potential differences around any loop ...
 $\sum V = 0$... equals zero.

RC circuits

(a) Capacitor initially uncharged



(b) Charging the capacitor



When the switch is closed, the charge on the capacitor increases over time while the current decreases.

R-C circuit, charging capacitor:

$$i = \frac{dq}{dt} = \frac{\mathcal{E}}{R} e^{-t/RC} = I_0 e^{-t/RC}$$

Current: i
 Battery emf: \mathcal{E}
 Time since switch closed: t
 Resistance: R
 Capacitance: C
 Rate of change of capacitor charge: $\frac{dq}{dt}$
 Initial current: $I_0 = \mathcal{E}/R$

R-C circuit, discharging capacitor:

$$i = \frac{dq}{dt} = -\frac{Q_0}{RC} e^{-t/RC} = I_0 e^{-t/RC}$$

Current: i
 Initial capacitor charge: Q_0
 Capacitance: C
 Time since switch closed: t
 Resistance: R
 Rate of change of capacitor charge: $\frac{dq}{dt}$
 Initial current: $I_0 = -Q_0/RC$

Energy:

50% -> resistor

50% -> capacitor

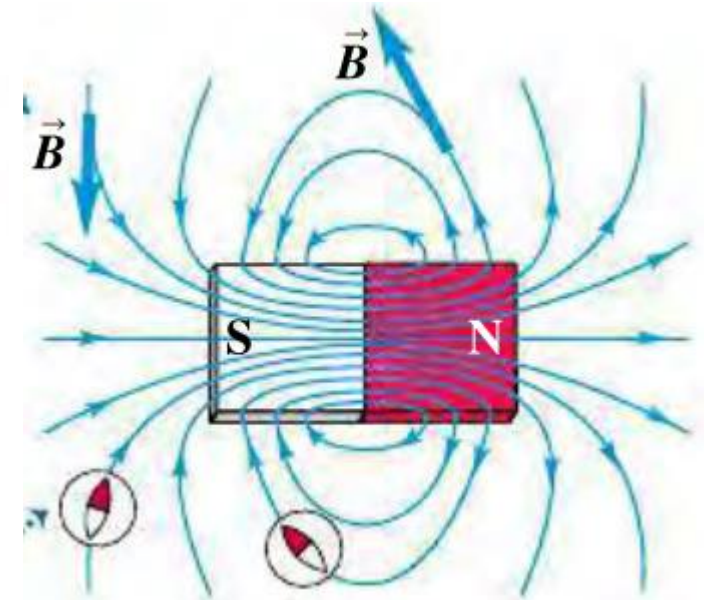
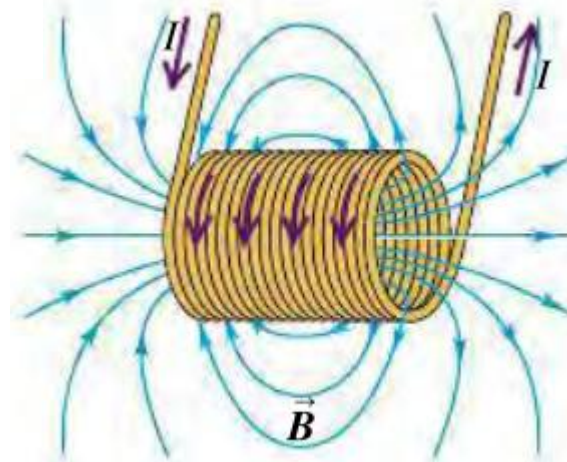
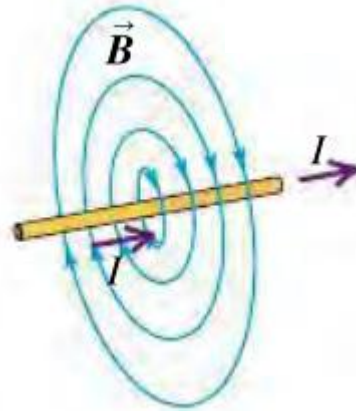
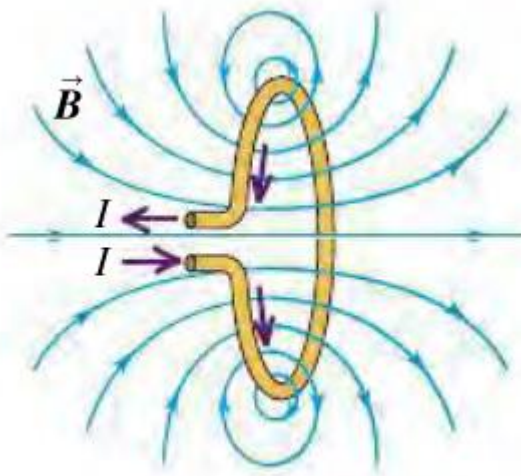
Refer to lecture notes



