Exploration of Generalized Linear Models

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Abstract

Our project investigates three different generalized linear models by applying them to the Palmer penguins dataset. This set is a collection of data about 344 observations studying 8 variables: species, island, bill length, bill depth, flipper length, body mass, sex, and year. Our report applies this data in different ways to the Gaussian, multinomial, and ANCOVA models. Through our study, we found that the Gaussian model used only flipper length as a significant regressor and this model was a better predictor than the original model used. The multinomial model showed that bill length and bill depth are both significant in predicting the species of penguin. The ANCOVA model showed that flipper length has a significant relationship with the body mass of penguins and when controlling for flipper length, species also had a significant impact on the body mass. When testing for a difference of means in body mass between species, it was concluded that they are not equal.

Introduction

Our report is an investigation into generalized linear models (GLMs). These models unify linear and nonlinear regression models to develop models for response variables whose distributions are nonnormal and are part of the exponential family (ex: normal, Poisson, binomial, exponential, and gamma distributions). The fundamental idea of GLMs is its two components: the response distribution and the link function. A link function is a function that relates the mean of the response distribution to a linear predictor. This function allows statisticians to map a nonlinear relationship to a linear one.

There are multiple advantages to using GLMs over simple linear regression. The main benefit is that the response variable can have any form of the exponential distribution; it does not need to be transformed to the normal distribution. GLMs are also more flexible and less susceptible to overfitting. There are many different types of GLMs. In our project, we specifically focus on the Gaussian, multinomial, and ANCOVA models.

To apply these models, we will utilize the Palmer's penguins dataset. This set was collected from the Palmer Archipelago in Antarctica. It consists of data from 344 penguins across three species (chinstrap, gentoo, adelie) collected from three different islands in the archipelago. Its variables include species, island, bill length (mm), bill depth (mm), flipper length (mm), body mass (g), sex, and year. The application of this data will allow us to learn more about these generalized linear models and notice the differences between the models we have chosen to study.

Programs Used and Packages Required

For this project, the use of R and RStudio were utilized in order to fit the data across all three GLMs. Certain packages were required in order to complete the functions for each model. These included the packages: palmerpenguins, tidyverse, caret, VGAM, nnet, rstatix, car, and multcomp.

The Data

```
head(palmerpenguins::penguins)
## # A tibble: 6 × 8
                        bill length mm bill depth mm flipper l...¹ body ...² sex
##
     species island
year
##
     <fct>
             <fct>
                                 <dbl>
                                                <dbl>
                                                            <int>
                                                                     <int> <fct>
<int>
                                                              181
                                                                      3750 male
## 1 Adelie
             Torgersen
                                  39.1
                                                 18.7
2007
## 2 Adelie Torgersen
                                  39.5
                                                 17.4
                                                              186
                                                                      3800 fema...
2007
## 3 Adelie Torgersen
                                  40.3
                                                 18
                                                              195
                                                                      3250 fema...
2007
## 4 Adelie
             Torgersen
                                  NA
                                                 NA
                                                               NA
                                                                        NA <NA>
2007
## 5 Adelie
             Torgersen
                                  36.7
                                                 19.3
                                                              193
                                                                      3450 fema...
2007
## 6 Adelie Torgersen
                                  39.3
                                                 20.6
                                                              190
                                                                      3650 male
2007
## # ... with abbreviated variable names ¹flipper_length_mm, ²body_mass_g
summary(palmerpenguins::penguins)
##
                           island
                                     bill_length_mm
                                                      bill_depth_mm
         species
##
   Adelie
                    Biscoe
                                     Min.
                                            :32.10
                                                      Min. :13.10
             :152
                              :168
    Chinstrap: 68
                    Dream
                              :124
                                     1st Qu.:39.23
##
                                                      1st Qu.:15.60
##
    Gentoo
             :124
                    Torgersen: 52
                                     Median :44.45
                                                      Median :17.30
##
                                     Mean
                                             :43.92
                                                      Mean
                                                            :17.15
                                                      3rd Qu.:18.70
##
                                     3rd Qu.:48.50
##
                                     Max.
                                             :59.60
                                                      Max.
                                                             :21.50
##
                                     NA's
                                                      NA's
                                             :2
                                                             :2
##
    flipper length mm
                       body_mass_g
                                          sex
                                                         year
                                      female:165
##
    Min.
           :172.0
                      Min.
                              :2700
                                                    Min.
                                                           :2007
##
    1st Qu.:190.0
                      1st Qu.:3550
                                      male :168
                                                    1st Qu.:2007
##
   Median :197.0
                      Median :4050
                                      NA's : 11
                                                    Median :2008
##
   Mean
           :200.9
                      Mean
                              :4202
                                                    Mean
                                                           :2008
##
    3rd Qu.:213.0
                      3rd Qu.:4750
                                                    3rd Qu.:2009
##
    Max.
           :231.0
                      Max.
                              :6300
                                                    Max.
                                                           :2009
    NA's
                      NA's
##
           :2
                              :2
```

