Lab 5

Karen Lopez

11:59PM March 16, 2019

Load the Boston housing data frame and create the vector y (the median value) and matrix X (all other features) from the data frame. Name the columns the same as Boston except for the first name it "(Intercept)".

```
data(Boston, package = "MASS")
summary(Boston)
```

```
##
                                                indus
         crim
                                                                  chas
                               zn
##
    Min.
            : 0.00632
                                   0.00
                                                                     :0.00000
                         Min.
                                           Min.
                                                   : 0.46
                                                             Min.
    1st Qu.: 0.08204
                                   0.00
##
                         1st Qu.:
                                           1st Qu.: 5.19
                                                             1st Qu.:0.00000
    Median: 0.25651
                         Median :
                                   0.00
                                           Median: 9.69
                                                             Median :0.00000
##
    Mean
            : 3.61352
                         Mean
                                 : 11.36
                                           Mean
                                                   :11.14
                                                             Mean
                                                                     :0.06917
##
    3rd Qu.: 3.67708
                         3rd Qu.: 12.50
                                           3rd Qu.:18.10
                                                             3rd Qu.:0.00000
##
            :88.97620
                                 :100.00
                                                   :27.74
    Max.
                         Max.
                                           Max.
                                                             Max.
                                                                     :1.00000
##
                                                                dis
         nox
                             rm
                                              age
##
    Min.
            :0.3850
                       Min.
                              :3.561
                                        Min.
                                                  2.90
                                                           Min.
                                                                  : 1.130
##
    1st Qu.:0.4490
                       1st Qu.:5.886
                                        1st Qu.: 45.02
                                                           1st Qu.: 2.100
##
    Median :0.5380
                       Median :6.208
                                        Median: 77.50
                                                           Median : 3.207
##
                                                : 68.57
    Mean
            :0.5547
                       Mean
                              :6.285
                                        Mean
                                                           Mean
                                                                  : 3.795
##
    3rd Qu.:0.6240
                       3rd Qu.:6.623
                                        3rd Qu.: 94.08
                                                           3rd Qu.: 5.188
##
                                                :100.00
    Max.
            :0.8710
                      Max.
                              :8.780
                                        Max.
                                                           Max.
                                                                  :12.127
##
         rad
                                           ptratio
                                                              black
                            tax
##
    Min.
            : 1.000
                              :187.0
                                        Min.
                                                :12.60
                                                          Min.
                                                                  : 0.32
                      Min.
    1st Qu.: 4.000
                       1st Qu.:279.0
                                        1st Qu.:17.40
                                                          1st Qu.:375.38
##
##
    Median : 5.000
                       Median :330.0
                                        Median :19.05
                                                          Median: 391.44
##
            : 9.549
                              :408.2
                                                :18.46
                                                                 :356.67
    Mean
                       Mean
                                        Mean
                                                          Mean
##
    3rd Qu.:24.000
                       3rd Qu.:666.0
                                        3rd Qu.:20.20
                                                          3rd Qu.:396.23
                                                :22.00
##
    Max.
            :24.000
                       Max.
                              :711.0
                                        Max.
                                                          Max.
                                                                 :396.90
##
        lstat
                           medv
##
    Min.
            : 1.73
                             : 5.00
                     Min.
    1st Qu.: 6.95
##
                      1st Qu.:17.02
##
    Median :11.36
                     Median :21.20
##
    Mean
            :12.65
                     Mean
                             :22.53
##
    3rd Qu.:16.95
                      3rd Qu.:25.00
##
    Max.
            :37.97
                     Max.
                             :50.00
str(Boston)
##
   'data.frame':
                     506 obs. of 14 variables:
##
    $ crim
              : num
                     0.00632 0.02731 0.02729 0.03237 0.06905 ...
##
    $ zn
                     18 0 0 0 0 0 12.5 12.5 12.5 12.5 ...
              : num
##
    $
                     2.31 7.07 7.07 2.18 2.18 2.18 7.87 7.87 7.87 7.87 ...
      indus
                num
##
    $
      chas
                int
                     0 0 0 0 0 0 0 0 0 0 ...
    $ nox
##
                     0.538 0.469 0.469 0.458 0.458 0.458 0.524 0.524 0.524 0.524 ...
               num
##
    $
      rm
              : num
                     6.58 6.42 7.18 7 7.15 ...
                     65.2 78.9 61.1 45.8 54.2 58.7 66.6 96.1 100 85.9 ...
```

296 242 242 222 222 222 311 311 311 311 ...

4.09 4.97 4.97 6.06 6.06 ...

1 2 2 3 3 3 5 5 5 5 ...

\$ age

\$ dis

\$ rad

##

\$ tax

num

: num

: int

: num

```
$ ptratio: num 15.3 17.8 17.8 18.7 18.7 18.7 15.2 15.2 15.2 15.2 ...
##
                    397 397 393 395 397 ...
    $ black : num
    $ lstat : num
                    4.98 9.14 4.03 2.94 5.33 ...
                     24 21.6 34.7 33.4 36.2 28.7 22.9 27.1 16.5 18.9 ...
##
    $ medv
             : num
y = Boston$medv
   as.matrix(cbind(1, Boston[, 1 : 13]))
Х
##
       1
             crim
                      zn indus chas
                                                             dis rad tax ptratio
                                        nox
                                               rm
                                                    age
          0.00632
                    18.0
                          2.31
                                   0 0.5380 6.575
                                                   65.2
                                                         4.0900
                                                                   1 296
##
  1
       1
                                                                             15.3
                         7.07
          0.02731
                     0.0
                                   0 0.4690 6.421
                                                         4.9671
                                                                             17.8
##
  2
                                                   78.9
                                                                   2 242
       1
          0.02729
                     0.0
                         7.07
                                  0 0.4690 7.185
                                                         4.9671
                                                                   2 242
##
   3
       1
                                                   61.1
                                                                             17.8
                                                         6.0622
## 4
          0.03237
                     0.0 2.18
                                  0 0.4580 6.998
                                                                   3 222
       1
                                                   45.8
                                                                             18.7
          0.06905
                                                                   3 222
## 5
       1
                     0.0 2.18
                                  0 0.4580 7.147
                                                   54.2
                                                          6.0622
                                                                             18.7
## 6
          0.02985
                     0.0
                          2.18
                                  0 0.4580 6.430
                                                   58.7
                                                          6.0622
                                                                   3 222
                                                                             18.7
       1
          0.08829
                    12.5
                          7.87
                                  0 0.5240 6.012
                                                   66.6
                                                         5.5605
## 7
       1
                                                                   5 311
                                                                             15.2
                    12.5 7.87
## 8
          0.14455
                                  0 0.5240 6.172
                                                   96.1
                                                          5.9505
                                                                   5 311
                                                                             15.2
       1
                         7.87
## 9
          0.21124
                    12.5
                                  0 0.5240 5.631 100.0
                                                          6.0821
                                                                   5 311
                                                                             15.2
       1
## 10
       1
          0.17004
                    12.5
                          7.87
                                  0 0.5240 6.004
                                                   85.9
                                                         6.5921
                                                                   5 311
                                                                             15.2
##
   11
       1
          0.22489
                    12.5
                          7.87
                                  0 0.5240 6.377
                                                   94.3
                                                         6.3467
                                                                   5 311
                                                                             15.2
          0.11747
                    12.5
                         7.87
                                  0 0.5240 6.009
                                                   82.9
                                                         6.2267
## 12
       1
                                                                   5 311
                                                                             15.2
## 13
          0.09378
                    12.5
                         7.87
                                  0 0.5240 5.889
                                                   39.0
                                                         5.4509
                                                                   5 311
                                                                             15.2
       1
                                  0 0.5380 5.949
                         8.14
                                                         4.7075
## 14
       1
          0.62976
                     0.0
                                                   61.8
                                                                   4 307
                                                                             21.0
## 15
       1
          0.63796
                     0.0 8.14
                                  0 0.5380 6.096
                                                   84.5
                                                         4.4619
                                                                   4 307
                                                                             21.0
##
  16
       1
          0.62739
                     0.0 8.14
                                   0 0.5380 5.834
                                                   56.5
                                                          4.4986
                                                                   4 307
                                                                             21.0
##
  17
          1.05393
                     0.0 8.14
                                   0 0.5380 5.935
                                                   29.3
                                                         4.4986
                                                                   4 307
                                                                             21.0
       1
##
   18
          0.78420
                     0.0
                         8.14
                                  0 0.5380 5.990
                                                   81.7
                                                          4.2579
                                                                   4 307
                                                                             21.0
       1
##
          0.80271
                     0.0 8.14
                                  0 0.5380 5.456
                                                   36.6
                                                         3.7965
                                                                   4 307
                                                                             21.0
  19
       1
## 20
          0.72580
                     0.0 8.14
                                   0 0.5380 5.727
                                                   69.5
                                                         3.7965
                                                                   4 307
                                                                             21.0
       1
## 21
       1
          1.25179
                     0.0 8.14
                                   0 0.5380 5.570
                                                   98.1
                                                          3.7979
                                                                   4 307
                                                                             21.0
##
  22
       1
          0.85204
                     0.0 8.14
                                   0 0.5380 5.965
                                                   89.2
                                                         4.0123
                                                                   4 307
                                                                             21.0
##
          1.23247
                     0.0 8.14
                                   0 0.5380 6.142
                                                                             21.0
  23
       1
                                                   91.7
                                                          3.9769
                                                                   4 307
          0.98843
                                   0 0.5380 5.813 100.0
                                                          4.0952
##
   24
       1
                     0.0 8.14
                                                                   4 307
                                                                             21.0
##
   25
          0.75026
                     0.0
                         8.14
                                   0 0.5380 5.924
                                                   94.1
                                                          4.3996
                                                                   4 307
                                                                             21.0
       1
##
   26
       1
          0.84054
                     0.0 8.14
                                   0 0.5380 5.599
                                                   85.7
                                                          4.4546
                                                                   4 307
                                                                             21.0
##
          0.67191
                     0.0 8.14
                                   0 0.5380 5.813
                                                   90.3
                                                          4.6820
                                                                   4 307
   27
       1
                                                                             21.0
## 28
          0.95577
                     0.0 8.14
                                   0 0.5380 6.047
                                                   88.8
                                                          4.4534
                                                                   4 307
                                                                             21.0
       1
## 29
          0.77299
                     0.0 8.14
                                  0 0.5380 6.495
                                                   94.4
                                                          4.4547
                                                                   4 307
                                                                             21.0
       1
## 30
       1
          1.00245
                     0.0 8.14
                                  0 0.5380 6.674
                                                   87.3
                                                         4.2390
                                                                   4 307
                                                                             21.0
          1.13081
                     0.0 8.14
                                   0 0.5380 5.713
##
  31
       1
                                                   94.1
                                                          4.2330
                                                                   4 307
                                                                             21.0
                                                                   4 307
##
  32
       1
          1.35472
                     0.0 8.14
                                   0 0.5380 6.072 100.0
                                                          4.1750
                                                                             21.0
##
   33
       1
          1.38799
                     0.0
                         8.14
                                   0 0.5380 5.950
                                                   82.0
                                                         3.9900
                                                                   4 307
                                                                             21.0
                                  0 0.5380 5.701
##
   34
       1
          1.15172
                     0.0 8.14
                                                   95.0
                                                         3.7872
                                                                   4 307
                                                                             21.0
##
   35
       1
          1.61282
                     0.0 8.14
                                  0 0.5380 6.096
                                                   96.9
                                                         3.7598
                                                                   4 307
                                                                             21.0
          0.06417
                     0.0 5.96
                                  0 0.4990 5.933
                                                   68.2
                                                         3.3603
                                                                   5 279
                                                                             19.2
## 36
       1
##
   37
       1
          0.09744
                     0.0 5.96
                                  0 0.4990 5.841
                                                   61.4
                                                         3.3779
                                                                   5 279
                                                                             19.2
##
  38
          0.08014
                     0.0 5.96
                                  0 0.4990 5.850
                                                   41.5
                                                         3.9342
                                                                   5 279
                                                                             19.2
       1
##
   39
       1
          0.17505
                     0.0
                          5.96
                                   0 0.4990 5.966
                                                   30.2
                                                         3.8473
                                                                   5 279
                                                                             19.2
          0.02763
                    75.0
                          2.95
                                  0 0.4280 6.595
                                                         5.4011
                                                                   3 252
##
   40
                                                   21.8
                                                                             18.3
       1
          0.03359
                    75.0
                                  0 0.4280 7.024
                                                                   3 252
##
   41
       1
                          2.95
                                                   15.8
                                                         5.4011
                                                                             18.3
## 42
       1
          0.12744
                     0.0 6.91
                                  0 0.4480 6.770
                                                    2.9
                                                         5.7209
                                                                   3 233
                                                                             17.9
## 43
          0.14150
                     0.0
                          6.91
                                   0 0.4480 6.169
                                                    6.6
                                                         5.7209
                                                                   3 233
                                                                             17.9
       1
                          6.91
                                  0 0.4480 6.211
                                                                   3 233
## 44
       1
          0.15936
                     0.0
                                                    6.5
                                                         5.7209
                                                                             17.9
                                  0 0.4480 6.069
## 45
       1
          0.12269
                     0.0
                          6.91
                                                   40.0 5.7209
                                                                   3 233
                                                                             17.9
```

	_ 1	0 47440		0.01	^	0 4400	F 600	00 0	F 4004	0.000	47.0
## 4				6.91		0.4480		33.8	5.1004	3 233	17.9
## 4	7 1			6.91	0	0.4480	5.786	33.3	5.1004	3 233	17.9
## 4	8 1	0.22927	0.0	6.91	0	0.4480	6.030	85.5	5.6894	3 233	17.9
## 4	9 1	0.25387	0.0	6.91	0	0.4480	5.399	95.3	5.8700	3 233	17.9
## 5	0 1	0.21977	0.0	6.91	0	0.4480	5.602	62.0	6.0877	3 233	17.9
## 5	1 1	0.08873	21.0	5.64	0	0.4390	5.963	45.7	6.8147	4 243	16.8
## 5				5.64		0.4390		63.0	6.8147	4 243	16.8
## 5				5.64		0.4390			6.8147	4 243	16.8
								21.1			
## 5				5.64		0.4390		21.4	6.8147	4 243	16.8
## 5				4.00		0.4100		47.6	7.3197	3 469	21.1
## 5	6 1	0.01311	90.0	1.22	0	0.4030	7.249	21.9	8.6966	5 226	17.9
## 5	7 1	0.02055	85.0	0.74	0	0.4100	6.383	35.7	9.1876	2 313	17.3
## 5	8 1	0.01432	100.0	1.32	0	0.4110	6.816	40.5	8.3248	5 256	15.1
## 5	9 1	0.15445	25.0	5.13	0	0.4530	6.145	29.2	7.8148	8 284	19.7
## 6				5.13		0.4530		47.2	6.9320	8 284	19.7
## 6				5.13		0.4530		66.2	7.2254	8 284	19.7
## 6				5.13		0.4530		93.4		8 284	19.7
									6.8185		
## 6				5.13		0.4530		67.8	7.2255	8 284	19.7
## 6				5.13		0.4530		43.4	7.9809	8 284	19.7
## 6	5 1	0.01951	17.5	1.38	0	0.4161	7.104	59.5	9.2229	3 216	18.6
## 6	6 1	0.03584	80.0	3.37	0	0.3980	6.290	17.8	6.6115	4 337	16.1
## 6	7 1	0.04379	80.0	3.37	0	0.3980	5.787	31.1	6.6115	4 337	16.1
## 6	8 1	0.05789	12.5	6.07	0	0.4090	5.878	21.4	6.4980	4 345	18.9
## 6	9 1	0.13554	12.5	6.07	0	0.4090	5.594	36.8	6.4980	4 345	18.9
## 7				6.07		0.4090		33.0	6.4980	4 345	18.9
## 7				10.81		0.4130		6.6	5.2873	4 305	19.2
## 7				10.81		0.4130		17.5	5.2873	4 305	19.2
## 7				10.81		0.4130		7.8	5.2873	4 305	19.2
## 7	4 1	0.19539	0.0	10.81	0	0.4130	6.245	6.2	5.2873	4 305	19.2
## 7	5 1	0.07896	0.0	12.83	0	0.4370	6.273	6.0	4.2515	5 398	18.7
## 7	6 1	0.09512	0.0	12.83	0	0.4370	6.286	45.0	4.5026	5 398	18.7
## 7	7 1	0.10153	0.0	12.83	0	0.4370	6.279	74.5	4.0522	5 398	18.7
## 7	8 1	0.08707	0.0	12.83	0	0.4370	6.140	45.8	4.0905	5 398	18.7
## 7				12.83		0.4370		53.7	5.0141	5 398	18.7
## 8				12.83		0.4370		36.6	4.5026	5 398	18.7
## 8				4.86		0.4260		33.5	5.4007	4 281	19.0
## 8				4.86		0.4260		70.4	5.4007	4 281	19.0
## 8				4.86		0.4260		32.2	5.4007	4 281	19.0
## 8		0.03551	25.0	4.86	0	0.4260	6.167	46.7	5.4007	4 281	19.0
## 8	5 1	0.05059	0.0	4.49	0	0.4490	6.389	48.0	4.7794	3 247	18.5
## 8	6 1	0.05735	0.0	4.49	0	0.4490	6.630	56.1	4.4377	3 247	18.5
## 8	7 1	0.05188	0.0	4.49	0	0.4490	6.015	45.1	4.4272	3 247	18.5
## 8	8 1	0.07151		4.49		0.4490		56.8	3.7476	3 247	18.5
## 8						0.4890		86.3	3.4217	2 270	17.8
## 9						0.4890		63.1	3.4145	2 270	17.8
## 9				3.41		0.4890		66.1	3.0923	2 270	17.8
## 9:				3.41		0.4890		73.9	3.0921	2 270	17.8
## 9				15.04		0.4640		53.6	3.6659	4 270	18.2
## 9		0.02875		15.04	0	0.4640	6.211	28.9	3.6659	4 270	18.2
## 9	5 1	0.04294	28.0	15.04	0	0.4640	6.249	77.3	3.6150	4 270	18.2
## 9	6 1	0.12204	0.0	2.89	0	0.4450	6.625	57.8	3.4952	2 276	18.0
## 9	7 1	0.11504	0.0		0	0.4450	6.163	69.6	3.4952	2 276	18.0
## 9				2.89		0.4450		76.0	3.4952	2 276	18.0
## 9				2.89		0.4450		36.9	3.4952	2 276	18.0
"π Э	J 1	0.00101	0.0	2.00	J	0.4400	1.020	50.5	0.4002	2 210	10.0