Magnetic field and magnetic forces

Magnetic field and magnetic forces

➤ Important models



Magnetic field and magnetic forces

Magnetic force on a moving charged particle

$$\vec{F} = q\vec{v} \times \vec{B}$$

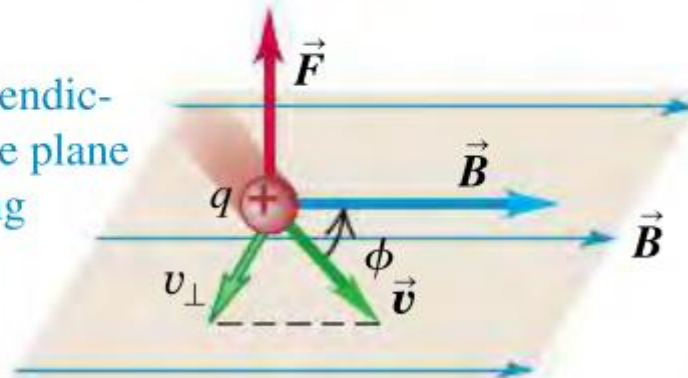
Particle's charge

Magnetic field

Particle's velocity

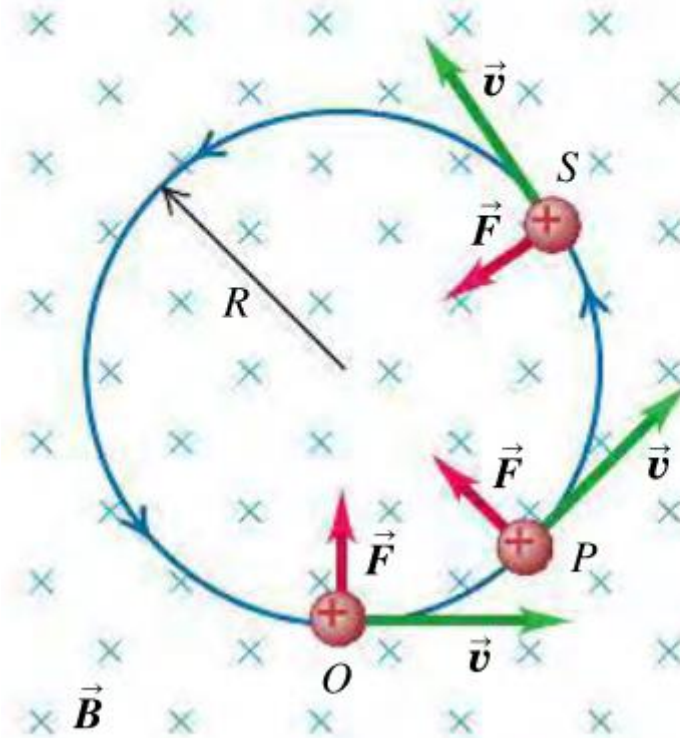
A charge moving at an angle ϕ to a magnetic field experiences a magnetic force with magnitude $F = |q|v_{\perp}B = |q|vB \sin \phi$.