Gaussian Model

What is a Gaussian Model

A Gaussian or normal distribution model is used to model functions with a finite number of points. This model is part of the exponential family of distributions. When performing a linear regression using a Gaussian model, the distribution of y given x is a Gaussian distribution with some mean mu and variance sigma². A linear relationship between the data and the parameters of the distribution is expected. The link function for the gaussian model is the identity function.

Assumption for a Gaussian Model

- 1. Cases are independent
- 2. The response fits a distribution in the exponential family
- 3. Linearity between the transformed expected response in terms of the link function and the explanatory variables

Setup

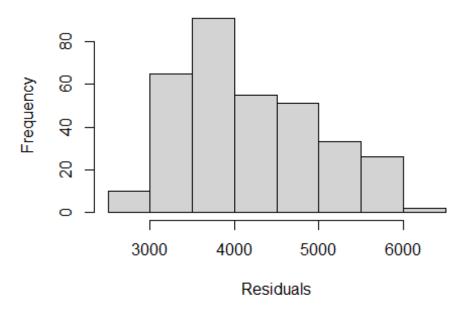
```
library(palmerpenguins)
library(tidyverse)
library(caret)
penguins_df <- na.omit(penguins)
continuous <- select_if(penguins_df, is.numeric)</pre>
```

Checking Assumption 1 and 2

Each case from the data set is independent.

```
hist(penguins_df$body_mass_g, xlab = 'Residuals', main = 'Histogram of
Residuals')
```

Histogram of Residuals



This doesn't exactly appear to be normally distributed however we will continue with the modeling.

Splitting the Data into Test and Training Sets

```
trainindex <- createDataPartition(penguins_df$species, p = 0.85, list =</pre>
FALSE)
training set <- penguins df[trainindex,]</pre>
testing_set <- penguins_df[-trainindex,]</pre>
model <- glm(body_mass_g ~ bill_length_mm + bill_depth_mm +</pre>
flipper length mm, data = training set)
summary(model)
##
## Call:
## glm(formula = body mass g \sim bill length mm + bill depth mm +
##
       flipper_length_mm, data = training_set)
##
## Deviance Residuals:
##
        Min
                    10
                          Median
                                         3Q
                                                   Max
## -1072.32
               -284.68
                          -19.63
                                     239.50
                                               1287.72
##
## Coefficients:
##
                       Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                                       <2e-16 ***
                      -6212.779
                                    606.915 -10.237
## bill_length_mm
                          5.845
                                      5.816
                                               1.005
                                                        0.316
                                     14.624
## bill depth mm
                         11.308
                                               0.773
                                                        0.440
```

```
## flipper length mm
                                   2.691 18.431 <2e-16 ***
                       49.600
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for gaussian family taken to be 152068.5)
##
##
      Null deviance: 179990518
                                on 284
                                        degrees of freedom
## Residual deviance: 42731251
                                on 281
                                        degrees of freedom
## AIC: 4215.4
##
## Number of Fisher Scoring iterations: 2
```

