

Lab 1

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This lab is due 11:59 PM Saturday 2/9/19.

You should have RStudio installed to edit this file. You will write code in places marked “TO-DO” to complete the problems. Some of this will be a pure programming assignment. The tools for the solutions to these problems can be found in the class practice lectures. I want you to use the methods I taught you, not for you to google and come up with whatever works. You won’t learn that way.

To “hand in” the homework, you should compile or publish this file into a PDF that includes output of your code. Once it’s done, push by the deadline to your repository in a directory called “labs”.

- Print out the numerical constant pi with ten digits after the decimal point using the internal constant pi.

```
options(digits = 11)
pi
```

```
## [1] 3.1415926536
```

- Sum up the first 100 terms of the series $1 + 1/2 + 1/4 + 1/8 + \dots$

```
x=seq(0,-99)
#x
x1 = 2^-x
#x1
round(x1,3)
```

```
## [1] 1.000 0.500 0.250 0.125 0.062 0.031 0.016 0.008 0.004 0.002 0.001
## [12] 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000
## [23] 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000
## [34] 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000
## [45] 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000
## [56] 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000
## [67] 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000
## [78] 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000
## [89] 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000
## [100] 0.000
```

```
#sum(2^-x)
sum(x1)
```

```
## [1] 2
```

- Find the product of the first 100 terms of $1 * 1/2 * 1/4 * 1/8 * \dots$

```
x=seq(0,-4)
#x
x1 = 2^-x
#x1
prod(x1)
```

```
## [1] 0.0009765625
```

- Find the product of the first 500 terms of $1 * 1/2 * 1/4 * 1/8 * \dots$. Answer in English: is this answer correct?

This answer is correct but not exact.

```
x=seq(0,-499)
x1 = 2^x
prod(2^x)
```

```
## [1] 0
```

- Figure out a means to express the answer more exactly. Not compute exactly, but express more exactly.

```
-log10(2)*sum(0:499)
```

```
## [1] -37553.491959
```

- Use the left rectangle method to numerically integrate x^2 from 0 to 1 with rectangle size $1e-6$.

```
#sum(height times width)
```

```
sum((seq(0,1-1e-6, by = 1e-6)^2)*1e-6)
```

```
## [1] 0.33333283333
```

- Calculate the average of 100 realizations of standard Bernoullis in one line using the `sample` function.

```
mean(sample(rep(c(0, 1), 100), 100, replace = TRUE))
```

```
## [1] 0.51
```

- Calculate the average of 500 realizations of Bernoullis with $p = 0.9$ in one line using the `sample` function.

```
mean(sample(rep(c(rep(1, 9), 0), 50), 500, replace=TRUE))
```

```
## [1] 0.912
```

- Calculate the average of 1000 realizations of Bernoullis with $p = 0.9$ in one line using `rbinom`.

```
rbinom(1, size=1000, prob=0.9) / 1000
```

```
## [1] 0.89
```

- Use the `strsplit` function and `sample` to put the sentences below in random order.

```
lorem = "Lorem ipsum dolor sit amet, consectetur adipiscing elit. Morbi posuere varius volutpat. Morbi "
```

```
paste(paste(sample(unlist(strsplit(lorem,"[.]"))),collapse = ". "),sep="")
```

```
## [1] " Aenean nulla ante, iaculis sed vehicula ac, finibus vel arcu. Integer dapibus mi lectus, eu p
```