	100 1	0.06860	0.0	2.89	0	0.4450	7.416	62.5	3.4952	2 276	18.0
##	101 1	0.14866	0.0	8.56		0.5200		79.9	2.7778	5 384	20.9
##	102 1	0.11432	0.0	8.56	0	0.5200	6.781	71.3	2.8561	5 384	20.9
##	103 1	0.22876	0.0	8.56	0	0.5200	6.405	85.4	2.7147	5 384	20.9
##	104 1	0.21161	0.0	8.56	0	0.5200	6.137	87.4	2.7147	5 384	20.9
##	105 1	0.13960	0.0	8.56	0	0.5200	6.167	90.0	2.4210	5 384	20.9
##	106 1	0.13262	0.0	8.56	0	0.5200	5.851	96.7	2.1069	5 384	20.9
##	107 1	0.17120	0.0	8.56	0	0.5200	5.836	91.9	2.2110	5 384	20.9
##	108 1	0.13117	0.0	8.56	0	0.5200	6.127	85.2	2.1224	5 384	20.9
##	109 1	0.12802	0.0	8.56	0	0.5200	6.474	97.1	2.4329	5 384	20.9
##	110 1	0.26363	0.0	8.56	0	0.5200	6.229	91.2	2.5451	5 384	20.9
##	111 1	0.10793	0.0	8.56	0	0.5200	6.195	54.4	2.7778	5 384	20.9
##	112 1	0.10084	0.0	10.01	0	0.5470	6.715	81.6	2.6775	6 432	17.8
##	113 1	0.12329	0.0	10.01	0	0.5470	5.913	92.9	2.3534	6 432	17.8
##	114 1	0.22212	0.0	10.01	0	0.5470	6.092	95.4	2.5480	6 432	17.8
	115 1	0.14231		10.01		0.5470		84.2	2.2565	6 432	17.8
	116 1	0.17134		10.01		0.5470		88.2	2.4631	6 432	17.8
	117 1	0.13158		10.01		0.5470		72.5	2.7301	6 432	17.8
	118 1	0.15098		10.01		0.5470		82.6	2.7474	6 432	17.8
	119 1	0.13058		10.01		0.5470		73.1	2.4775	6 432	17.8
	120 1	0.14476		10.01		0.5470		65.2	2.7592	6 432	17.8
	121 1	0.06899		25.65		0.5810		69.7	2.2577	2 188	19.1
	122 1	0.07165		25.65		0.5810		84.1	2.1974	2 188	19.1
	123 1	0.09299		25.65		0.5810		92.9	2.0869	2 188	19.1
	124 1	0.15038		25.65		0.5810		97.0	1.9444	2 188	19.1
	125 1	0.10030		25.65		0.5810		95.8	2.0063	2 188	19.1
	126 1	0.16902		25.65		0.5810		88.4	1.9929	2 188	19.1
	127 1	0.10302		25.65		0.5810		95.6	1.7572	2 188	19.1
	128 1	0.25915		21.89		0.6240		96.0	1.7883	4 437	21.2
	129 1	0.32543		21.89		0.6240		98.8	1.8125	4 437	21.2
	130 1	0.88125		21.89		0.6240		94.7	1.9799	4 437	21.2
	131 1	0.34006		21.89		0.6240		98.9	2.1185	4 437	21.2
	132 1			21.89		0.6240				4 437	
	133 1	1.19294		21.89		0.6240		97.7	2.2710	4 437	21.2
		0.59005				0.6240		97.9	2.3274		21.2
	134 1	0.32982		21.89				95.4	2.4699	4 437	21.2
	135 1 136 1	0.97617		21.89		0.6240			2.3460	4 437	21.2 21.2
		0.55778		21.89		0.6240		98.2	2.1107	4 437	
		0.32264							1.9669		21.2
	138 1			21.89					1.8498	4 437	21.2
	139 1			21.89					1.6686	4 437	21.2
	140 1	0.54452		21.89		0.6240				4 437	21.2
	141 1	0.29090		21.89		0.6240				4 437	21.2
	142 1	1.62864		21.89					1.4394	4 437	21.2
	143 1	3.32105		19.58					1.3216	5 403	14.7
	144 1	4.09740		19.58					1.4118	5 403	14.7
	145 1	2.77974		19.58					1.3459	5 403	14.7
	146 1	2.37934		19.58					1.4191	5 403	14.7
	147 1	2.15505		19.58		0.8710				5 403	14.7
	148 1	2.36862		19.58		0.8710				5 403	14.7
	149 1	2.33099		19.58		0.8710				5 403	14.7
	150 1	2.73397		19.58		0.8710				5 403	14.7
	151 1	1.65660		19.58					1.6180	5 403	14.7
##	152 1	1.49632		19.58					1.5916	5 403	14.7
##	153 1	1.12658	0.0	19.58	1	0.8710	5.012	88.0	1.6102	5 403	14.7

##	154 1	2.14918	0.0	19.58	0	0.8710	5.709	98.5	1.6232	5 403	14.7
##	155 1	1.41385	0.0	19.58	1	0.8710	6.129	96.0	1.7494	5 403	14.7
##	156 1	3.53501	0.0	19.58	1	0.8710	6.152	82.6	1.7455	5 403	14.7
##	157 1	2.44668	0.0	19.58	0	0.8710	5.272	94.0	1.7364	5 403	14.7
##	158 1	1.22358	0.0	19.58	0	0.6050	6.943	97.4	1.8773	5 403	14.7
##	159 1	1.34284	0.0	19.58	0	0.6050	6.066	100.0	1.7573	5 403	14.7
##	160 1	1.42502	0.0	19.58	0	0.8710	6.510	100.0	1.7659	5 403	14.7
##	161 1	1.27346	0.0	19.58	1	0.6050	6.250	92.6	1.7984	5 403	14.7
##	162 1	1.46336	0.0	19.58	0	0.6050	7.489	90.8	1.9709	5 403	14.7
##	163 1	1.83377	0.0	19.58	1	0.6050	7.802	98.2	2.0407	5 403	14.7
##	164 1	1.51902	0.0	19.58	1	0.6050	8.375	93.9	2.1620	5 403	14.7
##	165 1	2.24236	0.0	19.58	0	0.6050	5.854	91.8	2.4220	5 403	14.7
##	166 1	2.92400	0.0	19.58	0	0.6050	6.101	93.0	2.2834	5 403	14.7
##	167 1	2.01019	0.0	19.58	0	0.6050	7.929	96.2	2.0459	5 403	14.7
##	168 1	1.80028	0.0	19.58	0	0.6050	5.877	79.2	2.4259	5 403	14.7
##	169 1	2.30040	0.0	19.58	0	0.6050	6.319	96.1	2.1000	5 403	14.7
##	170 1	2.44953	0.0	19.58	0	0.6050	6.402	95.2	2.2625	5 403	14.7
##	171 1	1.20742	0.0	19.58	0	0.6050	5.875	94.6	2.4259	5 403	14.7
##	172 1	2.31390	0.0	19.58	0	0.6050	5.880	97.3	2.3887	5 403	14.7
##	173 1	0.13914	0.0	4.05	0	0.5100	5.572	88.5	2.5961	5 296	16.6
##	174 1	0.09178	0.0	4.05	0	0.5100	6.416	84.1	2.6463	5 296	16.6
##	175 1	0.08447	0.0	4.05	0	0.5100	5.859	68.7	2.7019	5 296	16.6
##	176 1	0.06664	0.0	4.05	0	0.5100	6.546	33.1	3.1323	5 296	16.6
##	177 1	0.07022	0.0	4.05	0	0.5100	6.020	47.2	3.5549	5 296	16.6
##	178 1	0.05425	0.0	4.05	0	0.5100	6.315	73.4	3.3175	5 296	16.6
##	179 1	0.06642	0.0	4.05	0	0.5100	6.860	74.4	2.9153	5 296	16.6
##	180 1	0.05780	0.0	2.46	0	0.4880	6.980	58.4	2.8290	3 193	17.8
##	181 1	0.06588	0.0	2.46	0	0.4880	7.765	83.3	2.7410	3 193	17.8
##	182 1	0.06888	0.0	2.46	0	0.4880	6.144	62.2	2.5979	3 193	17.8
##	183 1	0.09103	0.0	2.46	0	0.4880	7.155	92.2	2.7006	3 193	17.8
##	184 1	0.10008	0.0	2.46	0	0.4880	6.563	95.6	2.8470	3 193	17.8
##	185 1	0.08308	0.0	2.46	0	0.4880	5.604	89.8	2.9879	3 193	17.8
##	186 1	0.06047	0.0	2.46	0	0.4880	6.153	68.8	3.2797	3 193	17.8
##	187 1	0.05602	0.0	2.46	0	0.4880	7.831	53.6	3.1992	3 193	17.8
##	188 1	0.07875	45.0	3.44	0	0.4370	6.782	41.1	3.7886	5 398	15.2
##	189 1	0.12579	45.0	3.44	0	0.4370	6.556	29.1	4.5667	5 398	15.2
##	190 1	0.08370	45.0	3.44	0	0.4370	7.185	38.9	4.5667	5 398	15.2
##	191 1	0.09068	45.0	3.44	0	0.4370	6.951	21.5	6.4798	5 398	15.2
##	192 1	0.06911	45.0	3.44	0	0.4370	6.739	30.8	6.4798	5 398	15.2
##	193 1	0.08664	45.0	3.44	0	0.4370	7.178	26.3	6.4798	5 398	15.2
##	194 1	0.02187	60.0	2.93	0	0.4010	6.800	9.9	6.2196	1 265	15.6
##	195 1	0.01439	60.0	2.93	0	0.4010	6.604	18.8	6.2196	1 265	15.6
##	196 1	0.01381	80.0	0.46	0	0.4220	7.875	32.0	5.6484	4 255	14.4
##	197 1	0.04011	80.0	1.52	0	0.4040	7.287	34.1	7.3090	2 329	12.6
##	198 1	0.04666	80.0	1.52	0	0.4040	7.107	36.6	7.3090	2 329	12.6
##	199 1	0.03768	80.0	1.52	0	0.4040	7.274	38.3	7.3090	2 329	12.6
##	200 1	0.03150	95.0	1.47	0	0.4030	6.975	15.3	7.6534	3 402	17.0
##	201 1	0.01778	95.0	1.47	0	0.4030	7.135	13.9	7.6534	3 402	17.0
##	202 1	0.03445	82.5	2.03	0	0.4150	6.162	38.4	6.2700	2 348	14.7
##	203 1	0.02177	82.5	2.03	0	0.4150	7.610	15.7	6.2700	2 348	14.7
##	204 1	0.03510	95.0	2.68	0	0.4161	7.853	33.2	5.1180	4 224	14.7
##	205 1	0.02009	95.0	2.68	0	0.4161	8.034		5.1180	4 224	14.7
##	206 1			10.59		0.4890				4 277	18.6
##	207 1	0.22969	0.0	10.59	0	0.4890	6.326	52.5	4.3549	4 277	18.6

##	208 1	0.25199	0.0	10.59	0	0.4890	5.783	72.7	4.3549	4 277	18.6
##	209 1	0.13587	0.0	10.59	1	0.4890	6.064	59.1	4.2392	4 277	18.6
##	210 1	0.43571	0.0	10.59	1	0.4890	5.344	100.0	3.8750	4 277	18.6
##	211 1	0.17446	0.0	10.59	1	0.4890	5.960	92.1	3.8771	4 277	18.6
##	212 1	0.37578	0.0	10.59	1	0.4890	5.404	88.6	3.6650	4 277	18.6
##	213 1	0.21719	0.0	10.59	1	0.4890	5.807	53.8	3.6526	4 277	18.6
##	214 1	0.14052	0.0	10.59	0	0.4890	6.375	32.3	3.9454	4 277	18.6
##	215 1	0.28955	0.0	10.59	0	0.4890	5.412	9.8	3.5875	4 277	18.6
##	216 1	0.19802	0.0	10.59	0	0.4890	6.182	42.4	3.9454	4 277	18.6
##	217 1	0.04560	0.0	13.89	1	0.5500	5.888	56.0	3.1121	5 276	16.4
##	218 1	0.07013	0.0	13.89	0	0.5500	6.642	85.1	3.4211	5 276	16.4
##	219 1	0.11069	0.0	13.89	1	0.5500	5.951	93.8	2.8893	5 276	16.4
##	220 1	0.11425	0.0	13.89	1	0.5500	6.373	92.4	3.3633	5 276	16.4
##	221 1	0.35809	0.0	6.20	1	0.5070	6.951	88.5	2.8617	8 307	17.4
##	222 1	0.40771	0.0	6.20	1	0.5070	6.164	91.3	3.0480	8 307	17.4
##	223 1	0.62356	0.0	6.20	1	0.5070	6.879	77.7	3.2721	8 307	17.4
##	224 1	0.61470	0.0	6.20	0	0.5070	6.618	80.8	3.2721	8 307	17.4
##	225 1	0.31533	0.0	6.20	0	0.5040	8.266	78.3	2.8944	8 307	17.4
	226 1	0.52693	0.0	6.20		0.5040		83.0	2.8944	8 307	17.4
##	227 1	0.38214	0.0	6.20	0	0.5040	8.040	86.5	3.2157	8 307	17.4
	228 1	0.41238	0.0	6.20		0.5040		79.9	3.2157	8 307	17.4
##	229 1	0.29819	0.0	6.20		0.5040		17.0	3.3751	8 307	17.4
##	230 1	0.44178	0.0	6.20	0	0.5040	6.552	21.4	3.3751	8 307	17.4
	231 1	0.53700	0.0	6.20	0	0.5040	5.981	68.1	3.6715	8 307	17.4
	232 1	0.46296	0.0	6.20		0.5040		76.9	3.6715	8 307	17.4
	233 1	0.57529	0.0	6.20		0.5070			3.8384	8 307	17.4
	234 1	0.33147	0.0	6.20		0.5070			3.6519	8 307	17.4
	235 1	0.44791	0.0	6.20		0.5070		66.5	3.6519	8 307	17.4
	236 1	0.33045	0.0	6.20		0.5070		61.5	3.6519	8 307	17.4
	237 1	0.52058	0.0	6.20		0.5070			4.1480	8 307	17.4
	238 1	0.51183	0.0	6.20		0.5070		71.6	4.1480	8 307	17.4
	239 1	0.08244	30.0	4.93		0.4280		18.5	6.1899	6 300	16.6
	240 1	0.09252	30.0	4.93		0.4280		42.2	6.1899	6 300	16.6
	241 1	0.11329	30.0	4.93		0.4280			6.3361	6 300	16.6
	242 1	0.10612	30.0	4.93		0.4280		65.1	6.3361	6 300	16.6
	243 1	0.10290	30.0	4.93		0.4280			7.0355	6 300	16.6
	244 1	0.12757	30.0	4.93		0.4280		7.8	7.0355	6 300	16.6
		0.20608							7.9549		19.1
	246 1	0.19133	22.0	5.86		0.4310			7.9549	7 330	19.1
	247 1	0.33983	22.0	5.86		0.4310				7 330	19.1
	248 1	0.19657	22.0	5.86		0.4310				7 330	19.1
	249 1	0.16439	22.0	5.86		0.4310			7.8265	7 330	19.1
	250 1	0.19073	22.0	5.86		0.4310			7.8265	7 330	19.1
	251 1	0.14030	22.0	5.86		0.4310			7.3967	7 330	19.1
	252 1	0.21409	22.0	5.86		0.4310				7 330	19.1
	253 1	0.08221	22.0	5.86		0.4310			8.9067	7 330	19.1
	254 1	0.36894	22.0	5.86		0.4310		8.4		7 330	19.1
	255 1	0.04819	80.0	3.64		0.3920				1 315	16.4
	256 1		80.0	3.64		0.3920			9.2203	1 315	16.4
	257 1	0.01538	90.0	3.75		0.3940			6.3361	3 244	15.9
	258 1	0.61154	20.0	3.97		0.6470				5 264	13.0
	259 1	0.66351	20.0	3.97					1.8946	5 264	13.0
	260 1	0.65665	20.0	3.97					2.0107	5 264	13.0
	261 1	0.54011	20.0	3.97		0.6470				5 264	13.0
#	1	0.01011	20.0	3.31	J	0.0110	200	51.0		5 254	10.0

