### MODELLING AND SIMULATION USING MATLAB/SIMULINK AND ITS APPLICATIONS IN ELECTRIC POWER STEERING SYTEM.

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**Group project title** 

Study of Matlab/Simulink and application on simulation and analysis of mechanical components of the (complete) EPS system.



# INTRODUCTION

### a) Goal of the project

To study:

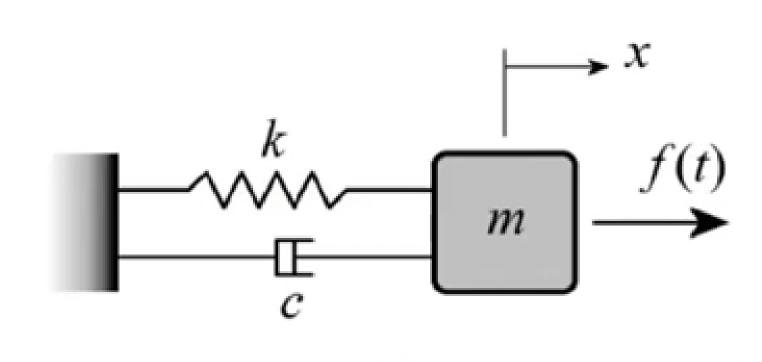
- How to model mechanical system
- How to use Matlab/Simulink with mass damper system
- How to determine EPS equation and simulate in Simulink by using above knowledge

#### b) Why Electric Power Steering system (EPS)

• Electrically assisted power steering is replacing the traditional hydraulic system where the pressure is provided via a pump driven by the vehicles engine. The hydraulic system is constantly running and by using the EPS the fuel consumption can be reduced. In electric and hybrid vehicles, the engine does not run continuously so electric power steering is the only possible solution

# THEORETICAL BASIS

#### a) Mass-Damper model



$$m\ddot{x} + c\dot{x} + kx = f(t)$$

$$\ddot{x} = \frac{1}{m}(f(t) - c\dot{x} - kx)$$

Figure: Mass - damper model and dynamic equation

#### b) EPS model

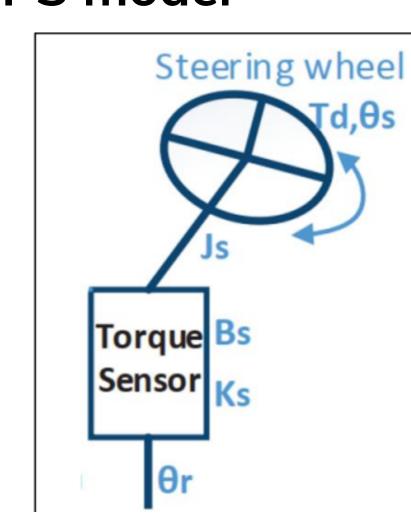


Figure: Overall structure of the steering input (Equation EPS.1)

$$J_s \times \frac{d^2_{\theta_s}}{dt^2} = T_d - K_s(\theta_s - \theta_r) - B_s \times \frac{d_{\theta_s}}{dt^2}$$

Name

Figure: Overall Rack and Pinion Dynamics (Equation EPS.2)

$$m \times \frac{d^2x}{dt^2} = \frac{1}{r_p} \left[ K_m(\theta_m - i_m\theta_r)i_m + K_s(\theta_s - \theta_r) \right] - B_r \times \frac{d_x}{dt} - K_r \times x - F_{resist} \quad \text{(Equation EPS.2)}$$

## SIMULATION DATA, PROCESS AND RESULT

#### a) Mass-Damper model

Parameter	Value
Mass of solid (m)	1.0 kg
Spring constant (k)	100 N/m
Damping coeff. (C)	0.15 N/(m/s)
Force applied (F)	100 N