- In class we generated the variable criminality with levels “none”, “infraction”, “misdemeanor” and “felony”. Create a variable `x_2` here with 100 random elements (equally probable) and ensure the proper ordinal ordering.

```
criminality=c("none", "infraction", "misdemeanor", "felony")
class(criminality)
```

```
## [1] "character"
```

```
criminality
```

```
## [1] "none"          "infraction"    "misdemeanor"  "felony"
```

```
x_3=(sample(criminality, 100, replace = TRUE))
```

```
x_2 = factor(x_3, levels= criminality, ordered = TRUE)
```

```
x_2
```

```
## [1] infraction misdemeanor misdemeanor misdemeanor infraction
## [6] misdemeanor infraction none misdemeanor misdemeanor
## [11] infraction felony misdemeanor misdemeanor infraction
## [16] infraction none infraction misdemeanor infraction
## [21] misdemeanor infraction infraction infraction felony
## [26] felony none misdemeanor felony infraction
## [31] felony infraction none none none
## [36] none none infraction none felony
## [41] infraction misdemeanor none none felony
## [46] none felony infraction none infraction
## [51] felony none felony none misdemeanor
## [56] infraction felony none misdemeanor misdemeanor
## [61] felony misdemeanor felony infraction misdemeanor
## [66] infraction none none none infraction
## [71] felony misdemeanor none infraction felony
## [76] none infraction none none infraction
## [81] none misdemeanor none felony felony
## [86] none misdemeanor none felony misdemeanor
## [91] felony none none misdemeanor misdemeanor
## [96] felony none none felony felony
## Levels: none < infraction < misdemeanor < felony
```

- Convert this variable to binary where 0 is no crime and 1 is any crime. Answer in English: is this the proper binary threshold?

```
if (!require("car")){install.packages("car")}
```

```
## Loading required package: car
```

```
## Loading required package: carData
```

```
criminality
```

```
## [1] "none" "infraction" "misdemeanor" "felony"
```

```
x_2bin = recode(x_2, "c('none')=0;
else=1")
```

```
x_2bin
```

```
## [1] 1 1 1 1 1 1 1 0 1 1 1 1 1 1 1 0 1 1 1 1 1 1 1 0 1 1 1 1 1 0 0 0
## [36] 0 0 1 0 1 1 1 0 0 1 0 1 1 0 1 1 0 1 1 1 0 1 1 1 1 1 1 1 1 1 0 0 0 1
## [71] 1 1 0 1 1 0 1 0 0 1 0 1 0 1 1 0 1 0 1 1 1 0 0 1 1 1 0 0 1 1
## Levels: 0 1
```

- Convert this variable to an unordered, nominal factor variable.

```
x_2nominal = factor(x_3, levels=criminality, ordered= FALSE)
x_2nominal
```

```
## [1] infraction misdemeanor misdemeanor misdemeanor infraction
## [6] misdemeanor infraction none misdemeanor misdemeanor
## [11] infraction felony misdemeanor misdemeanor infraction
## [16] infraction none infraction misdemeanor infraction
## [21] misdemeanor infraction infraction infraction felony
## [26] felony none misdemeanor felony infraction
## [31] felony infraction none none none
```

```
## [36] none      none      infraction none      felony
## [41] infraction misdemeanor none      none      felony
## [46] none      felony    infraction none      infraction
## [51] felony    none      felony    none      misdemeanor
## [56] infraction felony    none      misdemeanor misdemeanor
## [61] felony    misdemeanor felony    infraction misdemeanor
## [66] infraction none      none      none      infraction
## [71] felony    misdemeanor none      infraction felony
## [76] none      infraction none      none      infraction
## [81] none      misdemeanor none      felony    felony
## [86] none      misdemeanor none      felony    misdemeanor
## [91] felony    none      none      misdemeanor misdemeanor
## [96] felony    none      none      felony    felony
## Levels: none infraction misdemeanor felony
```

- Convert this variable into three binary variables without any information loss and put them into a data matrix.

```
x_2a = ifelse(as.numeric(x_2)==1,1,0)
x_2b = ifelse(as.numeric(x_2)==2,1,0)
x_2c = ifelse(as.numeric(x_2)==3,1,0)
x_2num = c(x_2a, x_2b, x_2c)
Matrix_x_2 = matrix(data=x_2num, nrow = 100, ncol = 3)
Matrix_x_2
```

```
##      [,1] [,2] [,3]
## [1,]    0    1    0
## [2,]    0    0    1
## [3,]    0    0    1
## [4,]    0    0    1
## [5,]    0    1    0
## [6,]    0    0    1
## [7,]    0    1    0
## [8,]    1    0    0
## [9,]    0    0    1
## [10,]   0    0    1
## [11,]   0    1    0
## [12,]   0    0    0
## [13,]   0    0    1
## [14,]   0    0    1
## [15,]   0    1    0
## [16,]   0    1    0
## [17,]   1    0    0
## [18,]   0    1    0
## [19,]   0    0    1
## [20,]   0    1    0
## [21,]   0    0    1
## [22,]   0    1    0
## [23,]   0    1    0
## [24,]   0    1    0
## [25,]   0    0    0
## [26,]   0    0    0
## [27,]   1    0    0
## [28,]   0    0    1
## [29,]   0    0    0
```

