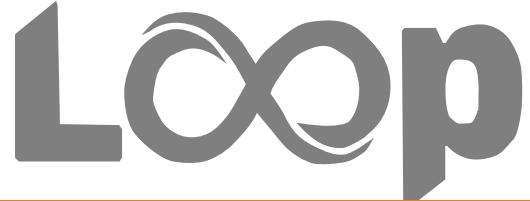


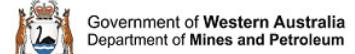
An integrated and interoperable platform enabling
3D stochastic geological modelling

Non-UWA (Personal)



Introduction to level-set inversion

Jeremie Giraud, Mark Lindsay, Mark Jessell



Government of Western Australia
Department of Mines and Petroleum



Providing geoscience data globally

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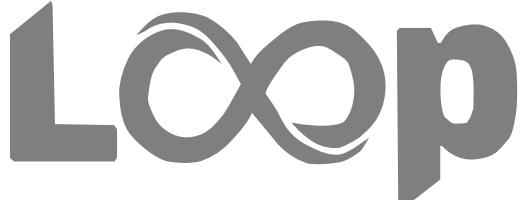
Jeremie Giraud has received funding from the European Union's Horizon 2020 research and innovation programme¹ under the Marie Skłodowska-Curie grant agreement No. 101032994.

¹ for more info about project:

<https://cordis.europa.eu/project/id/101032994>



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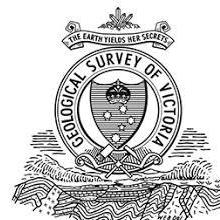
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Geological Survey of
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of Industry
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MONASH University



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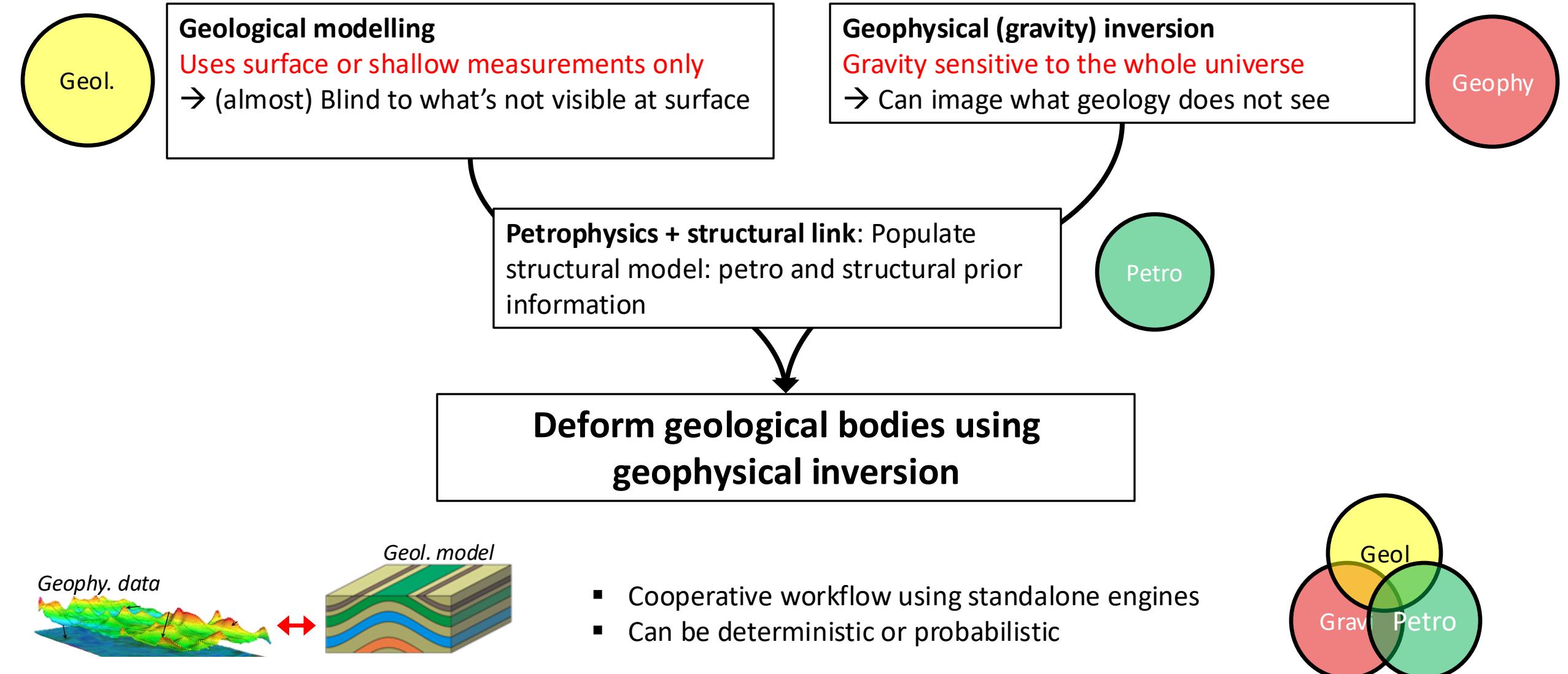
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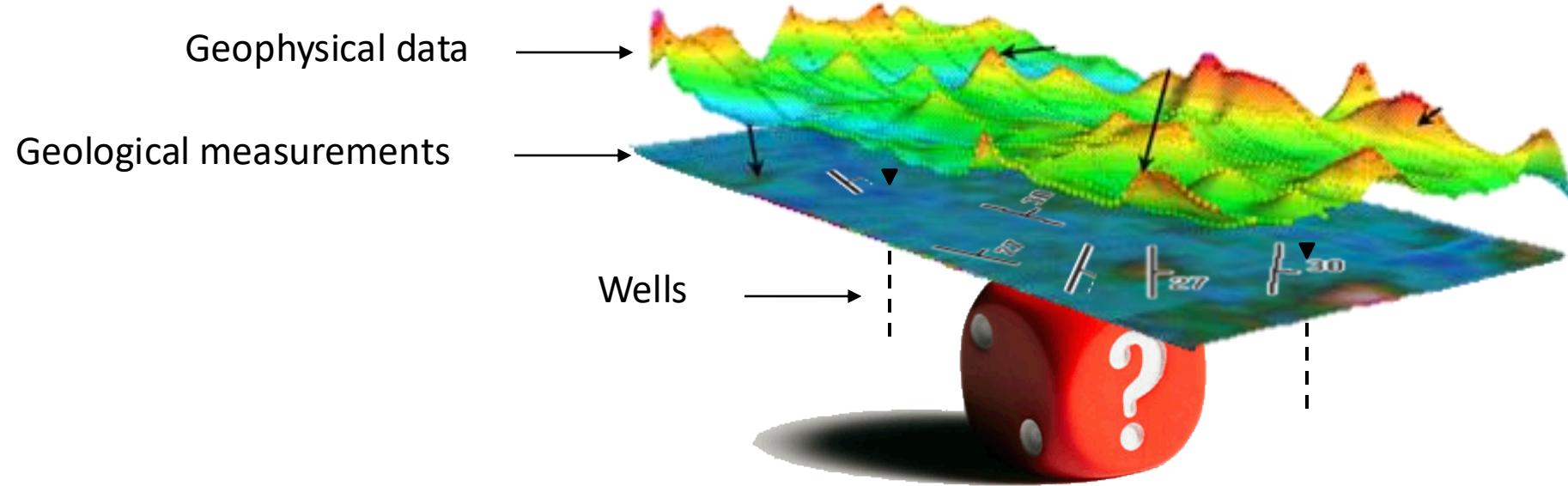
Overview

- Motivations
- Theoretical back
- Synthetic example
- Field application: Yerrida basin (WA)

Motivation and Objectives



Motivation and Objectives



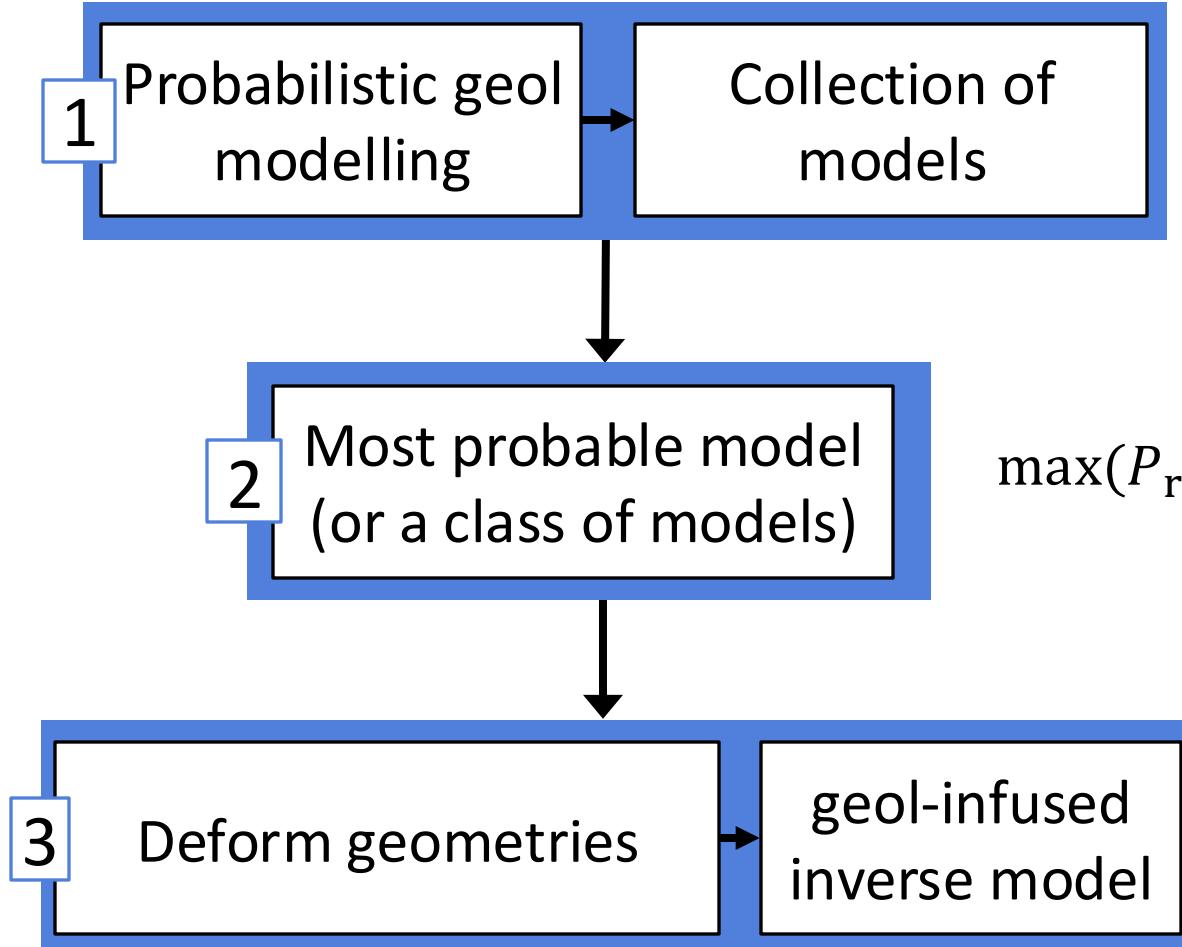
*Cooperative modelling with geological
modelling within geophysical inversion*

Workflow

Standalone geological modelling

Extraction of geological info.

Standalone gravity inversion



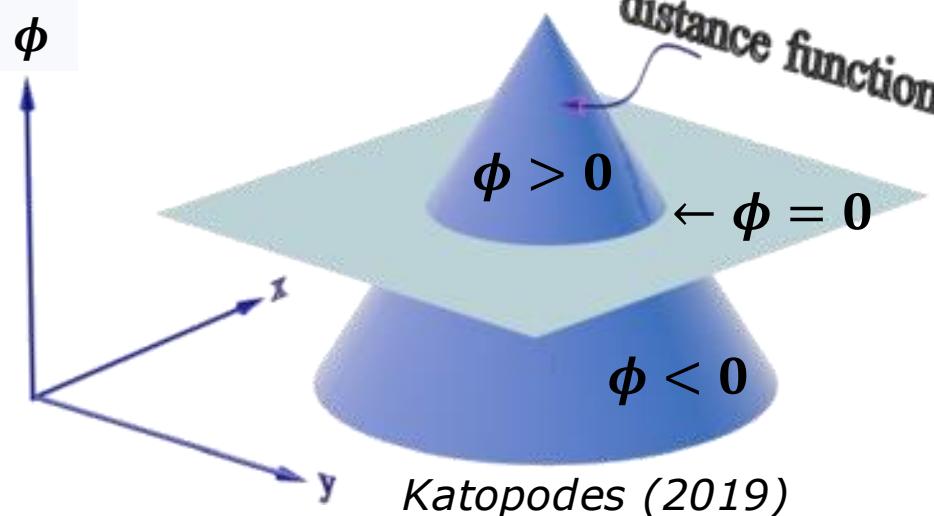
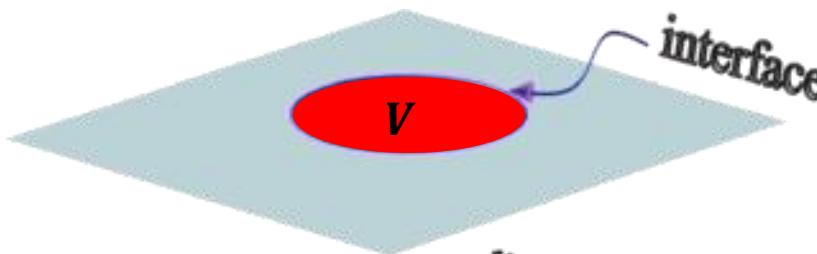
$$P_{\text{rock}=1,\dots,N} \in [0,1]$$

$$\max(P_{\text{rock}=1,\dots,N})$$

Geometrical inversion

1. Definition of interfaces (signed distance)

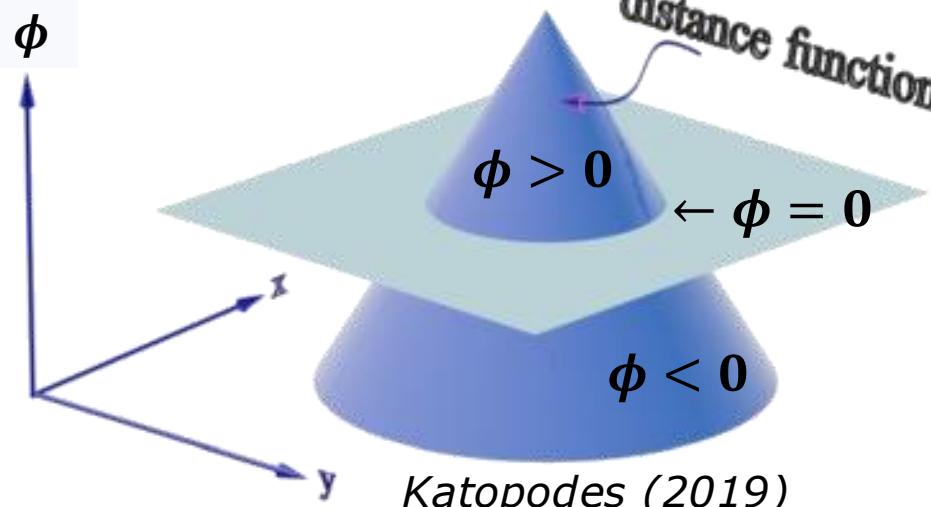
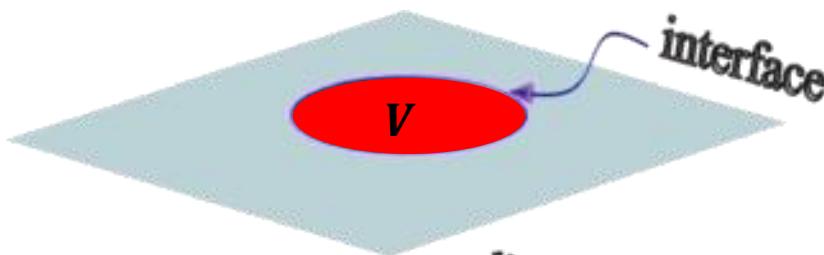
Signed distance $\phi_k \begin{cases} > 0 \text{ inside unit } k, \\ = 0 \text{ at the interface,} \\ < 0 \text{ outside unit } k, \end{cases}$



Geometrical inversion

1. Definition of interfaces (signed distance)

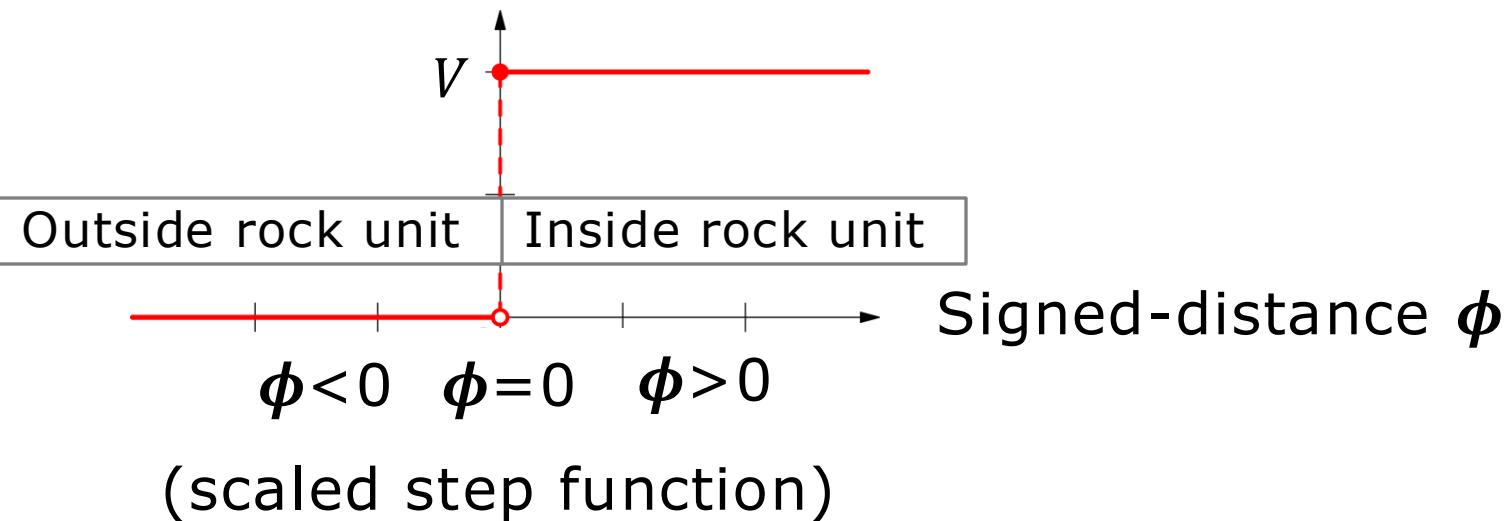
Signed distance ϕ_k $\begin{cases} > 0 \text{ inside unit } k, \\ = 0 \text{ at the interface,} \\ < 0 \text{ outside unit } k, \end{cases}$