Table: Mass-Damper parameters

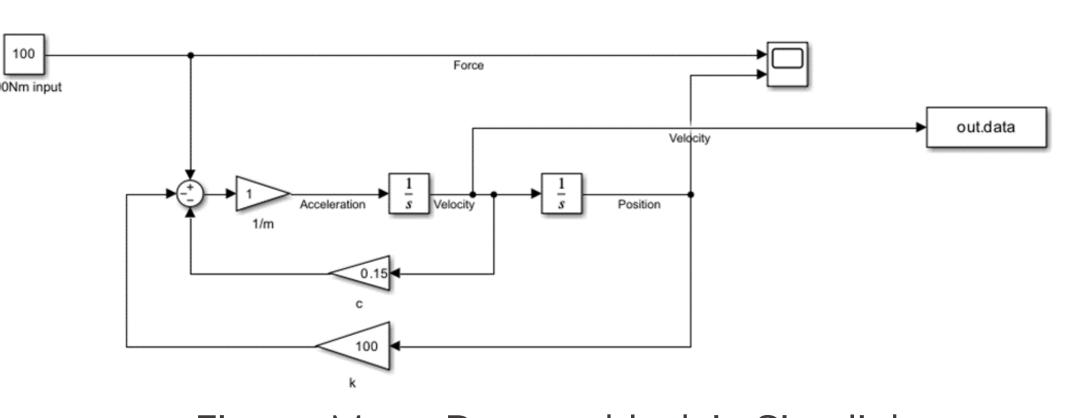


Figure: Mass-Damper block in Simulink

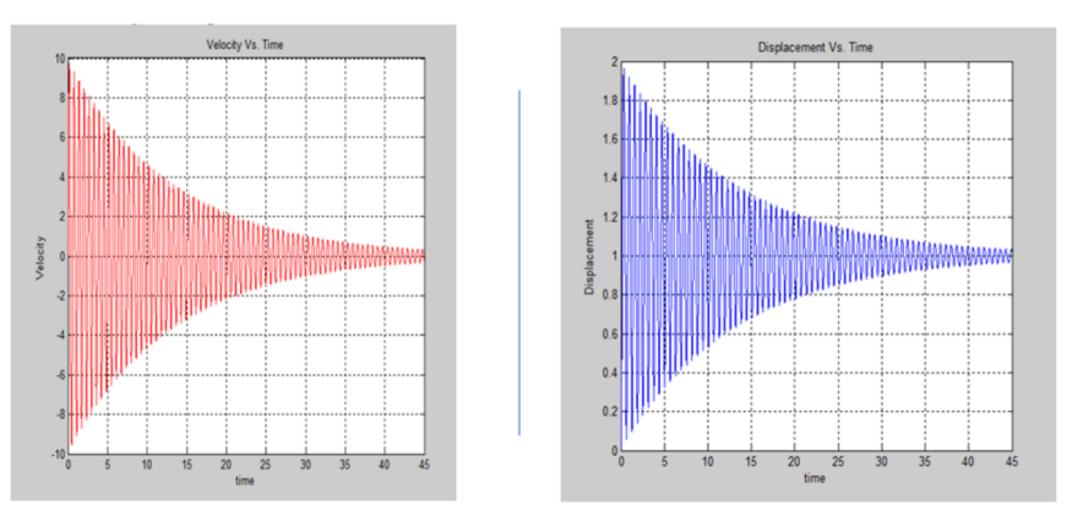


Figure: Result of Mass-Damper model simulation

Result: For the given parameters of the system, the position vs. time response in MATLAB gives the maximum value equal to 1.961 m. Similarly, the maximum velocity is found to be 9.761 m/s. After that, both will fluctuate in a downtrend to a specific number

### b) EPS model

$J_s$	0.0012 [kgm <sup>2</sup> ]	Inertia of steering wheel and steering column
$B_s$	0.26 [Nmrad <sup>-1</sup> ]	Viscous damping coefficient of steering column
$K_s$	115 [Nmrad <sup>-1</sup> ]	Rigidity of torsional bar
$ heta_s$	[Rad]	Turn angle of steering wheel
$ heta_r$	[Rad]	Turn angle of output steering axle
$T_d$	[Nm]	Input torque of steering wheel