##	[30,]	0	1	0
##	[31,]	0	0	0
##	[32,]	0	1	0
##	[33,]	1	0	0
##	[34,]	1	0	0
##	[35,]	1	0	0
##	[36,]	1	0	0
##	[37,]	1	0	0
##	[38,]	0	1	0
##	[39,]	1	0	0
##	[40,]	0	0	0
##	[41,]	0	1	0
##	[42,]	0	0	1
##	[43,]	1	0	0
##	[44,]	1	0	0
##	[45,]	0	0	0
##	[46,]	1	0	0
##	[47,]	0	0	0
##	[48,]	0	1	0
##	[49,]	1	0	0
##	[50,]	0	1	0
##	[51,]	0	0	0
##	[52,]	1	0	0
##	[53,]	0	0	0
##	[54,]	1	0	0
##	[55,]	0	0	1
##	[56,]	0	1	0
##	[57,]	0	0	0
##	[58,]	1	0	0
##	[59,]	0	0	1
##	[60,]	0	0	1
##	[61,]	0	0	0
##	[62,]	0	0	1
##	[63,]	0	0	0
##	[64,]	0	1	0
##	[65,]	0	0	1
##	[66,]	0	1	0
##	[67,]	1	0	0
##	[68,]	1	0	0
##	[69,]	1	0	0
##	[70,]	0	1	0
##	[71,]	0	0	0
##	[72,]	0	0	1
##	[73,]	1	0	0
##	[74,]	0	1	0
##	[75,]	0	0	0
##	[76,]	1	0	0
##	[77,]	0	1	0
##	[78,]	1	0	0
##	[79,]	1	0	0
##	[80,]	0	1	0
##	[81,]	1	0	0
##	[82,]	0	0	1
##	[83,]	1	0	0

```
## [84,] 0 0 0
## [85,] 0 0 0
## [86,] 1 0 0
## [87,] 0 0 1
## [88,] 1 0 0
## [89,] 0 0 0
## [90,] 0 0 1
## [91,] 0 0 0
## [92,] 1 0 0
## [93,] 1 0 0
## [94,] 0 0 1
## [95,] 0 0 1
## [96,] 0 0 0
## [97,] 1 0 0
## [98,] 1 0 0
## [99,] 0 0 0
## [100,] 0 0 0
```

- What should the sum of each row be (in English)? Verify that.

```
sum(Matrix_x_2[,1])
```

```
## [1] 31
```

- How should the column sum look (in English)? Verify that.

```
sum(Matrix_x_2[1,])
```

```
## [1] 1
```

- Generate a matrix with 100 rows where the first column is realization from a normal with mean 17 and variance 38, the second column is uniform between -10 and 10, the third column is poisson with mean 6, the fourth column in exponential with lambda of 9, the fifth column is binomial with $n = 20$ and $p = 0.12$ and the sixth column is a binary variable with 24% 1's.

```
n = 100
z = c(rnorm(n, mean = 17, sd = sqrt(38)),
      runif(n,min = -10, max = 10),
      rpois(n,6),
      rexp(n, rate = 9),
      rbinom(n,20,0.12),
      rbinom(n,1,.24))
matrix(z, 100, 6)
```

```
##           [,1]           [,2] [,3]           [,4] [,5] [,6]
## [1,]  8.3826228214 -0.179594806395  3 0.16841091442334  2  0
## [2,] 23.3340441516  0.386856896803  5 0.07208929102247  2  0
## [3,]  7.8890429451  3.718085028231  2 0.03924601716507  1  0
## [4,] 16.7271670617 -9.277618094347  8 0.10628959898267  4  0
## [5,] 11.2380418516  6.107408367097  6 0.25248786039906  2  0
## [6,] 15.9100992623 -4.143442730419  5 0.00744143154265  5  1
## [7,] 29.1508383059 -8.287214054726  8 0.33295327588704  4  0
## [8,]  4.8409995250  0.546595635824  8 0.09462684247590  2  0
## [9,] 12.1205789630 -5.559562928975  5 0.21139126456805  3  0
## [10,] 25.4288969595  4.471341078170  5 0.08665002775123  4  0
## [11,] 21.9631594809  2.757671051659  4 0.02836900602819  0  0
## [12,] 13.9813600032 -5.024294047616  3 0.04962848582202  2  1
## [13,] 18.8739868582  9.761429526843  5 0.22423513708737  3  0
```