##	262 1	0.53412	20.0	3.97	٥	0.6470	7 520	89.4	2.1398	5 264	13.0
	263 1	0.52014	20.0	3.97		0.6470		91.5	2.2885	5 264	13.0
	264 1	0.82526	20.0	3.97		0.6470		94.5	2.0788	5 264	13.0
	265 1	0.55007	20.0	3.97		0.6470		91.6	1.9301	5 264	13.0
	266 1	0.76162	20.0	3.97		0.6470		62.8	1.9865	5 264	13.0
	267 1	0.78570	20.0	3.97		0.6470		84.6	2.1329	5 264	13.0
##	268 1	0.57834	20.0	3.97	0	0.5750	8.297	67.0	2.4216	5 264	13.0
##	269 1	0.54050	20.0	3.97	0	0.5750	7.470	52.6	2.8720	5 264	13.0
##	270 1	0.09065	20.0	6.96	1	0.4640	5.920	61.5	3.9175	3 223	18.6
##	271 1	0.29916	20.0	6.96	0	0.4640	5.856	42.1	4.4290	3 223	18.6
##	272 1	0.16211	20.0	6.96	0	0.4640	6.240	16.3	4.4290	3 223	18.6
##	273 1	0.11460	20.0	6.96	0	0.4640	6.538	58.7	3.9175	3 223	18.6
##	274 1	0.22188	20.0	6.96	1	0.4640	7.691	51.8	4.3665	3 223	18.6
##	275 1	0.05644	40.0	6.41	1	0.4470	6.758	32.9	4.0776	4 254	17.6
##	276 1	0.09604	40.0	6.41	0	0.4470	6.854	42.8	4.2673	4 254	17.6
	277 1	0.10469	40.0	6.41		0.4470		49.0	4.7872	4 254	17.6
	278 1	0.06127	40.0	6.41		0.4470		27.6	4.8628	4 254	17.6
	279 1	0.07978	40.0	6.41		0.4470		32.1	4.1403	4 254	17.6
	280 1	0.21038	20.0	3.33		0.4429		32.2	4.1007	5 216	14.9
	281 1	0.21038	20.0	3.33		0.4429		64.5	4.6947	5 216	14.9
	282 1					0.4429					
		0.03705	20.0	3.33				37.2	5.2447	5 216	14.9
	283 1	0.06129	20.0	3.33		0.4429		49.7	5.2119	5 216	14.9
	284 1	0.01501	90.0	1.21		0.4010		24.8	5.8850	1 198	13.6
	285 1	0.00906	90.0	2.97		0.4000		20.8	7.3073	1 285	15.3
	286 1	0.01096	55.0	2.25		0.3890		31.9	7.3073	1 300	15.3
	287 1	0.01965	80.0	1.76		0.3850		31.5	9.0892	1 241	18.2
##	288 1	0.03871	52.5	5.32	0	0.4050	6.209	31.3	7.3172	6 293	16.6
##	289 1	0.04590	52.5	5.32	0	0.4050	6.315	45.6	7.3172	6 293	16.6
##	290 1	0.04297	52.5	5.32	0	0.4050	6.565	22.9	7.3172	6 293	16.6
##	291 1	0.03502	80.0	4.95	0	0.4110	6.861	27.9	5.1167	4 245	19.2
##	292 1	0.07886	80.0	4.95	0	0.4110	7.148	27.7	5.1167	4 245	19.2
##	293 1	0.03615	80.0	4.95	0	0.4110	6.630	23.4	5.1167	4 245	19.2
##	294 1	0.08265	0.0	13.92	0	0.4370	6.127	18.4	5.5027	4 289	16.0
##	295 1	0.08199	0.0	13.92	0	0.4370	6.009	42.3	5.5027	4 289	16.0
##	296 1	0.12932	0.0	13.92	0	0.4370	6.678	31.1	5.9604	4 289	16.0
	297 1	0.05372		13.92		0.4370		51.0	5.9604	4 289	16.0
	298 1	0.14103		13.92		0.4370		58.0	6.3200	4 289	16.0
	299 1	0.06466	70.0	2.24		0.4000		20.1	7.8278	5 358	14.8
	300 1	0.05561	70.0	2.24		0.4000		10.0	7.8278	5 358	14.8
	301 1	0.04417	70.0	2.24		0.4000		47.4	7.8278	5 358	14.8
	302 1	0.03537	34.0	6.09		0.4330		40.4	5.4917	7 329	16.1
	303 1					0.4330		18.4			16.1
		0.09266	34.0	6.09					5.4917	7 329	
	304 1	0.10000	34.0	6.09		0.4330		17.7	5.4917	7 329	16.1
	305 1	0.05515	33.0	2.18		0.4720		41.1	4.0220	7 222	18.4
	306 1	0.05479	33.0	2.18		0.4720		58.1	3.3700	7 222	18.4
	307 1	0.07503	33.0	2.18		0.4720		71.9	3.0992	7 222	18.4
	308 1	0.04932	33.0	2.18		0.4720		70.3	3.1827	7 222	18.4
	309 1	0.49298	0.0	9.90		0.5440		82.5	3.3175	4 304	18.4
	310 1	0.34940	0.0	9.90		0.5440		76.7	3.1025	4 304	18.4
	311 1	2.63548	0.0	9.90		0.5440		37.8	2.5194	4 304	18.4
	312 1	0.79041	0.0	9.90	0	0.5440	6.122	52.8	2.6403	4 304	18.4
##	313 1	0.26169	0.0	9.90	0	0.5440	6.023	90.4	2.8340	4 304	18.4
##	314 1	0.26938	0.0	9.90	0	0.5440	6.266	82.8	3.2628	4 304	18.4
##	315 1	0.36920	0.0	9.90	0	0.5440	6.567	87.3	3.6023	4 304	18.4