As we can see the only regression coefficient that has a low enough p value to reject the null hypothesis is for the flipper length variable so we will remake the model to only include that variable.

```
model <- glm(body_mass_g ~ flipper_length_mm, data = training_set)</pre>
summary(model)
##
## Call:
## glm(formula = body mass g ~ flipper length mm, data = training set)
##
## Deviance Residuals:
##
      Min
                 10
                      Median
                                   3Q
                                           Max
                        -9.7
## -1056.1
             -258.1
                                243.6
                                        1295.0
##
## Coefficients:
                      Estimate Std. Error t value Pr(>|t|)
##
                                                     <2e-16 ***
## (Intercept)
                     -5868.906
                                  336.112
                                           -17.46
                                            30.00
                                                     <2e-16 ***
## flipper length mm
                        50.130
                                    1.671
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for gaussian family taken to be 152109)
##
##
       Null deviance: 179990518
                                 on 284
                                         degrees of freedom
## Residual deviance: 43046833 on 283 degrees of freedom
## AIC: 4213.5
##
## Number of Fisher Scoring iterations: 2
```

Making Predictions with the Model

```
predictions <- predict.glm(model, testing_set, type = "link")
head(predictions)

## 1 2 3 4 5 6
## 3455.281 3906.452 3906.452 3405.151 3906.452 3304.891</pre>
```

Calculating RMSE of the Model

We will calculate the root mean squared error to evaluate the error of the model

```
RMSE <- sqrt(sum((predictions - testing_set$body_mass_g)^2) /
length(predictions))
RMSE
## [1] 412.4595</pre>
```

This number by itself doesn't give us too much information. However, we could compare it to the RMSE of other models to compare the effectiveness of different models.

Comparing RMSE

We will compare it to the RMSE of the original model we created.

```
model2 <- glm(body_mass_g ~ bill_length_mm + bill_depth_mm +
flipper_length_mm, data = training_set)
predictions2 <- predict.glm(model2, testing_set)
RMSE2 <- sqrt(sum((predictions2 - testing_set$body_mass_g)^2) /
length(predictions))
RMSE2
## [1] 411.7978</pre>
```

We can see that the previous model had a slightly lower RMSE indicating better predictive power.

Multinomial Logistic Model

What is a Multinomial Logistic Model

Multinomial Logistic regression is used to predict a single categorical variable using one or more other variables. It extends the approach for situations where the independent variable has more than two categories. This model can be used for classification. If our dependent variable is a categorical variable, we would be able to predict the factor level based on other variables that could be continuous. The link function for this model is the generalized logit.

Assumptions of Multinomial Logistic Models

- 1. Linearity
- 2. No Outliers
- 3. Independence
- 4. No Multicollinearity

Setup

```
library(caret)
library(tidyverse)
require(nnet)
library(VGAM)
library(car)
penguins df <- palmerpenguins::penguins
penguins df %>%
 group_by(species, island) %>%
 summarise(n_records = n())
## # A tibble: 5 × 3
## # Groups: species [3]
    species
              island n_records
##
##
    <fct>
              <fct>
                           <int>
## 1 Adelie
              Biscoe
                              44
## 2 Adelie
              Dream
                               56
## 3 Adelie
              Torgersen
                               52
## 4 Chinstrap Dream
                               68
## 5 Gentoo
              Biscoe
                              124
```

We can see that the Chinstrap and Gentoo species only appear to inhabit one island while the Adelie species inhabits three different islands islands.

```
penguins_df <- penguins_df %>%
   mutate(species_binary = ifelse(species == 'Adelie', 'Adelie', 'Other'))

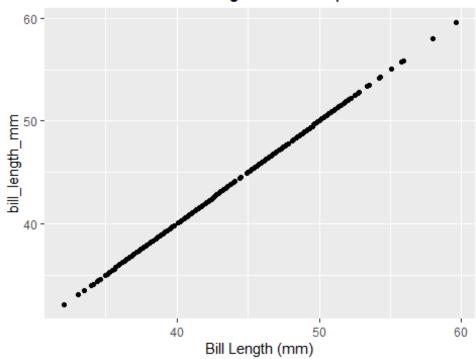
penguins_df$species_binary <- factor(penguins_df$species_binary, levels = c("Other", "Adelie"))</pre>
```

Checking Assumption 1

Linearity between the response and predictors.

```
ggplot(penguins_df, aes(x = bill_length_mm, y = bill_length_mm)) +
  geom_point() +
  ggtitle("Scatter Plot for Bill Length vs Bill Depth") +
  xlab("Bill Length (mm)")
```

Scatter Plot for Bill Length vs Bill Depth



```
ylab("Bill Depth (mm")

## $y
## [1] "Bill Depth (mm"

##
## attr(,"class")
## [1] "labels"
```

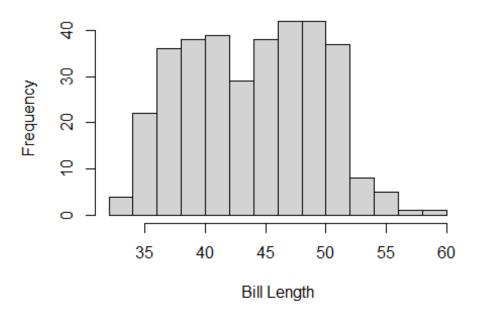
We can see that the relationship seems to be linear.

