

## 1 INTRODUCTION a) Goal of the project

- Learning how to use MATLAB/Simulink with the Mass-Spring-Damper model.
- Contribution to an analysis of the dynamic behavior of the mechanical components of EPS system
- Analysis of the complete system dynamics of EPS, and implementation of the EPS simulation model on Matlab/Simulink, with simulation results analysis.

b) **Limitation** : This project skips on the effect of motor and effect of forces acting from road to EPS system through wheels.

## 2 THEORETICAL BASIS AND METHOD

### a) Mass-Damper model

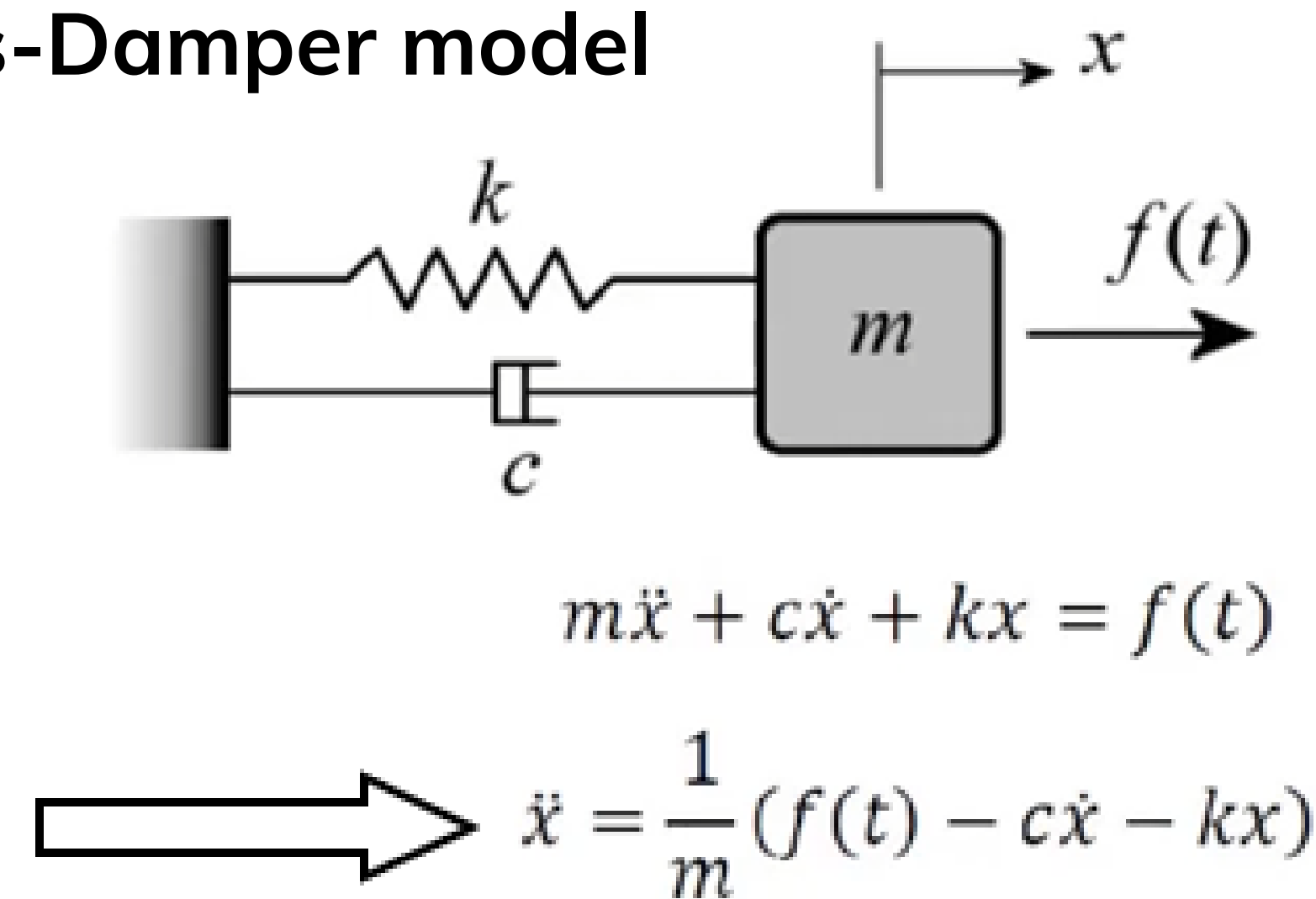


Figure: Mass - damper model and dynamic equation

### b) EPS model

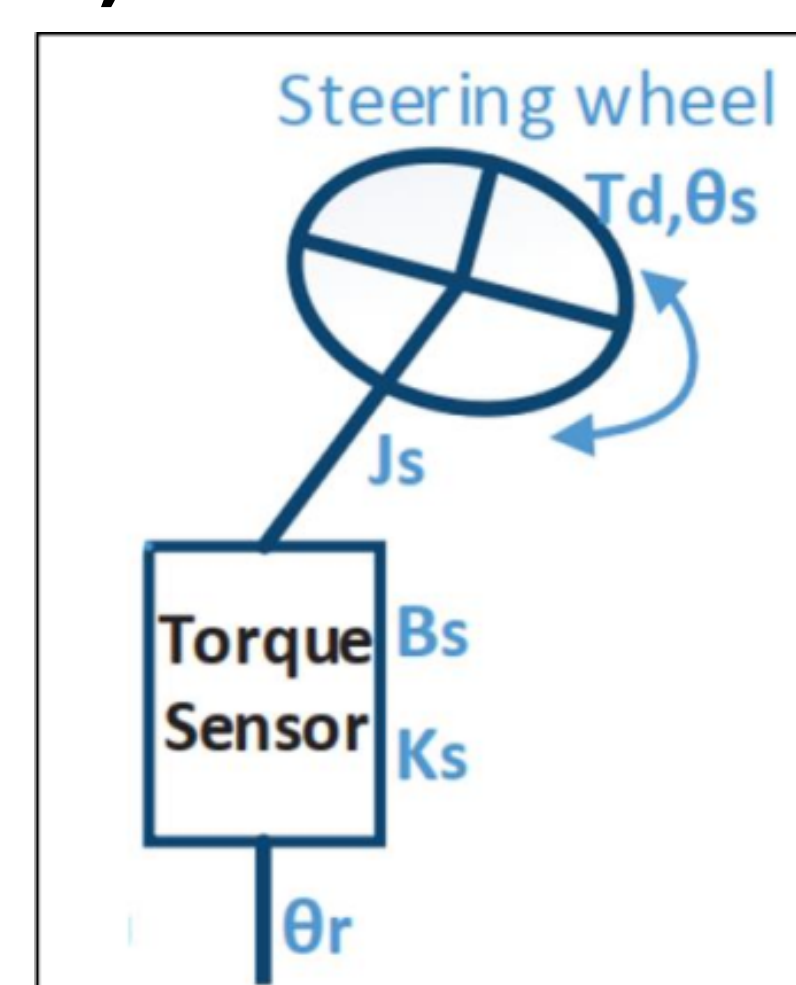


Figure: Overall structure of the steering input (Equation EPS.1)

$$J_s \times \frac{d^2 \theta_s}{dt^2} = T_d - K_s(\theta_s - \theta_r) - B_s \times \frac{d\theta_s}{dt}$$

$$m \times \frac{d^2 x}{dt^2} = \frac{1}{r_p} [K_m(\theta_m - i_m \theta_r) i_m + K_s(\theta_s - \theta_r)] - B_r \times \frac{dx}{dt} - K_r \times x - F_{resist}$$