2. Calculate density model with values V

$$m(\phi_1, \dots, \phi_N) = \sum_{k=1}^N \left[V_k H(\phi_k) \prod_{\substack{j=1 \\ j \neq k}}^N (1 - H(\phi_j)) \right]$$

Density contrast



Signed distance ϕ_k $\begin{cases} > 0 \text{ inside unit } k, \\ = 0 \text{ at the interface,} \\ < 0 \text{ outside unit } k, \end{cases}$

$$m(\phi_1, \dots, \phi_N) = \sum_{k=1}^N \left[V_k H(\phi_k) \prod_{\substack{j=1 \\ j \neq k}}^N (1 - H(\phi_j)) \right]$$

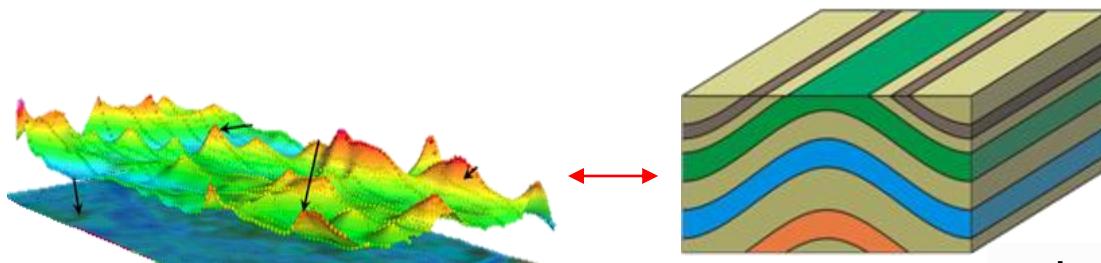
$$J^{\phi_k} = ??$$

1. Definition of interfaces

2. Calculate density model with values V_k

3. Link geophysical data to signed-distance

4. Calculate sensitivity of geophy data to interface location



geophy. data d

inverted property model m

$$J^m = \frac{\partial d}{\partial m} = \frac{\partial d}{\partial \phi_k} \frac{\partial \phi_k}{\partial m} = J^{\phi_k} \frac{\partial \phi_k}{\partial m},$$

$$\rightarrow J^{\phi_k} = \frac{\partial d}{\partial \phi_k} = J^m \frac{\partial m}{\partial \phi_k}$$

Multiple-body geometrical inversion

Non-UWA (Personal)

Signed distance ϕ_k $\begin{cases} > 0 \text{ inside unit } k, \\ = 0 \text{ at the interface,} \\ < 0 \text{ outside unit } k, \end{cases}$

1. Definition of interfaces

$$m(\phi_1, \dots, \phi_N) = \sum_{k=1}^N \left[V_k H(\phi_k) \prod_{\substack{j=1 \\ j \neq k}}^N (1 - H(\phi_j)) \right]$$

$$J^{\phi_k} = \frac{\partial d}{\partial \phi_k} = J^m \frac{\partial m}{\partial \phi_k}$$

2. Calculate density model with values V_k

3. Link geophysical data to signed-distance

4. Calculate sensitivity of geophy data to interface location

$$\frac{\partial m_j}{\partial (\phi_k)_j} = V_k \frac{\partial H((\phi_k)_j)}{\partial (\phi_k)_j} \prod_{\substack{s=1 \\ s \neq j}}^N [1 - H((\phi_s)_j)] - \sum_{t=1}^N \left[V_t H((\phi_t)_j) \prod_{\substack{u=1 \\ u \neq t \\ u \neq k}}^N [1 - H((\phi_u)_j)] \frac{\partial H((\phi_k)_j)}{\partial (\phi_k)_j} \right]$$

- Ensure topology is OK
- Try new geol model?
- Or update again?

5. Local inverse problem to optimize interface perturbation

$$\Psi(\delta\phi, r) = \|J^\phi \delta\phi^T - r\|_2^2 + \|\alpha W_s \circ \delta\phi\|_2^2 + \sum_{k=1}^N \|\beta_k W_p \circ (\delta\phi_k - v_k)\|_2^2$$

$$\phi^l = \phi^{l-1} + \delta\phi$$

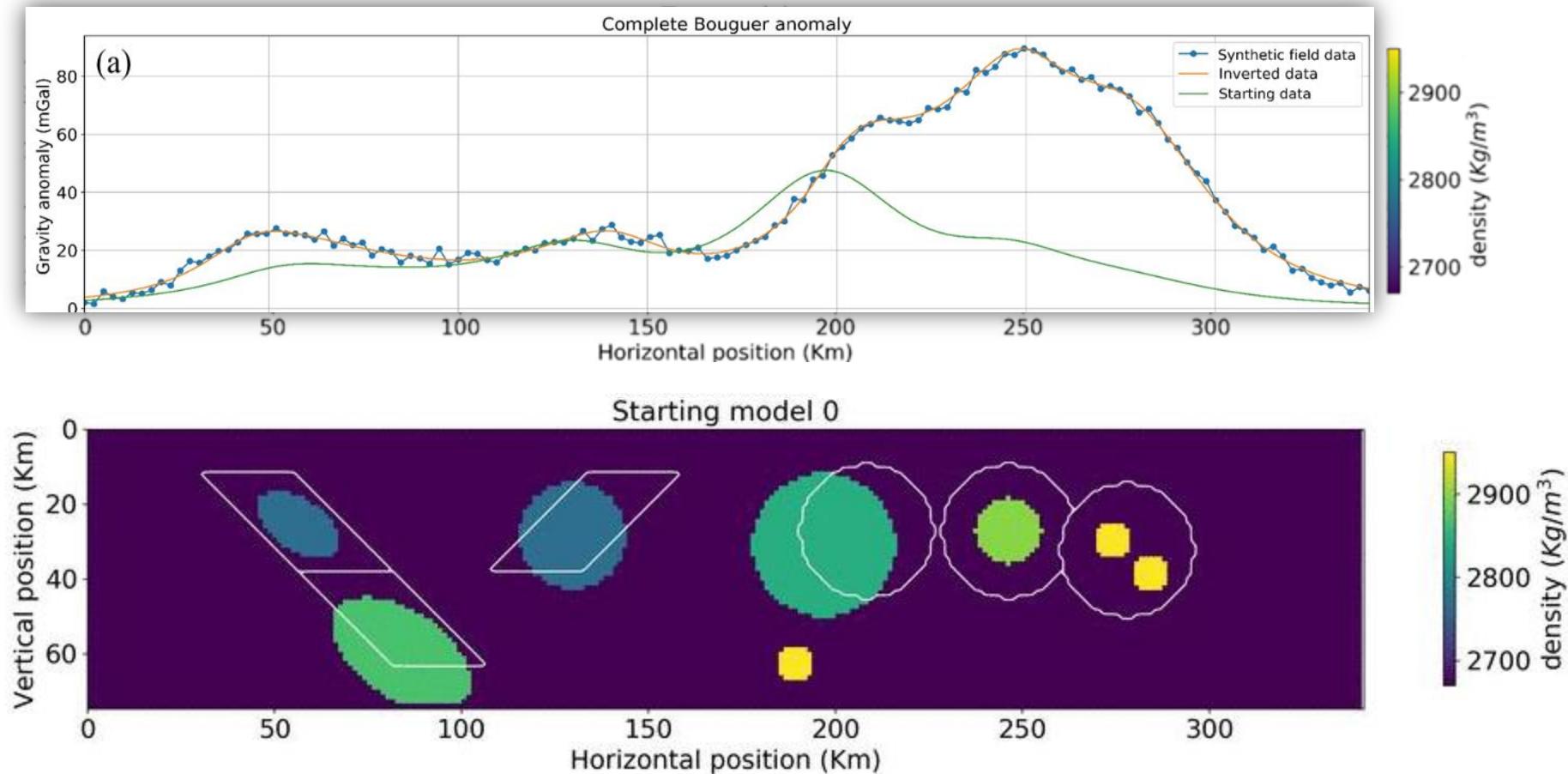
7. Increment signed-distances

$$\begin{bmatrix} J^{\phi_1}, J^{\phi_2}, \dots, J^{\phi_N} \\ \alpha W_s \\ \beta_1 W_p \\ \beta_2 W_p \\ \vdots \\ \beta_N W_p \end{bmatrix} \begin{bmatrix} \delta\phi_1 \\ \delta\phi_2 \\ \vdots \\ \delta\phi_N \end{bmatrix} = \begin{bmatrix} r \\ 0 \\ \beta_1 v_1 \\ \beta_2 v_2 \\ \vdots \\ \beta_N v_N \end{bmatrix}, \text{(LSQR)}$$

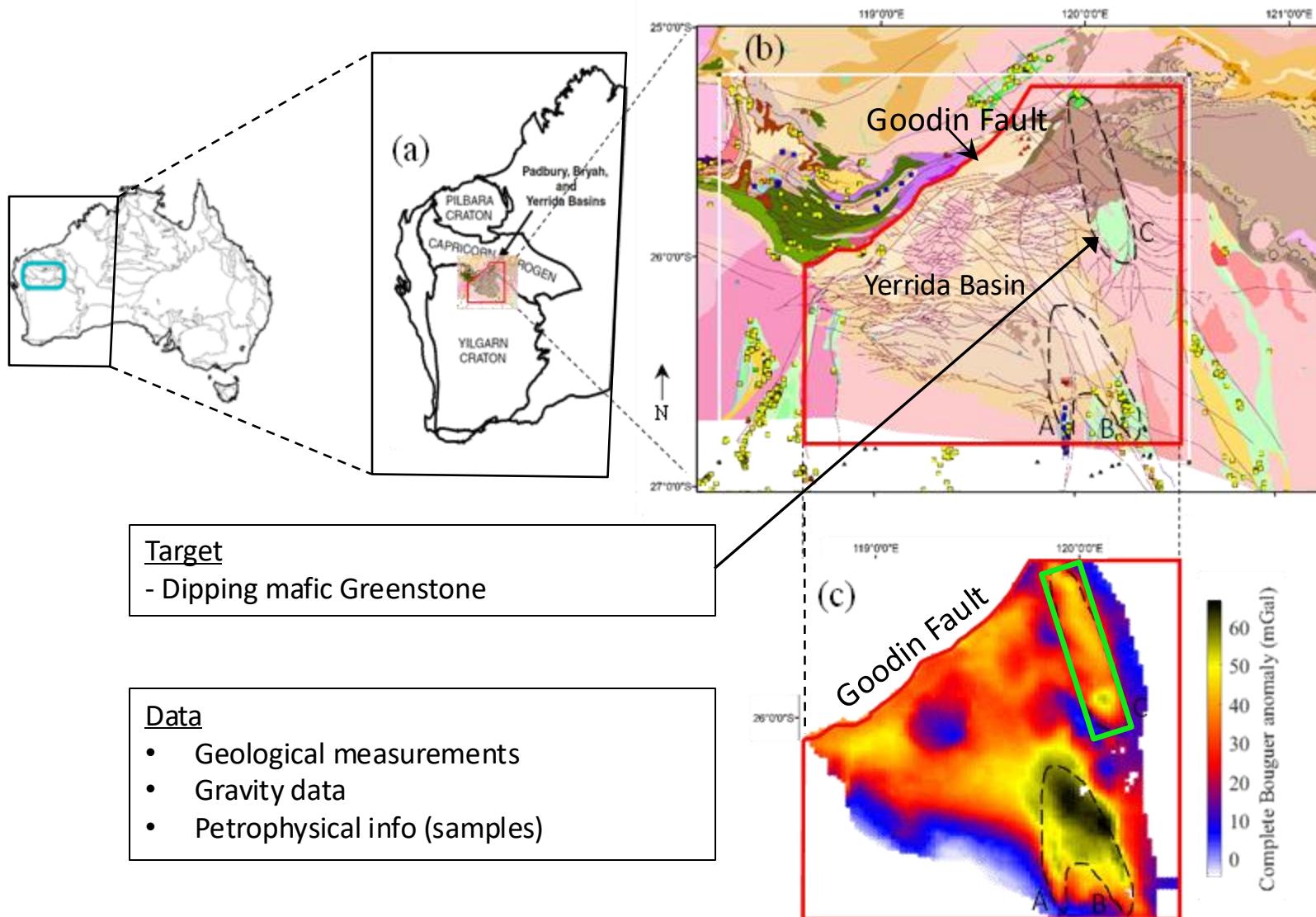
Synthetic case – test

Non-UWA (Personal)

Loop



Field application: Yerrida Basin

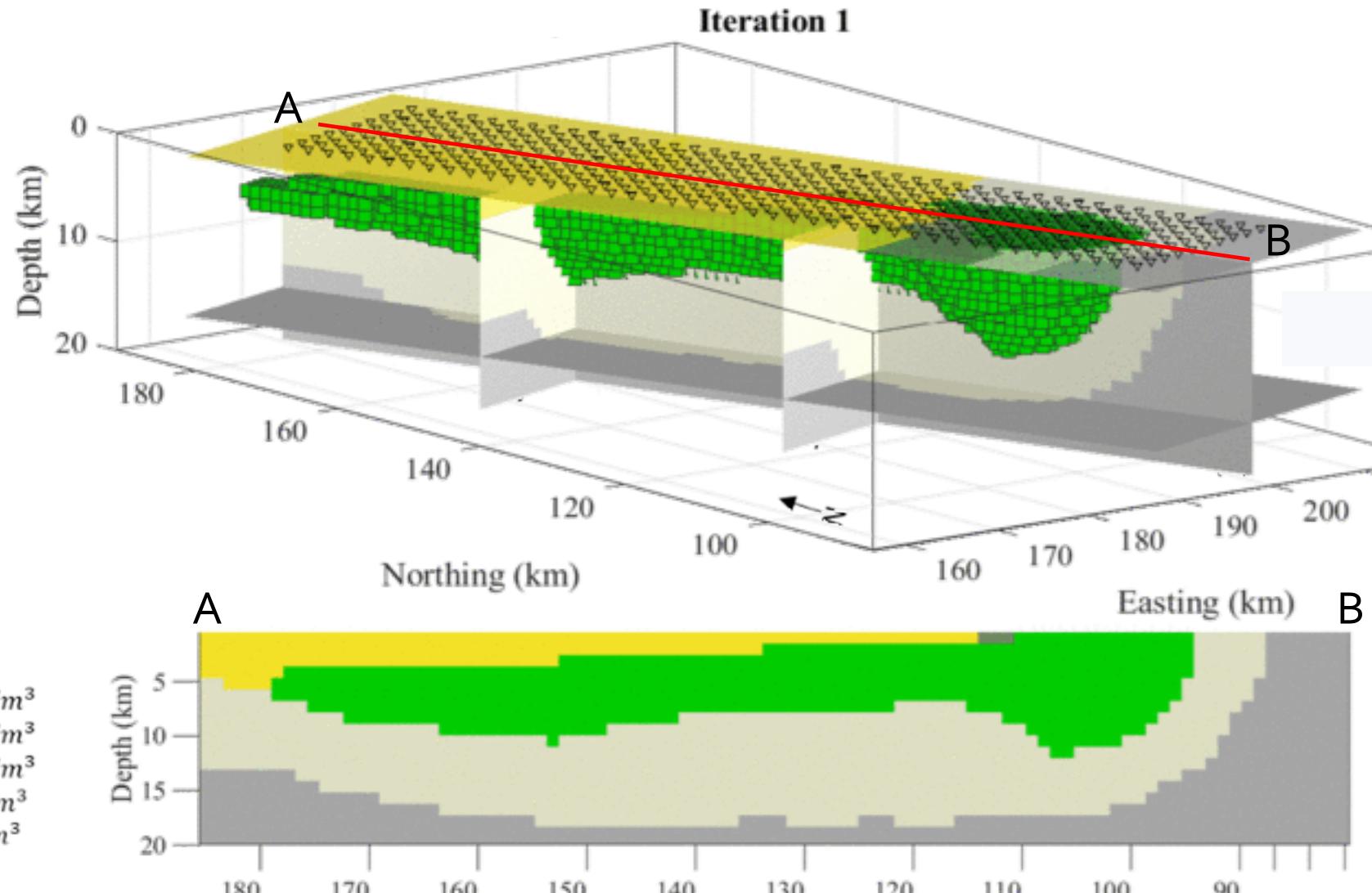


Field application: Yerrida basin

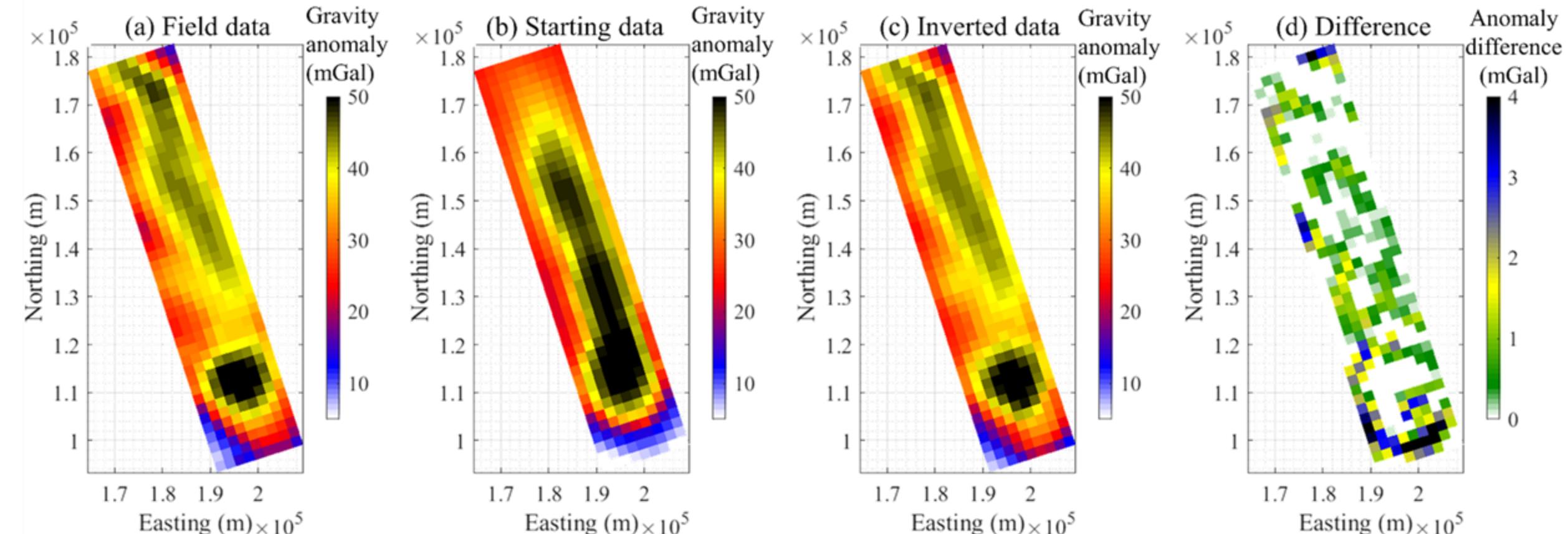
Non-UWA (Personal) Loop

- Greenstone possibly broken into several pieces
- In line with other recent studies (Lindsay et al., 2020, Giraud et al. 2020)
- Geological data probably poorly informed about deep structures