\vec{F} is perpendicular to the plane containing \vec{v} and \vec{B} .

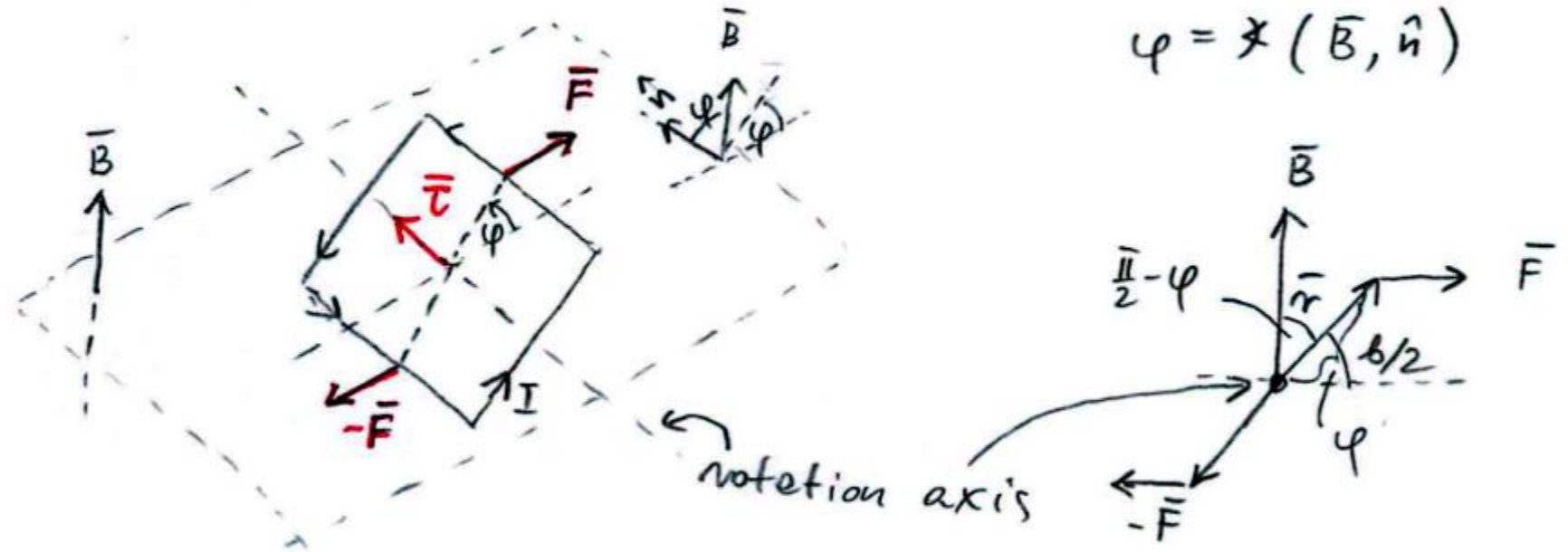
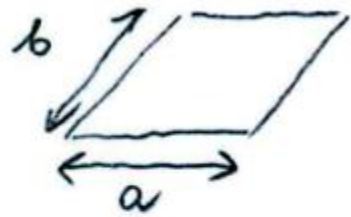


Magnetic field and magnetic forces

A charge moving at right angles to a uniform \vec{B} field moves in a circle at constant speed because \vec{F} and \vec{v} are always perpendicular to each other.