$K_r$	$91064  [\mathrm{N}m^{-1}]$	Linear rigidity
$B_r$	653.203 [Nmrad <sup>-1</sup> ]	Viscous damping coefficient of rack and pinion
$r_p$	0.007783 [m]	Pinion radius
X	m	Rack displacement
$m_r$	32 [kG]	Mass of the rack and pinion system

Vehicle speed

Torque Bs

Sensor Ks

**ECU** 

Motor

#### Table: EPS parameters

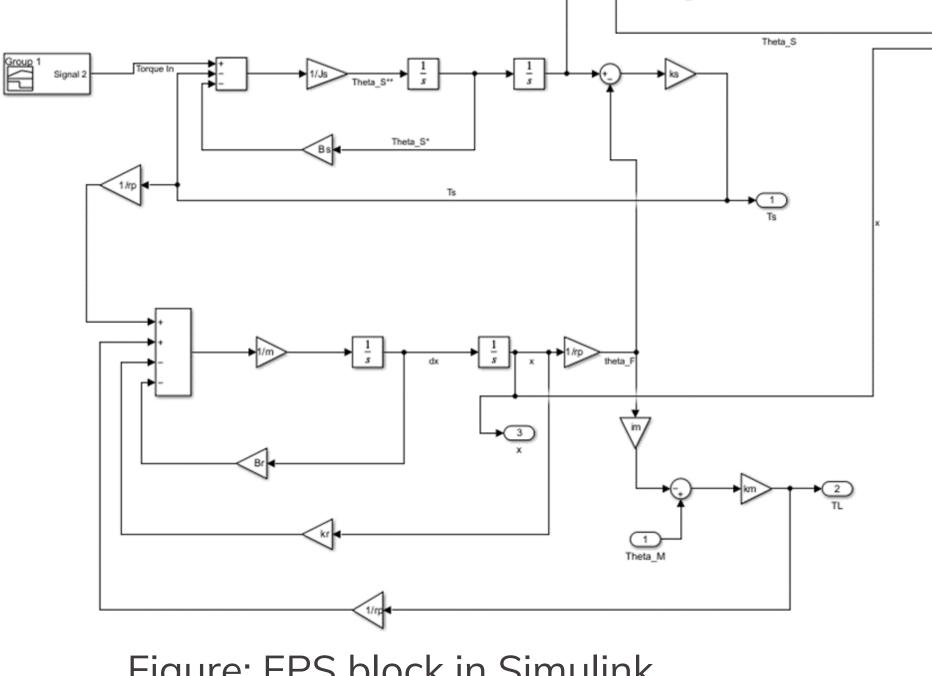
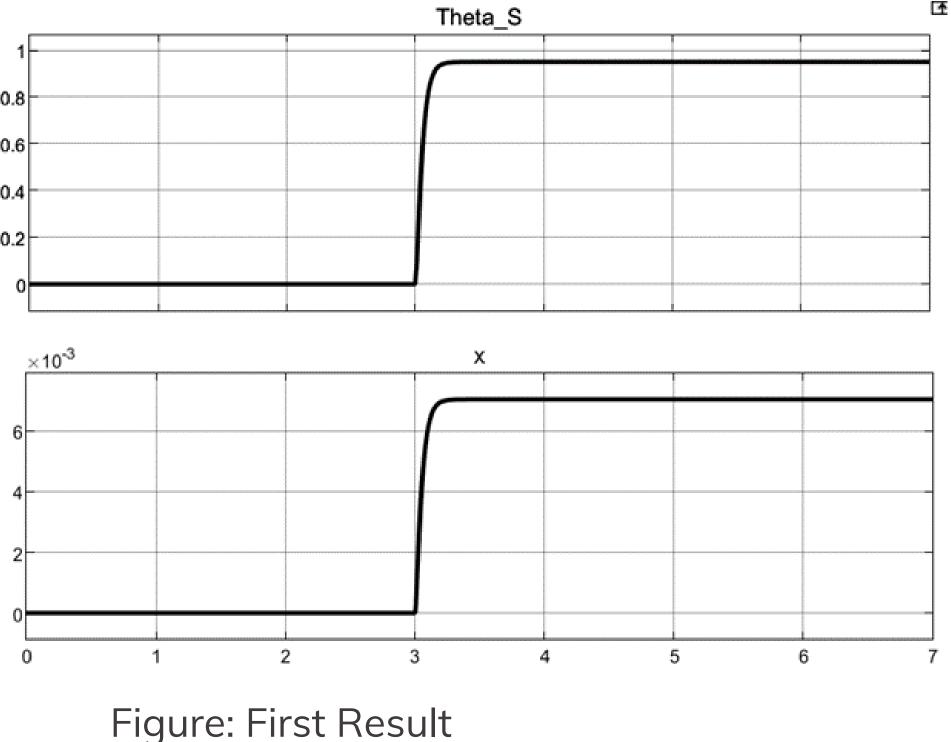
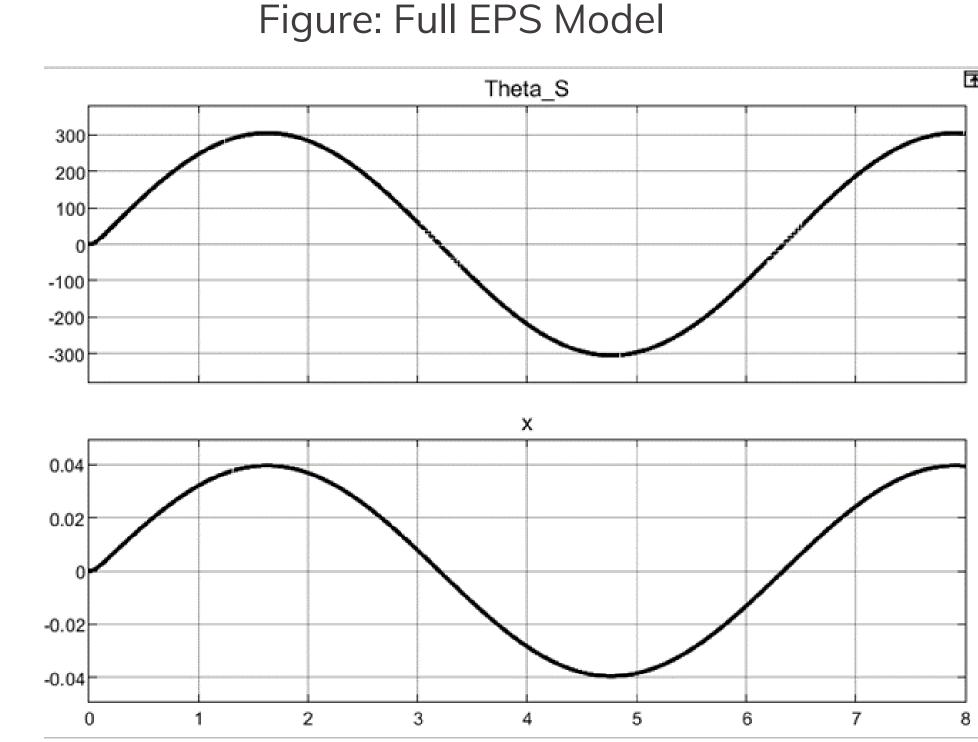


Figure: EPS block in Simulink





Fresist Kr Br rp

Figure: Second Result

First Result: The inputs to this system are the torque generated by the driver. Since we present a model of the power steering system, details of the tire dynamics are neglected. The outputs of the mechanical subsystem are the displacement of the rotational displacement of the steering column θS.As we can see from Fig. :First Result, with  $\theta$ S changed from 0 to nearly 1 rad, x jumped to approximately  $7x10^-3$  m. Input touque at 3s is 5Nm.

SecondResult: In second result, the input in steering wheel angle is generated in a sine shape which goes from -300 degrees to 300 degrees. As we can see, the rack displacement also changed in sine shape also, going from -0.04m from center to 0.04m (positive direction goes from left to right)