R-code for 'A time-heterogeneous D-vine copula model for unbalanced and unequally spaced longitudinal data'

Md Erfanul Hoque, Elif F. Acar and Mahmoud Torabi

The file contains the source code of the analysis of a subset of the Manitoba Follow-up Study data presented in Section 5 of A time-heterogeneous D-vine copula model for unbalanced and unequally spaced longitudinal data by Hoque, Acar and Torabi (2020).

Load required packages

```
library(here) # to specify the folder where something is located in
library(VineCopula) # required to work with D-vine copulas
library(nlme) # enables working with linear mixed models (LMMs)
library(condMVNorm) # required for predicting conditional quantiles of
                    # multivariate normal distributions
# Load data
# Note: Because of data confidentiality, the data set file is not included in this R p
load(here("data","Data_MFUS.Rdata")) # 'here' function will specify
                                      # the "data" folder to load
                                       # the required data
names (MFUS)
## [1] "id"
                  "followup" "px age"
                                                    "IHD"
                                                               "DBP"
                                        "bmi"
# Maximum number of measurements per individual
d <- max(table(MFUS$id))</pre>
## [1] 5
n <- length(unique(MFUS[,1]))</pre>
## [1] 462
```

Model fitting

We fit a linear mixed model (LMM), a time-homogeneous D-vine copula model (HOM–P) and a time-heterogeneous D-vine copula model (HET–P) to the data.

Linear mixed model (LMM)

```
## Linear mixed-effects model fit by maximum likelihood
   Data: MFUS
##
          AIC
                   BIC
                          logLik
##
     11736.46 11774.58 -5861.229
##
## Random effects:
## Formula: ~1 | id
           (Intercept) Residual
##
              4.850646 6.386818
## StdDev:
##
## Correlation Structure: Exponential spatial correlation
## Formula: ~px_age | id
## Parameter estimate(s):
##
        range
## 0.01524487
## Fixed effects: DBP ~ px age + bmi + IHD
                  Value Std.Error
                                    DF
                                         t-value p-value
## (Intercept) 51.75301 2.2942930 1249 22.557282 0.0000
## px_age
                0.20148 0.0347559 1249 5.796886 0.0000
## bmi
                0.73968 0.0959485 1249 7.709150 0.0000
## IHD
                0.76895 0.5821587 460 1.320862 0.1872
## Correlation:
##
          (Intr) px age bmi
## px age -0.218
```

D-vine copula models

For the D-vine copula models HOM–P and HET–P, we use the univariate marginal distribution implied by the fitted linear mixed model. We first transform the observed measurements to copula data using the distribution functions of $\mathcal{N}(x_{i,j}^{\mathsf{T}}\eta,\phi^2)$, where $\phi^2 = \operatorname{var}(\gamma_i) + \operatorname{var}(\varepsilon_{i,j})$.