Magnetic field and magnetic forces

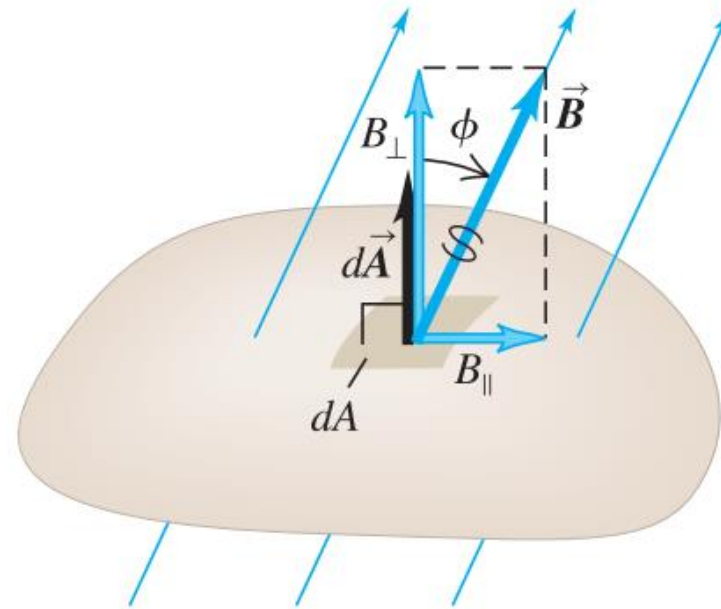


Magnetic field and magnetic forces

Gauss's law for magnetism:

The total magnetic flux through *any* closed surface ...

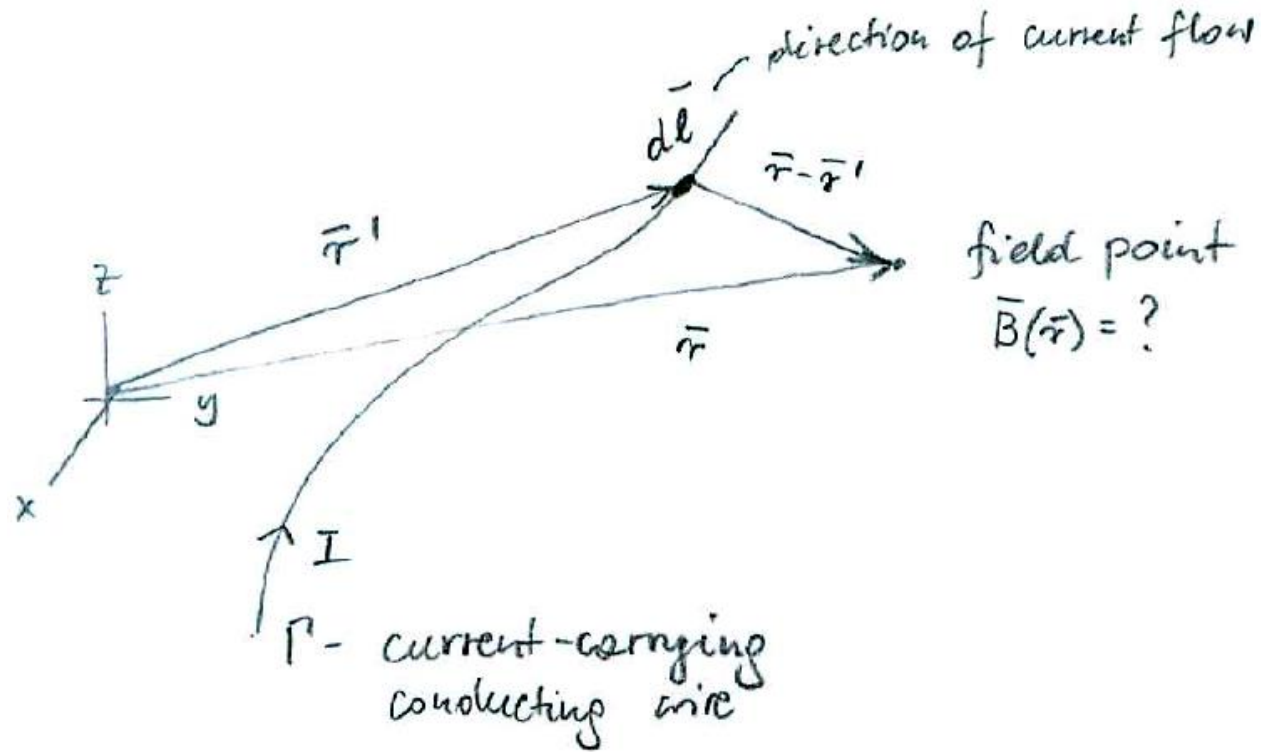
$$\oint \vec{B} \cdot d\vec{A} = 0 \quad \dots \text{equals zero.}$$