##	316 1	0.25356	0.0	9.90	0	0.5440	5 705	77.7	3.9450	4 3	04 18.4
	317 1	0.31827	0.0	9.90		0.5440		83.2	3.9986	4 3	
	318 1	0.24522	0.0	9.90		0.5440		71.7		4 3	
	319 1	0.40202	0.0	9.90		0.5440		67.2		4 3	
	320 1	0.47547	0.0	9.90		0.5440		58.8	4.0019	4 3	
	321 1	0.16760	0.0	7.38		0.4930		52.3	4.5404	5 2	
	322 1	0.18159	0.0	7.38		0.4930		54.3	4.5404	5 2	
	323 1	0.35114	0.0	7.38		0.4930		49.9	4.7211	5 2	
	324 1	0.28392	0.0	7.38		0.4930		74.3	4.7211	5 2	
	325 1	0.34109	0.0	7.38		0.4930		40.1	4.7211	5 2	
	326 1	0.19186	0.0	7.38		0.4930		14.7	5.4159	5 2	
	327 1	0.30347	0.0	7.38		0.4930		28.9	5.4159	5 2	
	328 1	0.24103	0.0	7.38		0.4930		43.7	5.4159	5 2	
##	329 1	0.06617	0.0	3.24	0	0.4600	5.868	25.8	5.2146	4 4	30 16.9
##	330 1	0.06724	0.0	3.24	0	0.4600	6.333	17.2	5.2146	4 4	30 16.9
##	331 1	0.04544	0.0	3.24	0	0.4600	6.144	32.2	5.8736	4 4	30 16.9
##	332 1	0.05023	35.0	6.06	0	0.4379	5.706	28.4	6.6407	1 3	04 16.9
##	333 1	0.03466	35.0	6.06	0	0.4379	6.031	23.3	6.6407	1 3	04 16.9
##	334 1	0.05083	0.0	5.19	0	0.5150	6.316	38.1	6.4584	5 2	24 20.2
##	335 1	0.03738	0.0	5.19	0	0.5150	6.310	38.5	6.4584	5 2	24 20.2
##	336 1	0.03961	0.0	5.19	0	0.5150	6.037	34.5	5.9853	5 2	24 20.2
##	337 1	0.03427	0.0	5.19	0	0.5150	5.869	46.3	5.2311	5 2	24 20.2
##	338 1	0.03041	0.0	5.19	0	0.5150	5.895	59.6	5.6150	5 2	24 20.2
##	339 1	0.03306	0.0	5.19	0	0.5150	6.059	37.3	4.8122	5 2	24 20.2
##	340 1	0.05497	0.0	5.19	0	0.5150	5.985	45.4	4.8122	5 2	24 20.2
##	341 1	0.06151	0.0	5.19	0	0.5150	5.968	58.5	4.8122	5 2	24 20.2
##	342 1	0.01301	35.0	1.52	0	0.4420	7.241	49.3	7.0379	1 2	34 15.5
##	343 1	0.02498	0.0	1.89	0	0.5180	6.540	59.7	6.2669	1 4	
##	344 1	0.02543	55.0	3.78	0	0.4840	6.696	56.4	5.7321	5 3	
	345 1	0.03049	55.0	3.78		0.4840		28.1	6.4654	5 3	
	346 1	0.03113	0.0	4.39		0.4420		48.5	8.0136	3 3	
	347 1	0.06162	0.0	4.39		0.4420		52.3	8.0136	3 3	
	348 1	0.01870	85.0	4.15		0.4290		27.7	8.5353	4 3	
	349 1	0.01501	80.0	2.01		0.4350		29.7	8.3440	4 2	
	350 1	0.02899	40.0	1.25		0.4290		34.5	8.7921	1 3	
	351 1	0.06211	40.0	1.25		0.4290		44.4	8.7921	1 3	
	352 1	0.07950	60.0	1.69		0.4110			10.7103	4 4	
	353 1	0.07244	60.0	1.69		0.4110			10.7103	4 4	
	354 1	0.01709	90.0	2.02		0.4100			12.1265	5 1	
	355 1	0.04301	80.0	1.91		0.4130			10.5857	4 3	
	356 1	0.10659	80.0	1.91		0.4130			10.5857	4 3	
	357 1	8.98296		18.10		0.7700		97.4		24 6	
	358 1	3.84970		18.10		0.7700		91.0	2.5052	24 6	
	359 1	5.20177		18.10		0.7700		83.4		24 6	
	360 1	4.26131		18.10		0.7700		81.3		24 6	
	361 1	4.54192		18.10		0.7700		88.0	2.5182	24 6	
	362 1	3.83684		18.10		0.7700		91.1	2.2955	24 6	
	363 1	3.67822		18.10		0.7700		96.2	2.2955	24 6	
	364 1			18.10							
		4.22239				0.7700		89.0	1.9047	24 6	
	365 1	3.47428		18.10		0.7180		82.9	1.9047	24 6	
	366 1	4.55587		18.10		0.7180			1.6132	24 6	
	367 1	3.69695		18.10		0.7180			1.7523	24 6	
		13.52220		18.10		0.6310			1.5106	24 6	
##	369 1	4.89822	0.0	18.10	0	0.6310	4.970	100.0	1.3325	24 6	66 20.2

```
## 370 1 5.66998
                    0.0 18.10
                                  1 0.6310 6.683 96.8 1.3567
                                                                  24 666
                                                                            20.2
## 371 1 6.53876
                    0.0 18.10
                                  1 0.6310 7.016 97.5
                                                                  24 666
                                                                            20.2
                                                         1.2024
                                                         1.1691
## 372 1 9.23230
                    0.0 18.10
                                  0 0.6310 6.216 100.0
                                                                  24 666
                                                                            20.2
## 373 1 8.26725
                    0.0 18.10
                                  1 0.6680 5.875
                                                   89.6
                                                         1.1296
                                                                            20.2
                                                                  24 666
## 374 1 11.10810
                    0.0 18.10
                                  0 0.6680 4.906 100.0
                                                         1.1742
                                                                  24 666
                                                                            20.2
## 375 1 18.49820
                    0.0 18.10
                                                                  24 666
                                                                            20.2
                                  0 0.6680 4.138 100.0
                                                         1.1370
## 376 1 19.60910
                    0.0 18.10
                                  0 0.6710 7.313
                                                   97.9
                                                         1.3163
                                                                  24 666
                                                                            20.2
                    0.0 18.10
## 377 1 15.28800
                                  0 0.6710 6.649
                                                   93.3
                                                         1.3449
                                                                  24 666
                                                                            20.2
## 378 1 9.82349
                    0.0 18.10
                                  0 0.6710 6.794
                                                   98.8
                                                         1.3580
                                                                  24 666
                                                                            20.2
## 379 1 23.64820
                    0.0 18.10
                                  0 0.6710 6.380
                                                   96.2
                                                         1.3861
                                                                  24 666
                                                                            20.2
## 380 1 17.86670
                    0.0 18.10
                                  0 0.6710 6.223 100.0
                                                         1.3861
                                                                  24 666
                                                                            20.2
## 381 1 88.97620
                    0.0 18.10
                                                         1.4165
                                                                            20.2
                                  0 0.6710 6.968
                                                   91.9
                                                                  24
                                                                    666
## 382 1 15.87440
                    0.0 18.10
                                  0 0.6710 6.545
                                                   99.1
                                                         1.5192
                                                                  24 666
                                                                            20.2
## 383 1 9.18702
                    0.0 18.10
                                  0 0.7000 5.536 100.0
                                                         1.5804
                                                                  24 666
                                                                            20.2
## 384 1 7.99248
                    0.0 18.10
                                  0 0.7000 5.520 100.0
                                                         1.5331
                                                                            20.2
                                                                  24 666
## 385 1 20.08490
                    0.0 18.10
                                  0 0.7000 4.368
                                                   91.2
                                                         1.4395
                                                                  24 666
                                                                            20.2
## 386 1 16.81180
                    0.0 18.10
                                  0 0.7000 5.277
                                                   98.1
                                                         1.4261
                                                                  24 666
                                                                            20.2
  387 1 24.39380
                    0.0 18.10
                                  0 0.7000 4.652 100.0
                                                         1.4672
                                                                  24 666
                                                                            20.2
## 388 1 22.59710
                    0.0 18.10
                                  0 0.7000 5.000
                                                         1.5184
                                                   89.5
                                                                  24 666
                                                                            20.2
## 389 1 14.33370
                    0.0 18.10
                                  0 0.7000 4.880 100.0
                                                         1.5895
                                                                  24 666
                                                                            20.2
## 390 1 8.15174
                    0.0 18.10
                                  0 0.7000 5.390
                                                   98.9
                                                         1.7281
                                                                  24 666
                                                                            20.2
## 391 1 6.96215
                    0.0 18.10
                                  0 0.7000 5.713
                                                   97.0
                                                         1.9265
                                                                  24 666
                                                                            20.2
## 392 1 5.29305
                    0.0 18.10
                                  0 0.7000 6.051
                                                         2.1678
                                                                            20.2
                                                   82.5
                                                                  24 666
## 393 1 11.57790
                    0.0 18.10
                                  0 0.7000 5.036
                                                         1.7700
                                                   97.0
                                                                  24 666
                                                                            20.2
## 394 1 8.64476
                    0.0 18.10
                                  0 0.6930 6.193
                                                   92.6
                                                         1.7912
                                                                  24 666
                                                                            20.2
## 395 1 13.35980
                    0.0 18.10
                                  0 0.6930 5.887
                                                   94.7
                                                         1.7821
                                                                  24 666
                                                                            20.2
## 396 1 8.71675
                    0.0 18.10
                                  0 0.6930 6.471
                                                   98.8
                                                         1.7257
                                                                    666
                                                                            20.2
                                                                  24
                                                         1.6768
## 397 1 5.87205
                    0.0 18.10
                                  0 0.6930 6.405
                                                   96.0
                                                                  24 666
                                                                            20.2
## 398 1 7.67202
                    0.0 18.10
                                  0 0.6930 5.747
                                                   98.9
                                                         1.6334
                                                                  24 666
                                                                            20.2
## 399 1 38.35180
                    0.0 18.10
                                  0 0.6930 5.453 100.0
                                                         1.4896
                                                                  24 666
                                                                            20.2
## 400 1 9.91655
                    0.0 18.10
                                  0 0.6930 5.852
                                                   77.8
                                                         1.5004
                                                                  24 666
                                                                            20.2
## 401 1 25.04610
                    0.0 18.10
                                  0 0.6930 5.987 100.0
                                                         1.5888
                                                                  24 666
                                                                            20.2
## 402 1 14.23620
                    0.0 18.10
                                  0 0.6930 6.343 100.0
                                                         1.5741
                                                                  24 666
                                                                            20.2
                    0.0 18.10
                                  0 0.6930 6.404 100.0
                                                         1.6390
## 403 1 9.59571
                                                                  24 666
                                                                            20.2
## 404 1 24.80170
                    0.0 18.10
                                  0 0.6930 5.349
                                                   96.0
                                                         1.7028
                                                                  24
                                                                     666
                                                                            20.2
## 405 1 41.52920
                    0.0 18.10
                                  0 0.6930 5.531
                                                   85.4
                                                         1.6074
                                                                  24 666
                                                                            20.2
## 406 1 67.92080
                    0.0 18.10
                                  0 0.6930 5.683 100.0
                                                         1.4254
                                                                  24 666
                                                                            20.2
## 407 1 20.71620
                    0.0 18.10
                                  0 0.6590 4.138 100.0
                                                         1.1781
                                                                            20.2
                                                                  24 666
## 408 1 11.95110
                    0.0 18.10
                                  0 0.6590 5.608 100.0
                                                         1.2852
                                                                  24 666
                                                                            20.2
## 409 1 7.40389
                    0.0 18.10
                                  0 0.5970 5.617 97.9
                                                                  24 666
                                                                            20.2
                                                         1.4547
## 410 1 14.43830
                    0.0 18.10
                                  0 0.5970 6.852 100.0
                                                         1.4655
                                                                  24 666
                                                                            20.2
## 411 1 51.13580
                    0.0 18.10
                                  0 0.5970 5.757 100.0
                                                         1.4130
                                                                  24 666
                                                                            20.2
## 412 1 14.05070
                    0.0 18.10
                                  0 0.5970 6.657 100.0
                                                         1.5275
                                                                  24 666
                                                                            20.2
## 413 1 18.81100
                    0.0 18.10
                                  0 0.5970 4.628 100.0
                                                         1.5539
                                                                  24 666
                                                                            20.2
## 414 1 28.65580
                    0.0 18.10
                                  0 0.5970 5.155 100.0
                                                         1.5894
                                                                  24 666
                                                                            20.2
## 415 1 45.74610
                    0.0 18.10
                                  0 0.6930 4.519 100.0
                                                         1.6582
                                                                  24 666
                                                                            20.2
## 416 1 18.08460
                    0.0 18.10
                                  0 0.6790 6.434 100.0
                                                         1.8347
                                                                  24 666
                                                                            20.2
                                  0 0.6790 6.782
## 417 1 10.83420
                    0.0 18.10
                                                   90.8
                                                         1.8195
                                                                  24 666
                                                                            20.2
## 418 1 25.94060
                    0.0 18.10
                                  0 0.6790 5.304
                                                   89.1
                                                         1.6475
                                                                  24 666
                                                                            20.2
## 419 1 73.53410
                    0.0 18.10
                                  0 0.6790 5.957 100.0
                                                         1.8026
                                                                  24 666
                                                                            20.2
## 420 1 11.81230
                    0.0 18.10
                                  0 0.7180 6.824
                                                   76.5
                                                         1.7940
                                                                  24 666
                                                                            20.2
## 421 1 11.08740
                    0.0 18.10
                                  0 0.7180 6.411 100.0
                                                         1.8589
                                                                  24 666
                                                                            20.2
## 422 1 7.02259
                    0.0 18.10
                                  0 0.7180 6.006
                                                   95.3
                                                         1.8746
                                                                  24 666
                                                                            20.2
## 423 1 12.04820
                    0.0 18.10
                                  0 0.6140 5.648 87.6 1.9512
                                                                  24 666
                                                                            20.2
```

```
## 424 1 7.05042
                     0.0 18.10
                                   0 0.6140 6.103
                                                   85.1 2.0218
                                                                  24 666
                                                                             20.2
                                  0 0.5840 5.565
## 425 1 8.79212
                     0.0 18.10
                                                                             20.2
                                                   70.6
                                                         2.0635
                                                                  24 666
                                   0 0.6790 5.896
                                                                  24 666
## 426 1 15.86030
                     0.0 18.10
                                                   95.4
                                                          1.9096
                                                                             20.2
## 427 1 12.24720
                     0.0 18.10
                                   0 0.5840 5.837
                                                   59.7
                                                          1.9976
                                                                             20.2
                                                                  24 666
## 428 1 37.66190
                     0.0 18.10
                                   0 0.6790 6.202
                                                   78.7
                                                          1.8629
                                                                  24 666
                                                                             20.2
## 429 1 7.36711
                     0.0 18.10
                                   0 0.6790 6.193
                                                   78.1
                                                          1.9356
                                                                  24 666
                                                                             20.2
## 430 1 9.33889
                     0.0 18.10
                                   0 0.6790 6.380
                                                   95.6
                                                          1.9682
                                                                  24 666
                                                                             20.2
                     0.0 18.10
## 431 1 8.49213
                                   0 0.5840 6.348
                                                   86.1
                                                          2.0527
                                                                  24 666
                                                                             20.2
## 432 1 10.06230
                     0.0 18.10
                                   0 0.5840 6.833
                                                   94.3
                                                          2.0882
                                                                  24 666
                                                                             20.2
## 433 1 6.44405
                     0.0 18.10
                                   0 0.5840 6.425
                                                   74.8
                                                          2.2004
                                                                  24 666
                                                                             20.2
## 434 1 5.58107
                     0.0 18.10
                                   0 0.7130 6.436
                                                   87.9
                                                          2.3158
                                                                  24 666
                                                                             20.2
## 435 1 13.91340
                     0.0 18.10
                                   0 0.7130 6.208
                                                   95.0
                                                          2.2222
                                                                             20.2
                                                                  24
                                                                     666
## 436 1 11.16040
                     0.0 18.10
                                   0 0.7400 6.629
                                                   94.6
                                                          2.1247
                                                                  24
                                                                     666
                                                                             20.2
                                   0 0.7400 6.461
                                                   93.3
## 437 1 14.42080
                     0.0 18.10
                                                          2.0026
                                                                  24
                                                                     666
                                                                             20.2
## 438 1 15.17720
                     0.0 18.10
                                   0 0.7400 6.152 100.0
                                                          1.9142
                                                                  24
                                                                             20.2
                                                                     666
## 439 1 13.67810
                     0.0 18.10
                                   0 0.7400 5.935
                                                   87.9
                                                          1.8206
                                                                  24
                                                                     666
                                                                             20.2
## 440 1 9.39063
                     0.0 18.10
                                   0 0.7400 5.627
                                                   93.9
                                                          1.8172
                                                                  24 666
                                                                             20.2
## 441 1 22.05110
                     0.0 18.10
                                   0 0.7400 5.818
                                                   92.4
                                                          1.8662
                                                                  24 666
                                                                             20.2
## 442 1 9.72418
                     0.0 18.10
                                   0 0.7400 6.406
                                                   97.2
                                                          2.0651
                                                                  24 666
                                                                             20.2
## 443 1 5.66637
                     0.0 18.10
                                   0 0.7400 6.219 100.0
                                                          2.0048
                                                                  24 666
                                                                             20.2
## 444 1 9.96654
                     0.0 18.10
                                   0 0.7400 6.485 100.0
                                                          1.9784
                                                                  24 666
                                                                             20.2
## 445 1 12.80230
                     0.0 18.10
                                   0 0.7400 5.854
                                                   96.6
                                                          1.8956
                                                                  24 666
                                                                             20.2
## 446 1 10.67180
                     0.0 18.10
                                   0 0.7400 6.459
                                                                             20.2
                                                   94.8
                                                          1.9879
                                                                  24 666
         6.28807
                     0.0 18.10
                                   0 0.7400 6.341
                                                   96.4
                                                          2.0720
## 447 1
                                                                  24 666
                                                                             20.2
## 448 1
         9.92485
                     0.0 18.10
                                   0 0.7400 6.251
                                                   96.6
                                                          2.1980
                                                                  24 666
                                                                             20.2
## 449 1
          9.32909
                     0.0 18.10
                                   0 0.7130 6.185
                                                   98.7
                                                          2.2616
                                                                  24 666
                                                                             20.2
## 450 1
          7.52601
                     0.0 18.10
                                   0 0.7130 6.417
                                                   98.3
                                                          2.1850
                                                                     666
                                                                             20.2
                                                                  24
                                   0 0.7130 6.749
                                                          2.3236
## 451 1
          6.71772
                     0.0 18.10
                                                   92.6
                                                                  24 666
                                                                             20.2
## 452 1
                     0.0 18.10
                                   0 0.7130 6.655
                                                   98.2
                                                          2.3552
                                                                  24 666
                                                                             20.2
          5.44114
## 453 1
          5.09017
                     0.0 18.10
                                   0 0.7130 6.297
                                                   91.8
                                                          2.3682
                                                                  24 666
                                                                             20.2
## 454 1
          8.24809
                     0.0 18.10
                                   0 0.7130 7.393
                                                   99.3
                                                          2.4527
                                                                  24 666
                                                                             20.2
## 455 1
          9.51363
                     0.0 18.10
                                   0 0.7130 6.728
                                                   94.1
                                                          2.4961
                                                                  24 666
                                                                             20.2
## 456 1
          4.75237
                     0.0 18.10
                                   0 0.7130 6.525
                                                   86.5
                                                          2.4358
                                                                  24 666
                                                                             20.2
## 457 1
          4.66883
                     0.0 18.10
                                   0 0.7130 5.976
                                                   87.9
                                                          2.5806
                                                                  24
                                                                     666
                                                                             20.2
## 458 1
          8.20058
                     0.0 18.10
                                   0 0.7130 5.936
                                                   80.3
                                                          2.7792
                                                                  24
                                                                     666
                                                                             20.2
                     0.0 18.10
                                  0 0.7130 6.301
                                                   83.7
                                                          2.7831
                                                                             20.2
## 459 1
          7.75223
                                                                  24 666
## 460 1
          6.80117
                     0.0 18.10
                                   0 0.7130 6.081
                                                   84.4
                                                          2.7175
                                                                  24 666
                                                                             20.2
## 461 1
          4.81213
                     0.0 18.10
                                   0 0.7130 6.701
                                                   90.0
                                                          2.5975
                                                                  24 666
                                                                             20.2
## 462 1
          3.69311
                     0.0 18.10
                                   0 0.7130 6.376
                                                   88.4
                                                          2.5671
                                                                  24 666
                                                                             20.2
         6.65492
                     0.0 18.10
                                   0 0.7130 6.317
                                                   83.0
                                                          2.7344
                                                                  24 666
                                                                             20.2
## 463 1
          5.82115
                     0.0 18.10
                                   0 0.7130 6.513
                                                          2.8016
## 464 1
                                                   89.9
                                                                  24 666
                                                                             20.2
## 465 1
          7.83932
                     0.0 18.10
                                   0 0.6550 6.209
                                                   65.4
                                                          2.9634
                                                                  24 666
                                                                             20.2
                                                          3.0665
## 466 1
          3.16360
                     0.0 18.10
                                   0 0.6550 5.759
                                                   48.2
                                                                  24 666
                                                                             20.2
## 467 1
          3.77498
                     0.0 18.10
                                   0 0.6550 5.952
                                                   84.7
                                                          2.8715
                                                                  24
                                                                     666
                                                                             20.2
## 468 1
         4.42228
                     0.0 18.10
                                   0 0.5840 6.003
                                                   94.5
                                                          2.5403
                                                                  24 666
                                                                             20.2
## 469 1 15.57570
                     0.0 18.10
                                   0 0.5800 5.926
                                                          2.9084
                                                                     666
                                                                             20.2
                                                   71.0
                                                                  24
## 470 1 13.07510
                     0.0 18.10
                                   0 0.5800 5.713
                                                   56.7
                                                          2.8237
                                                                  24 666
                                                                             20.2
                                                          3.0334
## 471 1
         4.34879
                     0.0 18.10
                                   0 0.5800 6.167
                                                   84.0
                                                                  24 666
                                                                             20.2
## 472 1
          4.03841
                     0.0 18.10
                                   0 0.5320 6.229
                                                   90.7
                                                          3.0993
                                                                  24 666
                                                                             20.2
## 473 1
          3.56868
                     0.0 18.10
                                   0 0.5800 6.437
                                                   75.0
                                                          2.8965
                                                                  24
                                                                     666
                                                                             20.2
## 474 1
          4.64689
                     0.0 18.10
                                   0 0.6140 6.980
                                                   67.6
                                                                             20.2
                                                          2.5329
                                                                  24 666
## 475 1
          8.05579
                     0.0 18.10
                                   0 0.5840 5.427
                                                   95.4
                                                          2.4298
                                                                  24 666
                                                                             20.2
## 476 1
          6.39312
                     0.0 18.10
                                  0 0.5840 6.162
                                                   97.4
                                                          2.2060
                                                                  24 666
                                                                             20.2
## 477 1 4.87141
                     0.0 18.10
                                  0 0.6140 6.484
                                                   93.6 2.3053
                                                                  24 666
                                                                             20.2
```

```
## 478 1 15.02340
                    0.0 18.10
                                  0 0.6140 5.304 97.3 2.1007
                                                                 24 666
                                                                           20.2
                                  0 0.6140 6.185
                                                  96.7
## 479 1 10.23300
                    0.0 18.10
                                                        2.1705
                                                                 24 666
                                                                           20.2
## 480 1 14.33370
                                                                 24 666
                    0.0 18.10
                                  0 0.6140 6.229
                                                  88.0
                                                        1.9512
                                                                           20.2
                    0.0 18.10
                                  0 0.5320 6.242
                                                        3.4242
## 481 1 5.82401
                                                  64.7
                                                                 24 666
                                                                           20.2
## 482 1 5.70818
                    0.0 18.10
                                  0 0.5320 6.750
                                                  74.9
                                                        3.3317
                                                                 24 666
                                                                           20.2
## 483 1 5.73116
                    0.0 18.10
                                  0 0.5320 7.061
                                                  77.0
                                                        3.4106
                                                                 24 666
                                                                           20.2
## 484 1 2.81838
                    0.0 18.10
                                  0 0.5320 5.762
                                                  40.3
                                                        4.0983
                                                                 24 666
                                                                           20.2
## 485 1 2.37857
                    0.0 18.10
                                  0 0.5830 5.871
                                                  41.9
                                                                           20.2
                                                        3.7240
                                                                 24 666
                                  0 0.5830 6.312
## 486 1 3.67367
                    0.0 18.10
                                                  51.9
                                                        3.9917
                                                                 24 666
                                                                           20.2
                    0.0 18.10
                                  0 0.5830 6.114
                                                                           20.2
## 487 1
         5.69175
                                                  79.8
                                                        3.5459
                                                                 24 666
                                                                           20.2
## 488 1
         4.83567
                    0.0 18.10
                                  0 0.5830 5.905
                                                  53.2
                                                        3.1523
                                                                 24 666
                    0.0 27.74
                                  0 0.6090 5.454
                                                        1.8209
## 489 1 0.15086
                                                  92.7
                                                                  4 711
                                                                           20.1
                    0.0 27.74
## 490 1 0.18337
                                  0 0.6090 5.414
                                                  98.3
                                                        1.7554
                                                                  4 711
                                                                           20.1
## 491 1
         0.20746
                    0.0 27.74
                                  0 0.6090 5.093
                                                  98.0
                                                        1.8226
                                                                  4 711
                                                                           20.1
## 492 1
         0.10574
                    0.0 27.74
                                  0 0.6090 5.983
                                                  98.8
                                                        1.8681
                                                                           20.1
                                                                  4 711
## 493 1
         0.11132
                    0.0 27.74
                                  0 0.6090 5.983
                                                  83.5
                                                        2.1099
                                                                  4 711
                                                                           20.1
## 494 1 0.17331
                    0.0 9.69
                                  0 0.5850 5.707
                                                        2.3817
                                                                           19.2
                                                  54.0
                                                                  6 391
                                  0 0.5850 5.926
## 495 1
         0.27957
                    0.0 9.69
                                                  42.6
                                                        2.3817
                                                                  6 391
                                                                           19.2
                                                  28.8
## 496 1 0.17899
                    0.0 9.69
                                  0 0.5850 5.670
                                                        2.7986
                                                                           19.2
                                                                  6 391
## 497 1 0.28960
                    0.0 9.69
                                  0 0.5850 5.390
                                                  72.9
                                                        2.7986
                                                                  6 391
                                                                           19.2
                                                  70.6
                                                                           19.2
## 498 1 0.26838
                    0.0 9.69
                                  0 0.5850 5.794
                                                        2.8927
                                                                  6 391
## 499 1 0.23912
                    0.0 9.69
                                  0 0.5850 6.019
                                                  65.3
                                                        2.4091
                                                                  6 391
                                                                           19.2
                    0.0 9.69
## 500 1 0.17783
                                  0 0.5850 5.569
                                                  73.5
                                                        2.3999
                                                                           19.2
                                                                  6 391
## 501 1 0.22438
                    0.0 9.69
                                  0 0.5850 6.027
                                                        2.4982
                                                                  6 391
                                                                           19.2
                                                  79.7
## 502 1 0.06263
                    0.0 11.93
                                  0 0.5730 6.593
                                                        2.4786
                                                                           21.0
                                                  69.1
                                                                  1 273
## 503 1 0.04527
                    0.0 11.93
                                  0 0.5730 6.120
                                                  76.7
                                                        2.2875
                                                                  1 273
                                                                           21.0
## 504 1 0.06076
                    0.0 11.93
                                  0 0.5730 6.976
                                                  91.0
                                                        2.1675
                                                                  1 273
                                                                           21.0
## 505 1 0.10959
                    0.0 11.93
                                  0 0.5730 6.794
                                                        2.3889
                                                  89.3
                                                                  1 273
                                                                           21.0
                    0.0 11.93
                                  0 0.5730 6.030
## 506 1 0.04741
                                                  80.8 2.5050
                                                                  1 273
                                                                           21.0
##
        black 1stat
## 1
       396.90
               4.98
## 2
       396.90 9.14
## 3
       392.83
               4.03
## 4
       394.63 2.94
## 5
       396.90
              5.33
## 6
       394.12 5.21
## 7
       395.60 12.43
## 8
       396.90 19.15
## 9
       386.63 29.93
## 10
       386.71 17.10
       392.52 20.45
## 11
## 12
       396.90 13.27
       390.50 15.71
## 13
## 14
       396.90 8.26
       380.02 10.26
## 15
       395.62 8.47
## 16
## 17
       386.85 6.58
       386.75 14.67
## 18
## 19
       288.99 11.69
## 20
       390.95 11.28
## 21
       376.57 21.02
## 22
       392.53 13.83
## 23
       396.90 18.72
## 24 394.54 19.88
```

```
## 25
       394.33 16.30
## 26
       303.42 16.51
       376.88 14.81
## 27
       306.38 17.28
## 28
## 29
       387.94 12.80
## 30
       380.23 11.98
## 31
       360.17 22.60
       376.73 13.04
## 32
## 33
       232.60 27.71
## 34
       358.77 18.35
## 35
       248.31 20.34
## 36
       396.90 9.68
       377.56 11.41
## 37
## 38
       396.90 8.77
## 39
       393.43 10.13
## 40
       395.63
               4.32
## 41
       395.62
               1.98
## 42
       385.41
               4.84
## 43
       383.37
               5.81
## 44
       394.46
               7.44
       389.39 9.55
## 45
## 46
       396.90 10.21
       396.90 14.15
## 47
## 48
       392.74 18.80
## 49
       396.90 30.81
## 50
       396.90 16.20
## 51
       395.56 13.45
## 52
       393.97
               9.43
       396.90
               5.28
## 53
## 54
       396.90
               8.43
## 55
       396.90 14.80
## 56
       395.93
               4.81
## 57
       396.90
               5.77
## 58
       392.90
               3.95
## 59
       390.68
               6.86
## 60
       396.90 9.22
## 61
       395.11 13.15
## 62
       378.08 14.44
## 63
       396.90
               6.73
       395.58 9.50
## 64
## 65
       393.24 8.05
## 66
       396.90 4.67
## 67
       396.90 10.24
## 68
       396.21 8.10
## 69
       396.90 13.09
## 70
       396.90
               8.79
## 71
               6.72
       383.73
## 72
       376.94
               9.88
## 73
       390.91
               5.52
               7.54
## 74
       377.17
## 75
       394.92
               6.78
       383.23 8.94
## 76
## 77
       373.66 11.97
## 78 386.96 10.27
```

```
## 79
       386.40 12.34
## 80
       396.06 9.10
       396.90 5.29
## 81
## 82
       395.63 7.22
## 83
       396.90
               6.72
## 84
       390.64 7.51
## 85
       396.90 9.62
## 86
       392.30 6.53
## 87
       395.99 12.86
## 88
       395.15 8.44
              5.50
## 89
       396.90
## 90
       396.06
              5.70
## 91
       392.18
              8.81
## 92
       393.55
              8.20
## 93
       395.01
              8.16
## 94
       396.33
              6.21
## 95
       396.90 10.59
## 96
      357.98 6.65
## 97
      391.83 11.34
## 98
       396.90 4.21
## 99 393.53 3.57
## 100 396.90 6.19
## 101 394.76 9.42
## 102 395.58 7.67
## 103 70.80 10.63
## 104 394.47 13.44
## 105 392.69 12.33
## 106 394.05 16.47
## 107 395.67 18.66
## 108 387.69 14.09
## 109 395.24 12.27
## 110 391.23 15.55
## 111 393.49 13.00
## 112 395.59 10.16
## 113 394.95 16.21
## 114 396.90 17.09
## 115 388.74 10.45
## 116 344.91 15.76
## 117 393.30 12.04
## 118 394.51 10.30
## 119 338.63 15.37
## 120 391.50 13.61
## 121 389.15 14.37
## 122 377.67 14.27
## 123 378.09 17.93
## 124 370.31 25.41
## 125 379.38 17.58
## 126 385.02 14.81
## 127 359.29 27.26
## 128 392.11 17.19
## 129 396.90 15.39
## 130 396.90 18.34
## 131 395.04 12.60
## 132 396.90 12.26
```

```
## 133 385.76 11.12
## 134 388.69 15.03
## 135 262.76 17.31
## 136 394.67 16.96
## 137 378.25 16.90
## 138 394.08 14.59
## 139 392.04 21.32
## 140 396.90 18.46
## 141 388.08 24.16
## 142 396.90 34.41
## 143 396.90 26.82
## 144 396.90 26.42
## 145 396.90 29.29
## 146 172.91 27.80
## 147 169.27 16.65
## 148 391.71 29.53
## 149 356.99 28.32
## 150 351.85 21.45
## 151 372.80 14.10
## 152 341.60 13.28
## 153 343.28 12.12
## 154 261.95 15.79
## 155 321.02 15.12
## 156 88.01 15.02
## 157 88.63 16.14
## 158 363.43 4.59
## 159 353.89 6.43
## 160 364.31 7.39
## 161 338.92 5.50
## 162 374.43 1.73
## 163 389.61 1.92
## 164 388.45 3.32
## 165 395.11 11.64
## 166 240.16 9.81
## 167 369.30 3.70
## 168 227.61 12.14
## 169 297.09 11.10
## 170 330.04 11.32
## 171 292.29 14.43
## 172 348.13 12.03
## 173 396.90 14.69
## 174 395.50 9.04
## 175 393.23 9.64
## 176 390.96 5.33
## 177 393.23 10.11
## 178 395.60 6.29
## 179 391.27 6.92
## 180 396.90 5.04
## 181 395.56 7.56
## 182 396.90 9.45
## 183 394.12 4.82
## 184 396.90 5.68
## 185 391.00 13.98
## 186 387.11 13.15
```

```
## 187 392.63 4.45
## 188 393.87 6.68
## 189 382.84 4.56
## 190 396.90
              5.39
## 191 377.68
              5.10
## 192 389.71
              4.69
## 193 390.49
              2.87
## 194 393.37
              5.03
## 195 376.70
              4.38
## 196 394.23
              2.97
## 197 396.90
              4.08
## 198 354.31
              8.61
## 199 392.20
              6.62
## 200 396.90
              4.56
## 201 384.30 4.45
## 202 393.77
              7.43
## 203 395.38 3.11
## 204 392.78 3.81
## 205 390.55 2.88
## 206 396.90 10.87
## 207 394.87 10.97
## 208 389.43 18.06
## 209 381.32 14.66
## 210 396.90 23.09
## 211 393.25 17.27
## 212 395.24 23.98
## 213 390.94 16.03
## 214 385.81 9.38
## 215 348.93 29.55
## 216 393.63 9.47
## 217 392.80 13.51
## 218 392.78 9.69
## 219 396.90 17.92
## 220 393.74 10.50
## 221 391.70 9.71
## 222 395.24 21.46
## 223 390.39 9.93
## 224 396.90 7.60
## 225 385.05
              4.14
## 226 382.00 4.63
## 227 387.38 3.13
## 228 372.08 6.36
## 229 377.51
              3.92
## 230 380.34 3.76
## 231 378.35 11.65
## 232 376.14 5.25
## 233 385.91
              2.47
## 234 378.95 3.95
## 235 360.20 8.05
## 236 376.75 10.88
## 237 388.45 9.54
## 238 390.07 4.73
## 239 379.41 6.36
## 240 383.78 7.37
```

```
## 241 391.25 11.38
## 242 394.62 12.40
## 243 372.75 11.22
## 244 374.71 5.19
## 245 372.49 12.50
## 246 389.13 18.46
## 247 390.18 9.16
## 248 376.14 10.15
## 249 374.71 9.52
## 250 393.74 6.56
## 251 396.28
              5.90
## 252 377.07
              3.59
## 253 386.09
              3.53
## 254 396.90
              3.54
## 255 392.89
              6.57
## 256 395.18
              9.25
## 257 386.34
              3.11
## 258 389.70
## 259 383.29 7.79
## 260 391.93
## 261 392.80 9.59
## 262 388.37 7.26
## 263 386.86 5.91
## 264 393.42 11.25
## 265 387.89 8.10
## 266 392.40 10.45
## 267 384.07 14.79
## 268 384.54 7.44
## 269 390.30 3.16
## 270 391.34 13.65
## 271 388.65 13.00
## 272 396.90 6.59
## 273 394.96
              7.73
## 274 390.77
              6.58
## 275 396.90
              3.53
## 276 396.90
              2.98
## 277 389.25
              6.05
## 278 393.45 4.16
## 279 396.90
              7.19
## 280 396.90 4.85
## 281 387.31 3.76
## 282 392.23 4.59
## 283 377.07
              3.01
## 284 395.52 3.16
## 285 394.72 7.85
## 286 394.72 8.23
## 287 341.60 12.93
## 288 396.90 7.14
## 289 396.90
              7.60
## 290 371.72
              9.51
## 291 396.90
              3.33
## 292 396.90
              3.56
## 293 396.90 4.70
## 294 396.90 8.58
```

```
## 295 396.90 10.40
## 296 396.90 6.27
## 297 392.85 7.39
## 298 396.90 15.84
## 299 368.24 4.97
## 300 371.58
             4.74
## 301 390.86 6.07
## 302 395.75
              9.50
## 303 383.61
              8.67
## 304 390.43
              4.86
## 305 393.68 6.93
## 306 393.36 8.93
## 307 396.90 6.47
## 308 396.90 7.53
## 309 396.90 4.54
## 310 396.24 9.97
## 311 350.45 12.64
## 312 396.90 5.98
## 313 396.30 11.72
## 314 393.39 7.90
## 315 395.69 9.28
## 316 396.42 11.50
## 317 390.70 18.33
## 318 396.90 15.94
## 319 395.21 10.36
## 320 396.23 12.73
## 321 396.90 7.20
## 322 396.90 6.87
## 323 396.90 7.70
## 324 391.13 11.74
## 325 396.90 6.12
## 326 393.68 5.08
## 327 396.90 6.15
## 328 396.90 12.79
## 329 382.44 9.97
## 330 375.21 7.34
## 331 368.57 9.09
## 332 394.02 12.43
## 333 362.25 7.83
## 334 389.71 5.68
## 335 389.40
## 336 396.90 8.01
## 337 396.90 9.80
## 338 394.81 10.56
## 339 396.14 8.51
## 340 396.90
              9.74
## 341 396.90 9.29
## 342 394.74 5.49
## 343 389.96 8.65
## 344 396.90 7.18
## 345 387.97 4.61
## 346 385.64 10.53
## 347 364.61 12.67
## 348 392.43 6.36
```

```
## 349 390.94 5.99
## 350 389.85 5.89
## 351 396.90 5.98
## 352 370.78 5.49
## 353 392.33
              7.79
## 354 384.46 4.50
## 355 382.80 8.05
## 356 376.04 5.57
## 357 377.73 17.60
## 358 391.34 13.27
## 359 395.43 11.48
## 360 390.74 12.67
## 361 374.56 7.79
## 362 350.65 14.19
## 363 380.79 10.19
## 364 353.04 14.64
## 365 354.55 5.29
## 366 354.70 7.12
## 367 316.03 14.00
## 368 131.42 13.33
## 369 375.52 3.26
## 370 375.33 3.73
## 371 392.05 2.96
## 372 366.15
               9.53
## 373 347.88 8.88
## 374 396.90 34.77
## 375 396.90 37.97
## 376 396.90 13.44
## 377 363.02 23.24
## 378 396.90 21.24
## 379 396.90 23.69
## 380 393.74 21.78
## 381 396.90 17.21
## 382 396.90 21.08
## 383 396.90 23.60
## 384 396.90 24.56
## 385 285.83 30.63
## 386 396.90 30.81
## 387 396.90 28.28
## 388 396.90 31.99
## 389 372.92 30.62
## 390 396.90 20.85
## 391 394.43 17.11
## 392 378.38 18.76
## 393 396.90 25.68
## 394 396.90 15.17
## 395 396.90 16.35
## 396 391.98 17.12
## 397 396.90 19.37
## 398 393.10 19.92
## 399 396.90 30.59
## 400 338.16 29.97
## 401 396.90 26.77
## 402 396.90 20.32
```

```
## 403 376.11 20.31
## 404 396.90 19.77
## 405 329.46 27.38
## 406 384.97 22.98
## 407 370.22 23.34
## 408 332.09 12.13
## 409 314.64 26.40
## 410 179.36 19.78
## 411
         2.60 10.11
## 412 35.05 21.22
## 413 28.79 34.37
## 414 210.97 20.08
## 415 88.27 36.98
## 416 27.25 29.05
## 417 21.57 25.79
## 418 127.36 26.64
## 419 16.45 20.62
## 420 48.45 22.74
## 421 318.75 15.02
## 422 319.98 15.70
## 423 291.55 14.10
## 424
        2.52 23.29
## 425
         3.65 17.16
## 426
        7.68 24.39
## 427
        24.65 15.69
## 428
       18.82 14.52
## 429
        96.73 21.52
## 430
        60.72 24.08
## 431
        83.45 17.64
        81.33 19.69
## 432
## 433 97.95 12.03
## 434 100.19 16.22
## 435 100.63 15.17
## 436 109.85 23.27
## 437
       27.49 18.05
## 438
        9.32 26.45
## 439 68.95 34.02
## 440 396.90 22.88
## 441 391.45 22.11
## 442 385.96 19.52
## 443 395.69 16.59
## 444 386.73 18.85
## 445 240.52 23.79
## 446 43.06 23.98
## 447 318.01 17.79
## 448 388.52 16.44
## 449 396.90 18.13
## 450 304.21 19.31
## 451
        0.32 17.44
## 452 355.29 17.73
## 453 385.09 17.27
## 454 375.87 16.74
## 455
         6.68 18.71
## 456 50.92 18.13
```

```
## 457
        10.48 19.01
         3.50 16.94
## 458
## 459 272.21 16.23
## 460 396.90 14.70
## 461 255.23 16.42
## 462 391.43 14.65
## 463 396.90 13.99
## 464 393.82 10.29
## 465 396.90 13.22
## 466 334.40 14.13
## 467
        22.01 17.15
## 468 331.29 21.32
## 469 368.74 18.13
## 470 396.90 14.76
## 471 396.90 16.29
## 472 395.33 12.87
## 473 393.37 14.36
## 474 374.68 11.66
## 475 352.58 18.14
## 476 302.76 24.10
## 477 396.21 18.68
## 478 349.48 24.91
## 479 379.70 18.03
## 480 383.32 13.11
## 481 396.90 10.74
## 482 393.07
               7.74
## 483 395.28
               7.01
## 484 392.92 10.42
## 485 370.73 13.34
## 486 388.62 10.58
## 487 392.68 14.98
## 488 388.22 11.45
## 489 395.09 18.06
## 490 344.05 23.97
## 491 318.43 29.68
## 492 390.11 18.07
## 493 396.90 13.35
## 494 396.90 12.01
## 495 396.90 13.59
## 496 393.29 17.60
## 497 396.90 21.14
## 498 396.90 14.10
## 499 396.90 12.92
## 500 395.77 15.10
## 501 396.90 14.33
## 502 391.99
               9.67
## 503 396.90
               9.08
## 504 396.90
               5.64
## 505 393.45
               6.48
## 506 396.90
               7.88
colnames(X)[1] = "Intercept"
```

