

Hamming Code (systematic)

- $P_1 = \text{XOR of bits at positions (0, 1, 3, 4, 6)}$
- $P_2 = \text{XOR of bits at positions (0, 2, 3, 5, 6)}$
- $P_3 = \text{XOR of bits at positions (1, 2, 4, 7)}$
- $P_4 = \text{XOR of bits at positions (4, 5, 6, 7)}$
- $P_5 = \text{XOR of all bits including } P_1 \text{ to } P_4$

Parity Bits					Original Bits							
5	4	3	2	1	7	6	5	4	3	2	1	0
1	1	0	0	1	0	0	1	0	0	1	1	0

Code word

Checking:

- $C_1 = \text{XOR of bits at positions (} P_1, 0, 1, 3, 4, 6 \text{)} == 0?$
- $C_2 = \text{XOR of bits at positions (} P_2, 0, 2, 3, 5, 6 \text{)} == 0?$
- $C_3 = \text{XOR of bits at positions (} P_3, 1, 2, 4, 7 \text{)} == 0?$
- $C_4 = \text{XOR of bits at positions (} P_4, 4, 5, 6, 7 \text{)} == 0?$
- $C_5 = \text{XOR of all bits including } P_1 \text{ to } P_5 == 0?$

No errors if $(C_1, C_2, C_3, C_4, C_5)$ equals $(0, 0, 0, 0, 0)$

Original data word

7	6	5	4	3	2	1	0
0	0	1	0	0	1	1	0

Bit position

Value 38

AN encoding (non-systematic)

Multiplication value with a constant A;
e.g., $A = 29$

$38 * 29 = 1102$ (hardened value)

1	1	10	9	8	7	6	5	4	3	2	1	0
2	1											
0	0	1	0	0	0	1	0	0	1	1	1	0

Code word

Hardening

Detection

Checking:

$\text{mod } A == 0?$

Example:
 $1102 \text{ mod } 29 = 0$

No errors when result equals zero