Mafic greenstone	230 Kg/m ³
Juderina	180 Kg/m ³
Mooloogool group	130 Kg/m ³
Non-mafic greenstone	30 Kg/m ³
Background	0 Kg/m ³



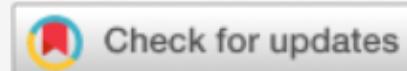
Field application: Yerrida basin



For more info

 Open Access | GEOPHYSICS | Volume 86, Issue 4

Generalization of level-set inversion to an arbitrary number of geologic units in a regularized least-squares framework



Authors:

Jérémie Giraud ,  Mark Lindsay, and Mark Jessell



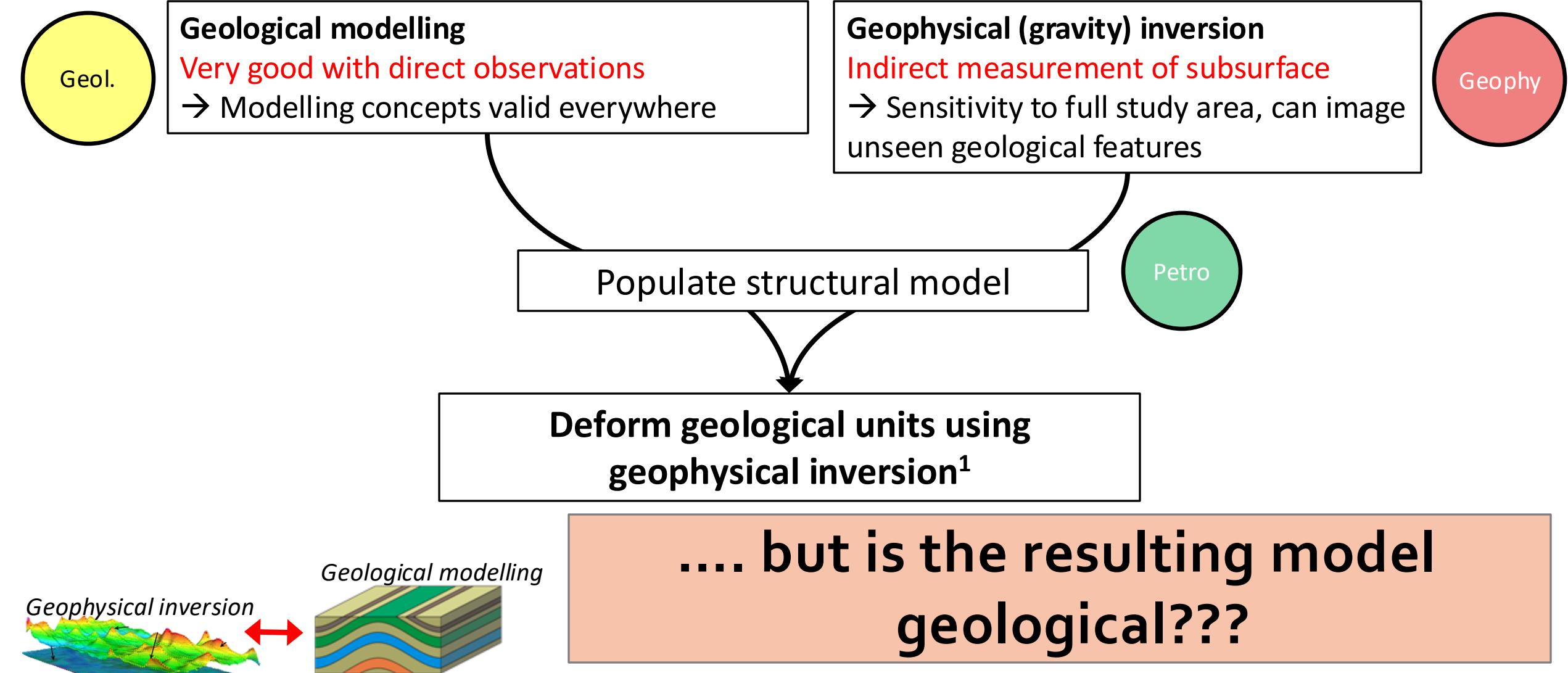
(works even from a distance!)

Jérémie Giraud, Mark Lindsay, Mark Jessell; Generalization of level-set inversion to an arbitrary number of geologic units in a regularized least-squares framework. *Geophysics*, 2021; 86 (4): R623–R637. doi: <https://doi.org/10.1190/geo2020-0263.1>

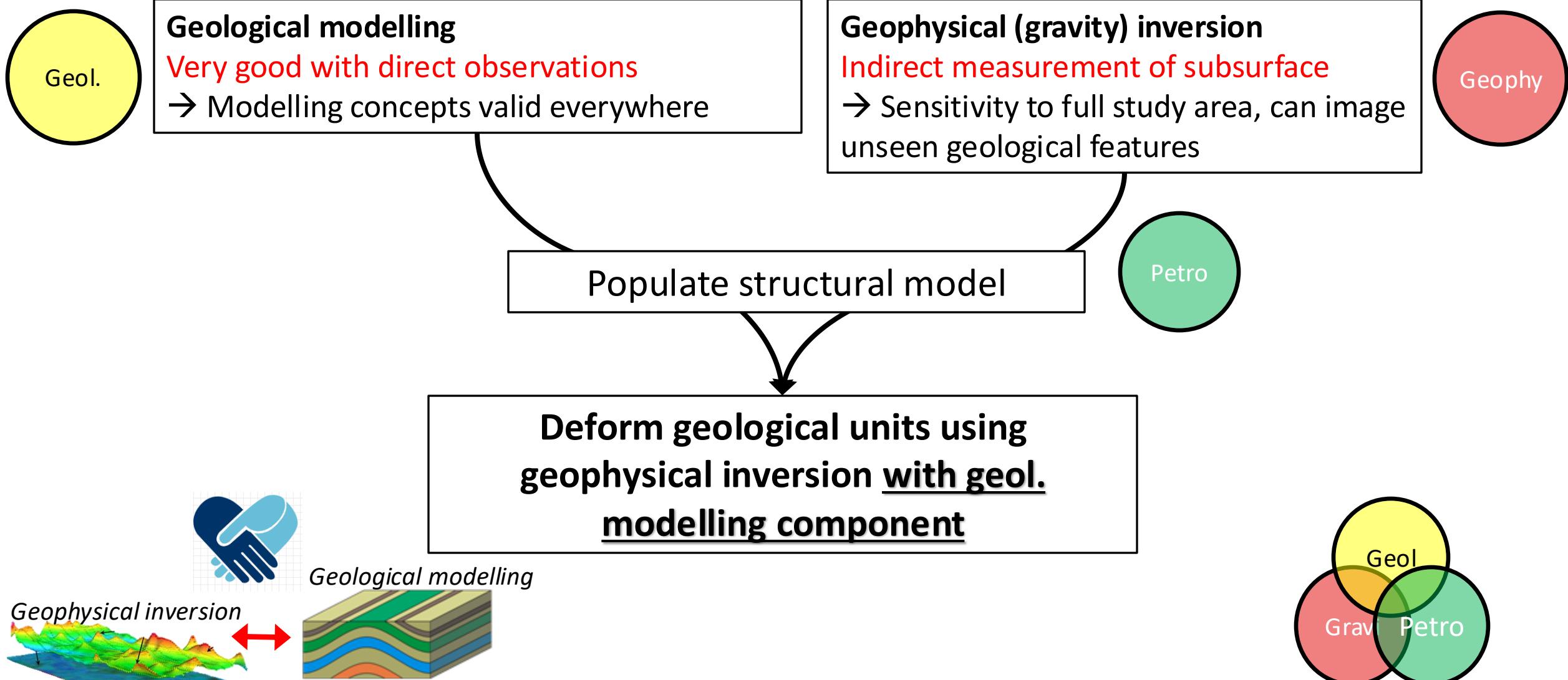
Questions?



Proposed approach



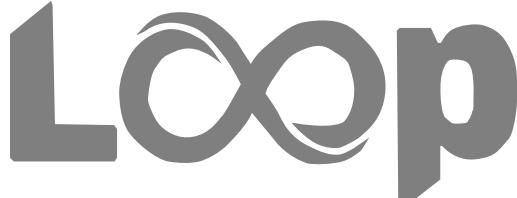
Proposed approach



Implicit geological modelling in a nutshell

Implicit modelling: geology

Non-UWA (Personal)

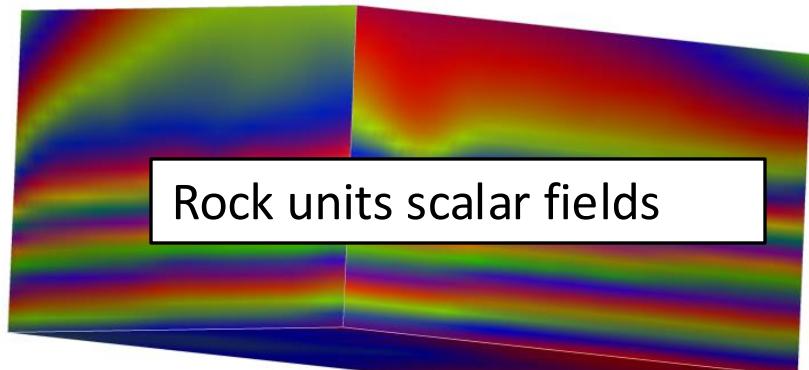


Implicit geological modelling in a nutshell

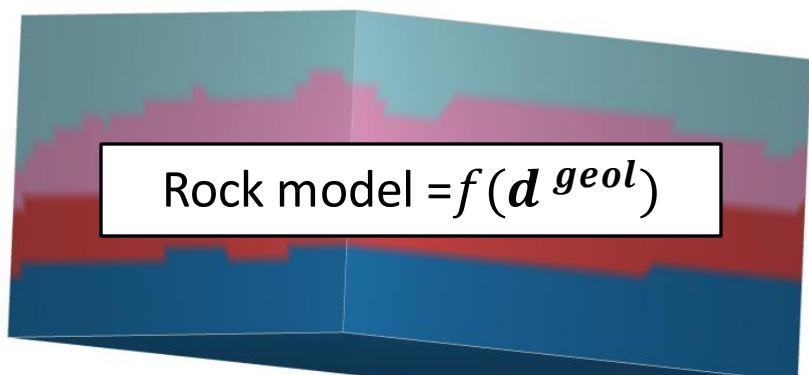


Ex.: Seismic horizons, borehole data, etc.

Implicit modelling¹
→ Age relationships
→ Structural rules

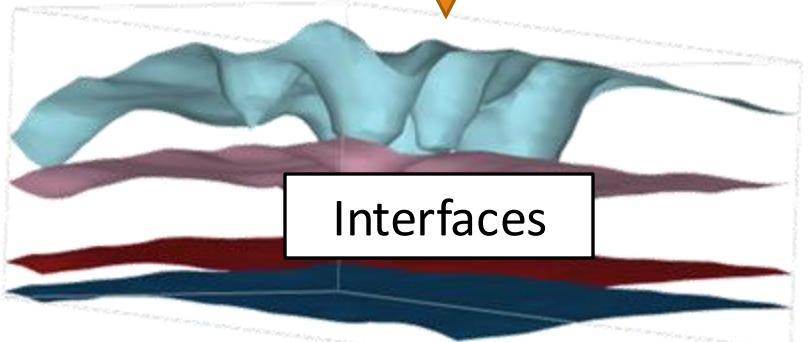


Ex.: Stratigraphic thickness



Ex.: Rock model with density values

Create and Populate mesh



Interfaces

Identification of iso-values

Geophysical problem formulation

Non-UWA (Personal)



Solve for update of distance $\delta\phi$ with geol. modelling component

Signed Geophy. data Geol. data
dist.

$$\Psi(\phi, d^{geophy}, d^{geol})$$

$$= \|d_{obs.}^{geophy} - d_{calc.}^{geophy}\|_2^2 +$$

Geophy. data misfit

Signed distances of geol. model

$$\|W^{-1}(\phi - \phi^{geol}(d_{obs.}^{geol}, d_{calc.}^{geol}))\|_2^2$$

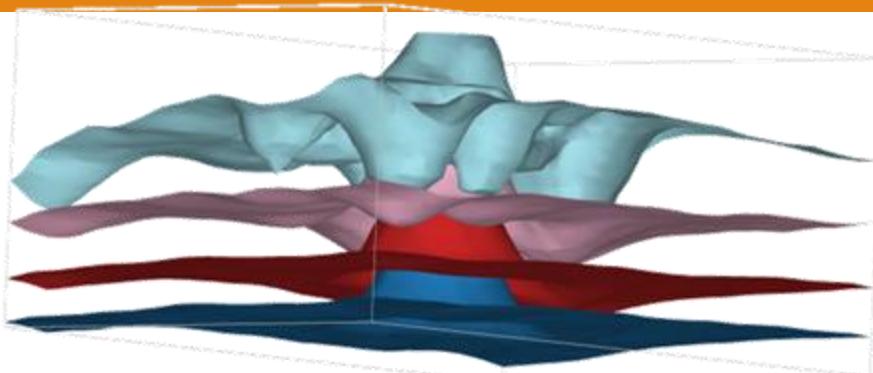
Regularisation

$d_{calc.}^{geol}$: geol data recovered from model proposed by geophysics

From geophysics to geology

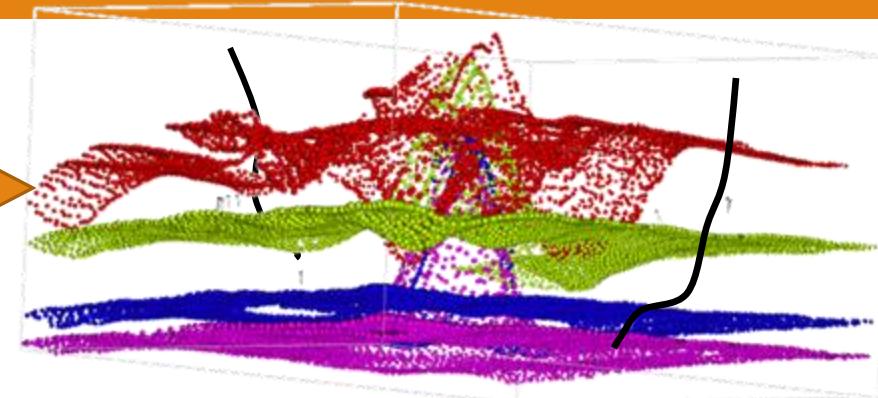
Non-UWA (Personal)

Loop



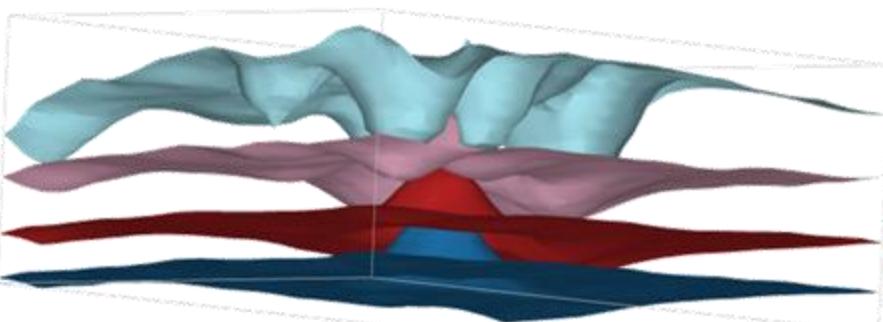
Geophysical model $\phi_*^n \rightarrow$ interfaces

Identification of contact locations and orientation data



+ seismic horizons, borehole data, etc. in d^{geol}

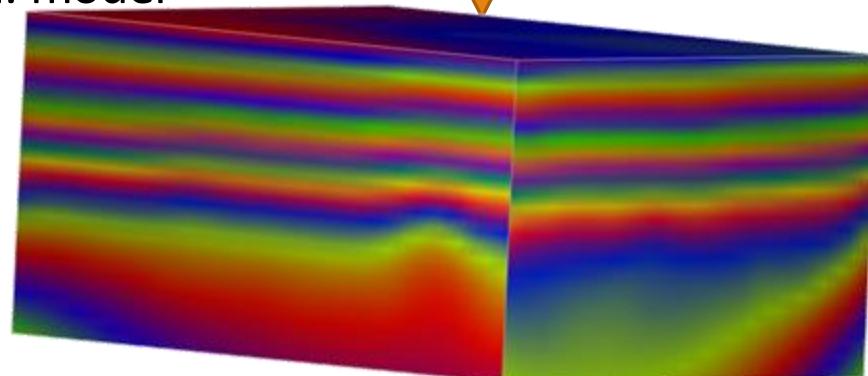
Implicit modelling¹
→ Age relationships
→ Structural rules



Modified model ('geological' version)
 $\rightarrow \phi^{geol}(\phi_*^n, d^{geol})$

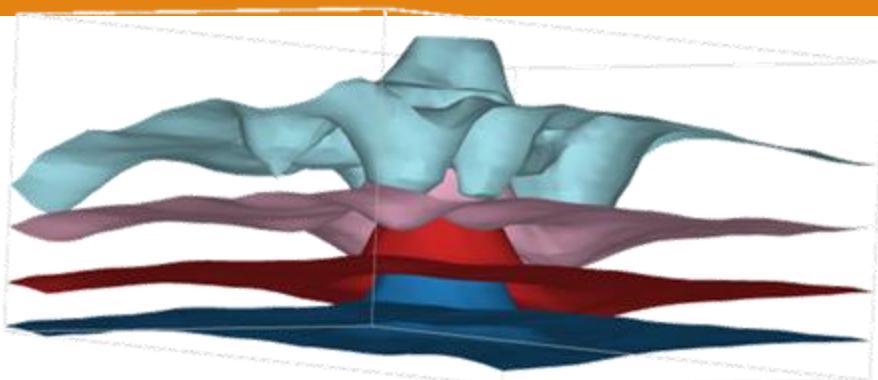
Identification of iso-values

Implicit geol. model



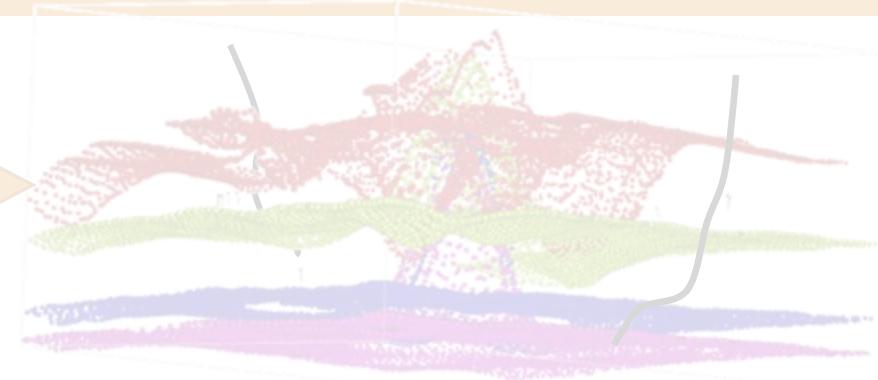
From geophysics to geology

Non-UWA (Personal)