Obtain copula data to fit D-vine copula models

```
# Standard deviation of the random effect gamma
sd.random <- as.numeric(VarCorr(LMM.Exp)[1, 2])</pre>
# Standard deviation of the error term epsilon_{i,j}
sd.error <- as.numeric(VarCorr(LMM.Exp)[2, 2])</pre>
# Standard deviation of Y_{i,j}
phi <- sqrt(sd.error^2 + sd.random^2)</pre>
# Transformation of the observations to the copula scale
u.vec <- pnorm(LMM.Exp$residuals[,1] / phi)</pre>
# Matrix to store the information, where unobserved measurements are
# denoted by 'NA'.
U.data <- matrix(NA, n, 5) # copula data matrix
j <- 0 # auxiliary counter
# For individual i fill the first d_i entries of the ith row in the
# matrix U.data with the transformed entries corresponding to the
# measurements of individual i
for (i in 1:n){
  k <- min(5, table(MFUS$id)[i])</pre>
  U.data[i, 1:k] \leftarrow u.vec[j + 1:k]
  j \leftarrow j + k
```

```
head(U.data) # show the copula data structure
                                [,3]
##
            Γ.17
                       [,2]
                                          [,4]
                                                    [.5]
## [1,] 0.3210778 0.98543447 0.6392163 0.6042819 0.5266832
## [2,] 0.3712734 0.64330496 0.2160685
                                            NA
                                                     NA
## [3,] 0.3653448 0.08711343
                                            NA
                                                     NA
## [4,] 0.4065085 0.29108635 0.5607451 0.6329385 0.4112875
## [5,] 0.6491174 0.32565800 0.5465238 0.1285328 0.1002344
## [6,] 0.7723560 0.89085685 0.7997230 0.8754386 0.9019637
Fit time-homogeneous D-vine copula model (HOM-P) to copula data
# Set of candidate families
family.set <-c(1,3,4,5,13,14)
# D-vine matrix with order 1-2-3-4-5
4,3,2,1,1),5,5, byrow=T)
# Fit HOM-P with fixed order 1:5
Dvine.HOM <- RVineCopSelect(data = U.data, # copula data
                     Matrix = Mat, # vine structure
                     familyset = family.set,
                     selectioncrit = "AIC" # selection criterion
)
## Warning: In RVineCopSelect: Some of the data are NA. Only pairwise complete
## observations are used.
# The above warning only confirms that the data are unbalanced.
Dvine.HOM
## D-vine copula with the following pair-copulas:
## Tree 1:
## 4,5 Gumbel (par = 1.45, tau = 0.31)
## 3,4 Gumbel (par = 1.29, tau = 0.22)
## 2,3 Gumbel (par = 1.25, tau = 0.2)
## 1,2 Gumbel (par = 1.24, tau = 0.19)
##
## Tree 2:
```

```
## 3,5;4 Survival Clayton (par = 0.34, tau = 0.15)
## 2,4;3 Gaussian (par = 0.2, tau = 0.13)
## 1,3;2 Survival Gumbel (par = 1.23, tau = 0.19)
##
## Tree 3:
## 2,5;3,4 Gaussian (par = 0.3, tau = 0.19)
## 1,4;2,3 Frank (par = 0.91, tau = 0.1)
##
## Tree 4:
## 1,5;2,3,4 Frank (par = 0.2, tau = 0.02)
## ---
## 1 \leftarrow V1, 2 \leftarrow V2, 3 \leftarrow V3, 4 \leftarrow V4,
## 5 <-> V5
# Copula log-likelihood value for HOM-P model
Cloglik HOMByPair<- sum(Dvine.HOM$pair.logLik);Cloglik HOMByPair
## [1] 147.8705
# Store the copula parameters and families from fitted HOM-P model
par<-Dvine.HOM$par
parset.HOM < -list(c(par[5,1], par[5,2], par[5,3], par[5,4]),
               c(par[4,1],par[4,2],par[4,3]),
               c(par[3,1],par[3,2]),
               c(par[2,1]))
fam<-Dvine.HOM$family
familyset.HOM \leftarrow list(c(fam[5,1],fam[5,2],fam[5,3],fam[5,4]),
                    c(fam[4,1],fam[4,2],fam[4,3]),
                    c(fam[3,1],fam[3,2]),
                    c(fam[2,1])
```