Checking Assumption 2

No significant outliers

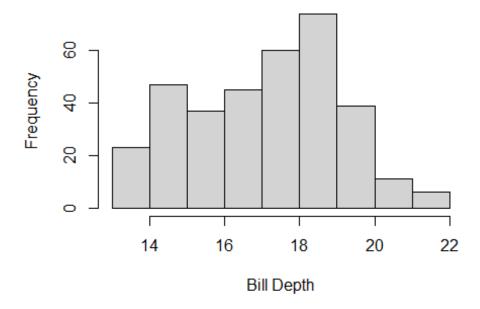
```
hist(penguins_df$bill_length_mm, xlab = "Bill Length", main = "Histogram of
Bill Length")
```

Histogram of Bill Length



hist(penguins_df\$bill_depth_mm, xlab = "Bill Depth", main = "Histogram of Bill Depth")

Histogram of Bill Depth



We can see that there are no significant outliers in the data.

Checking Assumption 3

Independence

```
fit <- vglm(species~island, multinomial, data = penguins_df)
anova(fit)

## Analysis of Deviance Table (Type II tests)

##
## Model: 'multinomial', 'VGAMcategorical'

##
## Link: 'multilogitlink'

##
## Response: species

##
## Df Deviance Resid. Df Resid. Dev Pr(>Chi)
## island 4 357.87 686 721.82 < 2.2e-16 ***

## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1</pre>
```

With the low p-value we would reject the null hypothesis and conclude that there is independence.

Checking Assumption 4

Little or no multicollinearity between the predictors

Since each of the variables we are using have a VIF < 5, multicollinearity is not an issue for our model.

Training Set, Testing Set, and Setting a Reference Level

The first step is the split the data into a training and testing set if both sets do not already exist for the desired data set.

```
index <- createDataPartition(penguins_df$species, p = 0.70, list = FALSE)
train <- penguins_df[index,]
test <- penguins_df[-index,]</pre>
```

Next we will set the reference level to the species Adelie since it is the only species that inhabits all the islands in this dataset.

```
train$species <- relevel(train$species, ref = "Adelie")
test$species <- relevel(test$species, ref = "Adelie")</pre>
```

Training the Model

```
multinom model <- multinom(species ~ bill length mm + bill depth mm, data =</pre>
train)
## # weights: 12 (6 variable)
## initial value 264.765562
## iter 10 value 26.606902
## iter 20 value 20.098640
## final value 20.073640
## converged
summary(multinom_model)
## Call:
## multinom(formula = species ~ bill length mm + bill depth mm,
##
       data = train)
##
## Coefficients:
             (Intercept) bill_length_mm bill_depth_mm
                                2.331506
## Chinstrap
               -28.75055
                                             -4.022688
## Gentoo
                16.57003
                                2.742346
                                             -7.907765
##
## Std. Errors:
##
             (Intercept) bill_length_mm bill_depth_mm
## Chinstrap
                              0.8731586
                15.40849
                                              1.820535
                21.21050
                              0.8873893
                                              2.085089
## Gentoo
## Residual Deviance: 40.14728
## AIC: 52.14728
```

Computing p-values For the Regression Coefficients

```
(z <- summary(multinom model)$coefficients /</pre>
summary(multinom_model)$standard.errors )
             (Intercept) bill_length_mm bill_depth_mm
## Chinstrap
              -1.8658902
                                2.670198
                                              -2.209619
## Gentoo
               0.7812185
                                3.090353
                                              -3.792531
(p \leftarrow (1 - pnorm(abs(z), 0, 1)) *2)
             (Intercept) bill_length_mm bill_depth_mm
              0.06205673
                             0.007580654 0.0271316270
## Chinstrap
## Gentoo
              0.43467400
                             0.001999189 0.0001491199
```

Since all of the p-values are small we will reject the null hypothesis that the regression coefficients are equal to 0. In general, it is good practice to set an alpha level before starting any tests and using a Bonferroni correction when testing.