Geophysical model $\phi_*^n \rightarrow$ interfaces

Identification of contact locations and orientation data

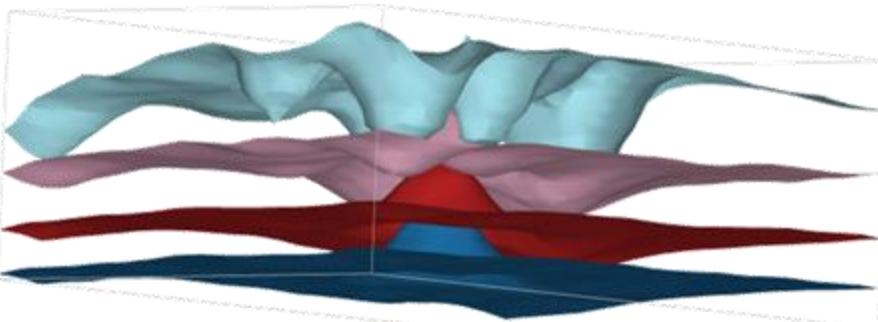


+ seismic horizons, borehole data, etc. as geological data

$$\phi^{geol}(\phi_*^n, d^{geol}) \rightarrow \text{Calculate } \left\| W^{-1} (\phi - \phi^{geol}(d_{obs.}^{geol}, d_{calc.}^{geol})) \right\|_2^2$$

Modified model ('geological' version)

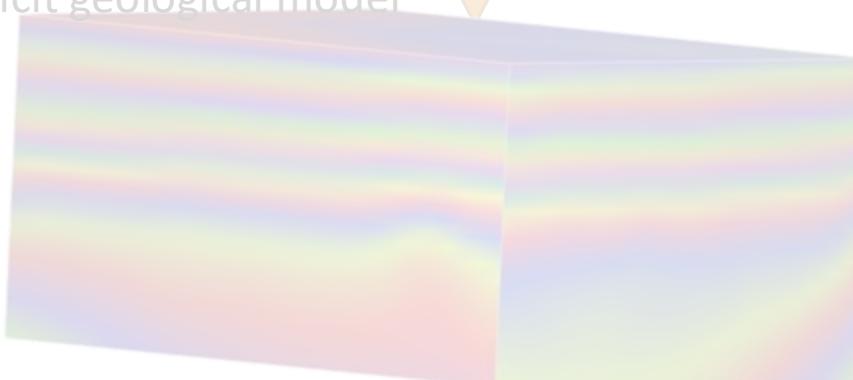
$$\rightarrow \phi^{geol}(\phi_*^n, d^{geol})$$



Identification of iso-values

→ Structural rules

Implicit geological model



In a nutshell: cost function

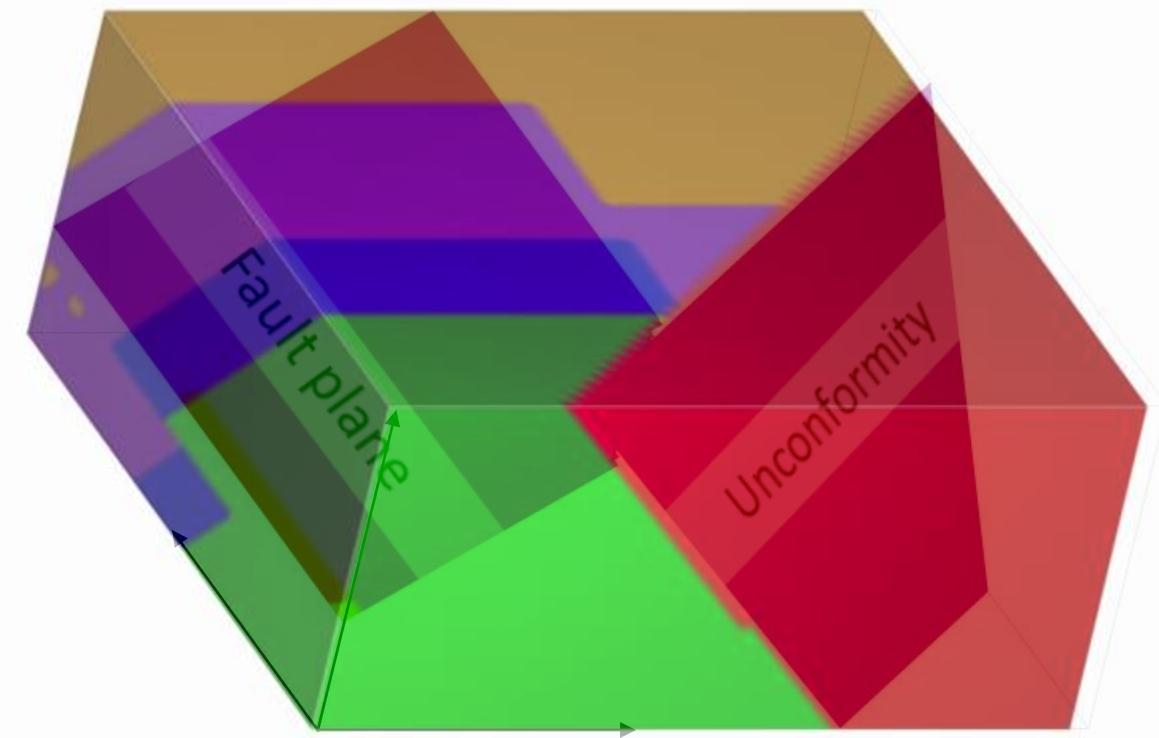
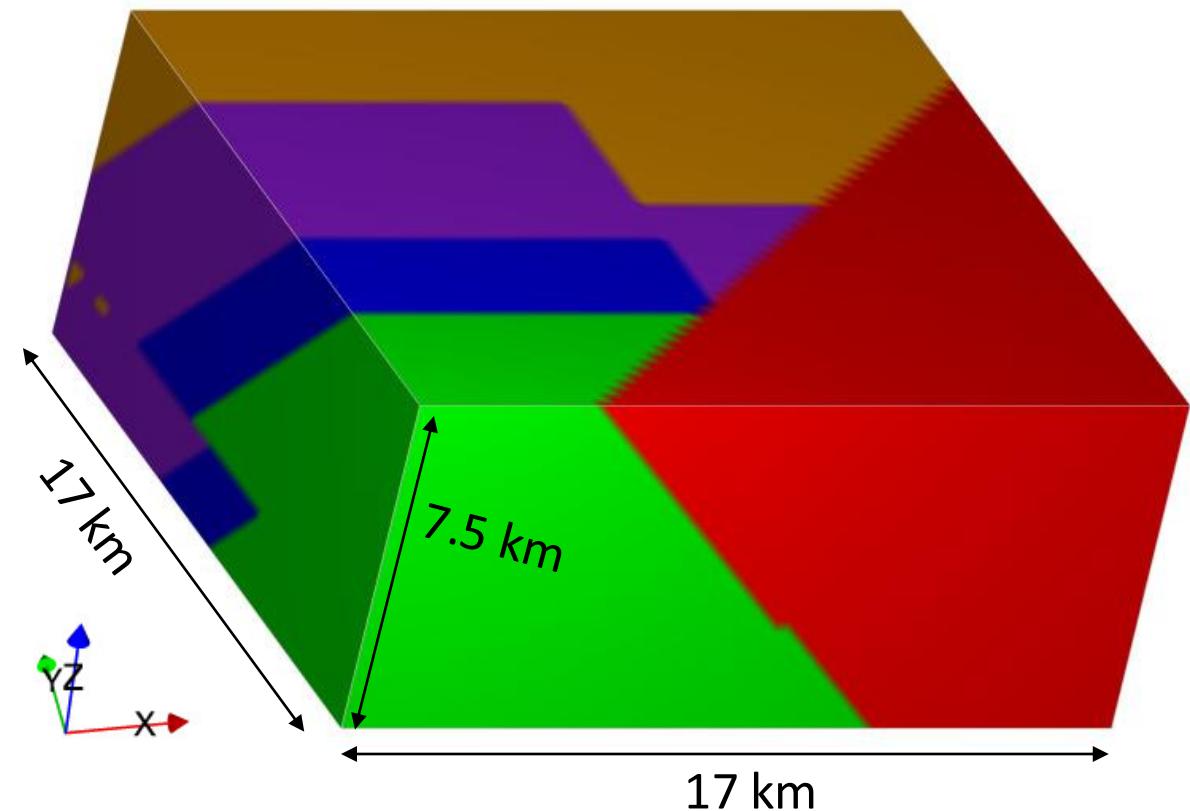
Iterative solver: at iteration n ...

Optimize implicit field ϕ , to reduce geophysical data misfit

Account for geological data $d_{obs}^{geol_1}$

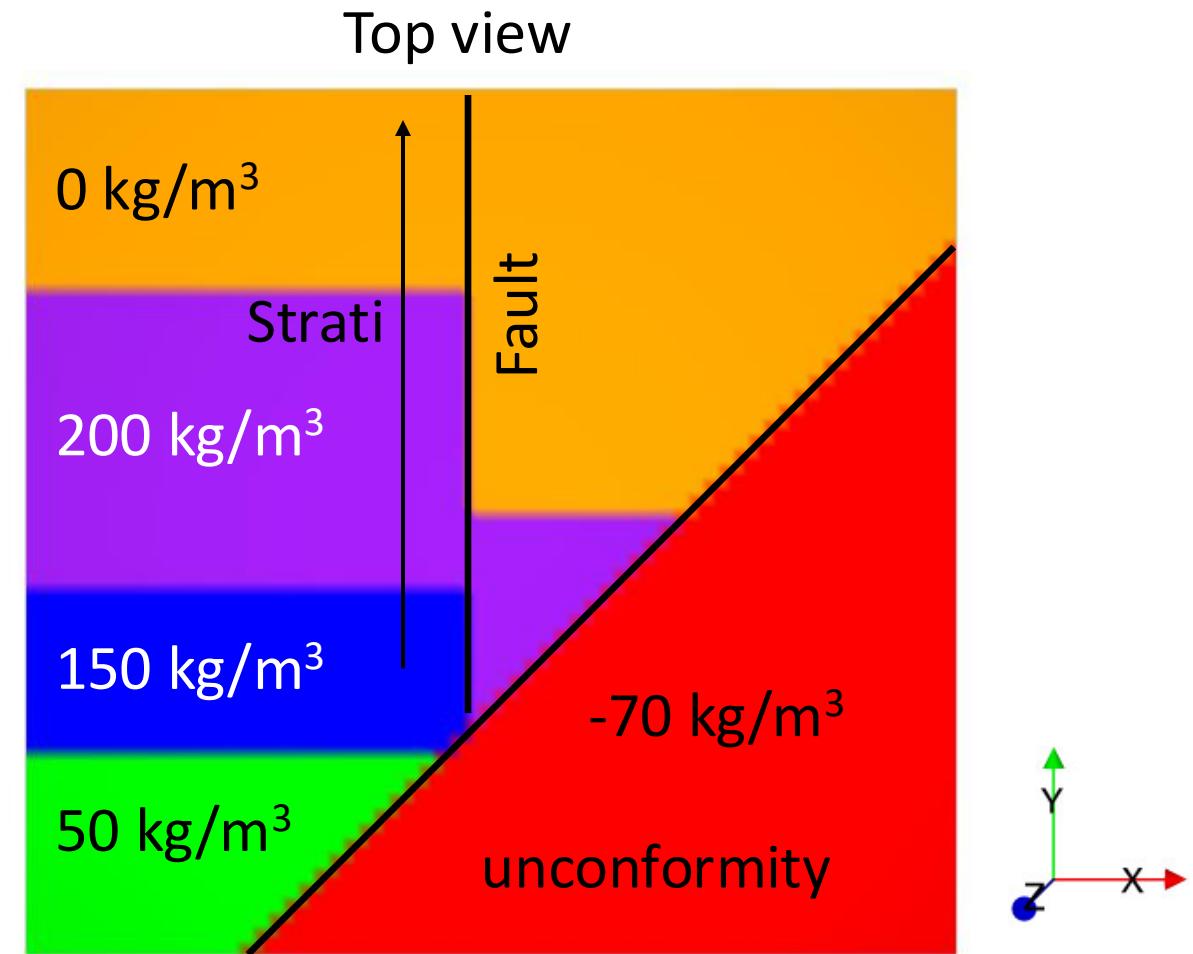
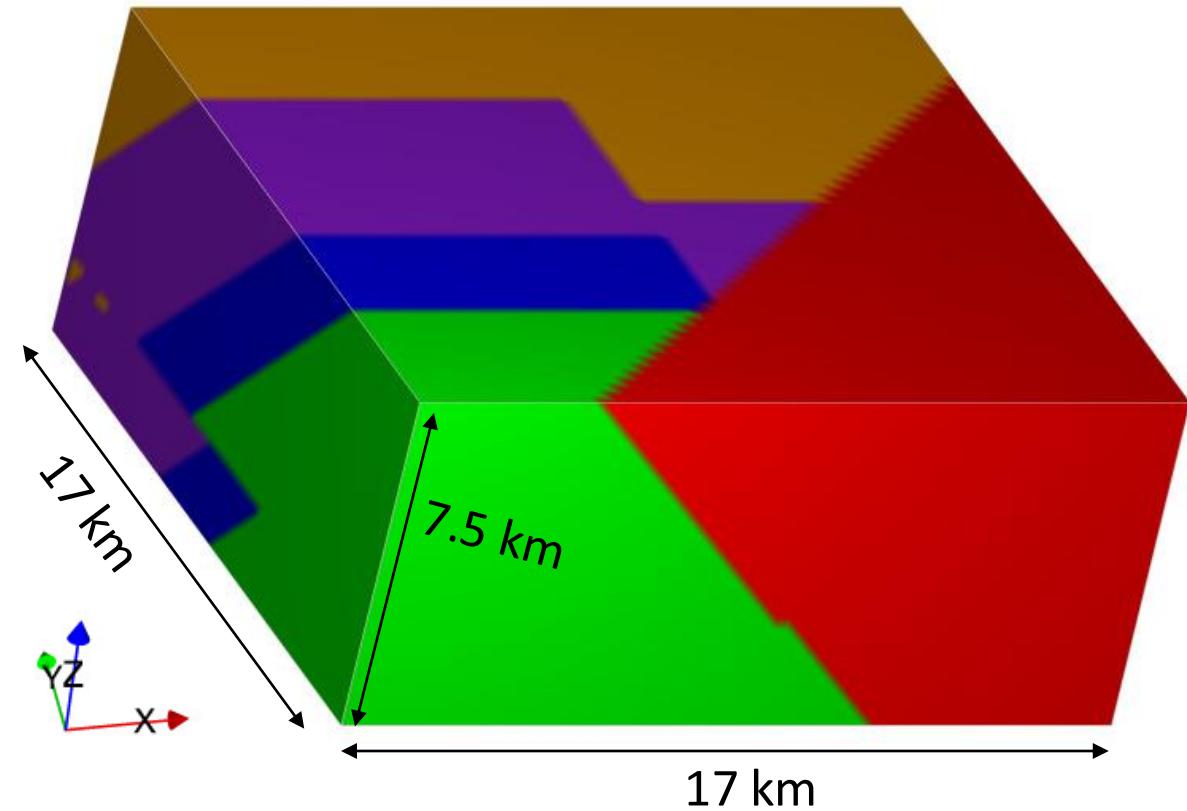
Synthetic test

