

## Chapter 2

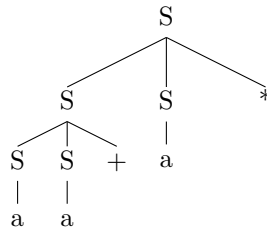
### 2.2.7 Exercises for Section 2.2

#### Exercise 2.2.1

a)

$$\begin{aligned} S &\rightarrow S1 S2 * \\ S1 &\rightarrow S3 S4 + \\ S2 &\rightarrow a \\ S3 &\rightarrow a \\ S4 &\rightarrow a \end{aligned}$$

b)



c) The language generated is the post-fix notation of numbers with multiplication and addition operands.

#### Exercise 2.2.2

- The language created is  $0^n 1^n$ , where  $n \in N^*$ .
- This language is the prefix notation of the addition and difference of the digit  $a$ .
- The language is  $[(^n)^n]^m$ , where  $m, n \in N$  and for every different  $m$  the  $n$  is different, so closed parenthesis of any depth and length.

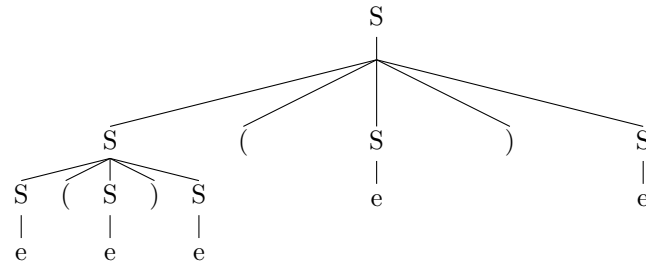
- d) The language is  $(a^n b^n)^m$ , where  $m, n \in \mathbb{N}$  and for different  $m$ , the  $n$  is also different. So different sequences of  $a$  and  $b$  where both letter have the same number of appearances.
- e) This is a grammar to create regular languages ([Wikipedia link](#)).

### 2.2.3

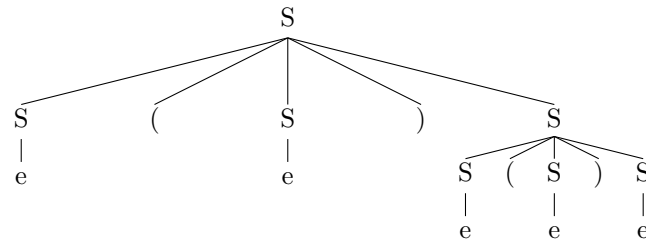
The grammars that are ambiguous are:

- Grammar c: Creating the string " $()()$ " can be done in two ways

Way A:

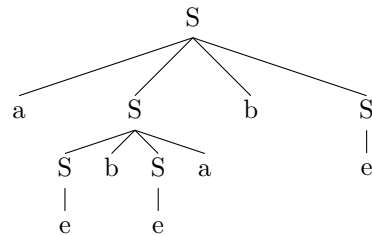


Way B:

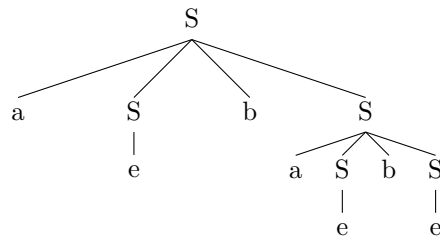


- Grammar d: Creating the string " $abab$ " can be done in two ways:

Way A:

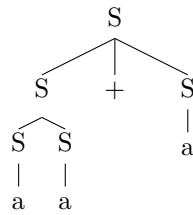


Way B:

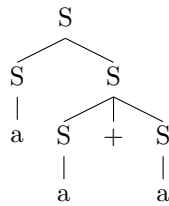


- Grammar e: Creating the string "a a+a" can be done in two ways:

Way A:



Way B:



#### Excercise 2.2.4

- a) This is called reverse polish notation ([Wikipedia Link](#))

$$expr \rightarrow expr\ expr\ op \mid digit$$

- b)