Converting the Coefficients to Odds by Taking the Exponentional of the Coefficients

By taking the exponential of the coefficients, we are able to see the change in the odds ratio with a 1 unit increase.

Model Prediction and Validation

```
multinom_preds <- predict(multinom_model, test, type = "class")
head(multinom_preds)

## [1] Adelie Adelie Adelie Adelie Adelie
## Levels: Adelie Chinstrap Gentoo</pre>
```

Viewing the First Few Predictions

```
head(round(fitted(multinom_model), 2))
     Adelie Chinstrap Gentoo
##
## 1
          1
                    0
## 2
          1
                    0
                           0
## 3
          1
                    0
                           0
## 5
          1
                    0
                           0
                    0
## 6
          1
                           0
## 7
                           0
```

Multinomial Regression predicts the probability of a particular observation.

Building a Classification Table

```
multinom_cm <- table(test$species, multinom_preds)</pre>
multinom cm
##
               multinom preds
##
                Adelie Chinstrap Gentoo
##
     Adelie
                    44
                                1
                               20
##
     Chinstrap
                     0
                                        0
     Gentoo
                                       36
```

Calculating Accuracy

```
round((sum(diag(multinom_cm))/sum(multinom_cm))*100,2)
## [1] 99.01
```

ANCOVA

What is ANCOVA

ANCOVA stands for analysis of covariance. Simply put, ANCOVA is a combination of ANOVA and linear regression as it deals with categorical and continuous variables. It is similar to ANOVA, analysis of variance, which tests for differences in mean responses to a categorical factor level. ANCOVA differs from ANOVA because it includes a continuous covariate in the model. The job of the covariate is to remove the unnecessary variation from the response variable. ANCOVA is useful when the covariate has a linear relationship with the dependent variable and does not have relationship with the categorical variable.

Assumptions of ANCOVA

- 1. Linearity between covariate and response at each level of the grouping variable
- 2. Homogeneity of regression slopes
- 3. Outcome variable is normally distributed
- 4. Homoscedasticity for all groups
- 5. No significant outliers

Setup

```
library(palmerpenguins)
library(tidyverse)
library(rstatix)
library(car)
library(multcomp)
df <- penguins
```

palmerspenguins contains the dataset penguins that we will be working with

tidyverse contains packages such as dplyr that is used for data manipulation and ggplot2 which is used for graphing

rstatix contains the function anova test

car contains the function Anova

multcomp contains the function glht

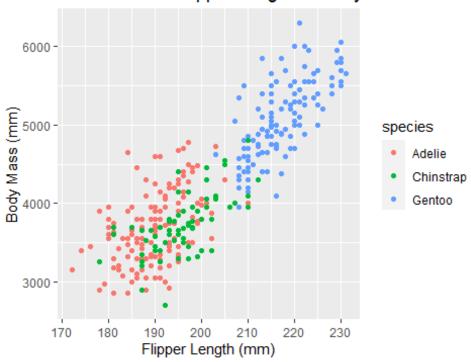
Checking assumption 1

Linearity between covariate and response at each level of the grouping variable

This can be done by graphing a scatter plot of the predictor vs the covariate grouped by the categorical variable. In this case, a scatter plot of flipper length vs body mass separated by species.

```
ggplot(df, aes(x = flipper_length_mm, y = body_mass_g, color = species)) +
  geom_point() +
  ggtitle('Scatter Plot of Flipper Length vs Body Mass for Each Species') +
  xlab('Flipper Length (mm)') +
  ylab('Body Mass (mm)')
```

Scatter Plot of Flipper Length vs Body Mass for Each



The predictor appears to be linear at every level of species.