Reference model



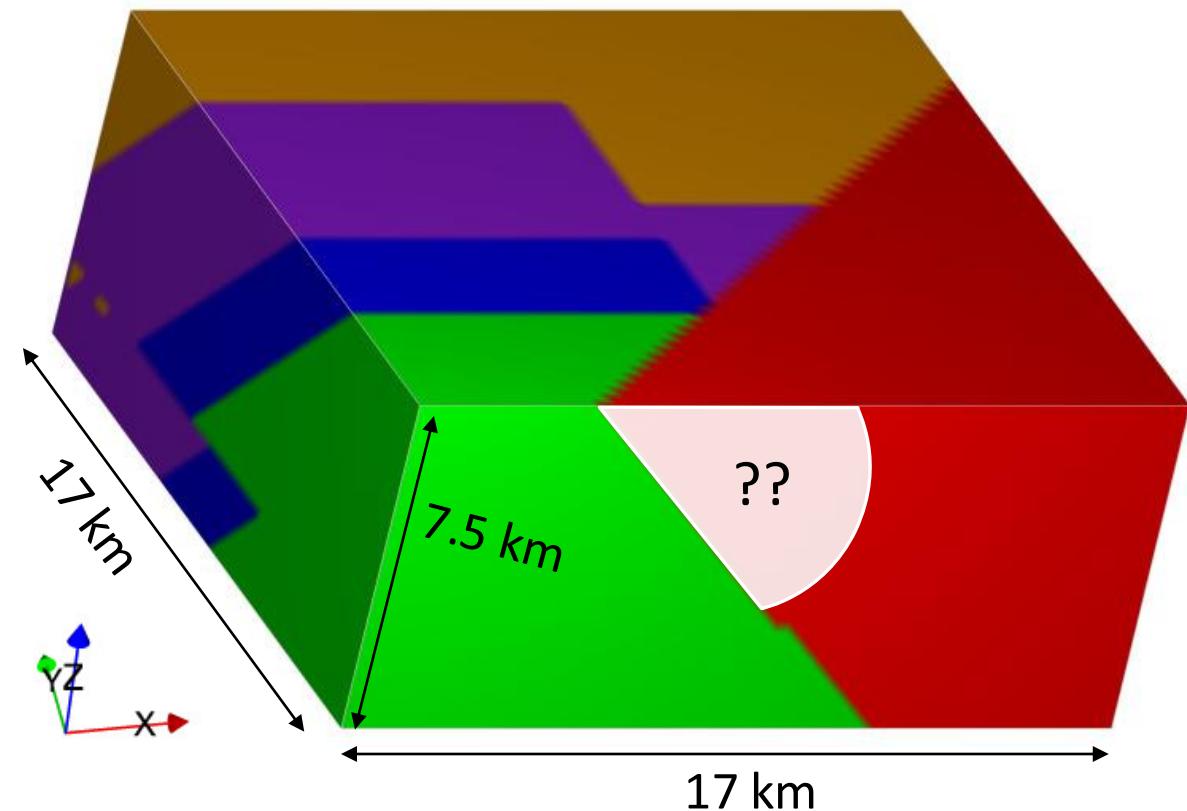
Synthetic test

Reference model

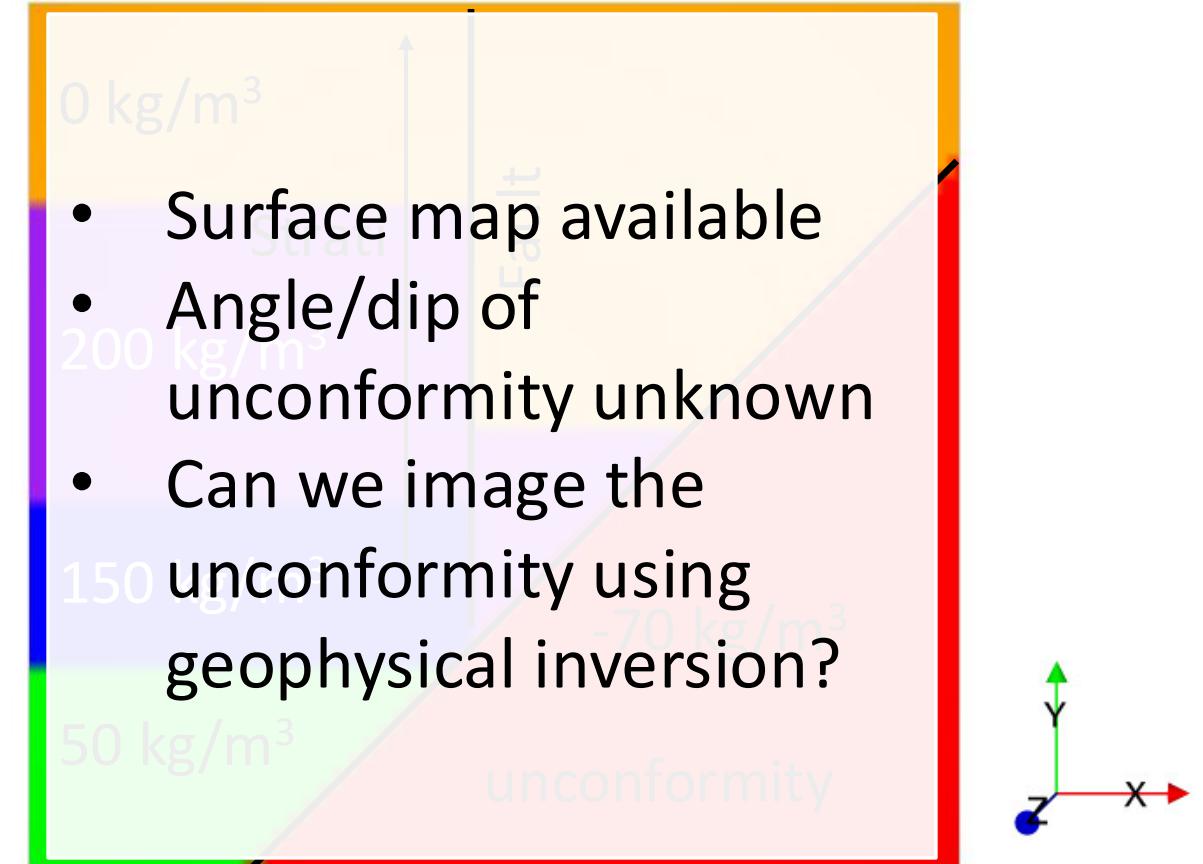


Synthetic test

Reference model

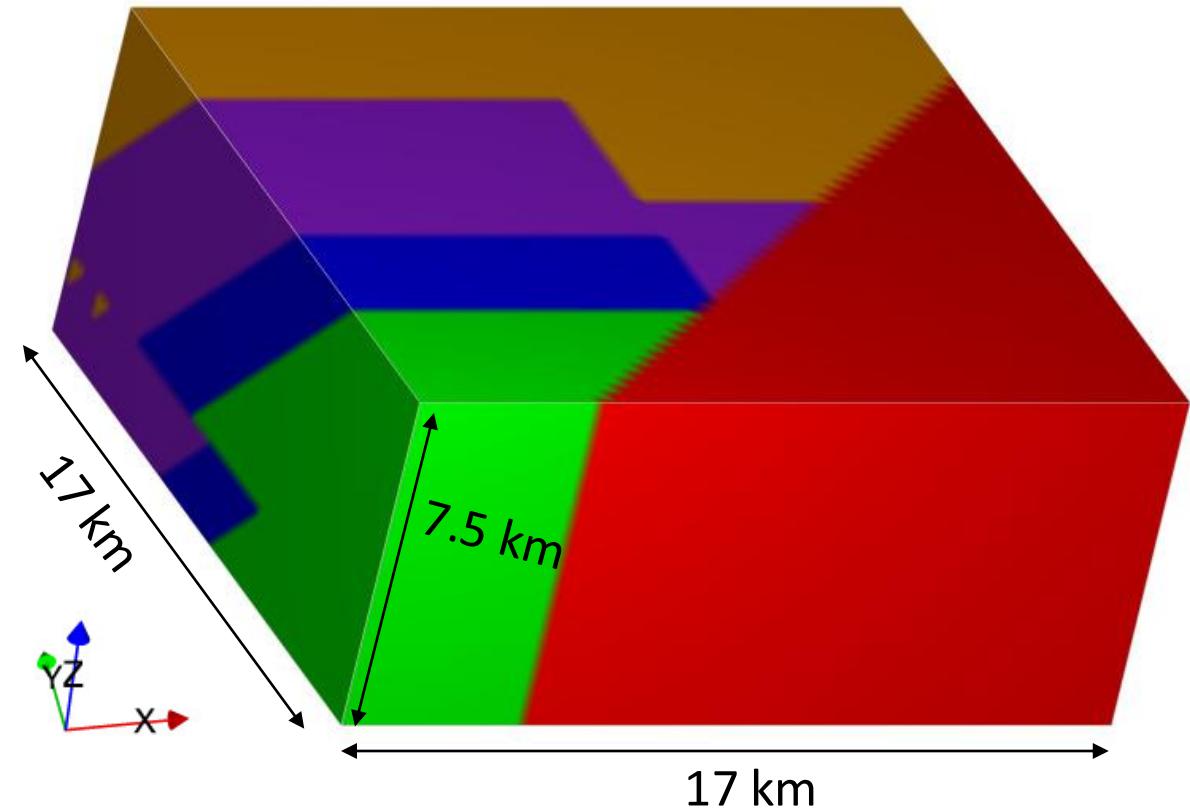


Top view



Synthetic test

Starting model



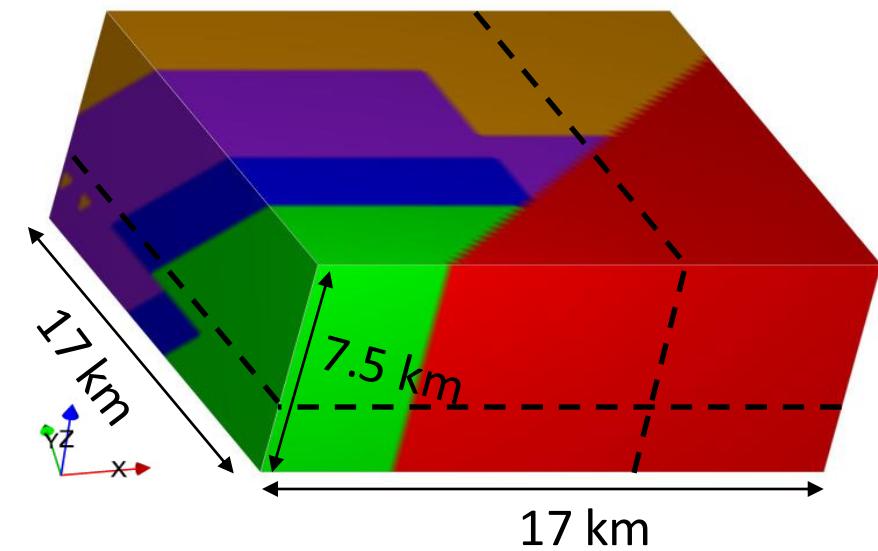
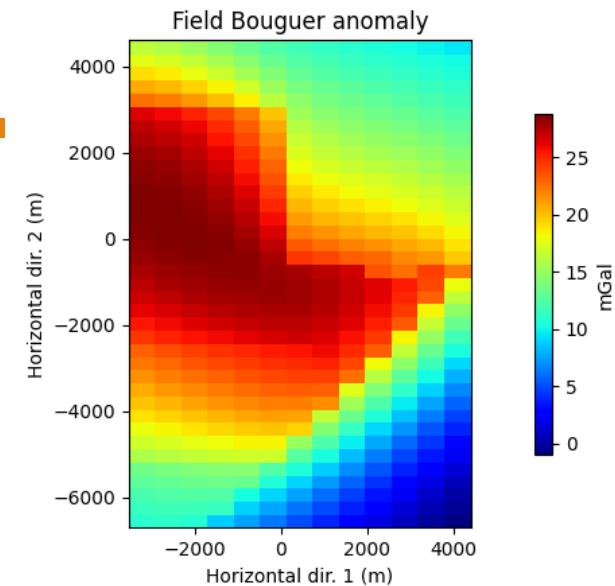
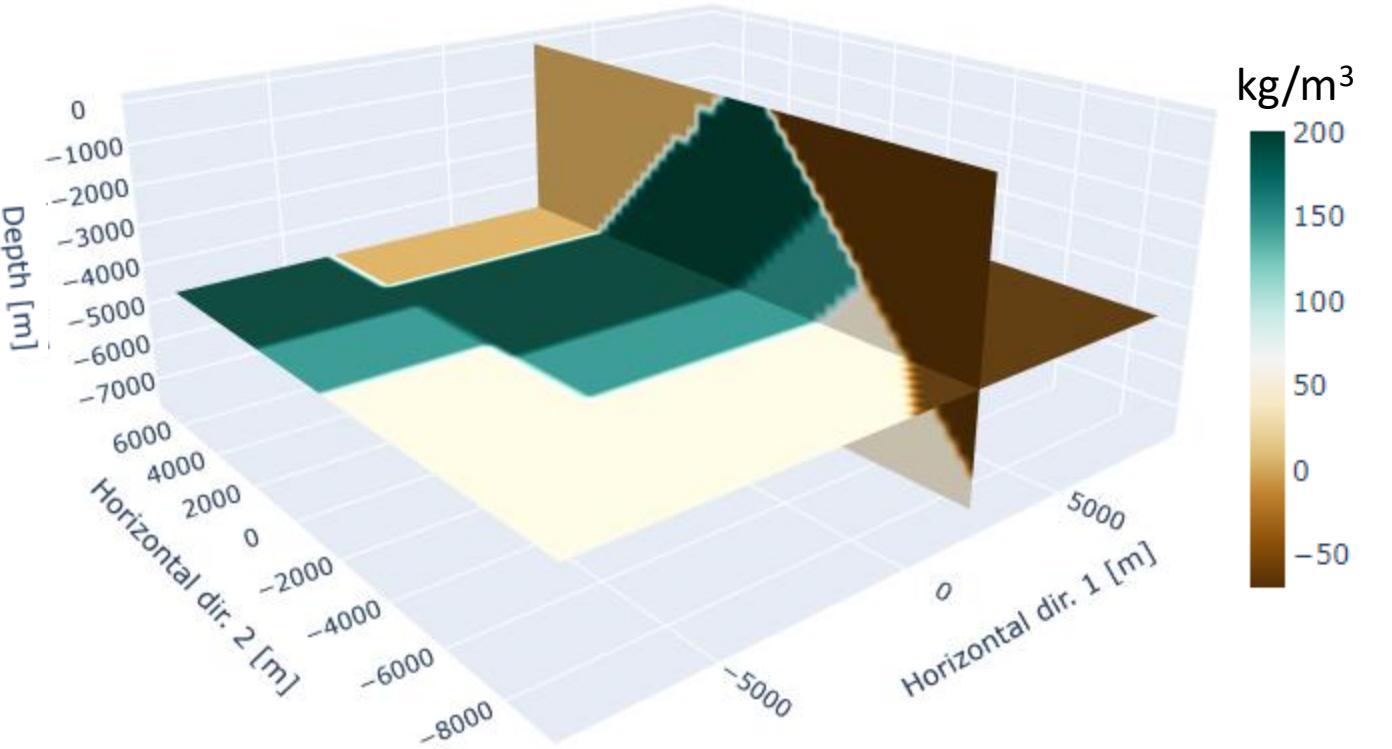
- Vertical contact (for the sake of testing) assuming no knowledge of contact angle
- Constraints only on unconformity
- Starting with large misfit

Synthetic test

Non-UWA (Personal)

loop

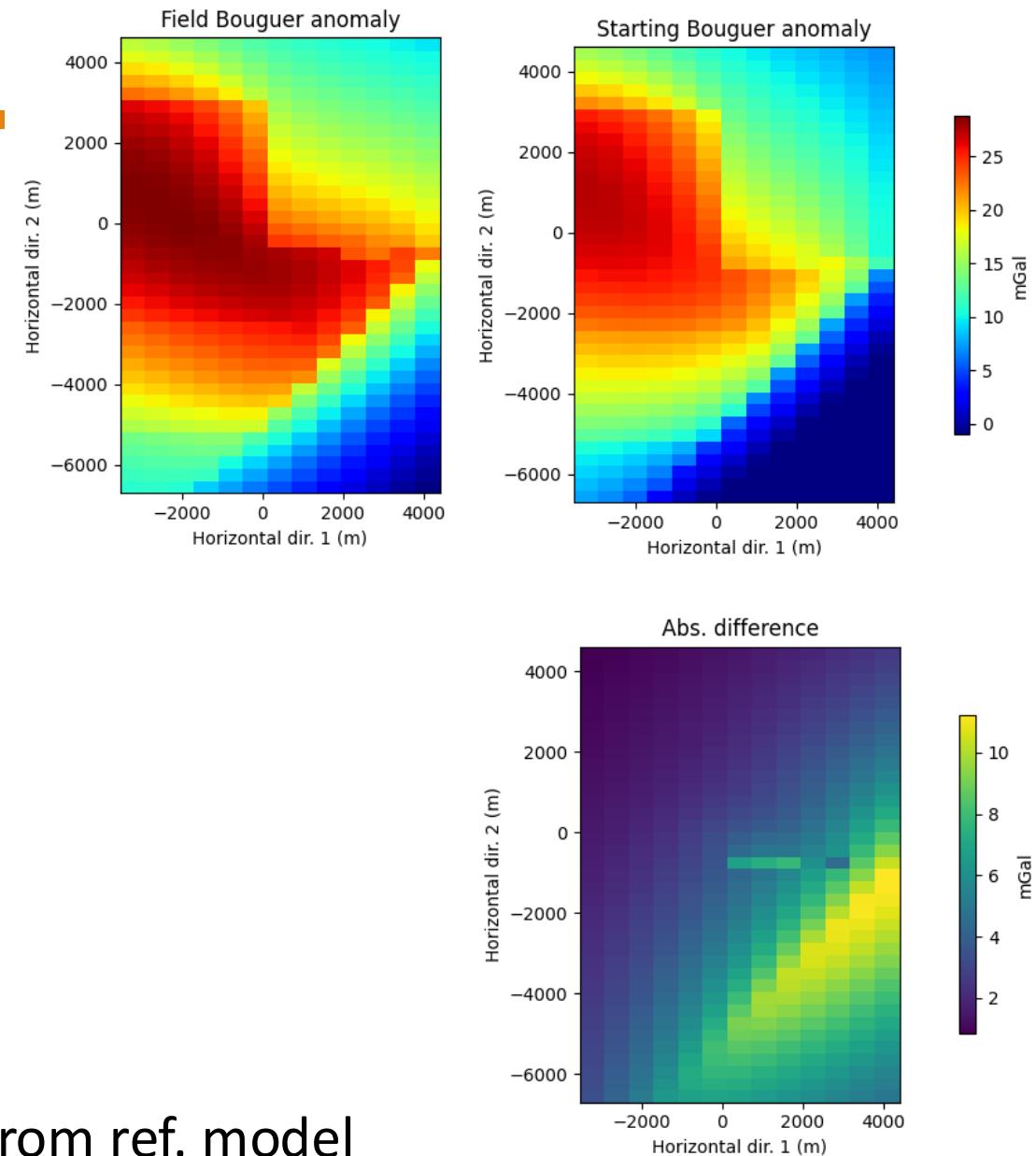
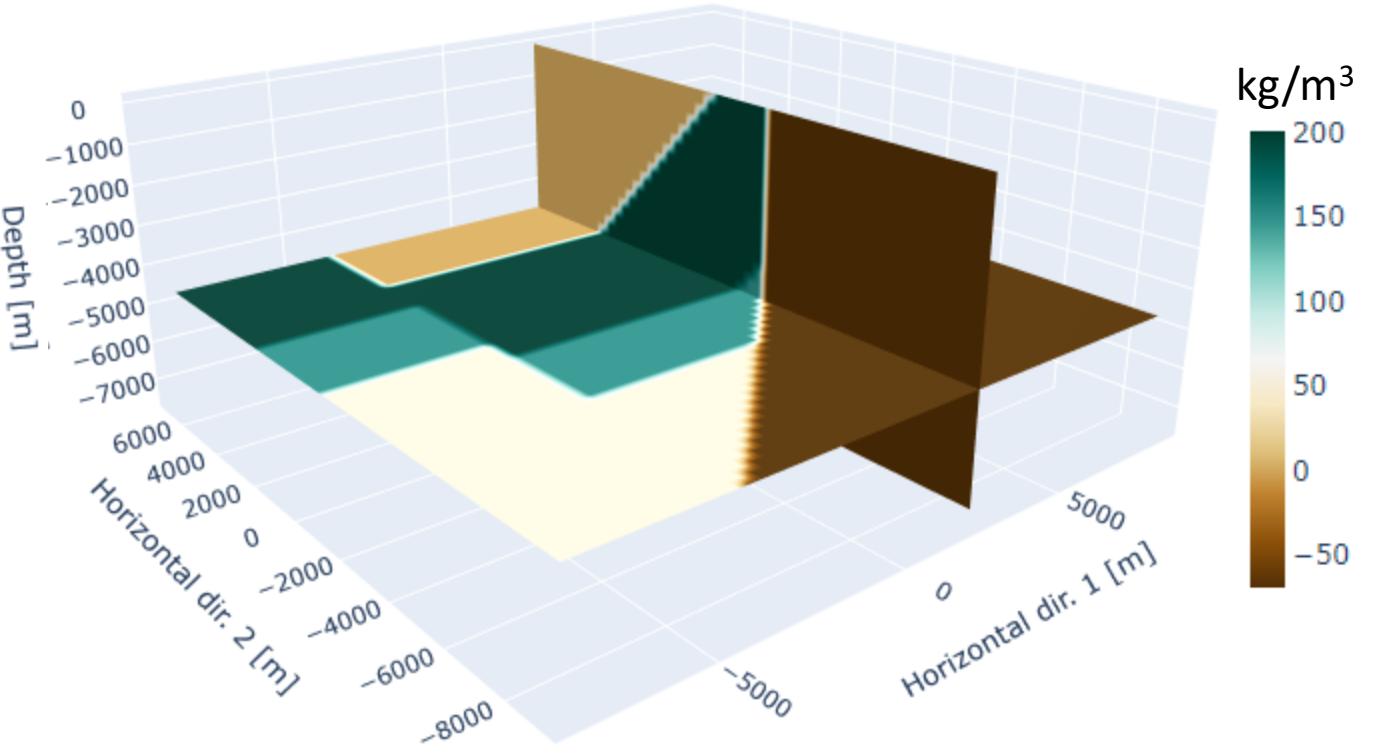
Reference model



Synthetic test 2

Non-UWA (Personal)