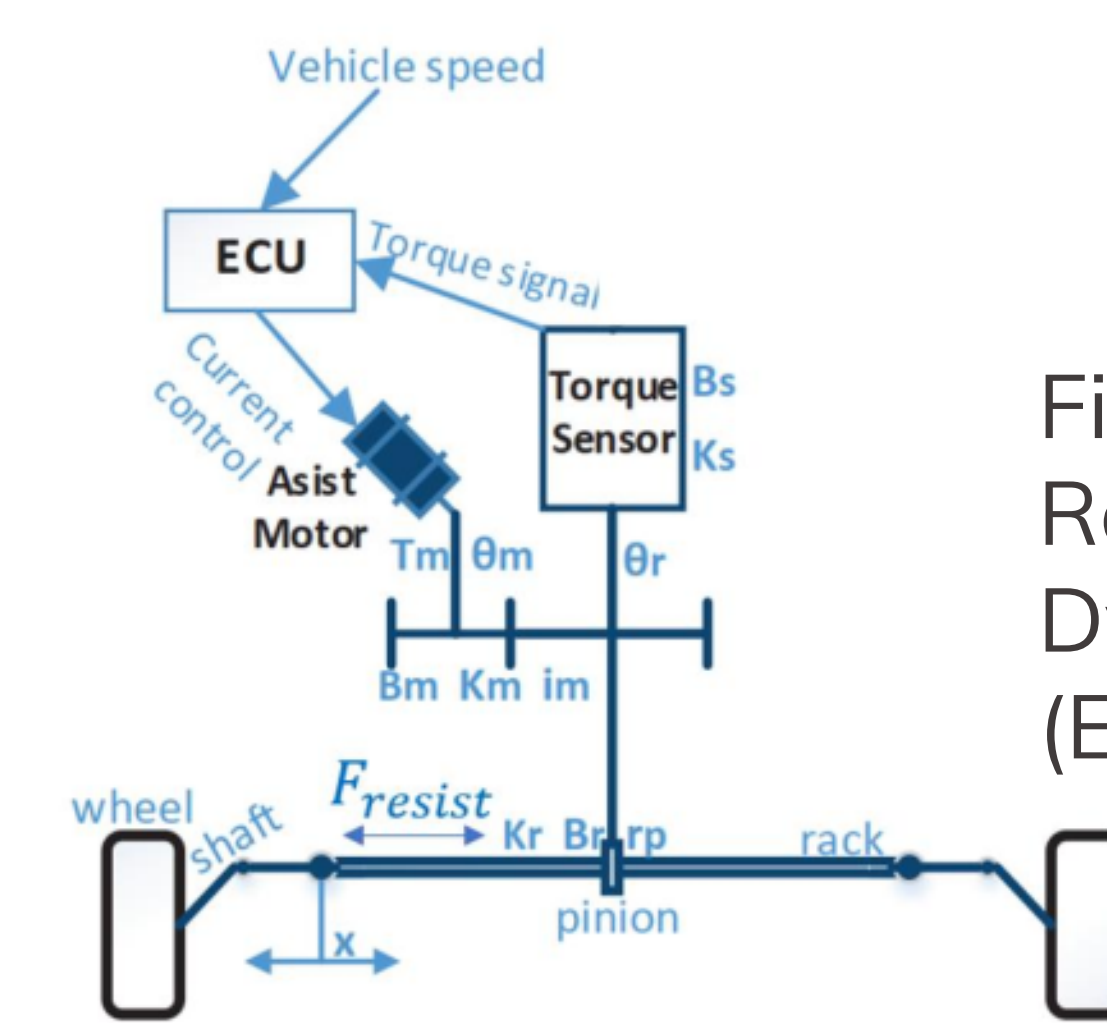
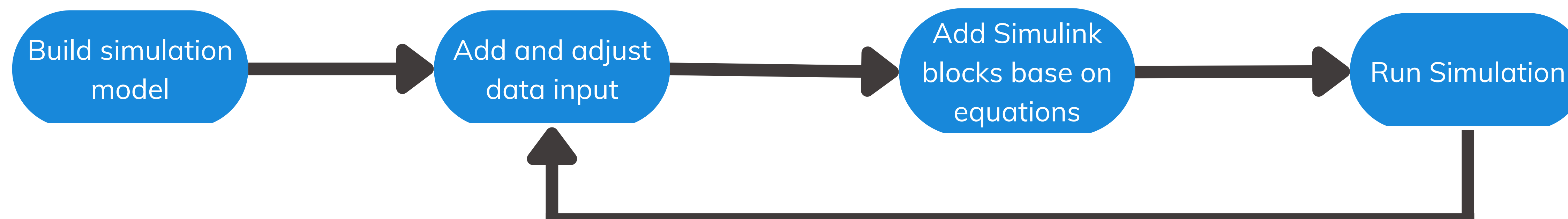


Figure: Overall Rack and Pinion Dynamics (Equation EPS.2)

(Equation EPS.1)

(Equation EPS.2)

### c) Simulation method



## 4 SIMULATION DATA, PROCESS AND RESULT

### a) Mass-Damper model

Parameter	Value
Mass of solid (m)	1.0 kg
Spring constant (k)	100 N/m
Damping coeff. (C)	0.15 N/(m/s)
Force applied (F)	100 N