Sources of magnetic field

Sources of magnetic field



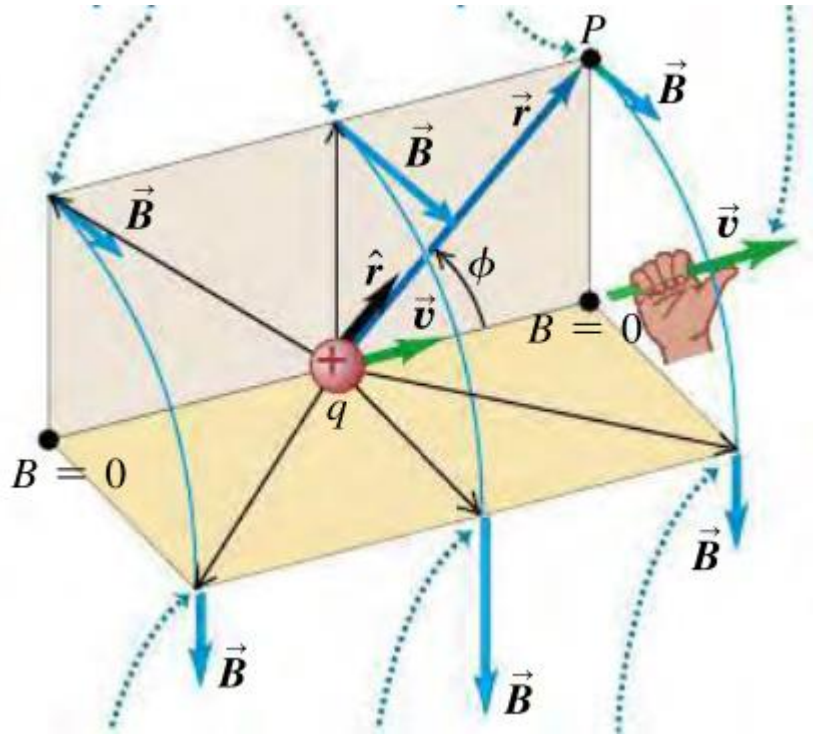
$$d\vec{l} \times \frac{\vec{r}-\vec{r}'}{|\vec{r}-\vec{r}'|^3} \otimes d\vec{B}$$

$$\vec{B}(\vec{r}) = \frac{\mu_0}{4\pi} \int \frac{I d\vec{l} \times (\vec{r}-\vec{r}')}{|\vec{r}-\vec{r}'|^3} =$$

$$= \frac{\mu_0}{4\pi} \int \frac{I d\vec{l} \times \left(\frac{\vec{r}-\vec{r}'}{|\vec{r}-\vec{r}'|} \right)}{|\vec{r}-\vec{r}'|^2} \rightarrow \text{unit vector}$$