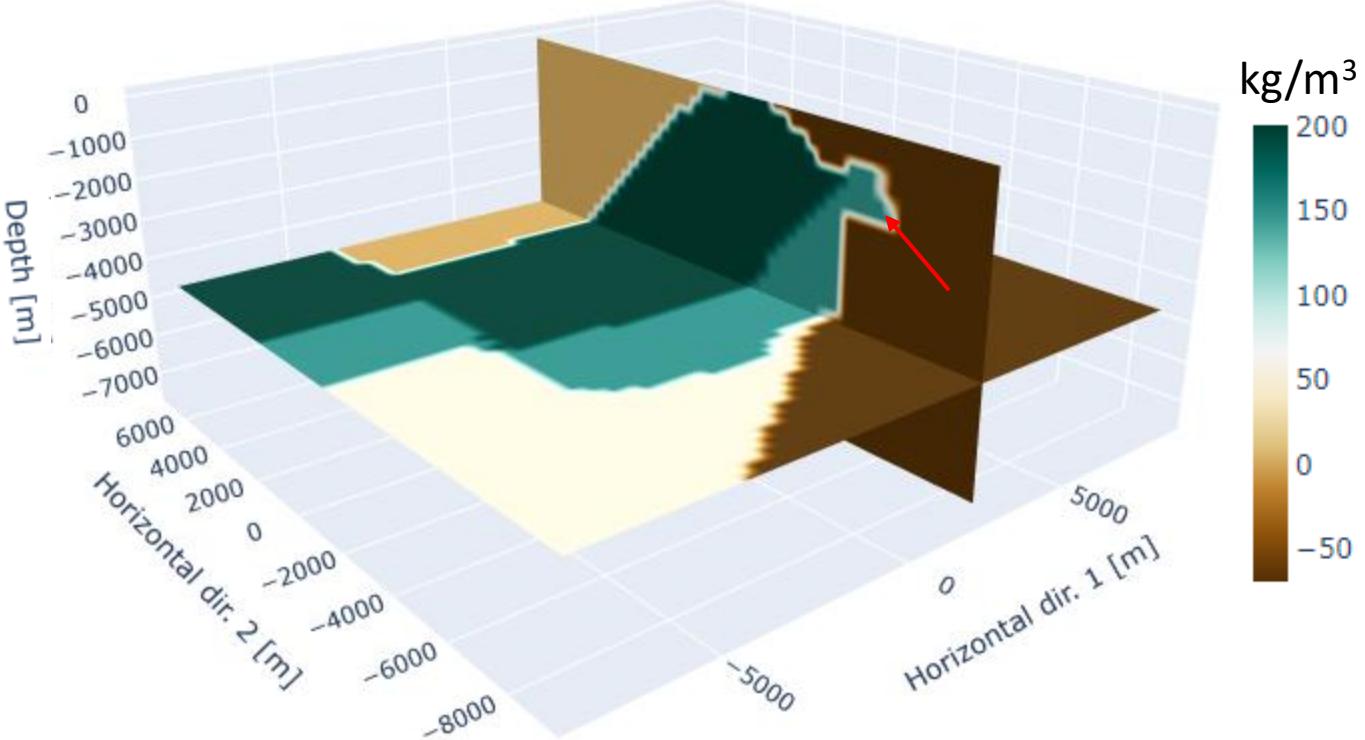
Starting model



- High data misfit
- Visually very different from ref. model

Synthetic test 2

No geological constraints or correction



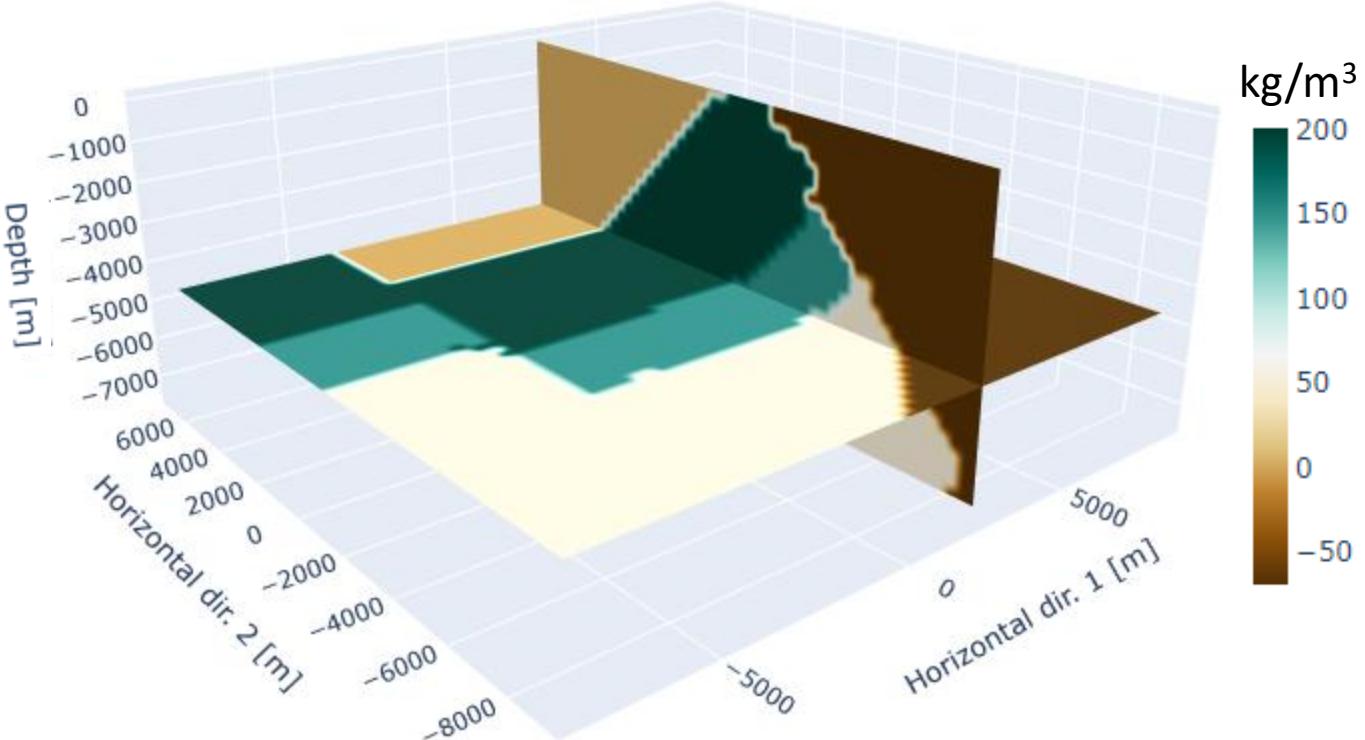
$$\psi(\delta\phi, r) = \|J^\phi \delta\phi - r\|_2^2 + \lambda_s \|W(\delta\phi - \delta\phi^{prior})\|_2^2$$

$$\phi^n = \phi^{n-1} + \delta\phi$$

- Low geophysical data misfit
- Geologically inconsistent

Synthetic test 2

Geological constraints term

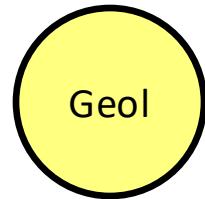
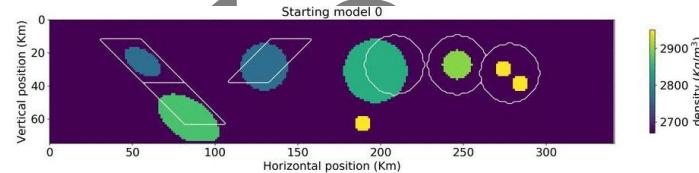


- Low geophysical data misfit
- ‘Better’ geologically

$$\Psi(\delta\phi, r) = \|J^\phi \delta\phi - r\|_2^2 + \lambda_s \|W(\delta\phi - \delta\phi^{geol}(\phi_*^{n-1}))\|_2^2$$

$$\phi^n = \phi^{n-1} + \delta\phi;$$

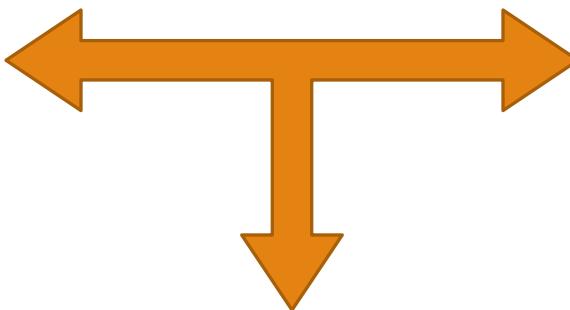
Conclusion and discussion



Geological modelling

Uses surface or shallow measurements only

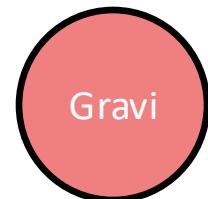
→ (almost) Blind to what's not directly visible



Geophysical (gravity) inversion

Gravity sensitive to the whole universe

→ Can image what surface geology does not see



Flexible

- Geological constraints optional
- Different ways to add geological info
- Constraints can be applied only to some areas or some units

Deform geological bodies with inversion using geological modelling

Gravity but obvious to extend to mag

Can use with

- 1D (borehole)
- 2D constraints (seismic)
- 3D subvolume

Next (Field application)

- Modelling in Pyrenees and Southern France
- Mineral exploration case in Northern Europe

Next (Methodology)

- Exploration of model space, random generation of units not sampled by geology

Field application: Pyrenees



In a nutshell: cost function

Iterative solver: at iteration n ...

Optimize implicit field ϕ , to reduce geophysical data misfit

Account for geological data $d_{obs.}^{geol_1}$

Context

Use of pre-existing regional geological model (PhD thesis of H. Wehr: Wehr 2017¹, Wehr et al. 2018²)

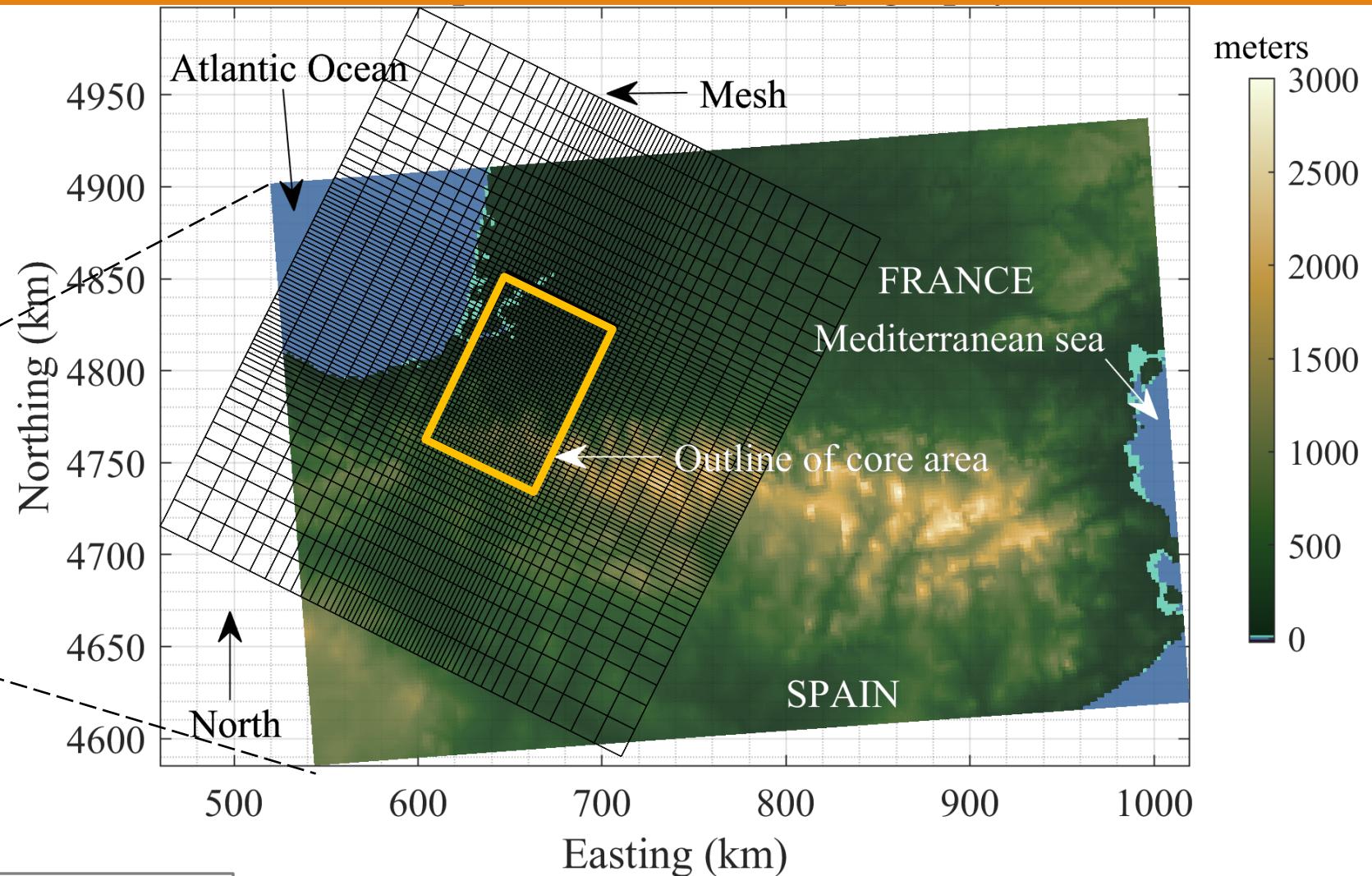
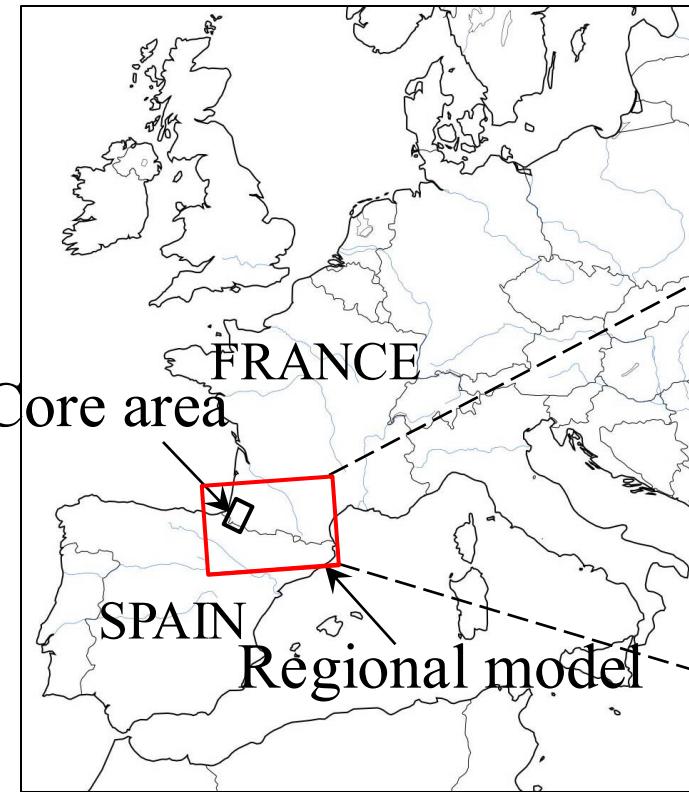
Comprehensive compilation of data

- Seismic
- Geological maps
- Boreholes
- Gravity
- Previous interpretations

Q1: Can we improve gravity data misfit?

Q2: Are there other plausible scenarios?

