ECO5002 Introduction to Economics

Quiz 3

(Total Points: 40, Due on August 15th, 2025)

Consider a consumption-saving model with periods from 0 to *T*:

$$\max_{\left\{\{c_t\}_{t=0}^T, \{b_{t+1}\}_{t=0}^{T-1}\right\}} \sum_{t=0}^T \beta^t \ln c_t$$
s.t.
$$c_t + \frac{b_{t+1}}{R} \le b_t + \overline{w}, \quad t \in \{0, 1, \cdots, T-1\}$$

$$c_T \le b_T + \overline{w}$$

where c denotes consumption, and b denotes saving (or borrowing). β , R, and \overline{w} are parameters, and the initial value of saving b_0 is exogenously given.

1. **(30pts)** Solve for an explicit expression of c_0 as a function of β , R, \overline{w} , and b_0 .

2. **(10pts)** If there is a constraint: $b_T \geq \overline{b} > 0$, where \overline{b} is very large and makes this constraint always bind, i.e., $b_T = \overline{b}$. Re-compute the optimal consumption level at time 0 (denoted by c_0^*) and show that $c_0^* < c_0$.