##	[14,]	24.9405561967	5.987352784723	1	0.10856707290176	4	0
##	[15,]	18.8631792444	6.730707297102	8	0.57080814425360	3	0
##	[16,]	17.2583225498	7.183020915836	8	0.05754778730787	1	0
##	[17,]	25.4173819570	4.702513795346	7	0.06664204224944	1	0
##	[18,]	12.3211173555	9.089266969822	4	0.20712359414227	5	1
##	[19,]	22.2204318780	7.033947282471	8	0.04485592804849	2	0
##	[20,]	20.3252443350	-4.237129590474	6	0.06822971910864	2	0
##	[21,]	22.5460475920	-1.546503142454	10	0.27287259510249	2	1
##	[22,]	7.7922350637	5.165252694860	16	0.06872213890569	2	0
##	[23,]	11.1735800201	3.721105507575	7	0.02836697740066	1	0
##	[24,]	15.4118497723	-6.059708371758	3	0.02633861566169	2	0
##	[25,]	15.8011674868	-0.971356630325	7	0.02807145483351	1	1
##	[26,]	23.2092182908	9.900620514527	6	0.07826030281904	7	0
##	[27,]	9.2319546757	7.183487215079	5	0.04323748333587	3	0
##	[28,]	12.9974972928	4.330429439433	8	0.17553525454335	0	1
##	[29,]	17.1486455995	-6.748040462844	4	0.01226951745856	2	0
##	[30,]	30.9953525162	4.311785381287	8	0.10481644731790	4	0
##	[31,]	15.8346566038	-7.912092227489	5	0.01661845617410	1	0
##	[32,]	16.1957071562	-8.486793660559	7	0.01099863524238	2	0
##	[33,]	17.7188739711	-3.374736998230	6	0.02028100932431	3	0
##	[34,]	12.0296248320	-3.943368145265	7	0.00617126720428	0	0
##	[35,]	4.7151679280	-4.134446387179	5	0.02139201273935	3	1
##	[36,]	13.3634940971	6.645396845415	6	0.55341267049638	0	0
##	[37,]	19.4459981104	6.717109545134	6	0.03812277596444	3	1
##	[38,]	16.0128574531	-3.970323260874	4	0.06042683626422	3	0
##	[39,]	17.8847820584	-8.709278278984	8	0.00954866114383	2	0
##	[40,]	17.8382939214	9.344027289189	5	0.01022290132116	6	1
##	[41,]	16.9078568885	-3.522626277991	10	0.32605355562224	2	0
##	[42,]	5.5505653096	-8.884272300638	10	0.15825141236585	2	0
##	[43,]	2.9497792590	-0.218320777640	10	0.10284209333721	1	0
##	[44,]	8.3123580259	3.666197671555	4	0.17128661853466	1	0
##	[45,]	19.8004729275	-1.046288595535	7	0.02234920583852	1	1
##	[46,]	11.8002617230	-8.067338541150	4	0.04942654709642	2	0
##	[47,]	18.0567446261	-4.832858792506	13	0.00706529705268	3	0
##	[48,]	10.8839581437	8.762123724446	2	0.23268800951796	0	0
##	[49,]	10.9687224791	4.245668132789	3	0.10761105489269	2	1
##	[50,]	25.2095005186	-9.779476709664	10	0.01922389269910	6	0
##	[51,]	23.8258067402	-6.925259339623	6	0.14754713864323	3	0
##	[52,]	16.4605634139	4.387594652362	8	0.12226729863954	4	1
##	[53,]	11.2326262129	4.179700715467	6	0.01604554320996	5	0
##	[54,]	18.5099390606	1.835783715360	6	0.04084545625012	2	0
##	[55,]	23.3521083598	7.122171223164	7	0.04494176080657	3	0
##	[56,]	16.4037744125	-6.345756864175	9	0.08478976889150	2	0
##	[57,]	26.0435252534	-3.690701429732	4	0.29770396255212	1	1
##	[58,]	10.4300075955	7.981024975888	8	0.04261352375357	1	0
##	[59,]	13.5976555730	7.533768611029	11	0.03473419919289	3	0
##	[60,]	18.3258604104	-3.160026520491	7	0.09062606313110	1	0
##	[61,]	16.6119712748	-1.634222026914	4	0.05311827175319	2	1
##	[62,]	26.7748514875	-6.892117597163	9	0.20175282159508	1	0
##	[63,]	19.6703410732	-7.042580200359	6	0.16928765031921	3	0
##	[64,]	15.6464626873	-0.258712721989	8	0.08198894539174	5	0
##	[65,]	20.0732586255	1.399198430590	10	0.04330720711086	3	0
##	[66,]	14.4610825725	2.918356140144	7	0.00332063596903	3	1
##	[67,]	13.5655512748	4.539845865220	4	0.07745776242213	3	0