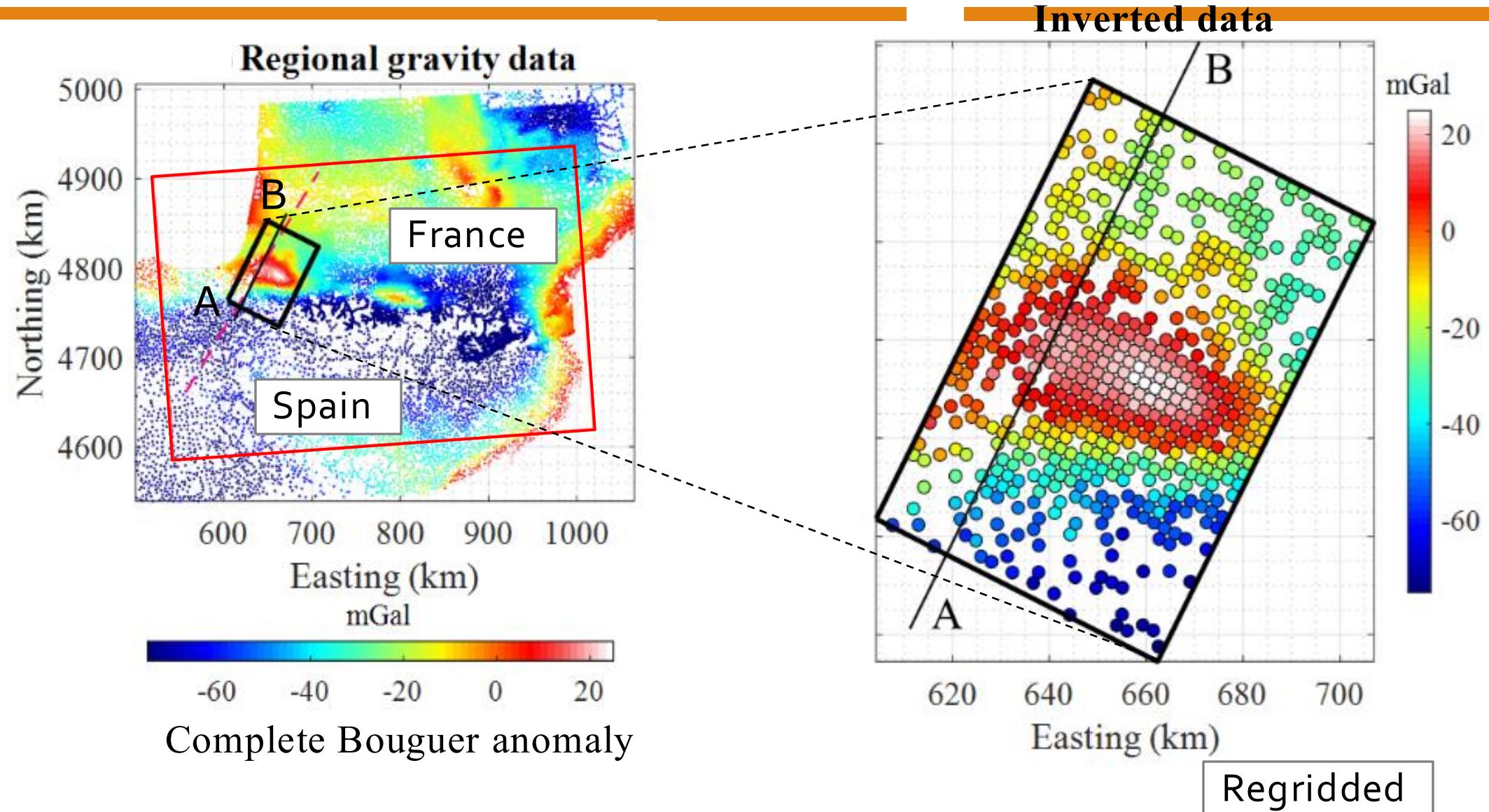
Context



Area of interest: complex, H₂ potential

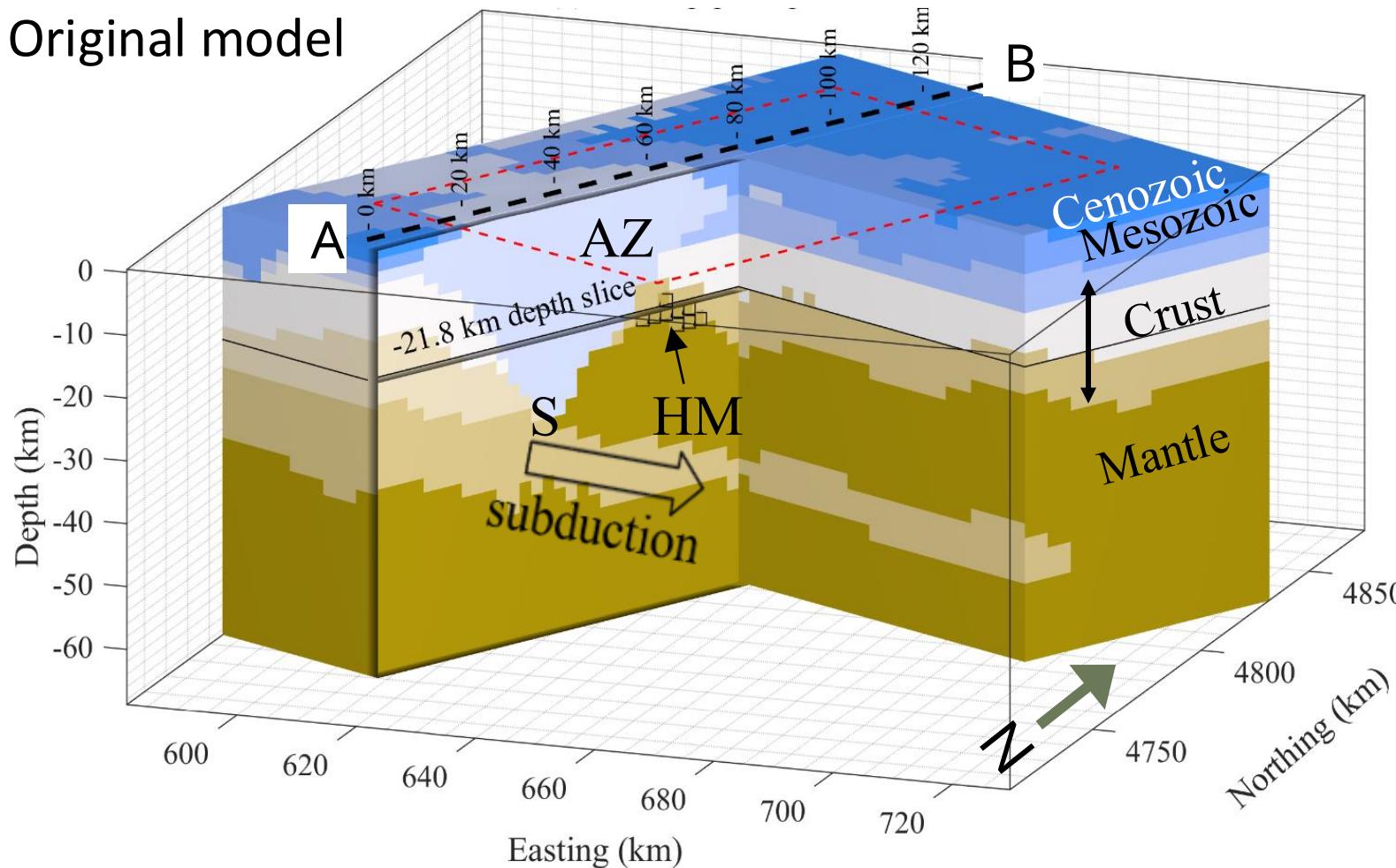
Context – Gravity data

Loop



Geological model

Original model



S: Singularity
(beginning of subduction)

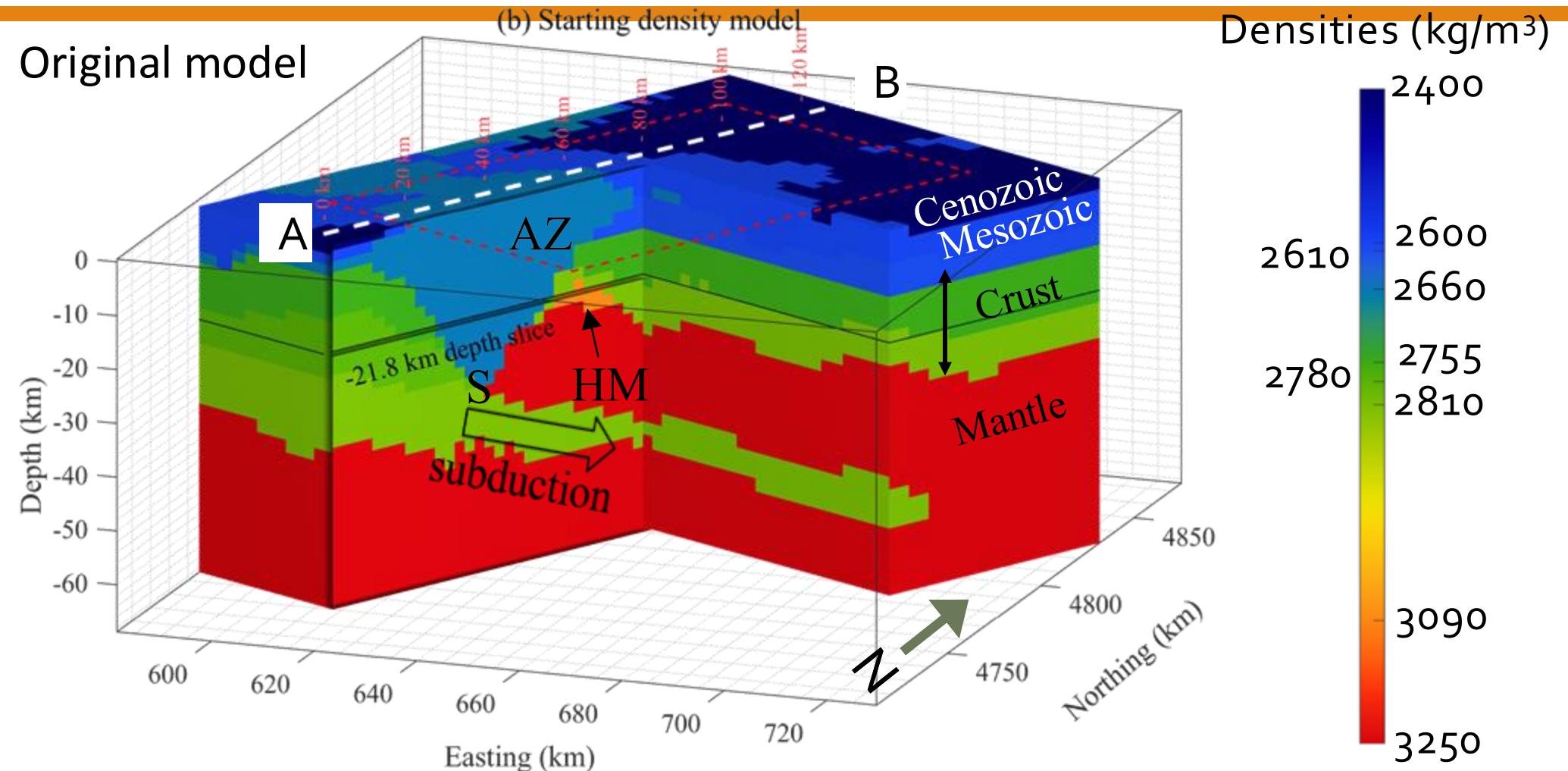
HM: Hydrated mantle.

AZ: Axial Zone

Subduction

Geological modelling and data: Wehr et al. 2018, Wehr 2017. Model: courtesy of BRGM

Geological model



S: Singularity, beginning of subduction.

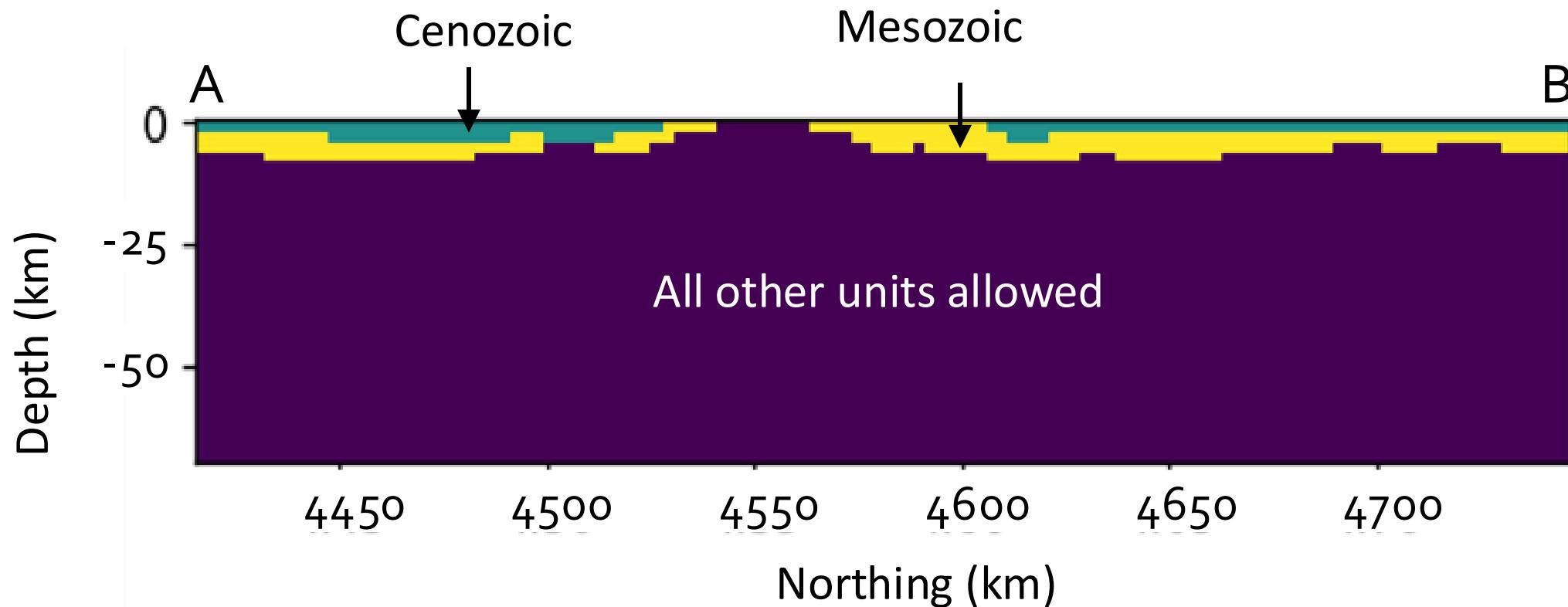
HM: Hydrated mantle

AZ: Axial Zone

Geological data

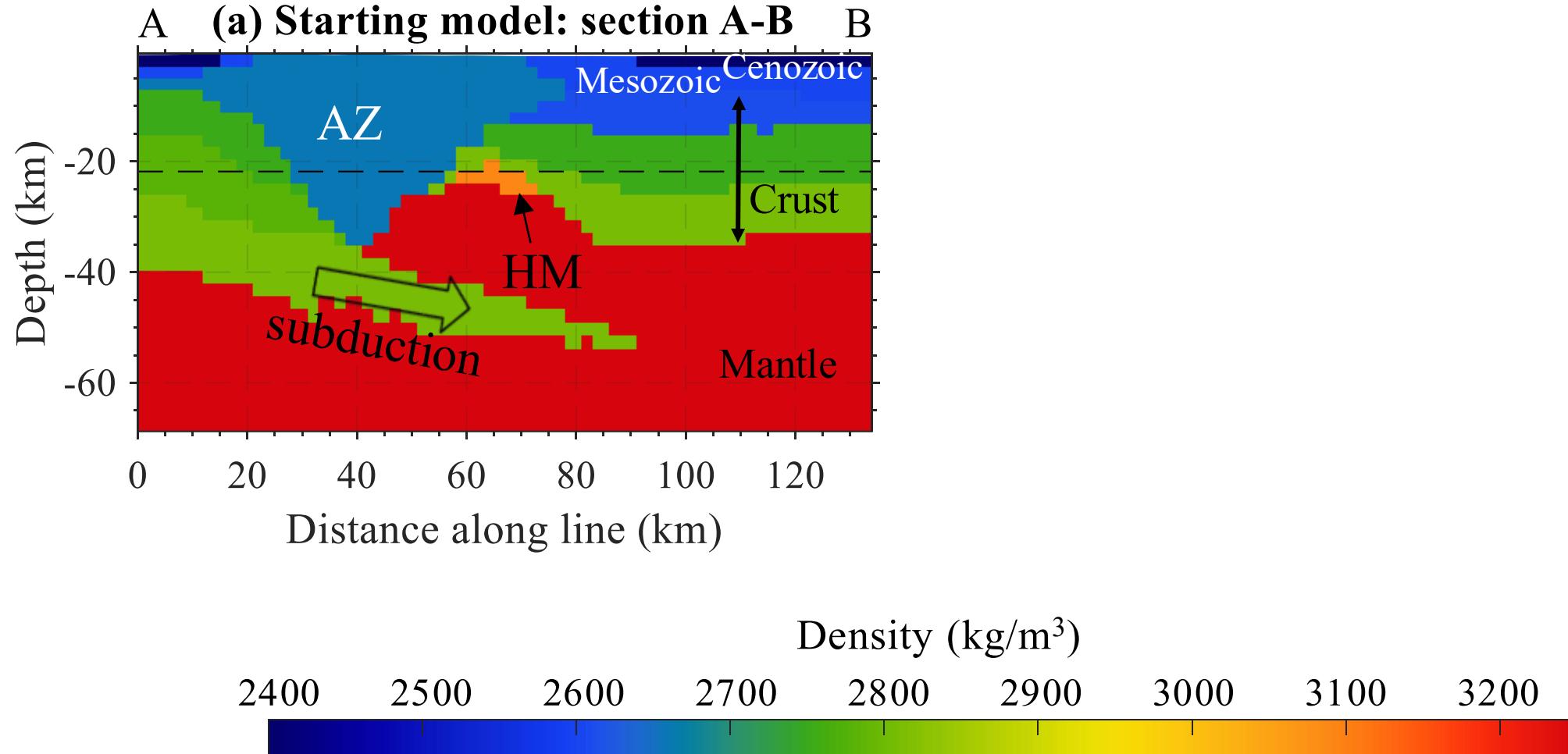
Contact and orientation data: mesozoic + cenozoic only in d_{obs}^{geol}

Other units: deep and uncertain → free to evolve



Starting from original model: A-B

Original scenario



Geological scenario generation

→ Reconcile geologically sensible scenarios with geophysical data



Densities (kg/m^3)