Table: Mass-Damper parameters

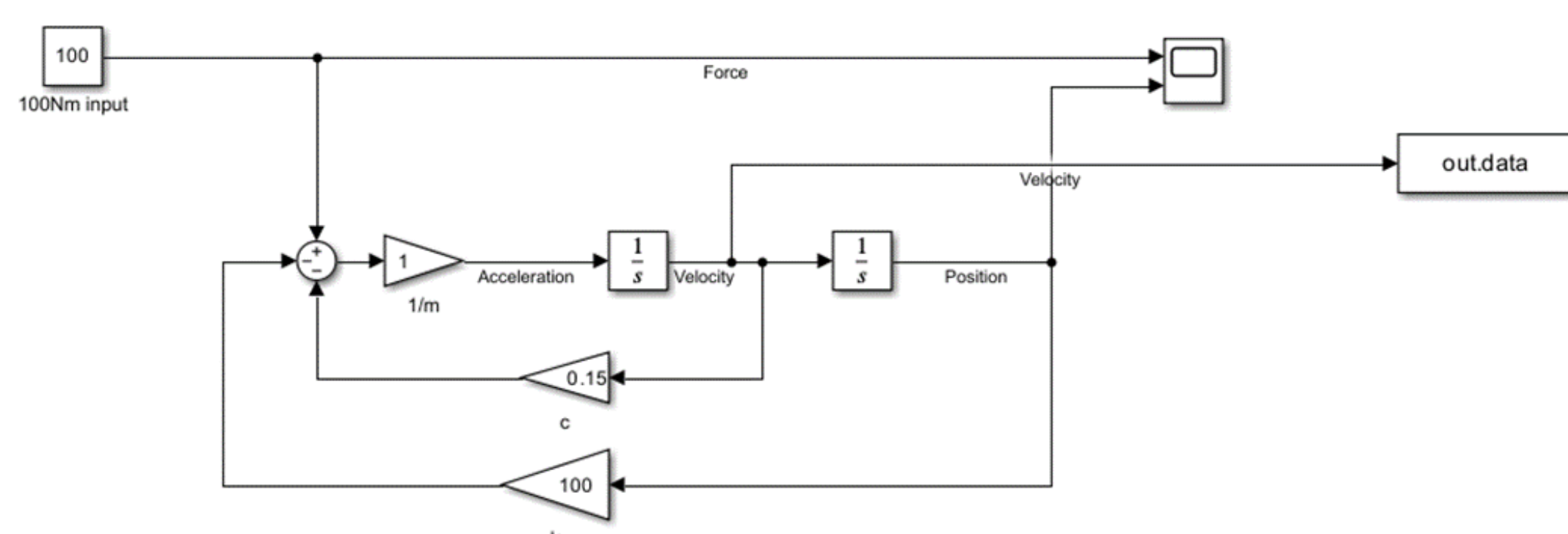


Figure: Mass-Damper block in Simulink

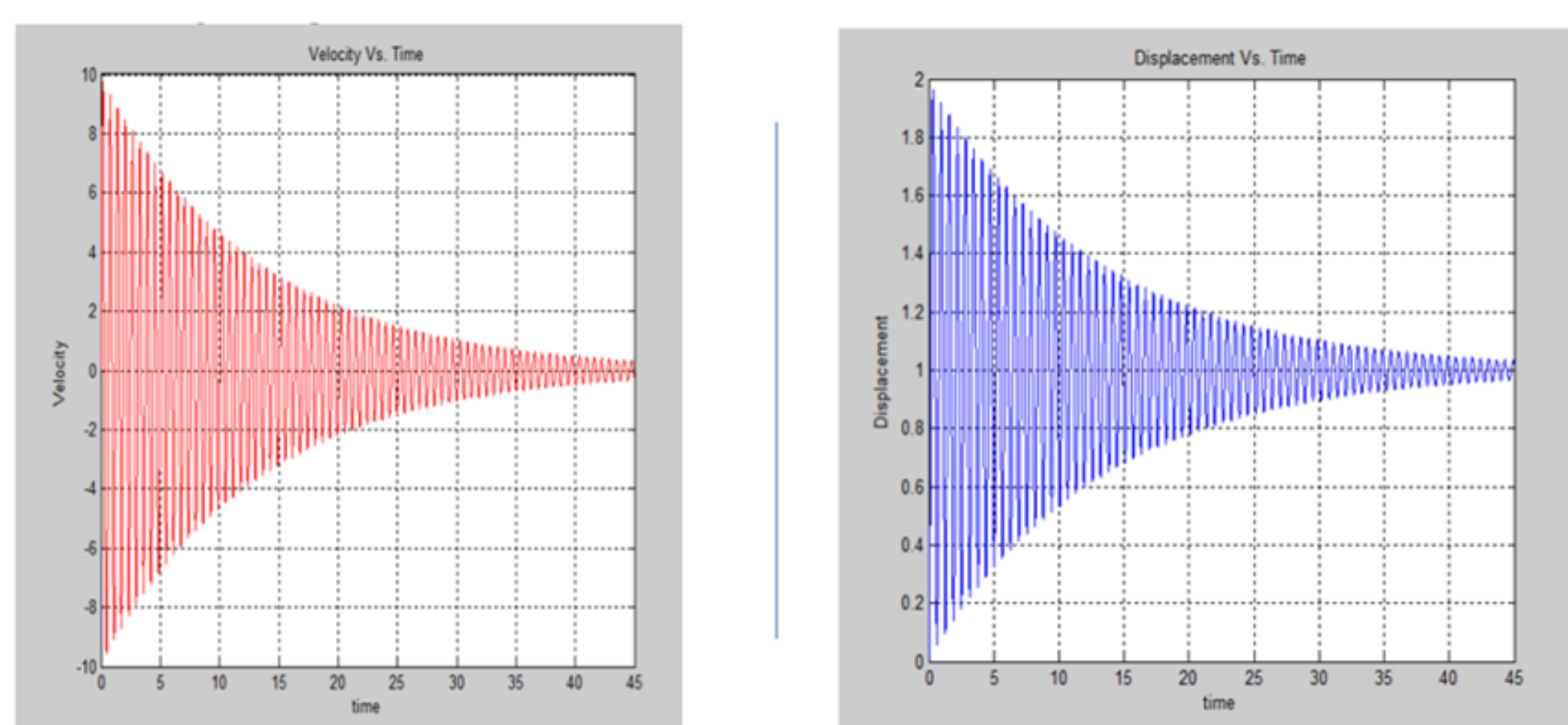


Figure: Result of Mass-Damper model simulation

Result: For the given parameters of the system, the position vs. time response in MATLAB gives the maximum value equal to 1.961 m. Similarly, the maximum velocity is found to be 9.761 m/s. After that, both will fluctuate in a downtrend to a specific number

### b) EPS model

Symbols	Value	Name
$J_s$	0.0012 [kgm <sup>2</sup> ]	Inertia of steering wheel and steering column
$B_s$	0.26 [Nmrad <sup>-1</sup> ]	Viscous damping coefficient of steering column
$K_s$	115 [Nmrad <sup>-1</sup> ]	Rigidity of torsional bar
$\theta_s$	[Rad]	Turn angle of steering wheel
$\theta_r$	[Rad]	Turn angle of output steering axle
$T_d$	[Nm]	Input torque of steering wheel

$K_r$	91064 [Nm <sup>-1</sup> ]	Linear rigidity
$B_r$	653.203 [Nmrad <sup>-1</sup> ]	Viscous damping coefficient of rack and pinion
$r_p$	0.007783 [m]	Pinion radius
$x$	m	Rack displacement
$m_r$	32 [kg]	Mass of the rack and pinion system