Fit time-heterogeneous D-vine copula model (HET-P) to copula data

To fit the HET–P model, we first calculate time interval between two measurements. The fitted model gives the estimated values of the model parameters for each pair copula.

```
# denoted by 'NA'
Visits <- data.frame(visit.times) # Final time variable to use in analysis
head(Visits)
##
      px_age.1 px_age.2 px_age.3 px_age.4 px_age.5
## 1 27.41410 34.03970 34.88296 35.38125 35.86858
## 6 28.49555 30.57906 34.87201
                                        NA
## 9 33.41821 39.43600
                              NA
                                        NA
                                                 NA
## 11 36.97741 38.97878 41.33060 43.82204 45.85626
## 16 29.08419 32.23272 35.46064 38.45038 38.80630
## 21 25.83436 28.89254 32.01916 32.02190 33.87269
## BEGIN fitted model
# Calculate the time intervals for Tree 1
t<- sapply(1:(d-1), function(j) Visits[,j+1] - Visits[,j])
colnames(t)<-c("t.12","t.23","t.34","t.45")</pre>
t.12<-t[,1];t.23<-t[,2];t.34<-t[,3];t.45<-t[,4]
# Respective ids of available time intervals in Tree 1
id1 <-sapply(1:(d-1), function(j) which(complete.cases(t[,j])))
id12<-id1[[1]];id23<-id1[[2]];id34<-id1[[3]];id45<-id1[[4]]
# Estimation of model parameters of pair copulas in Tree 1
fit<- sapply(1:(d-1), function(j) LBiCopFit(u1=U.data[,j], u2=U.data[,j+1],
          x=t[,j],family=family.set,repar="pearson",start = c(0.01,0.01)))
fit.beta.T1<- sapply(1:(d-1), function(j) c(fit[1,j],fit[2,j]))
11.T1<-sum(unlist(fit[3,])) #loglikelihood value in Tree 1</pre>
fam.T1<-fit[4,] # selected family of pair copulas in Tree 1</pre>
tau.T1<- sapply(1:(d-1), function(j) LDVine.rho2tau(unlist(fit.beta.T1[,j]),
                                                     t[, j][id1[[j]]]))
par.T1<- sapply(1:(d-1), function(j) BiCopTau2Par(fam.T1[[j]], tau.T1[[j]]))</pre>
# Obtain the pseudo-conditional marginals for Tree 2
vv<-list()</pre>
for (j in 1:(d-2)){
  vv[[j]] <- BiCopHfunc2(u1=U.data[,j][id1[[j]]],u2=U.data[,j+1][id1[[j]]],</pre>
                                  par.T1[[j]],family = fam.T1[[j]])
  vv[[(d-2)+j]] <- BiCopHfunc2(u1=U.data[,j+2][id1[[j+1]]],</pre>
           u2=U.data[,j+1][id1[[j+1]]],par.T1[[j+1]],family = fam.T1[[j+1]])
# Store pseudo-conditional marginals with respective ids
vv1.2 <-data.frame(id1[[1]],vv[[1]])</pre>
```

```
vv3.2 <-data.frame(id1[[2]],vv[[4]])</pre>
vv2.3 <-data.frame(id1[[2]],vv[[2]])</pre>
vv4.3 <-data.frame(id1[[3]],vv[[5]])</pre>
vv3.4 <-data.frame(id1[[3]],vv[[3]])</pre>
vv5.4 <-data.frame(id1[[4]],vv[[6]])</pre>
# Calculate the time intervals for Tree 2
t<- sapply(1:(d-2), function(j) Visits[,j+2] - Visits[,j])
t.13.2<-t[,1];t.24.3<-t[,2];t.35.4<-t[,3]
# Respective ids of available time intervals in Tree 2
id2 <-sapply(1:(d-2), function(j) which(complete.cases(t[,j])))</pre>
id13.2<-id2[[1]];id24.3<-id2[[2]];id35.4<-id2[[3]]
# List of available conditional data needed for estimation in Tree 2
condata1 <- list(vv1.2[id12%in%id13.2,2],vv3.2[id23%in%id13.2,2],
                vv2.3[id23%in%id24.3,2], vv4.3[id34%in%id24.3,2],
                vv3.4[id34%in%id35.4,2],vv5.4[id45%in%id35.4,2])
# Estimation of model parameters of pair copulas in Tree 2
fit<- sapply(1:(d-2), function(j) LBiCopFit(u1 = condata1[[2*j-1]],
                u2 = condata1[[2*j]], x=t[,j][id2[[j]]], family=family.set,
                repar="pearson", start = c(0.01, 0.01))
fit.beta.T2<- sapply(1:(d-2), function(j) c(fit[1,j],fit[2,j]))
11.T2<-sum(unlist(fit[3,])) #loglikelihood value in Tree 2
fam.T2<-fit[4,] # selected family of pair copulas in Tree 2
tau.T2<- sapply(1:(d-2), function(j) LDVine.rho2tau(unlist(fit.beta.T2[,j]),
                                                      t[, j] [id2[[j]]]))
par.T2<- sapply(1:(d-2), function(j) BiCopTau2Par(fam.T2[[j]], tau.T2[[j]]))</pre>
# Obtain the pseudo-conditional marginals for Tree 3
vvv<-list()</pre>
for (j in 1:(d-3)){
  vvv[[j]] <- BiCopHfunc2(u1=condata1[[2*j-1]], u2=condata1[[2*j]],</pre>
                                  par.T2[[j]],family = fam.T2[[j]])
  vvv[[(d-3)+j]] \leftarrow BiCopHfunc2(u1=condata1[[2*j+2]], u2=condata1[[2*j+1]],
                                  par.T2[[j+1]], family = fam.T2[[j+1]])