Run the OLS linear model to get b, the vector of coefficients. Do not use lm.

```
#bvector = (Xtranspose * X)inverseXtranspose * yvector
b = solve(t(X) %*% X ) %*% t(X) %*% y

Find the hat matrix for this regression H and find its rank. Is this rank expected?

We expect it to be 14 because H is a projection on to Y in the X col space.

H = X %*% solve(t(X) %*% X) %*% t(X)

dim(H)

## [1] 506 506

pacman :: p_load(Matrix)

rankMatrix(H)
```

```
## [1] 14
## attr(,"method")
## [1] "tolNorm2"
## attr(,"useGrad")
## [1] FALSE
## attr(,"tol")
## [1] 1.123546e-13
```

Verify this is a projection matrix by verifying the two sufficient conditions. Use the testthat library's expect_equal(matrix1, matrix2, tolerance = 1e-2).

```
pacman ::p_load(testthat)
expect_equal(H, t(H), tolerance = 1e-2)
expect_equal(H %*% H, H, tolerance = 1e-2)
```

Find the matrix that projects onto the space of residuals H_comp and find its rank. Is this rank expected?

```
I = diag(nrow(H))
H_comp = (I - H)
rankMatrix(H_comp)#numerical error
```

```
## [1] 497
## attr(,"method")
## [1] "tolNorm2"
## attr(,"useGrad")
## [1] FALSE
## attr(,"tol")
## [1] 1.123546e-13
```

Verify this is a projection matrix by verifying the two sufficient conditions. Use the testthat library.

```
expect_equal(H_comp, t(H_comp), tolerance = 1e-2)
expect_equal(H_comp %*% H_comp, H_comp, tolerance = 1e-2)
```

Calculate \hat{y} .

```
yhat = H %*% y
head(yhat)
```

```
## [,1]
## 1 30.00384
## 2 25.02556
## 3 30.56760
## 4 28.60704
## 5 27.94352
```

```
## 6 25.25628
```

Calculate e as the difference of y and \hat{y} and the projection onto the space of the residuals. Verify the two means of calculating the residuals provide the same results.

```
e_2 = H_comp %*% y # projecting y on to the space of residuals orthogonal to col space of X
expect_equal(e, e_2)
Calculate R^2 and RMSE.
#1 - SSE / SST
sse = sum(e^2)
sst = sum((y - mean(y))^2)
rsquared = 1 - sse / sst
rsquared
## [1] 0.7406427
mse = sse / nrow(X) - ncol(X)
rmse = sqrt(mse) #rmse is standard deviation of errors
rmse #std deviation of errors on 95%
## [1] 2.809774
Verify \hat{y} and e are orthogonal.
t(e) %*% yhat #= numerically 0; its an orthogonal projection is forced to make a right angle
##
                  [,1]
## [1,] -4.991142e-08
Verify \hat{y} - \bar{y} and e are orthogonal.
t(e) %*% (yhat - mean(y)) # project y - ybar got back yhat - ybar
##
## [1,] 2.832162e-09
Find the cosine-squared of y - \bar{y} and \hat{y} - \bar{y} and verify it is the same as R^2.
#theta
y_{minus_y_bar} = y - mean(y)
yhat_minus_y_bar = yhat - mean(y)
length_y_minus_y_bar = sqrt ( sum( y_minus_y_bar^2))
length_yhat_minus_y_bar = sqrt( sum( yhat_minus_y_bar^2))
theta = acos(( t(y_minus_y_bar) %*% yhat_minus_y_bar) / (length_y_minus_y_bar * length_yhat_minus_y_bar
theta * (180 / pi)
             [,1]
## [1,] 30.61531
cos_theta_squared = cos(theta)^2
cos_theta_squared
##
              [,1]
## [1,] 0.7406427
```

Verify the sum of squares identity which we learned was due to the Pythagorean Theorem (applies since the projection is specifically orthogonal).

```
length_y_minus_y_bar^2 - length_yhat_minus_y_bar^2 - sse
```

[1] 5.666152e-09

Create a matrix that is $(p+1) \times (p+1)$ full of NA's. Label the columns the same columns as X. Do not label the rows. For the first row, find the OLS estimate of the y regressed on the first column only and put that in the first entry. For the second row, find the OLS estimates of the y regressed on the first and second columns of X only and put them in the first and second entries. For the third row, find the OLS estimates of the y regressed on the first, second and third columns of X only and put them in the first, second and third entries, etc. For the last row, fill it with the full OLS estimates.

```
M = matrix(NA, nrow = ncol(X), ncol = ncol(X))
colnames(M) = colnames(X)
head(M)
##
        Intercept crim zn indus chas nox rm age dis rad tax ptratio black
## [1,]
               NA
                     NA NA
                              NA
                                    NA
                                        NA NA
                                               NA
                                                    NA
                                                        NA
                                                            NA
                                                                     NA
                                                                            NA
## [2,]
               NA
                     NA NA
                              NA
                                    NA
                                        NA NA
                                               NA
                                                    NA
                                                        NA
                                                             NA
                                                                     NA
                                                                            NA
## [3,]
               NA
                     NA NA
                              NA
                                    NA
                                        NA NA
                                               NA
                                                    NA
                                                        NA
                                                            NA
                                                                     NA
                                                                            NA
## [4,]
               NA
                     NA NA
                              NA
                                    NA
                                        NA NA
                                                NA
                                                    NA
                                                        NA
                                                            NA
                                                                     NA
                                                                            NA
## [5,]
               NA
                     NA NA
                              NA
                                        NA NA
                                                                     NA
                                                                            NΑ
                                    NA
                                               NA
                                                    NA
                                                        NA
                                                            NA
##
   [6,]
                NA
                     NA NA
                              NA
                                    NA
                                        NA NA
                                               NA
                                                    NA
                                                        NA
                                                             NA
                                                                     NA
                                                                            NA
##
        lstat
## [1,]
           NA
## [2,]
           NA
## [3,]
           NA
## [4,]
           NA
## [5,]
           NA
## [6,]
           NA
X_j = X[, 1, drop = FALSE]
b = solve(t(X_j) %*% X_j) %*% t(X_j) %*% y #mean(y) = intercept; intercept = null model
M[1, 1] = b
X_{j_2} = X[, 1:2]
b = solve(t(X_{j_2}) %*% X_{j_2}) %*% t(X_{j_2}) %*% y
b #OLS estimates your weights so however big based on cols
##
## Intercept 24.0331062
## crim
             -0.4151903
for(j in 1: ncol(M)){
 X_j = X[, 1: j, drop = FALSE] #1 then 1,2 then 1,2,3
  b = solve(t(X_j)) %*% X_j) %*% t(X_j) %*% y #X is stretching and so will be
 M[j, 1:j] = b # youre filling in the rows iteratively
round(M, 2)
         Intercept crim
                            zn indus chas
                                                                 dis
                                                                       rad
                                                                              tax
                                               nox
                                                     rm
                                                           age
##
    [1,]
             22.53
                       NA
                            NA
                                   NA
                                        NA
                                                NA
                                                     NA
                                                           NA
                                                                  NA
                                                                        NA
                                                                               NA
##
    [2,]
             24.03 -0.42
                            NA
                                   NA
                                        NA
                                                NA
                                                     NA
                                                           NA
                                                                  NA
                                                                        NA
                                                                               NA
   [3,]
             22.49 -0.35 0.12
                                   NA
##
                                        NA
                                                NA
                                                     NA
                                                            NA
                                                                  NA
                                                                        NA
                                                                               NA
##
   [4,]
             27.39 -0.25 0.06 -0.42
                                        NΑ
                                                NA
                                                     NΑ
                                                           NA
                                                                  NΑ
                                                                        NΑ
                                                                               NA
##
    [5,]
             27.11 -0.23 0.06 -0.44 6.89
                                                NA
                                                     NA
                                                            NA
                                                                  NA
                                                                         NA
                                                                               NA
##
    [6,]
             29.49 -0.22 0.06 -0.38 7.03
                                            -5.42
                                                     NA
                                                           NA
                                                                  NA
                                                                        NA
                                                                               NA
##
   [7,]
            -17.95 -0.18 0.02 -0.14 4.78
                                            -7.187.34
                                                                  NA
                                                                        NA
                                                                               NA
##
   [8,]
            -18.26 -0.17 0.01 -0.13 4.84
                                            -4.36 7.39 -0.02
                                                                  NΑ
                                                                        NΑ
                                                                               NΑ
```

```
[9,]
               0.83 -0.20 0.06 -0.23 4.58 -14.45 6.75 -0.06 -1.76
                                                                                NA
## [10,]
               0.16 -0.18 0.06 -0.21 4.54 -13.34 6.79 -0.06 -1.75 -0.05
                                                                               NA
               2.99 -0.18 0.07 -0.10 4.11 -12.59 6.66 -0.05 -1.73
## [11,]
                                                                       0.16 - 0.01
  [12,]
             27.15 -0.18 0.04 -0.04 3.49 -22.18 6.08 -0.05 -1.58
                                                                       0.25 -0.01
##
##
   [13,]
             20.65 -0.16 0.04 -0.03 3.22 -20.48 6.12 -0.05 -1.55
                                                                       0.28 -0.01
   [14,]
             36.46 -0.11 0.05 0.02 2.69 -17.77 3.81 0.00 -1.48
                                                                      0.31 -0.01
##
         ptratio black lstat
##
    [1,]
##
               NA
                     NA
                            NA
##
    [2,]
               NA
                     NA
                            NA
    [3,]
                     NA
                            NA
##
               NA
##
   [4,]
               NA
                     NA
                            NA
##
    [5,]
               NA
                     NA
                            NA
##
    [6,]
               NA
                     NA
                            NA
##
   [7,]
               NA
                     NA
                            NA
##
   [8,]
               NA
                     NA
                            NA
##
    [9,]
               NA
                     NA
                            NA
## [10,]
               NA
                     NA
                            NA
## [11,]
               NA
                     NA
                            NA
## [12,]
            -1.00
                     NA
                            NA
## [13,]
            -1.01
                   0.01
                            NA
## [14,]
            -0.95
                   0.01 -0.52
```