Table: EPS parameters

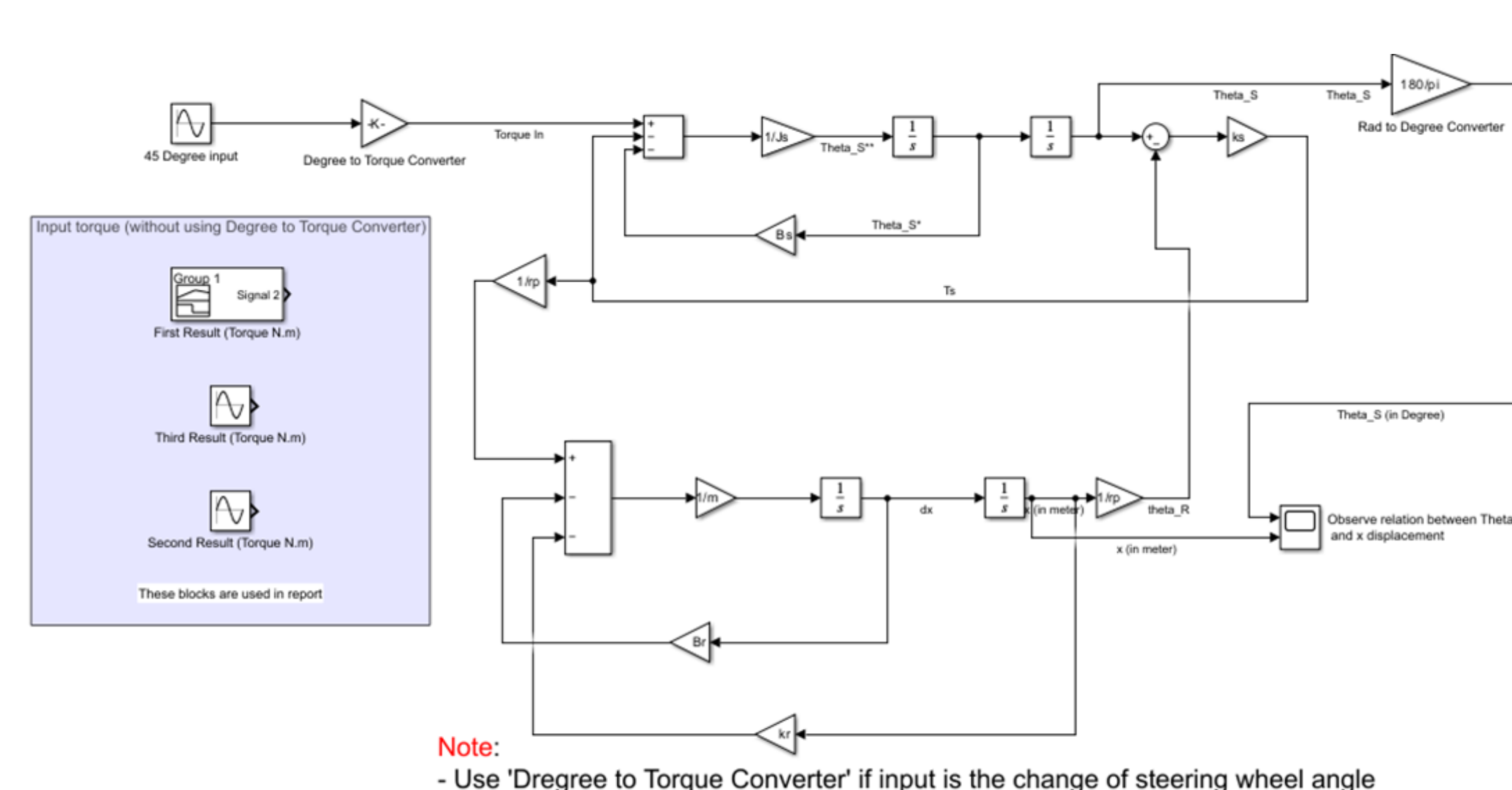


Figure: EPS block in Simulink

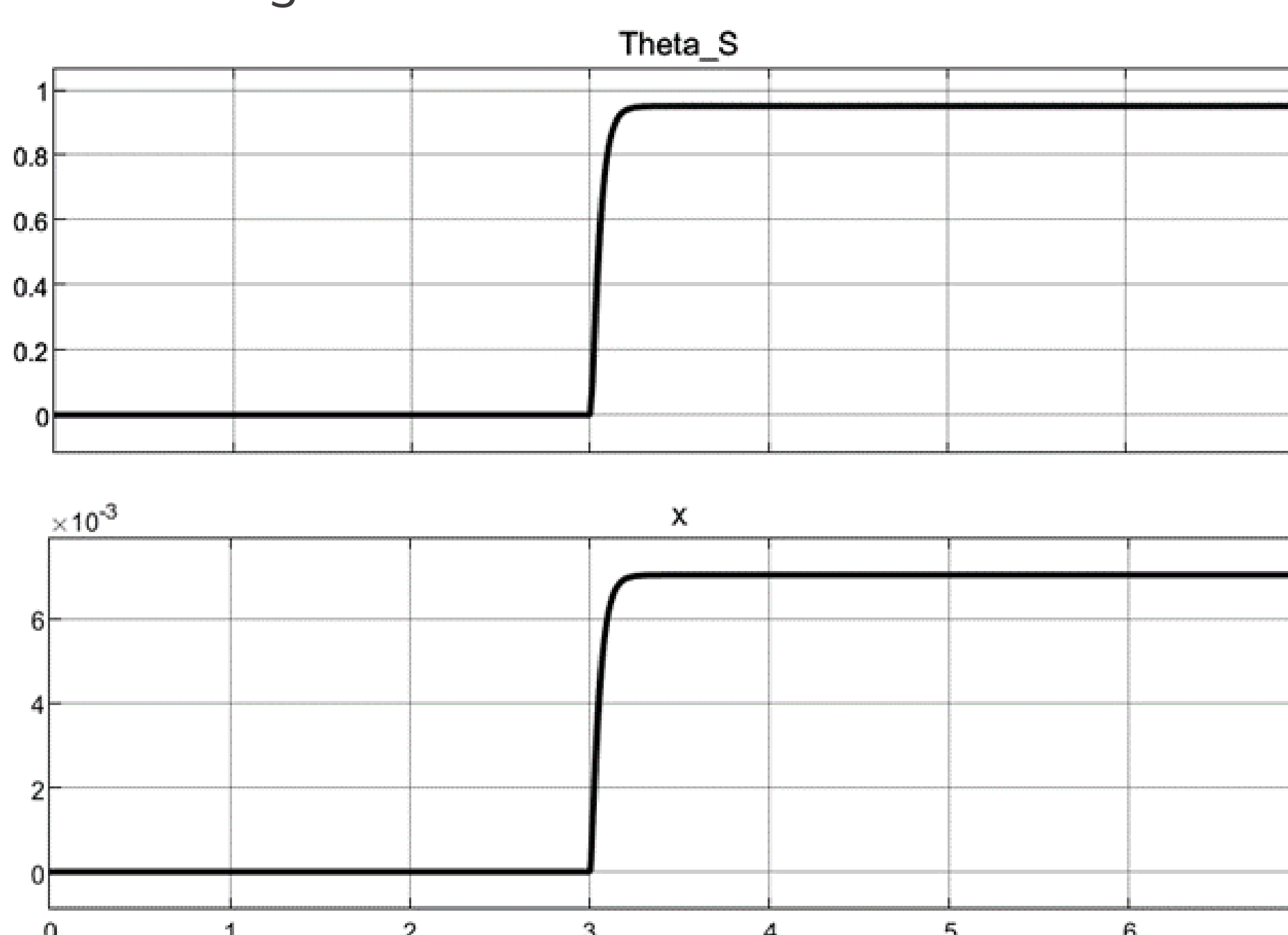


Figure: First Result

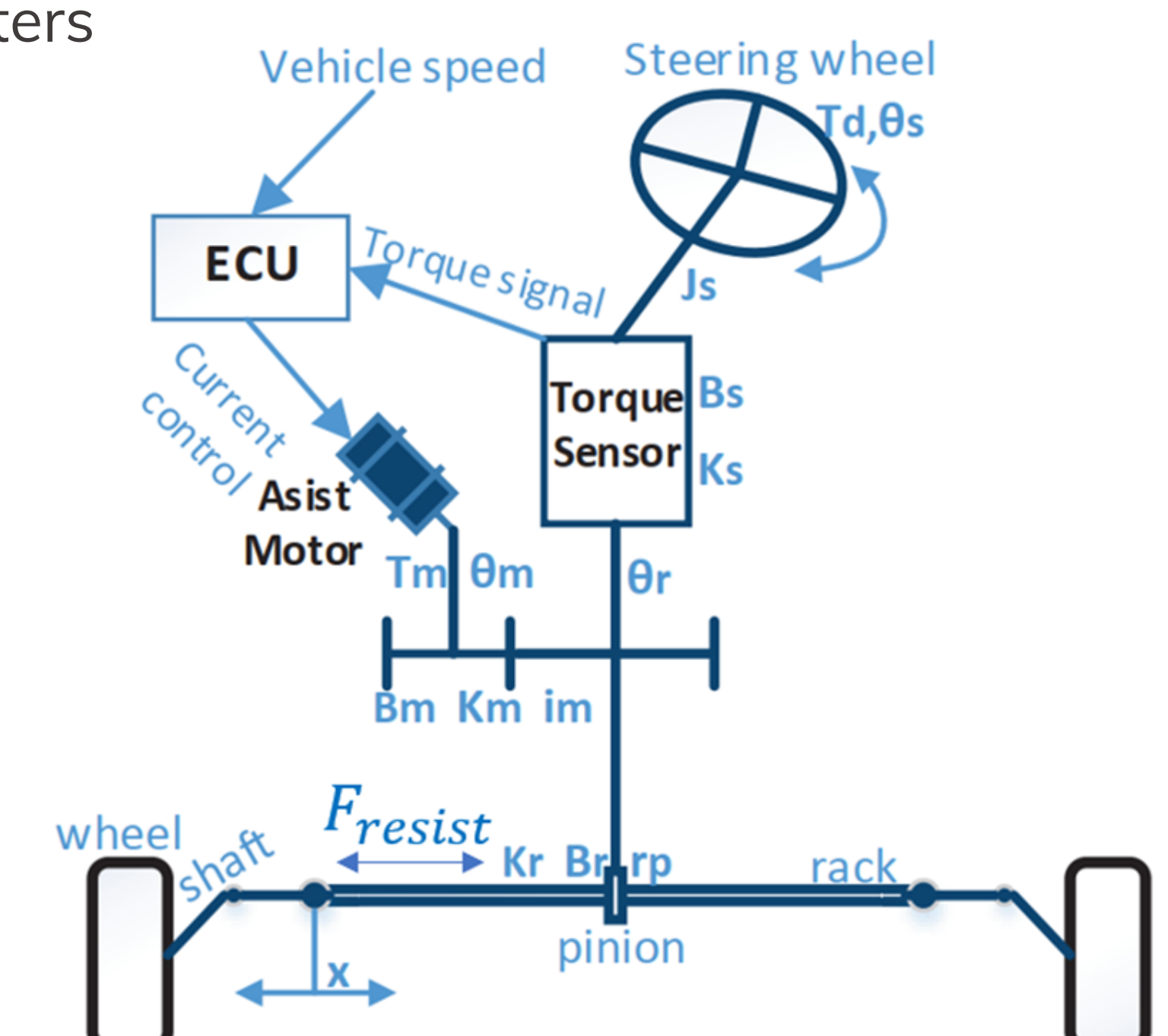


Figure: Full EPS Model

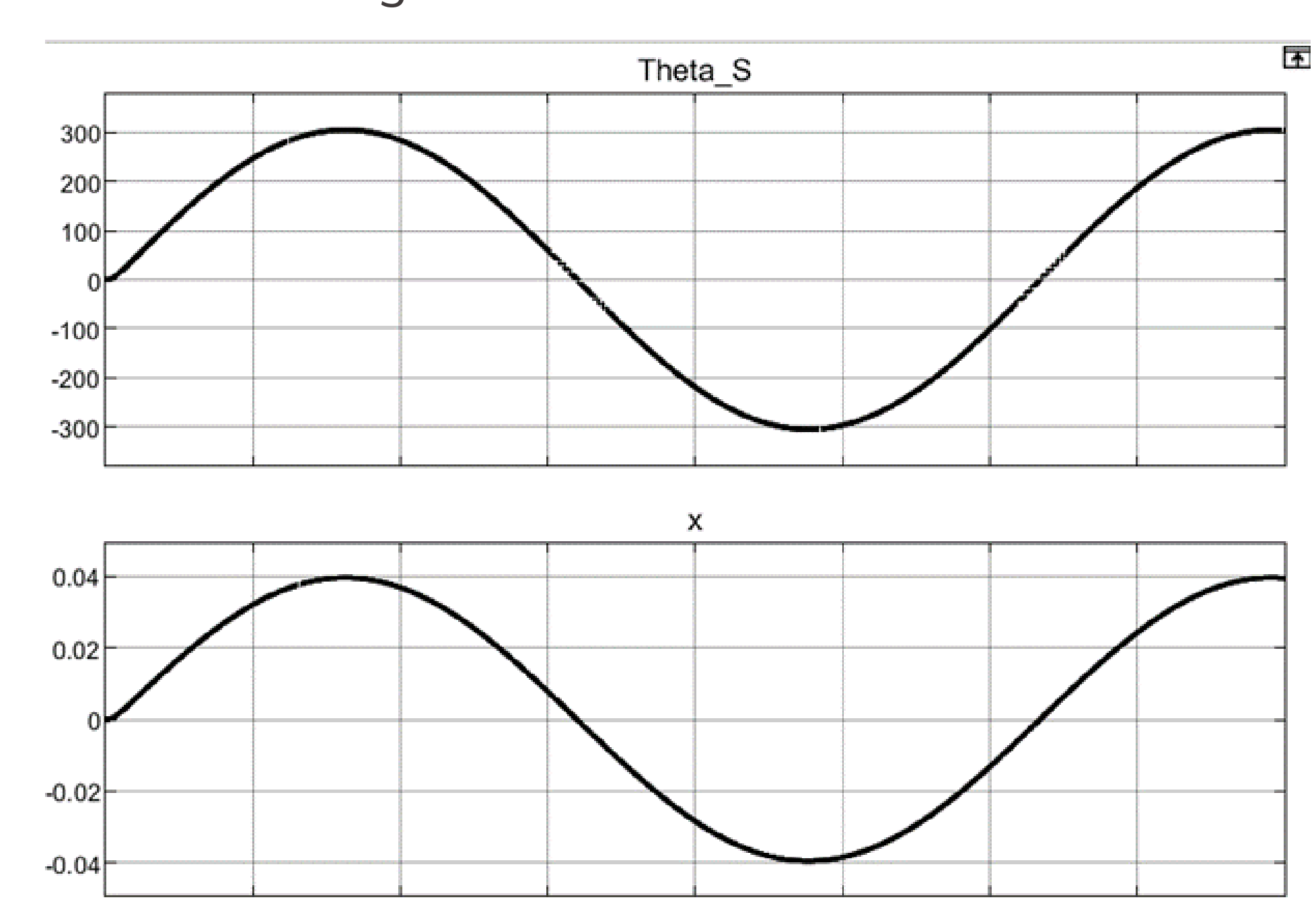


Figure: Second Result

First Result : The inputs to this system are the torque generated by the driver. Since we present a model of the power steering system, details of the tire dynamics are neglected. The outputs of the mechanical subsystem are the displacement of the rack, X, and the rotational displacement of the steering column  $\theta_s$ . As we can see from Fig :First Result , with  $\theta_s$  changed from 0 to nearly 1 rad, x jumped to approximately  $7 \times 10^{-3}$  m. Input torque at 3s is 5Nm.

SecondResult : In second result, the input in steering wheel angle is generated in a sine shape which goes from -300 degrees to 300 degrees. As we can see, the rack displacement also changed in sine shape also, going from -0.04m from center to 0.04m (positive direction goes from left to right)