# Store pseudo-conditional marginals with respective ids
vvv1.23 <-data.frame(id2[[1]],vvv[[1]])</pre>
vvv4.23 <-data.frame(id2[[2]],vvv[[3]])</pre>
vvv2.34 <-data.frame(id2[[2]],vvv[[2]])</pre>
```

```
vvv5.34 <-data.frame(id2[[3]],vvv[[4]])</pre>
# Calculate the time intervals for Tree 3
t<- sapply(1:(d-3), function(j) Visits[,j+3] - Visits[,j])
t.14.23<-t[,1];t.25.34<-t[,2]
# Respective ids of available time intervals in Tree 3
id3 <-sapply(1:(d-3), function(j) which(complete.cases(t[,j])))</pre>
id14.23<-id3[[1]];id25.34<-id3[[2]]
# List of available conditional data needed for estimation in Tree 3
condata2 <- list(vvv1.23[id13.2%in%id14.23,2],vvv4.23[id24.3%in%id14.23,2],
                 vvv2.34[id24.3%in%id25.34,2],vvv5.34[id35.4%in%id25.34,2])
# Estimation of model parameters of pair copulas in Tree 3
fit<- sapply(1:(d-3), function(j) LBiCopFit(u1 = condata2[[2*j-1]],
                u2 = condata2[[2*j]], x=t[,j][id3[[j]]], family=family.set,
                repar="pearson", start = c(0.01, 0.01))
fit.beta.T3<- sapply(1:(d-3), function(j) c(fit[1,j],fit[2,j]))</pre>
11.T3<-sum(unlist(fit[3,])) #loglikelihood value in Tree 3
fam.T3<-fit[4,] # selected family of pair copulas in Tree 3
tau.T3<- sapply(1:(d-3), function(j) LDVine.rho2tau(unlist(fit.beta.T3[,j]),
                                                      t[,i][id3[[i]]]))
par.T3<- sapply(1:(d-3), function(j) BiCopTau2Par(fam.T3[[j]], tau.T3[[j]]))</pre>
# Obtain the pseudo-conditional marginals for Tree 4
vvvv<-list()</pre>
for (j in 1:(d-4)){
  vvvv[[j]] <- BiCopHfunc2(u1=condata2[[2*j-1]], u2=condata2[[2*j]],</pre>
                                  par.T3[[j]],family = fam.T3[[j]])
  vvvv[[(d-4)+j]] \leftarrow BiCopHfunc2(u1=condata2[[2*j+2]], u2=condata2[[2*j+1]],
                                  par.T3[[j+1]], family = fam.T3[[j+1]])
}
# Store pseudo-conditional marginals with respective ids
vvvv1.234 <-data.frame(id3[[1]],vvvv[[1]])</pre>
vvvv5.234 <-data.frame(id3[[2]],vvvv[[2]])</pre>
# Calculate the time intervals for Tree 4
t<- sapply(1:(d-4), function(j) Visits[,j+4] - Visits[,j])
t.15.234<-t[,1]
# Respective ids of available time intervals in Tree 4
```

```
id4 <-sapply(1:(d-4), function(j) which(complete.cases(t[,j])))</pre>
id15.234<-id4[,1]
# List of available conditional data needed for estimation in Tree 4
condata3 <- list(vvvv1.234[id14.23%in%id15.234,2],</pre>
                 vvvv5.234[id25.34%in%id15.234,2])
# Estimation of copula parameters of pair copulas in Tree 4
fit<- sapply(1:(d-4), function(j) LBiCopFit(u1 = condata3[[2*j-1]],
               u2 = condata3[[2*j]], x=t[,j][id4[,j]], family=family.set,
               repar="pearson", start = c(0.01,0.01))
fit.beta.T4<- sapply(1:(d-4), function(j) c(fit[1,j],fit[2,j]))</pre>
11.T4<-sum(unlist(fit[3,])) #loglikelihood value in Tree 4
fam.T4<-fit[4,] # selected family of pair copulas in Tree 4
tau.T4<- sapply(1:(d-4), function(j) LDVine.rho2tau(unlist(fit.beta.T4[,j]),
                                                     t[,i][id4[,i]]))
par.T4<- sapply(1:(d-4), function(j) BiCopTau2Par(fam.T4[[j]], tau.T4[,j]))</pre>
## END fitted model
# Store parameter estimates
beta.fit <-list(fit.beta.T1,fit.beta.T2,fit.beta.T3,fit.beta.T4)</pre>
# Store the selected copula families
family.selected<-data.frame(fam.T1,fam.T2,fam.T3,fam.T4)</pre>
colnames(family.selected)<-c("fam.T1","fam.T1","fam.T1","fam.T1",</pre>
                              "fam.T2", "fam.T2", "fam.T2",
                              "fam.T3", "fam.T3", "fam.T4")
family.selected
     fam.T1 fam.T1 fam.T1 fam.T2 fam.T2 fam.T2 fam.T3 fam.T3 fam.T4
##
## 1
          4
                 4
                        4
                               13
                                      14
                                             14
                                                    13
                                                             5
                                                                    1
                                                                           1
# Copula log-likelihood value for HET-P model
Cloglik HETByPair <- 11.T1+11.T2+11.T3+11.T4; Cloglik HETByPair
## [1] 178.7816
# Store the copula parameters and families for quantile prediction
par.fit.HET <- list(par.T1,par.T2,par.T3,par.T4)</pre>
```