Checking Assumption 2

Homogeneity of regression slopes

This can be checked by seeing if the interaction is significant between the group variable and the predictor.

```
anova_test(df, body_mass_g ~ flipper_length_mm + species + flipper_length_mm
* species)
## ANOVA Table (type II tests)
##
##
                        Effect DFn DFd
                                              F
                                                        p p<.05
                                                                  ges
## 1
             flipper_length_mm
                                  1 336 180.398 3.22e-33
                                                              * 0.349
## 2
                       species
                                  2 336
                                         18.886 1.69e-08
                                                              * 0.101
## 3 flipper_length_mm:species
                                                              * 0.032
                                  2 336
                                          5.532 4.00e-03
```

The interaction between flipper length and species is insignificant therefore not homogeneous. We will proceed for the sake of the exploration of ANCOVA but we will conclude that the results are invalid.

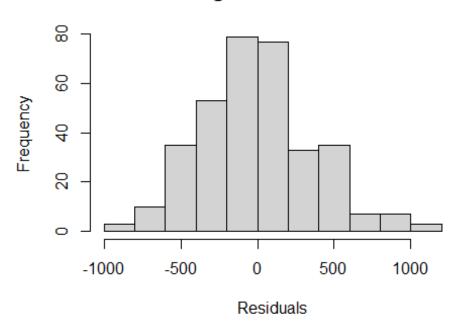
Checking Assumption 3

Outcome variable is normally distributed

This can be checked by viewing a histogram of the residuals

```
model <- lm(body_mass_g ~ flipper_length_mm * species, data = df)
hist(model$residuals, xlab = 'Residuals', main = 'Histogram of Residuals')</pre>
```

Histogram of Residuals



The histogram of the residuals appears to be approximately normally distributed.

Checking Assumption 4

Homoscedasticity for all groups

This can be checked using Bartlett's Test

```
newdf <- as.data.frame(cbind(df$species, model$residuals))
names(newdf) <- c('species', 'residuals')
bartlett.test(residuals ~ species, data = newdf)
##
## Bartlett test of homogeneity of variances
##
## data: residuals by species
## Bartlett's K-squared = 8.2283, df = 2, p-value = 0.01634</pre>
```

With a p-value of 0.3182 we would fail to reject the null hypothesis that the variances are the same across the three species if we were to use 0.01 as the alpha level. We can't use this assumption as it wouldn't result in failing to reject the null hypothesis.

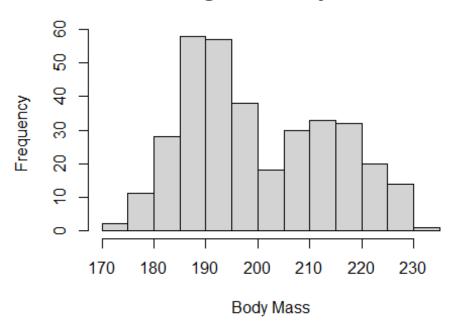
Checking Assumption 5

No significant outliers

This can be checked by viewing a histogram

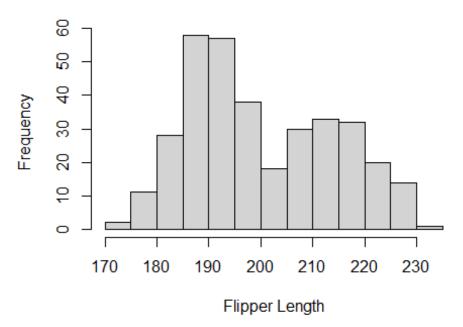
hist(df\$flipper_length_mm, xlab = 'Body Mass', main = 'Histogram of Body
Mass')

Histogram of Body Mass



hist(df\$flipper_length_mm, xlab = 'Flipper Length', main = 'Histogram of
Flipper Length')

Histogram of Flipper Length



There does not appear to be any significant outliers in the data.

With only 3 of our 5 assumptions holding, this exact ANCOVA would not yield valid results.

Running ANCOVA

We will perform ANCOVA with body mass as the response, flipper length as the covariate, and species as the factor variable.

```
fit <- aov(body_mass_g ~ flipper_length_mm + species, data = df)</pre>
Anova(fit, type = 'III')
## Anova Table (Type III tests)
##
## Response: body_mass_g
                               Df F value
                                              Pr(>F)
##
                       Sum Sq
## (Intercept)
                                   47.630 2.551e-11 ***
                      6717050
## flipper_length_mm 24776495
                                 1 175.687 < 2.2e-16 ***
## species
                      5187807
                                 2
                                    18.393 2.615e-08 ***
## Residuals
                     47666988 338
## Signif. codes:
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

When controlling for our covariate, flipper length, we can see that species has a significant impact on the body mass. We reject the null hypothesis and conclude that the mean body mass is not the same for each species.

The covariate, flipper length has a significant relationship with the body mass of penguins. There was also a significant effect of the species on the body mass after controlling for the effect of the flipper length.

Post Hoc Test

Next, we must run post hoc tests for comparing multiple means. We will perform this via Tukey contrasts.

