

II Counting Sort

A { 2, 1, 5, 3, 1, 2, 5 } B { }
 1 2 3 4 5 6 7 0 1 2 3 4 5 6

i=7
 B { , , , , , 5 } C { 0, 2, 4, 5, 5, 6, 7 }

i=6
 B { , , , 2, , 5 } C { 0, 2, 3, 5, 5, 6, 7 }

i=5
 B { , 1, , 2, , 5 } C { 0, 1, 3, 5, 5, 6, 7 }

i=4
 B { , 1, , 2, 3, , 5 } C { 0, 1, 3, 4, 5, 6, 7 }

i=3
 B { , 1, , 2, 3, 5, 5 } C { 0, 1, 3, 4, 5, 5, 7 }

i=2
 B { 1, 1, , 2, 3, 5, 5 } C { 0, 0, 3, 4, 5, 5, 7 }

i=1
 B { 1, 1, 2, 2, 3, 5, 5 } C { 0, 0, 2, 4, 5, 5, 7 }

I Heap Sort

a) - left & right $O(n)$ because we have to traverse the linked list

- parent: $O(2n) \rightarrow O(n)$ because we have to find the children first and then traverse to find the parent

b)

- find Max() = $O(1)$ Because Max is at the beginning of the heap

- insert (key): $O(n)$ b/c we need time to traverse to the place needed to be insert

- extract Max() = $O(n)$ b/c when we extract max, we have to reassign pointers of the heap to create a new heap with a new Max

III Hash Table

$$1) h(2) = 2 \bmod 10 = 2$$

$$h(21) = 21 \bmod 10 = 1$$

$$h(3) = 3 \bmod 10 = 3$$

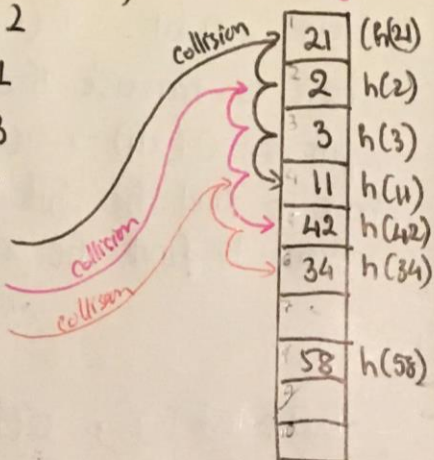
$$h(58) = 58 \bmod 10 = 8$$

$$h(11) = 11 \bmod 10 = 1$$

$$h(42) = 42 \bmod 10 = 2$$

$$h(34) = 34 \bmod 10 = 4$$

a) linear probing



b)

$$k.s = 14.10$$

$$= 140$$

$$= 1000\ 1101_2$$

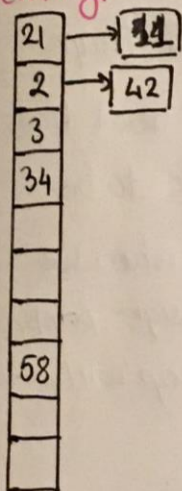
The right most $w=4$ bits: 1101

Convert the left most $p=3$ bit back to int:

$$\text{101} \quad 110 = \boxed{6}$$

$h(14) = 6$ using implementation described in the note

b) chaining



start at 0?

$$2) h(k) = \lfloor m(kA - \lfloor kA \rfloor) \rfloor \quad A=0.625 \quad m=8$$

$$h(8) = \lfloor 8 \cdot (8 \cdot 0.625 - \lfloor 8 \cdot 0.625 \rfloor) \rfloor$$

$$= \lfloor 8 \cdot (5 - 5) \rfloor = \boxed{0}$$

$$h(14) = \lfloor 8 \cdot (14 \cdot 0.625 - \lfloor 14 \cdot 0.625 \rfloor) \rfloor$$

$$= \lfloor 8 \cdot (8.75 - 8) \rfloor = \cancel{10.5} \neq 10.5$$

$$= \lfloor 6 \rfloor = \boxed{6}$$

$$h(5) = \lfloor 8 \cdot (5 \cdot 0.625 - \lfloor 5 \cdot 0.625 \rfloor) \rfloor$$

$$= \lfloor 8 \cdot (3.125 - 3) \rfloor$$

$$= \lfloor 1 \rfloor = \boxed{1}$$