Conditional Quantile Prediction

We select a subject that has 5 measurements. We pretend that the selected subject has only 4 measurements rather than 5 measurements and predict the conditional 5%-, 50%- and 95%-quantiles for its fifth measurement based on the first four measurements.

```
# id of selected individual and corresponding vector of measurements
id.sel <- 453
y.sel <- MFUS[MFUS$id == id.sel, 6]
y.sel

## [1] 80 70 90 70 90

# Covariate matrix (including intercept)
X.sel <- cbind(1, as.matrix(MFUS[MFUS$id == id.sel, c(3, 4, 5)]))
# Time variable for selected id
time.sel<- MFUS[MFUS$id==id.sel, 3]

# Estimated covariate vector of the fixed effects
b <- LMM.Exp$coefficients$fixed

# Quantile levels to be estimated
alpha.level <- c(0.05, 0.5, 0.95)</pre>
```

Linear Mixed Model (LMM)

Since $\mathbf{y}_i = (y_{i,1}, y_{i,2}, y_{i,3}, y_{i,4}, y_{i,5})^{\top}$ is assumed to be normally distributed, the univariate conditional distribution of $y_{i,5}$ given $(y_{i,1}, y_{i,2}, y_{i,3}, y_{i,4})^{\top}$ is univariate normal with a certain mean and variance depending on the parameters of the distribution of \mathbf{y}_i . Therefore, we first extract the covariance structure of the linear mixed model.

```
d < -5
Var.mat <- matrix(0, d , d)</pre>
for (i in 1:d){
  for (j in 1:d){
    Var.mat[i, j] <- exp(- abs(i-j)/Range.par)</pre>
  }
Var.mat <- Var.mat*sd.error^2 + sd.random^2</pre>
# Compute parameters of the conditional distribution of y_{i} \{i_{i}, j_{i}\} given
\# (y_{i,1}, y_{i,2}, y_{i,3}, y_{i,4})
cond.param <- condMVN(mean = X.sel%*%b,</pre>
                       sigma = Var.mat,
                       dependent.ind = 1.
                       given.ind = 2:5,
                       X.given = y.sel[1:(d-1)],
                       check.sigma = TRUE)
mu.cond <- cond.param$condMean # mean
sigma.cond <- sqrt(cond.param$condVar) # standard deviation</pre>
# Determine conditional quantiles for LMM
y.quant1 <- qnorm(alpha.level, mean = mu.cond, sd = sigma.cond)
y.quant1
```

[1] 64.12492 75.50962 86.89431

D-vine based copula models

For the D-vine copula models HOM–P and HET–P, we first transform the measurements to the uniform scale using the probability integral transformation. After that we calculate the D-vine quantile of the fifth measurement on the copula scale and then finally we transform these predictions to the original scale using the marginal quantile function of the fifth measurement.

```
u1.sel <- pnorm(q = y.sel[1], mean = X.sel[1, ]%*%b, sd = phi)
u2.sel <- pnorm(q = y.sel[2], mean = X.sel[2, ]%*%b, sd = phi)
u3.sel <- pnorm(q = y.sel[3], mean = X.sel[3, ]%*%b, sd = phi)
u4.sel <- pnorm(q = y.sel[4], mean = X.sel[4, ]%*%b, sd = phi)</pre>
```