```
posthoc <- glht(fit, linfct = mcp(species = 'Tukey'))</pre>
summary(posthoc)
##
##
     Simultaneous Tests for General Linear Hypotheses
## Multiple Comparisons of Means: Tukey Contrasts
##
##
## Fit: aov(formula = body mass g ~ flipper_length_mm + species, data = df)
## Linear Hypotheses:
                           Estimate Std. Error t value Pr(>|t|)
##
## Chinstrap - Adelie == 0
                           -206.51
                                         57.73
                                               -3.577 0.00105 **
## Gentoo - Adelie == 0
                             266.81
                                                 2.801 0.01411 *
                                         95.26
## Gentoo - Chinstrap == 0
                             473.32
                                         86.75
                                                 5.456 < 0.001 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Adjusted p values reported -- single-step method)
```

For the difference in means for each species, we reject the null hypothesis that they are equal and conclude that they are indeed not equal.

```
confint(posthoc)
##
##
     Simultaneous Confidence Intervals
## Multiple Comparisons of Means: Tukey Contrasts
##
## Fit: aov(formula = body_mass_g ~ flipper_length_mm + species, data = df)
##
## Quantile = 2.3339
## 95% family-wise confidence level
##
##
## Linear Hypotheses:
                           Estimate lwr
                                               upr
## Chinstrap - Adelie == 0 -206.5101 -341.2499
                                                -71.7704
## Gentoo - Adelie == 0
                            266.8096
                                       44.4699 489.1493
## Gentoo - Chinstrap == 0 473.3197 270.8604 675.7791
```

When we run a confidence interval for the difference in means, we can see that 0 is not in any of the intervals. In fact, none of the intervals are even close to 0.

Results

The Gaussian model yielded a model with only flipper length as a significant regressor to predict body mass with a lower RMSE than the original model (predicting body mass using bill length, bill depth, and flipper length).

The multinomial model showed that bill length and bill depth are both significant in predicting the species of penguin with a 94.06 accuracy.

The ANCOVA model showed that flipper length, the covariate, has a significant relationship with the body mass of penguins and when controlling for this covariate, species also had a significant impact on the body mass. When testing for a difference of means in body mass between species, it was concluded that they are not equal and a difference of means indeed exists.

Discussion

Although the three models all belong to the GLM family, each one is used in different situations and not all can perform the same functions. In our report, we used each model to analyze a different part of the dataset. The three models were useful for predicting the various response variables of the data. However, each model yielded different results.

The Gaussian model found that flipper length was a useful predictor of body mass. When compared to the original model, which used bill length, bill depth, and flipper length as predictors, the Gaussian model was shown to be a better predictor of body mass. However, these results may not be entirely accurate as the normality assumption is not completely satisfied.

The multinomial model identified bill length and bill depth as the most useful variables in predicting the species. In the summary table, each row corresponds to a model equation. The first row compares the species Chinstrap to the baseline species of Adelie. The second row compares Gentoo to the baseline species of Adelie. A unit increase of 1 results in a large odds ratio change. As the bill length increases, the species is more likely to be Chinstrap. As bill depth increases, the species is more likely to be Adelie. In the Gentoo model coefficients, Gentoos are less likely to be on Dream or Torgensen Islands than Adelie.

The ANCOVA model uses flipper length as the covariate. When controlling for this covariate, the species has a significant impact on the body mass. The covariate is also shown to have a significant relationship with the body mass of the penguins. Additionally, when testing for a difference of means in body mass between species, it was found that they are not equal. In the context of the data, this seems reasonable since penguin species are relatively different sizes. This ANCOVA, however, does not yield valid results since only three of the five assumptions hold for this model.

Each of the models contain different assumptions about the data, which has to be tested prior to fitting the data to the model. While the Palmer's penguins data can be applied to these three models, they cannot result in the same conclusions. The models predict different response variables and are used in different situations.

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