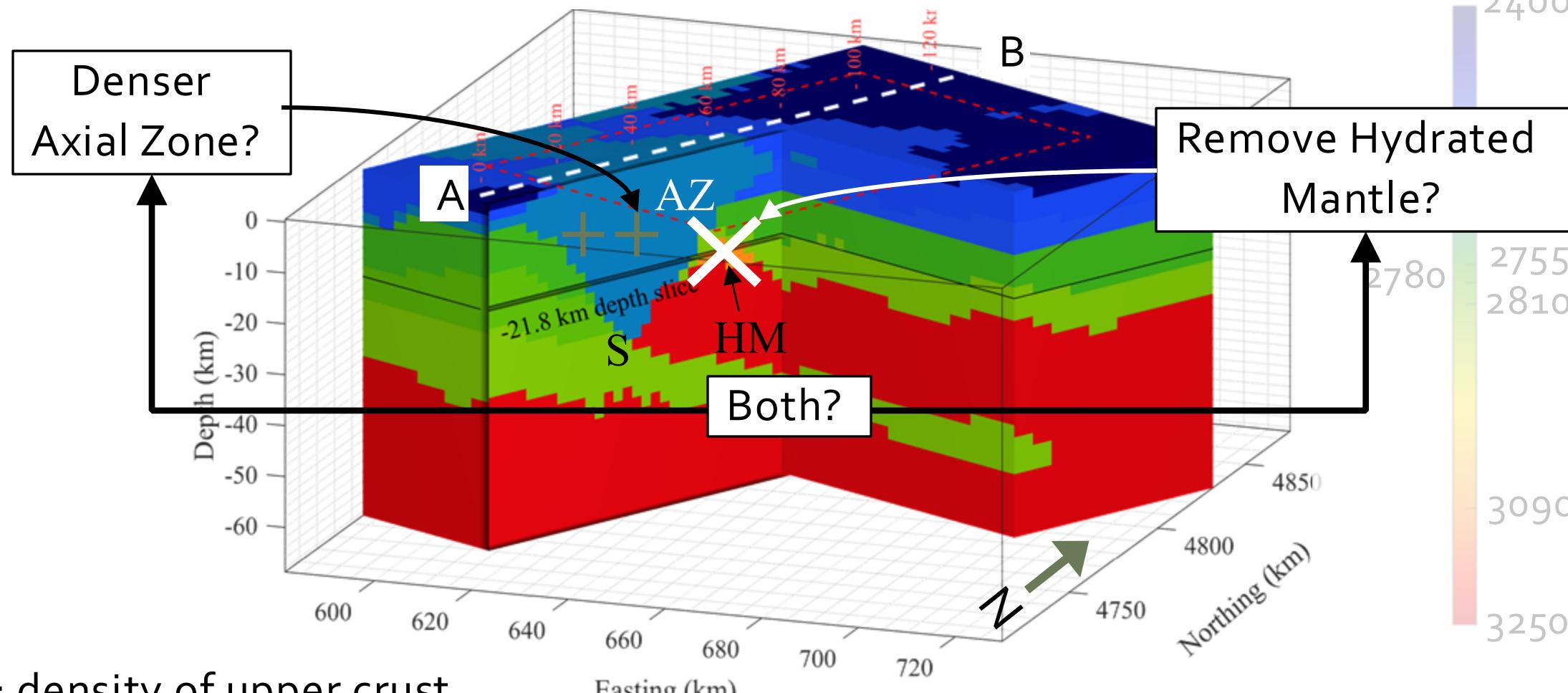
2400

2755

2810

3090

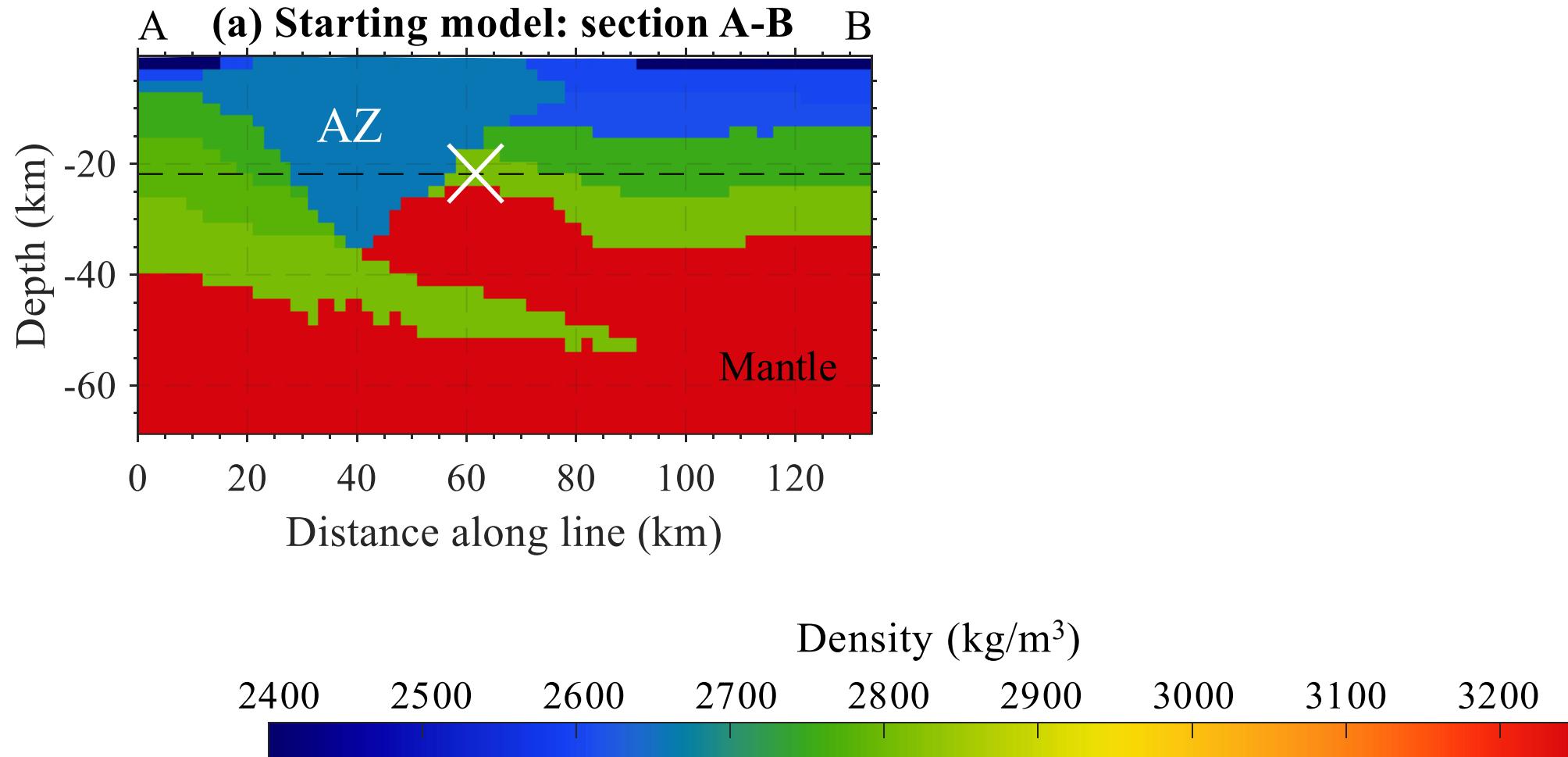
3250



- AZ: density of upper crust
- HM: density of lower curst

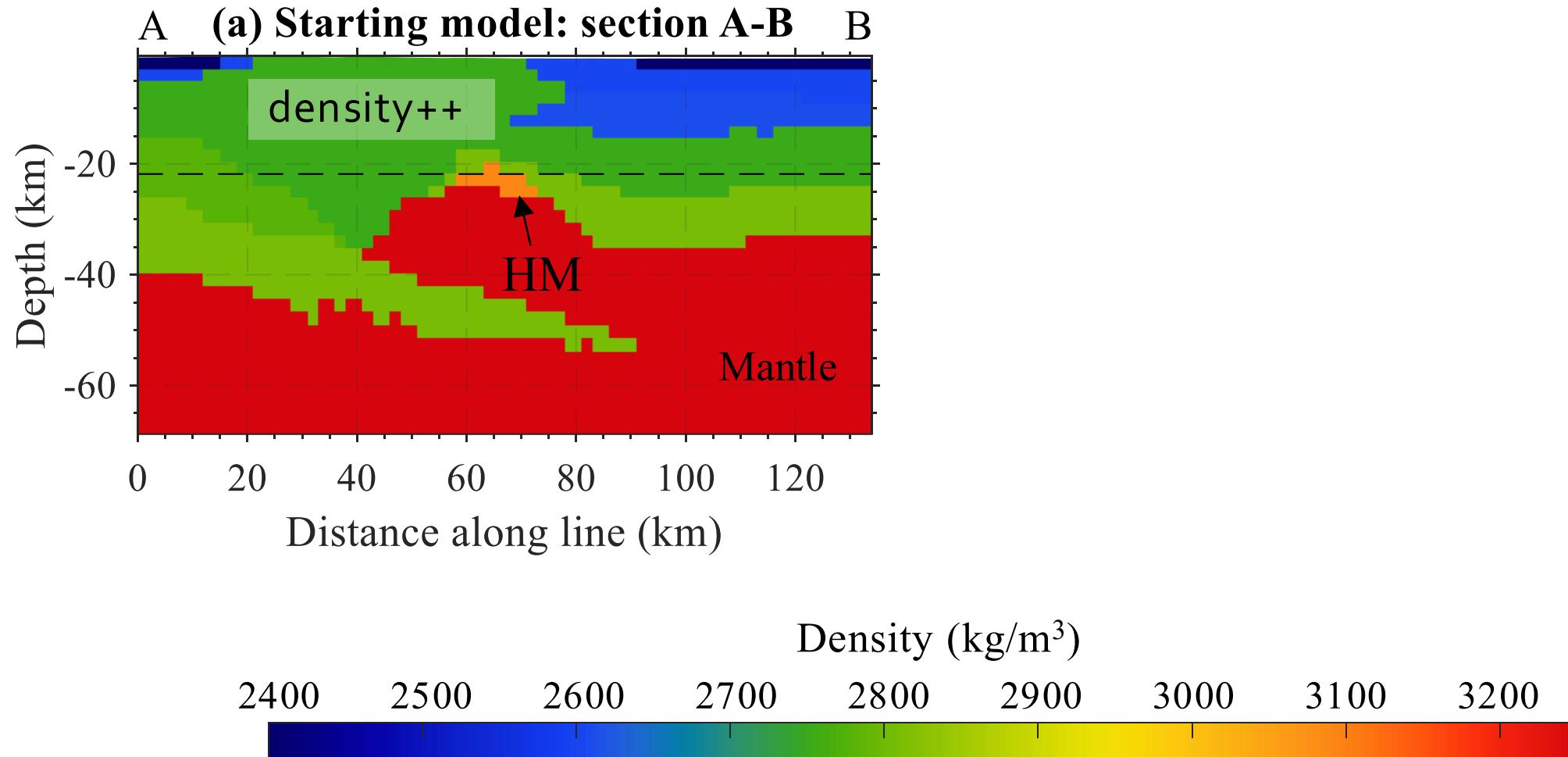
Death of hydrated mantle

Removing HM



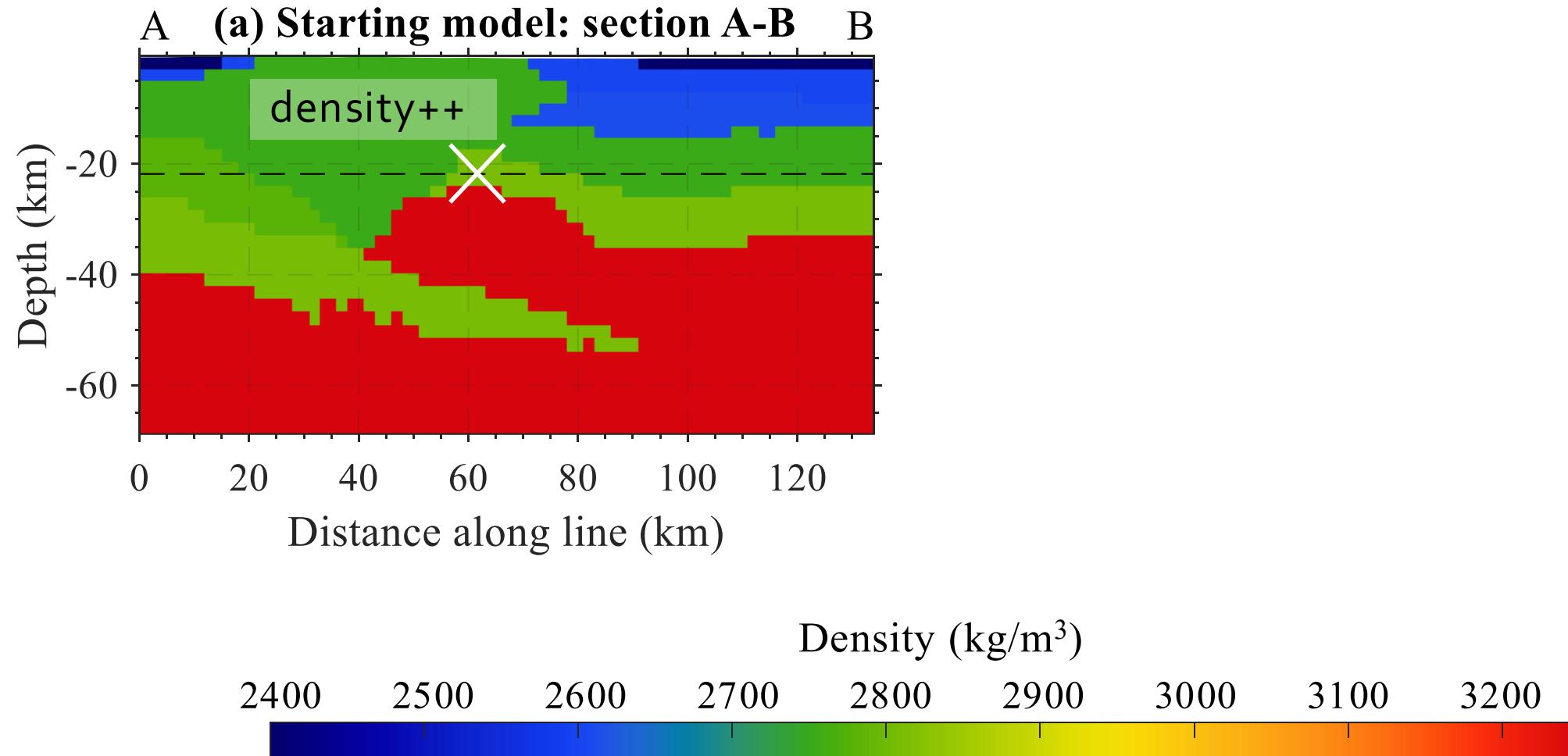
Denser axial zone

Denser AZ



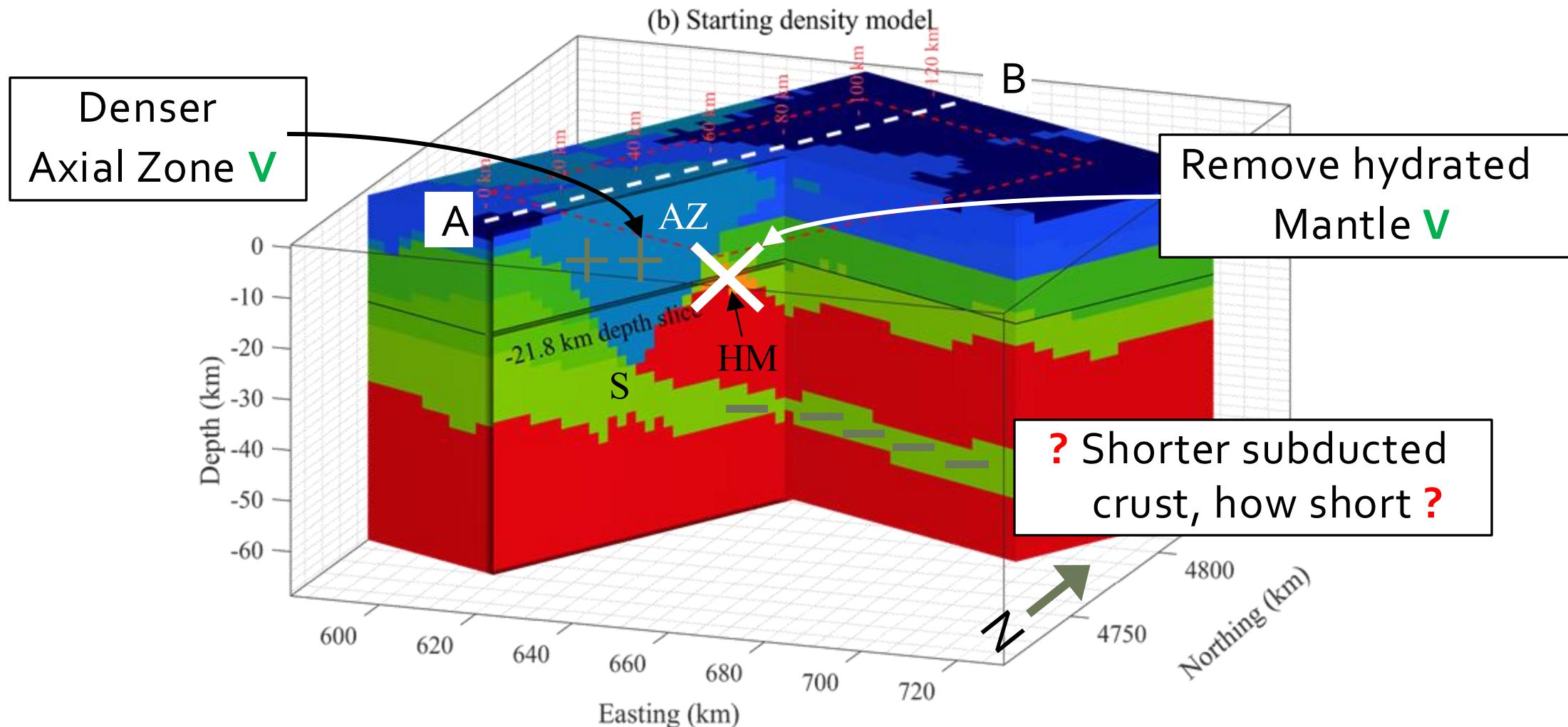
Denser axial zone + death of hydrated mantle

Removing HM, with denser AZ



Geological questions

Loop

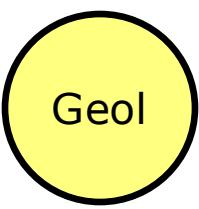
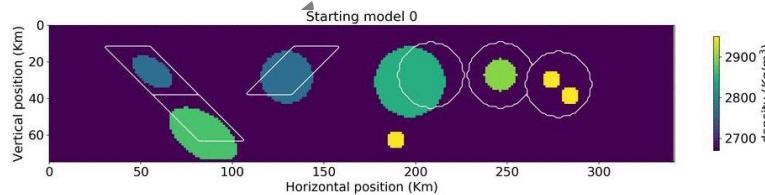


S: Singularity, beginning of subduction.

HM: Hydrated mantle.

AZ: Axial Zone

Conclusion and discussion



Geological modelling

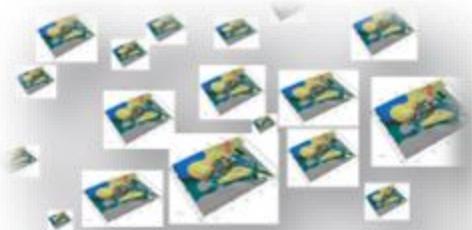
Uses surface or shallow measurements only
→ (almost) Blind to what's not visible at surface (or by seismic)



Geophysical (gravity) inversion

Gravity sensitive to the whole universe
→ Can image what geology does not see

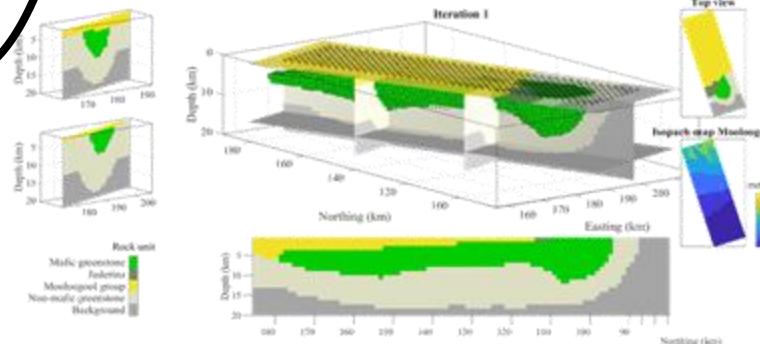
Easy to extend to mag



Feed back to geology

Many models
+ other disciplines
(e.g., seismic, EM...)

Deform geological bodies
using inversion



Intra-unit variation → semi-discrete inv.

Conclusion and discussion



Geol

Geological modelling

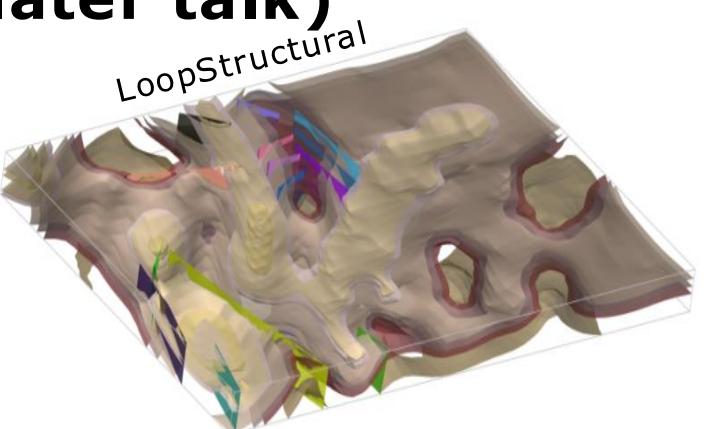
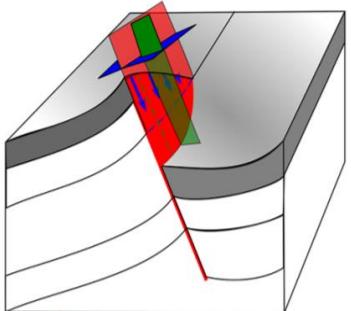
Uses surface or shallow measurements only
→ (almost) Blind to what's not visible at surface (or by seismic)

Gravi

Geophysical (gravity) inversion

Gravity sensitive to the whole universe
→ Can image what geology does not see

- Move to probabilistic world (**and trans-d: OK, see later talk**)
- Make it more geol. Driven (**coupling with LoopStructural: OK, see later talk**)



Seismic imaging

Sparse, 'precise' (accurate?) information

→ Use 2D or small 3D seismic to constrain level-set inversion

Constraining 3D geometric gravity inversion with 2D reflection seismic profile using a generalized level-set approach: application to Eastern Yilgarn craton

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Questions?

