DIFFRACTION (large) aperture opaque object Schen again, geometric optics fails Diffraction Interference VS large number of wavelets contribution few wovelets contribute (continuous distribution of point dounces) diffraction regimes of far-field (Fraunhofor) near-field F = size of aperture

wavelength x distance (Fresnel) aperture F>> 1 F21

Digression: wavelength vs. Altraction effects
Why do roolis waves propagate unhindered, whereas
for visible light an opaque object creates optical sheolow,

Single-slit diffraction Some polarietis, (Frounhofer) apertuse multiple discrete sources Interference from

$$\begin{cases} S_1 - \frac{r_1}{r_2} = \frac{r_1}{r_2} = \frac{r_2}{r_1} = \frac{r_1}{r_2} = \frac{r_2}{r_1} = \frac{r_2}{r_2} = \frac{r_1}{r_2} = \frac{r_2}{r_2} = \frac{r_2}{r_2} = \frac{r_1}{r_2} = \frac{r_2}{r_2} = \frac{r_2}$$

Note. Will use complex representation for amplitudes E (physical meaning E= Re E)

distance small Compared with wevelenoth

Amplitudes at P approximately equal $E_0(r_1) \approx E_0(r_2) \approx ... \approx E_0(r_N) \approx E_0(r_1)$

$$E_o(r_i) \approx E_o(r_i) \approx \dots \approx E_o(r_N) \approx E_o(r_i)$$

Net electric field at P (complex)

$$\widetilde{E} = E_{o}(r) e^{i(kr_{i} - \omega t)} + \overline{E}_{o}(r) e^{i(kr_{i} - \omega t)} + \dots + \overline{E}_{o}(r) e^{i(kr_{i} - \omega t)} = E_{o}(r) e^{i(kr_{i} - \omega t)} + E_{o}(r) e^{i(kr_{i} - \omega t)} + E_{o}(r) e^{i(kr_{i} - \omega t)} = E_{o}(r) e^{i(kr_{i} - \omega t)} + E_{o}(r) e^{i(kr_{i} - \omega t)} + E_{o}(r) e^{i(kr_{i} - \omega t)} + E_{o}(r) e^{i(kr_{i} - \omega t)} = E_{o}(r) e^{i(kr_{i} - \omega t)} + E_{o}(r) e^{i(kr_{i} - \omega t)} + E_{o}(r) e^{i(kr_{i} - \omega t)} = E_{o}(r) e^{i(kr_{i} - \omega t)} + E_{o}(r) e^{i(kr_{i} - \omega t)} = E_{o}(r) e^{i(kr_{i} - \omega t)} + E_{o}(r) e^$$

Phase difference for neighboring sources

e.g.
$$r_3 - r_1 = (r_3 - r_2) + (r_2 - r_1)$$

Denote kd Sino = 8

$$\widetilde{E} = E_{o}(r) e^{i(kr,-\omega t)} \left[1 + e^{i\delta} + (e^{i\delta})^{2} + \dots + (e^{i\delta})^{N-1} \right] =$$

$$= E_{o}(r) e^{i(kr,-\omega t)} \frac{1 - e^{i\delta N}}{1 - e^{i\delta}} = E_{o}(r) e^{i(kr,-\omega t)} \frac{e^{i\frac{\delta N}{2}}}{e^{i\frac{\delta N}{2}}} \frac{e^{-i\frac{\delta N}{2}}}{e^{-i\frac{\delta}{2}} - e^{i\frac{\delta}{2}}} =$$

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$$= E_{o}(r) e^{i(kr,-\omega t)} \frac{e^{i\frac{\delta N}{2}}}{e^{-i\frac{\delta}{2}}} =$$

$$= E_{o}(r) e^{i\frac{\delta N}{2}} =$$

$$= E_{$$

where R=r, + 1 (N-1) & 12(N-1)d{ - R = r, + & (N-1) BC

maximum if

 $d\sin\theta_{\rm m} = \lambda \, {\rm m}$

Intensity

$$I = I_0 \left(\frac{\sin \frac{N\delta}{2}}{\sin \frac{\delta}{2}} \right)^2$$
Lo single-source intersity

Continuous distribution of sources over the aperture

$$D = \begin{cases} y & \text{with} \\ 0 & \text{R} \end{cases}$$

$$N \rightarrow \infty$$
 so that $\frac{N + o_{iN}}{D} \rightarrow cousk = E_{A}$

$$\widetilde{E}(\widetilde{r}) = \frac{E_{A}}{\widehat{r}} e^{i(kr - \omega t)}$$

$$F(\widetilde{r}) \approx R - y \sin \theta$$

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$$E = \frac{E_A}{R} \int_{-D_0}^{D/2} e^{i(k \, r(y) - \omega t)} dy$$

Result

$$\beta = \frac{kD \sin \theta}{2}$$

Intensity

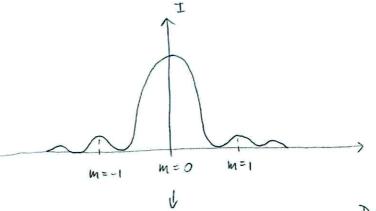
$$I = I_{max} \left(\frac{\sin \beta}{\beta} \right)^2$$

$$I = I_{\text{max}} \left(\frac{\sin \frac{\pi \lambda \sin \theta}{\lambda}}{\pi \lambda \sin \theta} \right)^{2}$$

Bright fringes

$$\frac{\text{ITD Sin Q}}{\lambda} = mT$$

$$\frac{y}{\sin \theta} = \frac{m\lambda}{\hbar} \quad m = 0, \pm 1, \pm 2$$



Diffraction on rectangular aperture a

$$\widetilde{E} = \iint d\widetilde{E}$$
aperhure

Hence

$$I = I_{\max} \left(\frac{\sin x}{x} \right)^2 \left(\frac{\sin \beta}{\beta} \right)^2$$

Internity

$$I(\theta) = I_{\text{max}} \left(\frac{2J_1(\text{ka sin }\theta)}{\text{ka sin }\theta} \right)^2$$



Radii of the dork rings are given by zeros of the Bessel function of the 1st kind, order 1.

Augular positions of first three dark fringes: $8in \Theta_1 = 1.12 \frac{\lambda}{2a}$ $8in \Theta_2 = 2.23 \frac{\lambda}{2a}$ $8in \Theta_3 = 3.24 \frac{\lambda}{2a}$

Why circular operture is important?

- -> Human eyes circulat greature
- -> Rayleigh criterion: Two objects are said to be distinguishable if the center of one diffraction pattern (corresponding to one of the diffracts) coincides with the first minimum of the other."

Hence, the augular reparation of image centers,

 $8in AO = 1.22 \frac{\lambda}{2a}$

Question/exercise: A mobile phone camera's lens has a diameter of 2 mm. What is the maximum distance at which this camera can be used to resolve facial features?