Law of Biot and Savart

Sources of magnetic field



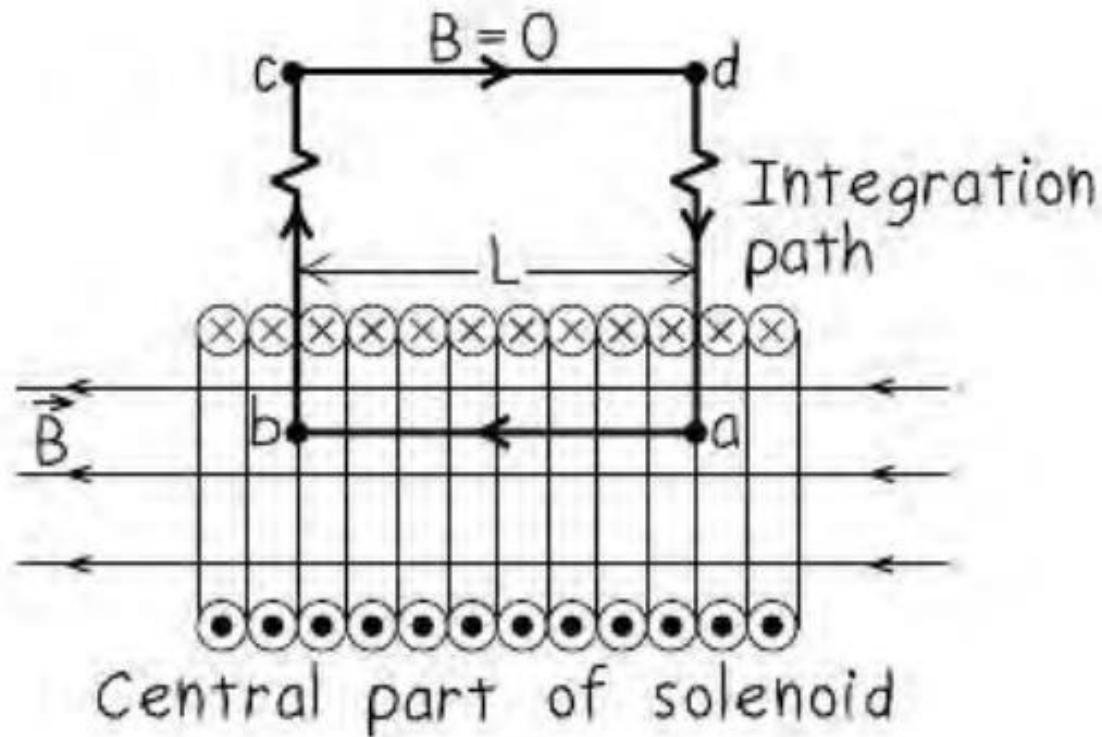
Magnetic field due to a point charge with constant velocity

$$\vec{B} = \frac{\mu_0}{4\pi} \frac{q\vec{v} \times \hat{r}}{r^2}$$

Magnetic constant Charge Velocity Unit vector from point charge toward where field is measured Distance from point charge to where field is measured

(* Not mentioned in lecture notes)

Sources of magnetic field



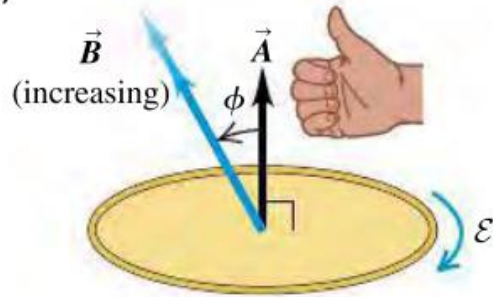
Solenoid: n turns
per unit length



Electromagnetic induction

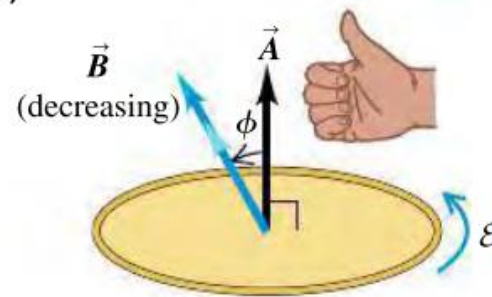
Electromagnetic induction

(a)



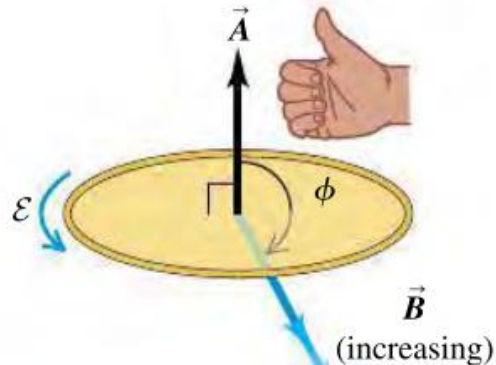
- Flux is positive ($\Phi_B > 0$) ...
- ... and becoming more positive ($d\Phi_B/dt > 0$).
- Induced emf is negative ($\mathcal{E} < 0$).