Time-homogeneous D-vine copula model (HOM-P)

```
# Calculate the quantiles on the coupla scale
u_quant.p5 <- DvineQuant (p = alpha.level[1], u = data.frame(u1.sel,</pre>
                     u2.sel, u3.sel, u4.sel), family.set = familyset.HOM,
                     par.set = parset.HOM)
u quant.p50 <- DvineQuant (p = alpha.level[2], u = data.frame(u1.sel,
                     u2.sel, u3.sel, u4.sel), family.set = familyset.HOM,
                     par.set = parset.HOM)
u quant.p95 <- DvineQuant (p = alpha.level[3], u = data.frame(u1.sel,
                     u2.sel, u3.sel, u4.sel), family.set = familyset.HOM,
                     par.set = parset.HOM)
# Transform the estimated quantiles from the copula scale to the
# original scale
y_{quant.p5} \leftarrow q_{norm}(p = u_{quant.p5}, mean = X.sel[5, ]%*%b, sd = phi)
y quant.p50 \leftarrow qnorm(p = u quant.p50, mean = X.sel[5, ]%*%b, sd = phi)
y quant.p95 \leftarrow qnorm(p = u quant.p95, mean = X.sel[5, ]%*%b, sd = phi)
y.quant2<-c(y_quant.p5,y_quant.p50,y_quant.p95)</pre>
y.quant2
```

[1] 65.95408 77.50066 89.47259

Time-heterogeneous D-vine copula model (HET–P)

```
# Estimated copula parameters from fitted HET-P model
par.id <- sapply(1:(d-1), function(j) which(id1[[j]] == id.sel))
par.T1 <- sapply(1:(d-1), function(j) par.T1[[j]][par.id[j]])

par.id <- sapply(1:(d-2), function(j) which(id2[[j]] == id.sel))
par.T2 <- sapply(1:(d-2), function(j) par.T2[[j]][par.id[j]])

par.id <- sapply(1:(d-3), function(j) which(id3[[j]] == id.sel))
par.T3 <- sapply(1:(d-3), function(j) par.T3[[j]][par.id[j]])

par.id <- sapply(1:(d-4), function(j) which(id4[,j] == id.sel))
par.T4 <- sapply(1:(d-4), function(j) par.T4[,j][par.id[j]])

# Store the estimated copula parameters from fitted HET-P model
parset.HET = list(par.T1, par.T2, par.T3,par.T4)</pre>
```

```
# Calculate the quantiles on the coupla scale
u quant.p5 <- DvineQuant (p = alpha.level[1], u = data.frame(u1.sel,
                   u2.sel, u3.sel, u4.sel), family.set = familyset.HET,
                   par.set = parset.HET)
u_quant.p50 <- DvineQuant (p = alpha.level[2], u = data.frame(u1.sel,</pre>
                   u2.sel, u3.sel, u4.sel), family.set = familyset.HET,
                   par.set = parset.HET)
u quant.p95 <- DvineQuant (p = alpha.level[3], u = data.frame(u1.sel,
                   u2.sel, u3.sel, u4.sel), family.set = familyset.HET,
                   par.set = parset.HET)
# Transform the estimated quantiles from the copula scale to the
# original scale
y quant.p5 <- qnorm(p = u quant.p5, mean = X.sel[5, ]%*%b, sd = phi)
y quant.p50 <- qnorm(p = u quant.p50, mean = X.sel[5, ]%*%b, sd = phi)
y_{quant.p95} \leftarrow q_{norm}(p = u_{quant.p95}, mean = X.sel[5, ]%*%b, sd = phi)
y.quant3<-c(y quant.p5,y quant.p50,y quant.p95)</pre>
y.quant3
## [1] 66.48062 81.31704 93.44709
# Save the prediction results in "results" folder
# This is the part of result from table 9 (Subject 3) of manuscript.
y.quant<-rbind(y.quant1,y.quant2,y.quant3)</pre>
rownames(y.quant)<-c("LMM","HOM","HET")</pre>
colnames(y.quant) < -c("5\%", "50\%", "95\%")
y.quant;y.sel
##
             5%
                     50%
                               95%
## LMM 64.12492 75.50962 86.89431
## HOM 65.95408 77.50066 89.47259
## HET 66.48062 81.31704 93.44709
## [1] 80 70 90 70 90
write.table(round(y.quant,2),file=here("results","y.quant.txt"))
write.table(y.sel,file=here("results","y.sel.txt"))
```