#ran OLS regressions with more and more features where b is the wieghts, the y hat ... as you add more

Examine this matrix. Why are the estimates changing from row to row as you add in more predictors? The weights change therefore changing the estimates because as you add more predictors you explain more and reduce your residual

Clear the workspace and load the diamonds dataset.

```
pacman::p_load(ggplot2)
data(diamonds, package = "ggplot2")
summary(diamonds)
```

```
##
        carat
                                          color
                              cut
                                                         clarity
                                 : 1610
                                                             :13065
##
    Min.
            :0.2000
                       Fair
                                          D: 6775
                                                     SI1
##
    1st Qu.:0.4000
                                 : 4906
                                          E: 9797
                                                     VS2
                                                             :12258
                       Good
##
    Median :0.7000
                       Very Good: 12082
                                          F: 9542
                                                     SI2
                                                             : 9194
##
    Mean
            :0.7979
                       Premium
                               :13791
                                          G:11292
                                                     VS1
                                                             : 8171
##
    3rd Qu.:1.0400
                       Ideal
                                 :21551
                                          H: 8304
                                                     VVS2
                                                             : 5066
    Max.
            :5.0100
                                          I: 5422
                                                     VVS1
                                                             : 3655
##
##
                                          J: 2808
                                                     (Other): 2531
                          table
##
        depth
                                           price
                                                               X
           :43.00
                                                                : 0.000
##
    Min.
                     Min.
                             :43.00
                                       Min.
                                               :
                                                  326
                                                        Min.
##
    1st Qu.:61.00
                     1st Qu.:56.00
                                       1st Qu.:
                                                  950
                                                        1st Qu.: 4.710
##
    Median :61.80
                     Median :57.00
                                       Median: 2401
                                                        Median : 5.700
##
    Mean
            :61.75
                             :57.46
                                               : 3933
                                                                : 5.731
                     Mean
                                       Mean
                                                        Mean
                     3rd Qu.:59.00
##
    3rd Qu.:62.50
                                       3rd Qu.: 5324
                                                         3rd Qu.: 6.540
##
    Max.
            :79.00
                     Max.
                             :95.00
                                       Max.
                                               :18823
                                                                :10.740
                                                        Max.
##
##
                             z
           у
            : 0.000
##
                              : 0.000
    Min.
                      Min.
    1st Qu.: 4.720
                       1st Qu.: 2.910
##
##
    Median : 5.710
                       Median: 3.530
##
    Mean
           : 5.735
                       Mean
                              : 3.539
                       3rd Qu.: 4.040
##
    3rd Qu.: 6.540
```

```
## Max. :58.900 Max. :31.800
```

Extract y, the price variable and "c", the nominal variable "color" as vectors.

```
y = diamonds$price
c = diamonds$color
table(c) #nominal so convert to binary
```

```
## c
## D E F G H I J
## 6775 9797 9542 11292 8304 5422 2808
```

Convert the "c" vector to X which contains an intercept and an appropriate number of dummies. Let the color G be the reference category as it is the modal color. Name the columns of X appropriately. The first should be "(Intercept)". Delete G.

```
X = rep(1, nrow(diamonds))
X = cbind(X, diamonds$color == 'D') #want a dummy
X = cbind(X, diamonds$color == 'E')
X = cbind(X, diamonds$color == 'F')
X = cbind(X, diamonds$color == 'H')
X = cbind(X, diamonds$color == 'I')
X = cbind(X, diamonds$color == 'J')
colnames(X) = c("Intercept", "is_D", "is_E", "is_F", "is_H", "is_I", "is_J")
head(X)
```

```
Intercept is_D is_E is_F is_H is_I is_J
##
## [1,]
                  1
                             1
                                   0
                        0
## [2,]
                                   0
                                         0
                                                     0
                        0
                              1
                                               0
                  1
## [3,]
                        0
                              1
                                   0
                                         0
                  1
                                                     0
## [4,]
                              0
                                   0
                                         0
                                                     0
                  1
                        0
## [5,]
                  1
                        0
                              0
                                                     1
## [6,]
                        0
                              0
                                         0
```

Repeat the iterative exercise above we did for Boston here.

```
M = matrix(NA, nrow = ncol(X), ncol = ncol(X))
colnames(M) = colnames(X)
X_j = X[, 1, drop = FALSE]
b = solve(t(X_j) %*% X_j) %*% t(X_j) %*% y
M[1, 1] = b
X_j_2 = X[ , 1:2]
b = solve(t(X_j_2) %*% X_j_2) %*% t(X_j_2) %*% y
b
```

```
## [,1]
## Intercept 4042.3784
## is_D    -872.4243

for(j in 1 : ncol(M)){
    X_j = X[, 1 : j, drop = FALSE]
    b = solve(t(X_j) %*% X_j) %*% t(X_j) %*% y
    M[j, 1:j] = b
}
round(M, 2)
```

```
##
        Intercept
                        is_D
                                 is_E
                                          is_F
                                                  is_H
                                                           is_I
                                                                    is_J
## [1,]
          3932.80
                          NA
                                   NA
                                            NA
                                                    NA
                                                             NA
                                                                     NA
```

```
## [2,]
          4042.38 -872.42
                                          NA
                                                          NA
                                                                  NA
                                  NA
                                                  NA
## [3,]
          4295.54 -1125.59 -1218.79
                                          NΑ
                                                          NΑ
                                                  NΑ
                                                                  NΑ
## [4,]
          4491.23 -1321.28 -1414.48 -766.34
                                                          NA
                                                                  NA
          4493.17 -1323.22 -1416.42 -768.28
                                                          NA
                                                                  NA
## [5,]
                                              -6.50
## [6,]
          4262.94 -1092.99 -1186.19 -538.06 223.72
                                                                  NΑ
          3999.14 -829.18 -922.38 -274.25 487.53 1092.74 1324.68
## [7,]
```

Why didn't the estimates change as we added more and more features?

The estimates did change.

#T0-D0

Create a vector y by simulating n = 100 standard iid normals. Create a matrix of size 100×2 and populate the first column by all ones (for the intercept) and the second column by 100 standard iid normals. Find the R^2 of an OLS regression of $y \sim X$. Use matrix algebra.

```
y <- c(rnorm(100))
#y
X <- as.matrix(cbind(1, y ), nrow = 100, ncol = 2)
colnames(X) <- c("intercept", "y")

#X

b = solve( t(X) %*% X) %*% t(X) %*%y
H = X%*% solve(t(X) %*% X) %*% t(X)
yhat = X %*% b

e <- y - yhat
sse <- sum(e^2)
sst = sum((y-mean(y))^2)
Rsquared = 1- sse/sst
Rsquared</pre>
```

[1] 1

from the last problem. Find the \mathbb{R}^2 of an OLS regression of y ~ X. You can use the summary function of an lm model.