(b)



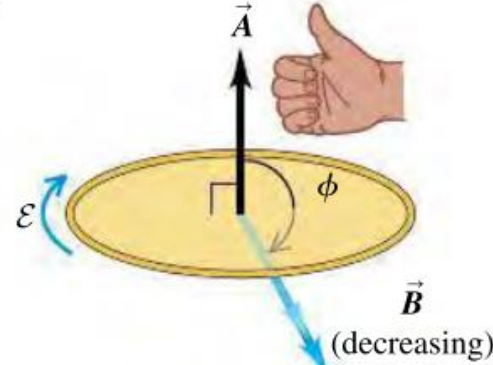
- Flux is positive ($\Phi_B > 0$) ...
- ... and becoming less positive ($d\Phi_B/dt < 0$).
- Induced emf is positive ($\mathcal{E} > 0$).

(c)



- Flux is negative ($\Phi_B < 0$) ...
- ... and becoming more negative ($d\Phi_B/dt < 0$).
- Induced emf is positive ($\mathcal{E} > 0$).

(d)



- Flux is negative ($\Phi_B < 0$) ...
- ... and becoming less negative ($d\Phi_B/dt > 0$).
- Induced emf is negative ($\mathcal{E} < 0$).

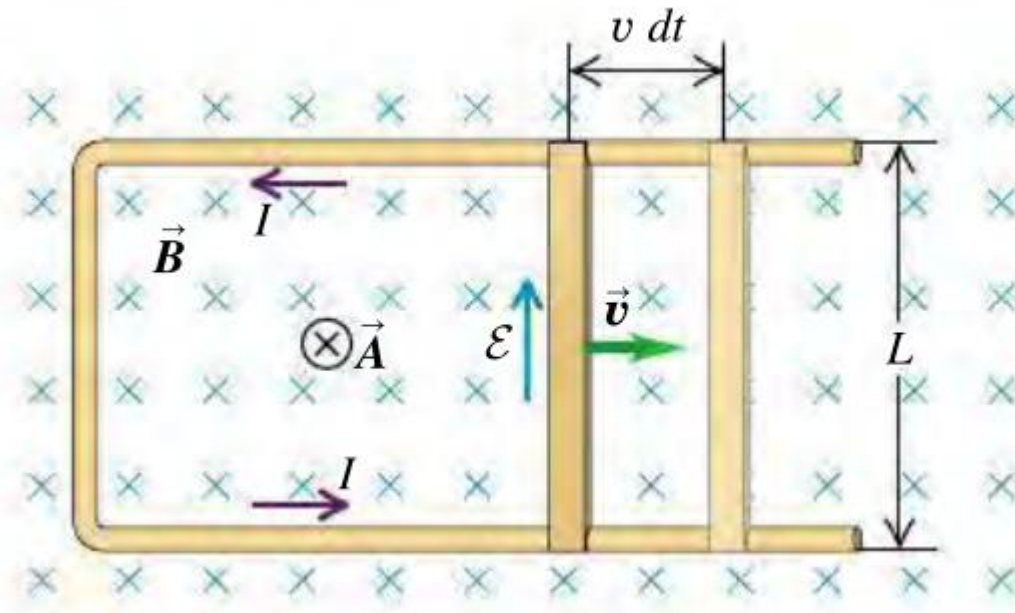
Magnetic field generated by induced EMF is in opposite direction to $d\Phi$

Lenz's Law

The direction of any magnetic induction effect is such as to oppose the cause of the effect.