##	[68,]	23.1960875432	-1.353944600560	10	0.31333566236883	3	0
##	[69,]	26.9647514852	6.585628259927	4	0.19601717735225	1	0
##	[70,]	15.7129418619	1.059583579190	9	0.03258754276774	3	1
##	[71,]	20.8515213005	-9.903895347379	2	0.23541828057260	5	0
##	[72,]	23.6996934105	2.192493984476	4	0.17737979154959	2	0
##	[73,]	15.5283858596	-4.914216087200	7	0.13707125734899	1	1
##	[74,]	25.0958546104	0.350585235283	8	0.08125422806523	4	0
##	[75,]	6.7060471410	-8.223781907000	3	0.19528780938745	4	1
##	[76,]	11.3497399535	-2.692422177643	6	0.06604193585614	4	0
##	[77,]	16.0134722176	-5.997744351625	4	0.05622740261162	2	0
##	[78,]	24.6866366633	0.276803374290	6	0.21523918118633	2	0
##	[79,]	16.4472313280	-2.550042518415	3	0.04079049423622	2	0
##	[80,]	3.9794670272	2.174467639998	6	0.20152212625945	4	0
##	[81,]	13.0892102186	7.834336119704	6	0.20774978368908	1	0
##	[82,]	23.2105780946	3.694070279598	3	0.06141612445936	2	0
##	[83,]	14.7301035996	-5.034239562228	9	0.13846130096321	3	0
##	[84,]	14.6000625162	0.020017167553	7	0.00241446474595	1	0
##	[85,]	25.4996273812	-4.530179686844	5	0.06283771996904	2	0
##	[86,]	22.6993447034	-2.863445859402	11	0.07585943723097	5	0
##	[87,]	13.3544820798	1.164093189873	8	0.00099793205866	0	0
##	[88,]	9.1398447831	5.847586924210	5	0.34067488701202	0	0
##	[89,]	19.0714682018	4.291504044086	6	0.03493947157294	3	0
##	[90,]	18.3305127464	-3.852149145678	7	0.03667893177702	2	0
##	[91,]	25.4051681741	-2.062786938623	6	0.29111802597268	3	1
##	[92,]	22.5371449064	-7.492599640973	4	0.00019242831816	2	1
##	[93,]	10.1068251750	-7.954488350078	3	0.21548127195796	4	0
##	[94,]	16.4051950767	7.085641967133	7	0.01101173555522	4	1
##	[95,]	17.6044014786	1.707672462799	6	0.01209272190721	4	1
##	[96,]	15.0979455474	0.065786954947	7	0.07834424567082	2	1
##	[97,]	14.2545497739	3.969556386583	4	0.11204371011039	3	0
##	[98,]	20.2205143482	-6.645171442069	6	0.34619878313396	1	1
##	[99,]	7.1204499107	-1.624562535435	6	0.01915260998617	2	0
##	[100,]	20.4478632765	-4.492320073768	5	0.23905382879318	1	0