Write a for loop to each time bind a new column of 100 standard iid normals to the matrix X and find the R^2 each time until the number of columns is 100. Create a vector to save all R^2 's. What happened??

```
ols1.2 <- lm(y~X)
summary(ols1.2)</pre>
```

```
## Warning in summary.lm(ols1.2): essentially perfect fit: summary may be
## unreliable
##
## Call:
## lm(formula = y ~ X)
##
## Residuals:
##
          Min
                      1Q
                                             30
                             Median
                                                       Max
## -3.723e-16 -1.974e-17 1.277e-17 3.136e-17
                                                1.553e-16
##
## Coefficients: (1 not defined because of singularities)
                Estimate Std. Error
                                      t value Pr(>|t|)
##
## (Intercept) 0.000e+00 7.666e-18 0.000e+00
```

```
## Xintercept
                     NA
                                              <2e-16 ***
              1.000e+00 7.686e-18 1.301e+17
## Xy
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 7.599e-17 on 98 degrees of freedom
## Multiple R-squared:
                           1, Adjusted R-squared:
## F-statistic: 1.693e+34 on 1 and 98 DF, p-value: < 2.2e-16
y=rnorm(100)
X=matrix(data=c(rep(1,100),rnorm(100)),ncol=2,nrow=100)
rsquared=c()
while(ncol(X)<100){
 b=solve(t(X)%*%X)%*%t(X)%*%y
 yhat=X%*%b
 e=y-yhat
 sse=sum(e^2)
 sst=sum(y-mean(y)^2)
 rsquared=c(1-(sse/sst),rsquared)
 X=cbind(X,rnorm(100))
}
rsquared
   [1]
         4.198422 15.818744 16.351078 29.893565 29.893570 33.762151
  [7] 33.772956 63.820598 65.944337 93.165409 115.808009 122.243044
## [13] 125.114702 127.081540 136.607174 171.396146 180.397104 203.734912
## [19] 204.569166 238.736195 240.317969 240.624343 243.744347 277.239647
## [25] 278.836654 283.087619 290.244791 290.269332 310.482128 311.621434
## [31] 321.811211 322.822142 323.395544 340.332171 344.419657 344.420054
## [37] 347.785998 354.939812 356.867370 358.510015 370.867321 373.765967
## [43] 374.077417 380.866713 393.138587 401.308143 402.836991 404.604467
## [49] 404.637620 448.386194 488.891369 491.388367 491.925200 511.854539
## [55] 541.007194 550.127084 566.359786 578.969588 581.750393 587.348177
## [61] 587.551914 593.561747 593.813595 594.657813 595.912117 596.538331
## [67] 605.079097 633.206909 638.460678 643.447904 650.945296 651.138144
## [73] 652.703218 663.990150 665.591088 665.609901 666.411604 673.144646
## [79] 689.131164 710.264638 712.890863 713.032318 715.150793 725.180083
## [85] 726.600907 726.675530 726.685960 741.539985 753.305974 766.256101
## [91] 768.503909 782.204820 782.219231 782.253158 785.154995 844.201640
## [97] 848.029746 849.346862
X
##
                      [,2]
                                   [,3]
                                                [,4]
##
     [1,]
            1 0.244105027 -0.992787873 0.606509842 2.125336613
            1 -1.247164597 0.512141594 -0.276171349 -0.165839273
##
     [2,]
##
     [3,]
            1 -0.401203706 -0.305188191 0.120959862 -0.889893884
##
     [4,]
            1 0.501479642 -0.672177968 -0.877708103 0.369700377
##
     [5,]
            [6,]
            1 -1.898699545 -1.080080687 -0.510470439 -0.795827312
##
##
     [7,]
            1 -1.738488450 -0.345477590 1.037186266 -1.079896458
     [8,]
            1 1.264611246 1.121316297 -1.632591660 0.901578669
```

```
[9,]
##
            1 -0.651284765 1.561450308 -0.311459991 0.195526517
##
    ſ10.]
            1 -0.452317359
                           0.192865156 1.038822439 -1.348415452
##
    [11,]
               [12,]
##
            1 -0.285675879 -0.386397814 -0.279275239 -0.485257574
    [13,]
            1 -1.152800949
                           2.868052196 -1.605128317 -0.233086488
##
    [14,]
            1 -0.058332950 -0.773888448 -0.176066070 -1.062030883
    ſ15.]
                           0.867447924 0.073531354 -1.486920069
            1 -0.369716347
    [16,]
               1.242302808 -0.142445905 0.662174532 -1.244713902
##
##
    [17,]
            1 -0.894654636 -0.902953251
                                       1.714850049 0.914119564
##
               0.126054190 0.560633835
                                       0.965243964 -0.258265052
    [18,]
    [19,]
               0.009273322 -0.586355247
                                        0.255202763 0.834826919
    [20,]
            1 -0.910136724 0.947599038
                                       0.187455076 -1.048205961
##
##
    [21,]
              0.782223294 0.947520802 0.343746417 0.291621272
            1
##
    [22,]
               1.175522679 0.772515044 0.003364871
                                                    1.155747154
##
    [23,]
            1 -0.953155951 -1.376274186 -0.387542647 0.310830703
##
    [24,]
               ##
    [25,]
              0.714311170 -0.486336429 -0.698870700 0.268237929
##
    [26,]
            1 -1.441378968 0.257567794 0.946067035 -0.470708995
    [27,]
            1 -0.336457526 -0.774225793 -1.027160126 1.314925711
##
                                       1.889699221 0.721300420
##
    [28,]
            1 -0.007215555 0.214646676
##
    [29,]
            1 -0.693804733 -1.421620565
                                       0.144316186 -0.742224706
##
    [30,]
            1 0.840930333 -0.513775575
                                       0.142553034 0.640195956
##
    [31,]
            1 -0.716250360 1.074377031 0.945507565 -0.315881186
    Γ32.1
            1 -0.637140160 -0.514839472 0.526643883 -1.121330523
##
##
    [33,]
            1 -0.246374488 1.081402991 0.344274368 -0.291711762
    [34,]
            1 0.161042953 0.695770315 -0.173814304 0.897651795
##
    [35,]
            1 -0.471178051 -1.959869329 -2.006681531 -1.039808357
    [36,]
              0.005523703 -0.083117181 -0.987671878 -0.219759290
            1
            1 -2.127199922 1.441399327 0.357482807 0.294766327
##
    [37,]
    [38,]
            1 1.959278126 -0.487437156
                                       0.599601756 -1.401439149
##
    [39,]
            1 -1.050738815 0.082968525 0.547498024 -0.709604388
##
    [40,]
            1 -0.992936334 -0.287854937 -0.163328768 1.378762484
            1 -0.034610691 -2.504826582 -0.570829257 0.848685374
##
    [41,]
    [42,]
            1 -2.447520082 -0.622745481 -1.234552088 0.110472518
##
##
    [43,]
            1 -0.723057363 -1.092741235
                                       0.816714644 -0.901740398
##
    [44,]
              0.198066303 -0.316530779
                                       1.782658920 -0.145190802
##
    [45,]
               0.207612131 0.815221513
                                       0.055918732 -1.674025632
##
    [46,]
               0.162510545 -0.355133925
                                       0.686215724 -1.216944798
##
    [47,]
               0.423710856
                           0.137645366
                                       1.432864824 0.021211725
##
    [48,]
               0.065558548 0.397505981
                                       0.774223249 -1.299432313
            1
    [49,]
               0.987213909 1.678458874
                                        0.697926013 -1.979685041
##
    [50,]
               0.399211091 -0.991111673
                                       1.284976517 -0.638101921
    [51.]
            1 -0.607427763 -1.446022414
                                       1.129780933 0.630662709
##
            1 -0.847817471 -0.333820419 -0.886733709 1.087631373
    [52,]
    [53,]
            1 -0.280712120  0.502650070 -0.220185281  0.832249291
    [54,]
                           0.001773399 -0.002273068 -1.319904856
##
            1 -0.231469535
##
    [55,]
            1 -0.031092596 1.371407679
                                       1.283828502 0.664041371
##
            1 -0.492154672 -0.101682540 2.595007401 -0.896412601
    [56,]
    [57,]
            1 -0.530545095 -2.610047966 -1.335902389 -0.936536247
                                       1.723896321 -0.154923642
##
    [58,]
               0.341131173 1.182353884
                                       1.979534474 -0.539828682
##
    [59,]
            1 1.187389218 1.261710576
##
    [60,]
            1 -1.502018721 -0.020734531 -1.442099351 1.710134023
##
    [61.]
            1 -1.204774428 -1.206443633 0.065718080 -1.064150950
            ##
    [62,]
```

```
[63,]
##
           1 1.219587775 0.573079926 0.262692453 0.133347847
##
   [64.]
           ##
   [65,]
              0.619598412  0.599911439  -1.193836487  0.707646142
##
   [66,]
           1 -0.247922007 0.139210190 -0.485712219 0.003793644
   [67,]
              0.173288126 -0.890240429 -0.741293449 -1.578847524
##
   [68,]
             0.236497177 -0.439316366 0.228954093 0.490361073
   [69.]
           1 -1.615279108 0.596893699 0.452365274 0.516266267
   [70,]
##
           1 - 0.506071981 - 0.798410419 0.010815944 - 1.267131485
##
   [71.]
           1 -1.620532236 1.892115969 -0.075820636 0.258187048
##
   [72,]
           1 -0.475048371 0.364623069 1.048122738 0.135855401
   [73,]
           1 0.023928860 2.237702515 -0.269862391 1.315114239
##
   [74,]
           1 -0.153301591 -0.152506729   0.302492049 -1.542160059
##
   [75,]
           1 -1.275222910 -1.851883859 0.641501038 -0.060297526
##
   [76,]
           1 -0.513148082 0.526533569 0.179659190 0.688366734
##
   [77,]
           ##
   [78,]
             0.316757363
                          2.742297978 -0.660474608 -0.567220693
##
   [79,]
           1 -0.726731129  0.871621543 -0.107420637  0.878906122
##
   [80,]
              [81,]
              2.555407651 1.213738037 0.233997217 0.001132816
##
##
   [82,]
              1.557714354  0.627227976  -0.966484483
                                                0.306956726
##
   [83,]
             1.683528750
                         1.716831336 -0.543224477
                                                 0.358344413
##
   [84,]
           ##
   [85,]
   [86.]
                          0.016071453 -1.100951562 -0.269006135
##
           1
              0.262081475
##
           1 -0.792882797 1.708778001 -0.171731747 -1.422642079
   [87,]
   [88,]
             0.111672372  0.686778465  -1.480403404  -0.907955660
##
   [89,]
              1.343699996 1.223630074 1.236359676 0.886880345
              0.909746853 -0.326148175 -1.143823106 -0.875403447
   [90,]
           1
             0.968199655 -1.270469430 -1.268706917 -0.061952792
##
   [91,]
##
   [92,]
           1 0.319076190 0.489129639 0.900440803 0.759159928
##
   [93,]
           1 -1.304233660 1.524537489
                                     1.194565090 0.078029939
##
   [94,]
           1 -0.154220731 -0.444723237 0.055133436 -0.365984400
           1 0.673618876 0.252963901 0.870883399 -1.043325052
##
   [95,]
   [96,]
           1 0.287131305 -0.932915934 0.386913477 -1.681357574
##
##
   [97,]
             0.500505148 -1.073133763 -0.195004095 1.427055257
##
   [98.]
           1 -0.740044440 0.362517529 -0.493048811 0.238839229
##
   [99.]
           1 -0.280318829 -0.817922568 -0.257415120 -0.209667795
##
  [100,]
           1 -0.599850240 1.455552744 1.260630271 -1.874126372
##
               [,6]
                          [,7]
                                     [,8]
                                                  [,9]
                                                             [,10]
##
    [1,] -0.55592413  0.22212210  0.51087560 -2.2093224393 -0.460040196
        1.57112255 1.17290515 0.31654572 0.5830868754 1.225684452
##
##
    [3,] -2.02450022 -0.27559418 0.50754695 0.0817268057 -0.177311916
##
    [4,] 0.85346849 1.27600888 0.74228951 0.2539444472 0.607610762
##
    [5,] 0.41911228 -1.15541868 -0.36883250 -1.9641629640
                                                      0.224429912
##
         0.56343867 -0.56457317 0.35880538 -0.3047424208 0.273585347
    [7,] 0.11266346 0.80183939 -1.59491247 -0.5551920118 0.372407962
##
##
    [9,] -0.99672555 -0.77537501 2.18761636 -1.0666461435 0.325196947
##
   [10,] -0.17525887 0.95306755 -0.52964249 1.7723769244 -2.284348518
##
   [11,] -0.02030755 -0.61298756 -1.13827483 0.0451087847 -0.360463586
##
   [12,] -0.01857266 -0.27669317 0.92840120 -0.4213988885 -0.444359617
##
   [13,] -1.19853576  0.61576366  -0.33834191  0.0816067174  -0.571103451
##
   [14,] 0.17520458 -1.44973585 0.09737896 -0.3373594276 -1.865435302
   [15,] 0.28527208 -0.33777510 0.77249376 -0.2956284676 -0.143245676
```

```
[16,] -1.38629839 -0.28792855 1.40877587 0.2285880835 -1.244081419
##
   [17,] -1.73684994 -0.90687539 -0.10615813 -0.3715985892 0.251841350
   [18,] 0.32025298 0.49568484 1.59240437 0.4188940315 0.606913106
##
   [19,] 0.38950118 -0.75367600 0.91369110 -0.4453275895 1.186377379
##
   [20,] 1.08931344 0.33191333 0.92712588 2.4272839205 -1.776922646
##
   [21,] -1.62620652 1.10344651 1.22255656 -1.1110393955 -0.212053539
   [22.] -0.17302725 -2.22116772 -1.11496252 1.5256425140 0.005031776
##
   [23,] 0.10563424 0.35834245 -0.13933118 -3.0776856258 -0.221412048
##
   [24,] -0.29281916  0.14249035 -0.17261704 -0.4058788952  0.312548673
##
   [25,] 1.22739229 1.37555285 0.56116197 1.0915770193 -0.568943930
   [27,] 1.40299233 2.13737000 0.07438096 0.4654804403 -1.238196136
##
##
   [28,] -0.08773104 1.81084704 1.49729904 -0.5873409923 0.239572101
   [29,] 0.45210814 1.23316735 -1.09468881 -0.5330408238 0.215615245
##
##
   [30,] -1.16346021 -0.98492464 0.56154545 -0.6490036523 0.117120080
##
   [31,] 0.19025387
                    ##
         1.42228810 0.16010745
   [32,]
                               1.55593490 0.1130383561 -1.105304695
   [33,] -0.06938864 1.47058131 0.68077911 0.2424695304 1.445073050
   [34,] 0.18518939 0.28827607 -0.08421409 -0.2689947042 1.260134351
##
##
   [35.]
         1.04395999 0.41264640 -1.39575812 1.0047684753 -1.160467621
##
   [36,] -0.37390135 -1.39423037 -0.55673905 -1.1184233160 -1.015813492
   [37,] 0.57194254 0.06826086 -0.60745243 0.6089622044 1.971945855
##
   [38,]
         1.93119516  0.06491117  -0.23546252  0.0155679455  1.740335607
         0.08135308 -1.02363269 -0.14028935 0.1509506365 -0.928821584
##
   [39.]
##
   [40,] 0.90591490 2.05353039 0.36988924 0.8847769219 -0.466088660
   [41,] -1.25720833 -1.38591236 -0.39447900 -0.4153462599 -0.753365593
##
   [42,] 0.76155374 -0.20140197 -1.59775066 0.3520772098 0.612907644
   [43,] -0.45632390 1.40709041 -1.36481315 0.3151521145 0.606962450
   [44,] -2.22771874 -0.94179151 -0.23326262 0.0330416470 1.340122965
   [45,] 0.82661728 0.47315476 0.32373229 -2.1165158909 -0.124935313
##
   [46,] -1.10012190 1.20773136 1.13006548 1.4728436125 1.044394790
##
   [47,] 0.36246131 -0.92521195 -0.31958441 1.0038269784 0.022907973
   [48,] -0.18878089 0.78661893 0.34137593 1.7281758751 0.353562587
   [49,] 0.42629262 1.27800731 0.19028148 1.3391972656 -0.184647286
##
##
   [50,]
         1.57538761 -0.44998243 0.33351887 0.6316956808 0.731493731
##
   [51,] 1.17067197 0.88552701 -0.11468132 -2.3418737239 -0.459216905
##
   [52,] -1.62623979 0.71166567 0.31947209 0.0001903259 1.120522505
##
   [53,] 1.79575527 -0.53568958 0.04908304 1.2304386390 -1.142466892
   [54,] 0.96379547 -0.31585716 -0.03303898 -0.1839846518 -0.048512656
##
##
   [55,] -1.15565111 -0.37801001 1.09270280 -1.3316720143 1.241354663
   [56,] 0.45546695 0.07926853 -1.21995825 0.5609080030 0.829118465
   [57,] 0.86981479 0.04766679 0.40487596 0.9857731878 0.634753367
##
##
   [58.] 0.40775513 0.52777624 1.35522458 -0.1764093866
                                                        2.202813741
   ##
   [60,] 1.36234071 0.10953825 1.21579267 0.9728475951 -1.087287953
   [61,] 1.68317307 -0.22230431 -0.76606691 0.3362097420 -0.196673485
##
##
   [62,] -0.60015801 0.76977629 1.36851729 -0.7877871977 -1.325411668
   [63,] 0.19232281 1.57199307 1.54328451 0.4875744776 1.255503687
##
   [64,] -1.62575101 -0.83706978 0.42232958 1.4156441287 -0.166978234
##
   [65,]
         0.17742898 0.29619018 -0.70815579 -0.1340353287 -0.759529282
##
   [66,] 1.28591660 1.40576484 -0.39349372 0.9870498440 0.709636355
##
   [67,] 1.73327157 -0.59699315 0.25865877 0.2271674787 1.283429949
##
   [68,] 0.18308185 -0.83165046 -0.38374278 1.1789447635 0.235229683
   [69,] -0.65057005 -0.52256174 -0.03749619 1.8832592531 -1.225069714
```

```
[70,]
          ##
          0.18194746 -0.44610422 0.28715133 -0.7706947668 -0.867579565
   [71.]
         1.16759609 2.17972145 -0.97011042 -1.6035628808 2.008600113
   [72,]
   [73,]
          1.24325271 0.12882955 2.51199074 1.2634653857
##
                                                        0.777836107
##
   [74,]
          0.08135062 -1.65800382
                               0.17921843 -0.2961358837
                                                        0.858743408
   [75,] 0.21193145 0.02337813
                               1.87751033 0.4093636388
##
                                                        0.701519503
         1.56482668 1.02504359 0.25941951 0.5448075408 0.939523643
##
   [77,] -0.26960996  0.45464409  0.48075875  0.1735512460  -1.576298647
##
   [78,] 0.13852416 0.65296730 -0.42939399 0.5423777792 0.242984169
##
   [79,] 0.51972225 -0.29869697 0.50763851 -1.6864680854 0.828042817
   [80,] -0.07247829 -0.51065888 0.22080694 0.7053335013 -1.543339400
   [81,] -0.55449655 -1.14875946 -0.29544269 1.1050754137 1.059359660
##
   [82,] -0.94824539  0.56393750  1.48241935 -2.0048529542 -0.946628967
   [83,] -0.36597137  0.64077889  0.73597267  0.2549289657  -0.875801214
##
##
   [84,] -0.40683822 1.02774973 1.02101355 -0.2179085268 -0.467750419
##
   [85,] 0.15775510 -0.58902476
                               1.33015663 -0.5378900386 -1.078992137
##
   [86,] -0.64379046 -1.89069095 0.95203221 1.3461249127 0.410620538
   [87,] -0.20511124 -1.93146228 -0.83540137 -0.2693855295
                                                       0.402999987
   [88,] 0.56509752 1.14807102 0.75641027 0.6517590019 1.004926452
   [89,] -0.60323205 -0.30883838 1.01779833 -0.6208743953 -0.875440341
##
   [90,] 0.32274924 0.34089682 -1.40333529 0.8226552025 0.653402056
   [91,] -0.16863955 -0.05242506 -0.51781129 0.0506805128 0.433575628
   ##
   [93,] -0.92105012 -0.80627950 -1.19877095 0.4368785560 -0.727818940
   [94,] -0.09277503 -0.75042498  0.33521320 -0.3684940082 -2.054608622
##
   [95,] 0.85202278 -0.60864314 0.13648672 -2.2375273704 -1.036236213
##
   [96,] 1.47993293 0.81590314 0.96953923 0.5775815429 -1.066195693
   [97,] 0.50070652 1.17237539 -0.27714727 -0.6462560748 -0.487022068
##
   [98,] -0.35250021 0.19508169 0.84690804 -0.8425168144 -1.209775212
   [99,] -0.07330527 -0.60806382 1.47963913 0.1470844381 -0.030703636
  [100,] -0.45488936 -1.18353048 0.44197377 0.0976650492 1.172371043
##
##
               [,11]
                           [,12]
                                      [,13]
                                                 [,14]
                                                             [,15]
    [1,] 0.07435194 0.919608801 -2.37904752 -0.46588280 0.201306169
##
    [2,] 0.13220962 0.424141241 -0.26043704 -0.46200706 0.377185941
##
##
    [3,]
         1.15484741 1.522248690 0.27899066 -1.62774608
                                                      0.766487702
##
    [4,] 1.66402023 0.627362796 0.10152093 0.85756320 -0.331067291
##
    [5,] -0.40478980 -1.580072239 -0.04226172 -0.06676696 -1.912781276