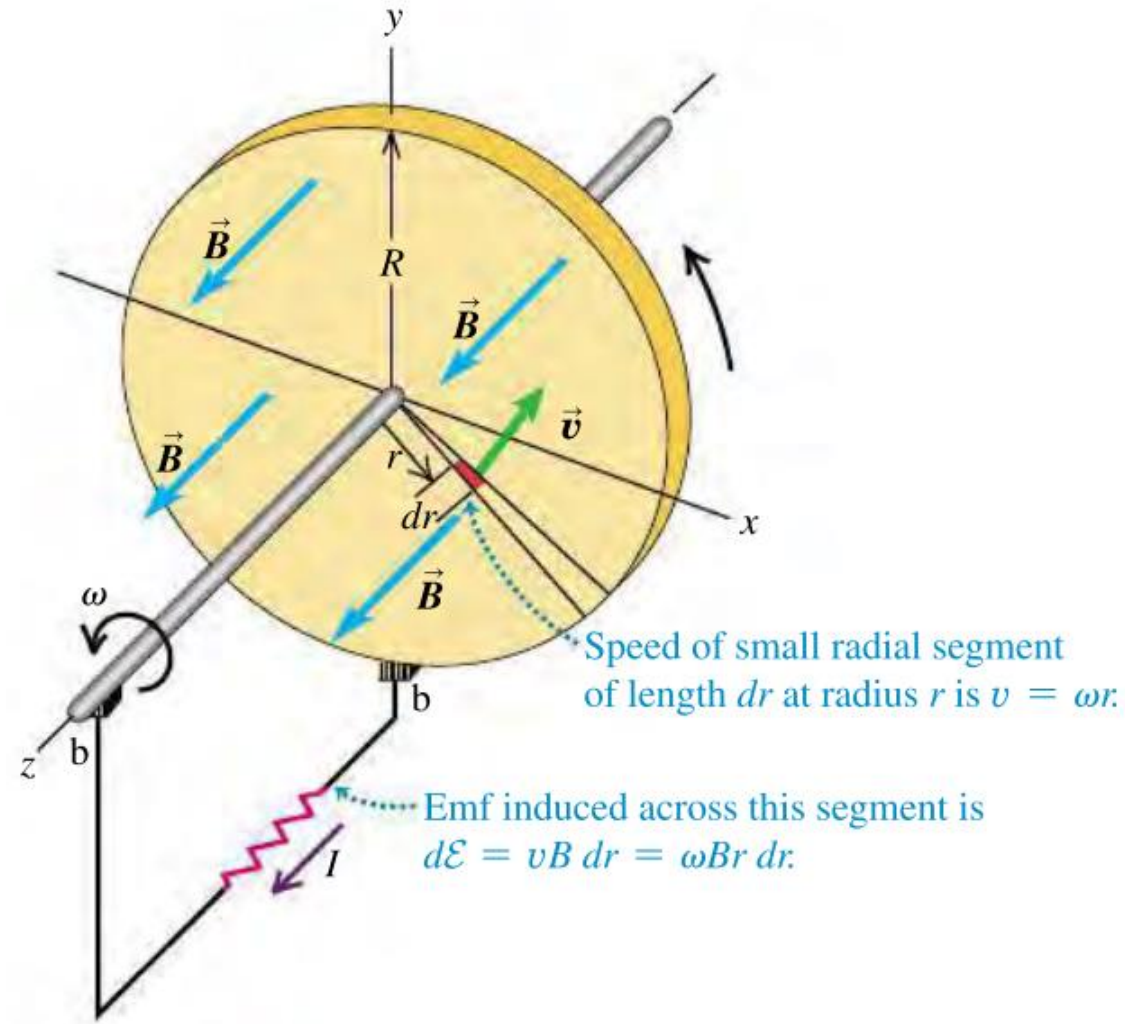


Slide-wire Generator



$$\begin{aligned}\mathcal{E} &= -\frac{d\Phi_B}{dt} = -B\frac{dA}{dt} \\ &= -B\frac{Lv\,dt}{dt} = -BLv\end{aligned}$$

Faraday's disk



Displacement Current

