Preface

> I am writing a longer [book] than usual because there is not enough time to write a short one. (Blaise Pascal, paraphrased.)

This book is a sequel to [Mur22]. and provides a deeper dive into various topics in machine learning (ML). The previous book mostly focused on techniques for learning functions of the form $f : \mathcal{X} \rightarrow \mathcal{Y}$, where f is some nonlinear model, such as a deep neural network, $\mathcal{X}$ is the set of possible inputs (typically $\mathcal{X} = \mathbb{R}^D$), and $\mathcal{Y} = \{1, \ldots, C\}$ represents the set of labels for classification problems or $\mathcal{Y} = \mathbb{R}$ for regression problems. Judea Pearl, a well known AI researcher, has called this kind of ML a form of "glorified curve fitting" (quoted in [Har18]).

In this book, we expand the scope of ML to encompass more challenging problems. For example, we consider training and testing under different distributions; we consider generation of high dimensional outputs, such as images, text, and graphs, so the output space is, say, $\mathcal{Y} = \mathbb{R}^{256 \times 256}$; we discuss methods for discovering "insights" about data, based on latent variable models; and we discuss how to use probabilistic models for causal inference and decision making under uncertainty.

We assume the reader has some prior exposure to ML and other relevant mathematical topics (e.g., probability, statistics, linear algebra, optimization). This background material can be found in the prequel to this book, [Mur22], as well several other good books (e.g., [Lin+21b; DFO20]).

Python code (mostly in JAX) to reproduce nearly all of the figures can be found online. In particular, if a figure caption says "Generated by `gauss_plot_2d.ipynb`", then you can find the corresponding Jupyter notebook at probml.github.io/notebooks#gauss_plot_2d.ipynb. Clicking on the figure link in the pdf version of the book will take you to this list of notebooks. Clicking on the notebook link will open it inside Google Colab, which will let you easily reproduce the figure for yourself, and modify the underlying source code to gain a deeper understanding of the methods. (Colab gives you access to a free GPU, which is useful for some of the more computationally heavy demos.)

In addition to the online code, probml.github.io/supp contains some additional supplementary online content which was excluded from the main book for space reasons. For exercises (and solutions) related to the topics in this book, see [Gut22].

Contributing authors

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About the cover

The cover illustrates a variational autoencoder (Chapter 21) being used to map from a 2d Gaussian to image space.

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Changelog

- 2022-07-29. First official release.
- 2022-08-08. Changes listed at https://github.com/probml/pml2-book/issues/125.
- 2022-08-12. Changes listed at https://github.com/probml/pml2-book/issues/133.
- 2022-08-15. Changes listed at https://github.com/probml/pml2-book/issues/137. (First printing from MIT Press.)
- 2022-10-16. Changes listed at https://github.com/probml/pml2-book/issues/170.
- 2022-12-23. Changes listed at https://github.com/probml/pml2-book/issues/193.
- 2023-01-02. Changes listed at https://github.com/probml/pml2-book/issues/199.