##
    [6,] -2.05344974 -1.376610633 -0.35945505 1.84981133 0.835503536
##
    [7,] -0.42887115 -0.735031192 0.08066691
                                           1.52243581
                                                       1.278742369
##
    [8,] 1.98967959 -0.961919394 0.76011137 0.76122335
                                                       0.454627141
    [9,] 0.98665423 0.371368699 0.71014916 0.82679893 0.679562953
##
    [10,] 1.00917631 -0.285543540 0.60557769 -0.91618128 -1.907022263
    [11,] -0.61579603  0.986617851 -0.37933395  1.17757853  0.860659973
##
   [12,] 1.09287981 -1.217177003 0.43940002 -0.58818888 -0.565113358
   [13,] 1.36249092 0.837386754 0.33941278 -0.18856245 -0.375570142
   [14,] 0.62013304 -0.893432336 -0.14141271 0.39688654 0.153724015
##
##
   [15,] -0.40222596 -0.671430832 1.04334174 0.13376052 2.247016233
   [16,] 0.81370081 -0.673594188 -0.04774418 0.02527600 0.393924032
##
   [17,] 0.07945110 0.951909057 0.46793653 0.76725448 0.555646766
##
   [18,] -0.14898249  0.392974540  0.37688703  0.33050864 -1.477327311
##
   ##
   [20,] -1.38510367 -0.114597727 0.06810265 1.53255462 -0.829875555
##
   [21,] 0.22538336 -1.017430668 0.37793094 0.17756937 0.058388581
   [22,] -1.04663700 -0.584562107 -1.17145368 -0.08490203 -0.668325953
```

```
[23,] -0.61054061  0.832692882  1.31591159 -1.90774949 -1.270584031
##
   [24,] 0.55727754 -0.638408068 0.06274440 -2.06644669 0.487992119
   [25,] -0.49295952  0.056096272  0.43478060 -0.70628589  0.466193777
##
   [26,] -1.20905031 0.502623840 -0.26030999 0.55221346 1.444024458
##
   [27,] 0.86962617 -0.152014530 0.56447560 0.62166693
                                                        0.617806834
##
   [28,] 1.63759161 -1.304696177 -0.49144387 -0.88232510 0.479250864
   [29.] -1.57370153 -0.860750962 -0.53106795 -0.34213534 -0.772044956
          0.88998037 1.362508090 0.88258804 -0.52949928 0.718042727
##
   [30.]
   [31,] 0.33760223 1.754468000 -0.83042245 -0.09853462 1.210872576
##
##
   [32,] 1.41222411 -1.006681230 -1.64201922 -1.50118995 -0.659067746
   [33,] -1.34508321  0.503479198 -1.36688055  0.27525917
                                                        0.642603201
   [34,] -0.01363390  0.557461908 -0.03975096  0.40481743  0.490380928
##
##
   [35,] 1.02937483 0.838389681 0.33217603 0.45895688
                                                       1.651716517
   [36,] 0.23014348 0.649923626 2.13502709 0.60158820 0.793247660
##
##
   [37,] 0.68897953 0.778778689 1.24702262 -0.56881240 0.069279853
##
   [38,] -1.08240718  0.234952276 -1.39868636  0.42209458  1.580786999
         ##
   [39,]
##
   [40,]
         0.90592225 0.008947202 0.34528097 0.06226247 0.909535340
   [41,] 0.48767582 1.110815249 0.08248399 -0.65670191 -0.575341682
##
##
   [42,] 0.55578775
                    ##
   [43,] -0.82572241 0.153361973 -1.40390641 0.49535556 -1.681561043
   [44,] 0.56900918 -1.780210050 0.73621449 -1.85174444 -1.973590164
   [45,] -0.09549953 1.673068975 -0.61624385 -0.63056647 -0.753818639
##
   [46,] -1.51620400 0.063285105 0.42699980 -0.82178786 -1.127400985
   [47,] 0.35581650 -0.715053963 -0.07741085 -0.01241235 1.336026498
##
   [48,] 1.41793602 -0.633038195 -0.70911372 -2.17976796 -0.095623605
##
   [49,] 0.99480043 1.217901060 -0.15187325 1.11050325 0.948140034
   [50,] -0.41461751 0.107244054 1.68078119 0.20789099
                                                        0.306337886
##
   [51,] -1.80006913 2.113092335 0.56084887 -0.85271753 0.334758010
   [52,] 1.02163550 -0.711028801 1.53808647 0.24815293 -0.209462829
   [53,] -1.83325850 -0.747334175 -1.74676807 1.12549911 0.602833577
##
##
   [54,] -0.04955286  0.525304473 -0.18049379  0.62770788  1.514531817
   [55,] -1.12058752 -0.571791602 -0.45821660 -0.63086909
                                                        0.613169840
   [56,] 0.17472707 0.842092837 2.40945274 -1.09520471 1.378460073
##
##
   [57,]
         1.03109005 1.060779595 0.11944988
                                            0.35190096 -0.416689064
##
   [58,] 1.55703389 -2.354055478 1.12221975
                                            0.54729967
                                                       1.295632918
##
   [59,] 0.71868424 1.397338884 -2.91162316
                                            0.56805990 0.733034022
##
   [60,]
          0.75599047 \; -0.347555054 \; -0.35563347 \quad 0.66737545 \quad 0.040864706
   [61,]
         1.87737939 -1.045612632 -0.41688582 -1.14999552
                                                        0.225015480
##
##
   [62,] -0.72573395  0.244321403  1.74071447 -0.89613448 -0.008666661
   [63,] -1.97706268 -0.331892406 -0.92778062 1.04988886 -0.108150391
   [64,] -0.20919197  0.404215394 -0.78957028 -0.83064126  0.829537385
##
##
   [65,] 0.19924885 -1.077357758 -1.65856608 1.42635742 -0.870919637
##
   [66,] -0.77665400 -0.353586978 2.70304755 -1.93177212 -0.074569759
   [67,] -0.67161014 0.087403040 0.57757687 -0.86442356 0.534712727
   ##
##
   [69,] -0.97897966 -1.194947017 -1.16229568 -1.31867322 1.743116105
   [70,] 2.26971184 0.986019752 0.07761861 -2.14866166 0.223728428
##
   [71,] 1.42276991 -0.378704481 0.73717147 -0.44281614 -0.109740590
   [72,] -0.13978308 1.113640586 -1.51155786 -0.63027279 0.075328448
##
##
   [73,] 0.60027863 -1.166854555 -2.33587245 -0.46087556 0.069447842
##
   [74,] -1.97800755  0.435303160  0.73502051  1.45237028  0.943464775
##
   [75,] -0.23387556 -0.293507505 0.58554897 -0.90296929 0.950719158
   [76,] 1.43240898 -0.174170775 0.53522849 -0.73617522 1.436147742
```

```
[77,] 0.39042915 -0.609646260 -0.30537501 -1.60668709 -0.811440848
   [78,] -1.08757502 0.236640114 -1.23250688 -0.84221434 1.501227692
##
   [79,] -1.62796339 0.060366020 1.10561980 -0.55483043 -1.384692381
   [80,] 0.37170332 -0.125999074 -0.49109132 0.28326312 -0.310853184
##
   [81,] 0.79218427 0.021330584 0.01934859
                                            1.64015476 0.963024534
   [82,] 0.48677085 -0.912978206 -0.14886984 0.68153785 -0.678151928
##
   [83,] -0.53151412  0.382883459 -0.11230607 -0.26406260 -2.165205510
   [84,] -0.71985345 1.208716183 1.18272395 1.17726355 0.426176466
##
##
   [85,] -0.70406721 -0.448829432 1.16861924 0.60715402 0.487507485
##
   [86,] -0.55137213 1.166412453 -0.84622326 -0.23760935 -0.035825203
   [87,] 1.49530455 -0.287064560 1.20220496 -0.75940211 -1.309390033
   [88,] -0.25515146 -0.093390185 -0.94074722 0.19722937 0.484721379
##
   [89,] -0.15680796 -0.187758452 -0.25441890 -0.20626724 1.011024194
##
   [90,] 0.99180593 0.104923192 -0.45703976 1.35929122 -0.489680084
   [91,] -0.74284735 1.134858400 -0.77185858 -0.48994889 -0.461569418
##
##
   [92,] 0.14981819 -0.215477203 0.03514759 -2.28826925 -0.496728929
   [93,] 0.18908354 -0.451154915 -0.01267722 -1.52595742 -0.305250626
##
   [94,] -1.08780812 -1.395509116 -1.62673438 0.35205742 -0.420630134
   [95,] 0.09860758 0.516193471 0.02912090 -0.92619575 -0.726244017
   [96,] -0.37533928 1.978757734 0.28034374 1.78318062 0.060792335
##
##
   [97,] 1.91025239 -0.191650666 -0.08637830 1.53354812 1.800835926
   [98,] 0.95461730 0.630871770 -1.18352080 0.87477551 -0.451603841
   [99,] -0.47506228 -0.576572776 -0.87989700 -2.13086114 0.505431195
##
   [100.] -0.51181802    1.640687791 -0.03910180    0.12504769    0.329935127
##
##
                [,16]
                            [,17]
                                       [,18]
                                                   [,19]
                                                              [,20]
##
    [1,] -0.411454711 -1.054255887 1.38219916 0.51281921 -0.05724647
##
    [2,] -0.523042761 1.148897865 -0.45133952 -1.10042815 0.06082689
##
    [3,] 0.224979186 1.048927936 0.06042582 -0.35905441 -1.17415772
##
    [4,] -0.497403471 -1.396412740 -1.09740475 -0.56355308 -0.49166463
     [5,] -0.097923089 -0.417062505 -1.95543222 0.04684655 -0.75856708
##
    [6,] -0.331850741 -1.255365029 -0.68697368 0.95977085 -0.23910371
##
##
    [7,] -0.359183588  0.681702015 -0.48374797 -0.86063697  0.34846053
##
    [8,] -0.756266996 -1.785878062 0.04032160 -1.07052844 0.21621922
    [9,] -0.244372926 1.094356112 -0.40870075 -0.28968498 0.16485156
##
##
    [10,] -0.548567007 -1.993744287 -0.62927476 -1.32204578 -0.79549703
   [11,] -0.210587771 0.194950666 -0.30090191 -1.31473701 0.54660031
##
   [12,] -0.464679327 -0.613577913 -0.69504900 2.11551419 0.15303843
##
   [13,] 0.742951032 -0.189811460 0.75089130 0.62496406 1.22008324
   [14,] -0.262034076   0.558256956   -0.33776536   -0.17238493   -0.91323567
   [15,] 0.170604976 -0.673652904 -0.46710587 -1.34451492 -1.83866449
##
   [17,] -1.486341169 -0.351357623 0.47333520 0.80064474 0.07817466
##
   [18,] 1.356043187 0.215050256 -1.66080943 -0.67492801 -1.00957900
##
   [19,] 1.232968918 1.081190612 -0.38218174 0.51790816 1.04316017
   [21,] 1.215564818 -0.083846544 0.02082977 -0.94218876 -0.60239504
##
##
   [23,] 0.315065699 0.125147995 0.45190497 0.16479576 0.69757585
##
   [24,] -0.916271262 -0.026992697 2.38383678 -0.31300386 -0.34112125
##
   [25,] -0.845948290  0.716579452  1.09296511 -0.18339052 -1.56803660
##
   [26,] 0.714379341 -0.485478318 -0.41341327 0.42295586 1.12293174
##
   [27,] -1.138424379   0.041274123 -1.04290991   1.01558102   1.26224651
   [28,] -1.402582488  0.947120597 -0.04432434  0.14832826  0.53793898
##
   [29,] 0.686258230 -0.987988692 0.49918625 0.41422469 0.40414657
```

```
[30,] 0.761844531 -0.869648510 -0.66438173 -0.93795654 -1.08488013
    [31,] 1.852725468 -1.236271362 0.84170791 -0.60355150 -0.40713641
##
    [32,] -0.498571390  0.932361087  1.07390877  -0.54308677  -1.11350780
    [33,] 1.167564082 1.304420624 1.05034457 0.81646541 0.63842980
##
##
    [34,] -0.452128702 -0.309632429 -0.64818684 0.69902744 -0.27070405
##
    [35,] -0.630841448    1.689860085    -0.29177303    0.38591963    -0.83612166
    [36.] 0.325188611 -0.858545023 0.66478123 -0.85402428 0.07056113
##
    [37,] -2.839956091 -1.851657158 0.17624868 -0.08142540 0.96855379
##
    [38,] -0.977710725  0.004589249  0.35299188  1.48780851  0.61348201
##
    [39,] -0.733784858 -0.902294199 -0.17178266 1.13903212 -0.12216435
   [40,] 1.902670918 -0.670461833 -0.11209293 0.99357722 -1.17307357
    [41,] 0.521411889 -1.747381885 1.92370470 -0.02540879 -1.81107421
##
    [42,] -1.909516205 -0.093645756 -1.23692017 -0.94202887 0.66965913
   [43,] 0.872776990 1.473597680 -0.66676691 -1.98930961 0.24878380
##
##
    [44,] 0.876510667 0.896157546 0.09330542 0.16670089 0.69953495
##
    [45,] -0.259820162 -0.619957110 0.96653432 -1.92765163 1.12158786
##
    [46,] 0.557168804 -0.554014110 1.82376340 0.64017896 -0.38189834
    [47,] -0.506940088 0.022732454 -0.73928909 0.39704820 0.50662613
   [48,] 0.625363800 -0.329823467 0.01503736 0.63140282 0.96979616
##
    [49,] -0.282240619 -0.304053593 -1.52157582 -1.09637053 -0.30086358
##
    [50,] -1.393101625 0.111494272 1.21448532 0.92569729 -1.77377254
    [51,] 0.008512222 1.728525414 0.70487618 -0.58463586 -0.21622603
##
    [52,] 0.908017713 0.580037148 -1.06549959 -0.04357812 -0.41960138
    [53,] -0.207241234 -1.110177248 0.07282409 2.02905845 0.22906310
##
    [54,] 1.297040350 -0.373240256 -1.66976058 -0.75839743 1.10703889
##
    [55,] 1.505370487 0.809135520 0.46783150 0.45393527
                                                           1.42622403
##
    [56,] 0.396374111 -1.968548128 0.47053569 -1.25118747 1.02525706
    [57,] 2.449520487 -1.325420425 -2.39583122 -0.06625960 -0.39194278
##
    [58,] -0.015503702 1.075593960 -0.26262261 -0.15813477 0.82984346
    [59,] -0.193901404 1.390629341 1.60017125 1.08854696 2.43999425
    [60,] 0.699631844 0.141830335 0.12354077 0.42797389 -0.10563742
##
##
    [61,] -1.814044944 -0.329959616 -1.64983402 -1.68233552 -1.28531456
    [62,] -0.115968046 -0.847811966 -0.01003016 0.03440109 0.57157254
    [63,] -0.776615629 0.758237261 0.57676705 0.59029897 0.35010039
##
##
    [64,] -0.121363077 -0.288794186 -0.41045250 -0.73328887 -0.66196854
##
    [65,] 0.366130232 1.266819645 0.68506930 -0.40211576 0.78355815
##
    [66,] 0.342157051 -0.282061789 -1.05467277 1.81050748 1.53995289
##
    [67,] -1.890843570 -0.007999673 0.35759083 -0.92894051 -0.61609394
    [68,] -0.886315112  0.425331443  0.37922314 -1.37184508 -3.16205910
##
##
    [69,] 0.203115313 0.202744056 -0.08369126 -0.86302194 1.49806925
    [70,] 1.544257767 -1.054587963 -0.13821147 -0.64976939 -1.01416787
    [71,] 0.878698240 -1.857629813 0.21799855 0.66165775 -0.89254318
##
##
    [72,] -0.929528757 -0.059210729 0.29586893 0.62938981 0.44865106
##
    [73,] -2.729293376  0.652275275  0.85358515 -0.41264300  1.10408049
    [74,] -0.917322123  0.599911611  0.20309354 -0.25692637  1.06532514
    [75,] -0.169116751 -0.058712493 2.62926033 0.55082365 1.06173571
##
##
    [76,] -2.145836245 0.527115845 1.71469611
                                               1.01308834 -0.66468324
##
    [77,] -1.000843515 -0.916954163 -0.76506668 0.61749749 2.33883997
   [78,] 0.317742870 -0.888471313 -1.80288602 2.03108351 -1.45350517
    [79,] -0.105043124  0.075733589  1.29874331  0.10850501
##
                                                            0.79416020
##
    [80,] 1.706900395 1.446032549 -0.50310384 0.02832838 0.19314380
##
    [81,] 1.086102187 -2.034861339 1.60470968 -1.17693559 0.15912379
##
    [82,] 1.387924461 0.198032763 -0.13271227 -0.44752696 0.81203731
    [83,] 0.005035105 0.518424225 0.02077083 -0.84057661 -0.94062611
```

```
[84,] 1.138312544 -0.604136731 0.45720728 -0.71693518 -0.33193233
##
   [85,] -1.853822403 -1.097456990 -1.37256684 -0.68530351 0.17895583
   [86,] 0.118217518 -0.051464744 -0.11282042 -1.20416914 0.02643375
   [87,] -0.015093722  0.905425982  0.58672403  0.98261030 -0.65969991
   [88,] -0.857132716  0.226408304  0.74059636  0.40167037 -1.44754798
   [89,] -0.244957851 -0.677441645 -1.09956463 0.28555828 0.60914222
##
   [90.] -0.676267239 -0.225655138 -1.04973091 -0.92254897 0.52998811
   [91,] -0.688085570 1.330746752 1.04496069 -1.12372331 -0.09110064
##
##
   [92,] 0.608137569 -0.064539394 1.90648434 -1.32469046 0.04497134
##
   [93,] 0.455644231 -0.040419118 1.18921631 1.34317418 -0.45869359
   [94,] 2.187527129 0.894828109 -0.20120773 -2.92184930 -0.44718955
   [95,] 1.262680412 -1.400728928 -0.90236194 0.09129016 -0.27577862
##
   [96,] 0.514972288 0.559214689 0.33629113 -1.29500935 -0.51194628
   [97,] -1.836850036 -1.849646603 0.08076761 1.21675506 0.47543162
##
##
   [98,] -0.650723951 -0.219909522 0.29803723 0.07699907 -0.37989947
   [99,] 1.461716708 0.503369088 -1.14027970 0.75596474 0.56188420
##
   [100,] -0.735907368 -0.217490144 1.35643360 0.13579091 -1.45567360
##
##
                [,21]
                             [,22]
                                          [,23]
                                                     [,24]
##
    [1,] 1.486544494 -0.3235989214 -0.204312998 -0.18215015 0.629410253
##
         1.429418779 -0.8024237324 0.537098693 0.84847919 0.142172457
##
    [3,] 0.415724694 -1.1027839317 -0.703231253 0.25963593 0.436682371
##
    [4,] -1.152715655 0.5218578046 -0.342783955 -0.93043023 -0.705647521
    [5,] 2.338262397 0.9914110790 -0.970191464 -1.60063756 0.749354744
##
    [6,] -0.855526847 -0.0034909374 0.731360766 -0.04227521 -0.414940840
##
    ##
    [8,] -0.185103197  0.5642470515  0.081515445 -1.68702573  0.900726897
##
    [9,] -0.768259623 -0.7514553646 -0.769186650 0.29585635 0.577981012
   [10,] 2.105095898 -0.3589839726 -0.904308632 -0.44039941 0.545156901
   [11,] -0.085556123 -2.9898983065 -0.344406756 -0.11495783 0.198644983
   [12,] 1.034214973 -1.4688587991 -0.773090826 -0.86402382 1.634676761
   [13,] -0.607445686 1.6444449663 -0.360232416 -0.46877585 -1.520737906
##
##
   [14,] -2.086421946 -0.7396844227 1.013527859 -0.86024458 0.119770365
   [15,] -1.458895990 1.0017528413 -0.252485219 -0.95649209 -0.971567690
          2.202578957 -0.4221935248 -1.149012625 -1.12206912 -2.322941952
##
   [16,]
##
   [17,] 0.648551390 -0.0357759973 -0.308124732 0.14905423 -0.181778045
##
   [18,] 0.650806147 0.1202490670 0.849491084 -0.48016287 -0.139937498
##
   Г19.]
          0.924327470 1.9629828650 0.606606837 1.58646455 -1.424406361
##
   [20,]
          1.050480921 -0.3628995072 1.621191797 -1.67786134 -0.680074807
          0.338043523 -0.5091880076 0.996435663 -0.34928365 0.142498485
##
   [21,]
##
   [22,] 0.508809207 -1.0381482718 1.262935201 -0.33532962 0.003166990
   [23,] 0.979491475 -0.6319293105 0.480346087 -0.84140750 2.047036099
   [24,] -0.197404753 -1.4220666348 0.734535028 -0.92773151 -1.760767873
##
   [25,] -1.227254205 -0.1596757902 0.734115292 2.05308909 -0.408897667
##
   [26,] 0.042020695 1.4672438590 -0.211003233 -0.40320574 -0.962753621
   [27,] 1.363072997 0.7125175341 0.932932075 -1.54761466 -0.772508380
   [28,] 0.488160608 0.6005861251 -1.066335584 2.70931697 -2.006684440
##
##
   [29,] -0.487981832   0.3325938102 -1.001404705   0.37388753   1.115854623
##
   [30,] 0.437187915 0.8605630279 1.080490612 -1.03321489 -1.015642274
   [31,] 1.908224070 1.2554213358 0.944674027 0.04119959 -0.134947035
   [32,] 0.915341808 0.7418908272 1.645398062 0.04273542 0.218332632
##
##
   ##
   [34,] -0.959567734 -2.0875954140 0.536193183 -1.12361635 1.311898854
##
   [35,] 0.419559756 1.3206640670 -0.784389236 2.46238294 0.576075789
   [36,] -1.257902389 -0.2360539338 0.455169545 1.41823134 -1.286948374
```

```
[37,] 0.254069758 1.1705813997 0.362691537 -1.99350073 0.249972851
##
   [38,] -0.995990867 -0.8453241462 -0.779457674 -1.09182552 2.475615211
   [39,] -0.639618651 2.0904464451 -1.475516214 -0.30259885 0.007316852
##
   [40,] 1.126444249 -1.5879908799 -1.073415080 3.73059009 -2.072149234
   [41,] -1.682286115 -1.1670743775 1.407841311 0.37217228 0.256377641
##
   [42,] -0.354833358 -0.9326486771 0.012747114 -0.23208600 -1.194714571
   [43,] -0.728046115 -0.4775987323 0.127142820 -0.55095480 0.858599217
   [44,] 1.019438932 -0.5520600322 -0.944347975 -0.09301349 0.310156676
##
   [45,] -1.004307377 0.5853150488 -1.448737090 0.08333380 0.599589528
   [46,] 0.269327887 -0.5010669019 -0.424351384 -0.22514200 0.410011070
   [47,] -0.701146649 -0.9984973456  0.529748246 -0.24988464 -0.372169867
   [48,] -0.513054545 1.6840479053 -0.924578653 -0.04862039 -0.117925560
##
   [49,] -0.289158429  0.6832639588  0.809886687  0.57695503  0.204250435
   [50,] 0.636659574 -1.3910765353 -1.116320289 0.54701531 -0.401015531
##
##
   [51,] -1.530353878 1.1599038076 1.992398836 -0.27378057 -1.488023177
##
   [52,]
          0.751772893 -0.1372553220 -1.419825571 0.14591443 -0.987738923
##
         [53,]
   [54,] 0.174267082 0.0683090089 -0.050675273 2.00146985 -0.307343355
   [55,] 1.579508775 -0.5975078963 -1.543158291 1.15063605 -0.569063028
##
         1.427547786 -0.6064602386 2.788799303 0.14996446 -1.193947041
##
##
   [57,] -0.003259892 0.6118397901 0.477436311 0.39149972 0.506624336
   [58,] 0.178271728 -0.1480896634 1.225795740 -0.63053026 -0.194827374
   [59,] -0.412907265 -1.5710764248 -0.441708153 -0.28224372 0.303088647
##
   [60.] 0.877775829 0.4994005007 0.472827042 -0.89270932 -0.833926240
##
   [61,] 1.381377262 -0.1905808158 1.477475490 0.09665693 0.424822207
##
   [62,] -2.529703152  0.0441404092  0.300844925  -0.20944654  -0.744037551
##
   [63,] 0.220601929 -0.6270918428 0.998951267 0.51492590 -0.235359375
   [64,] -0.946376282 1.5309132691 -1.049588282 1.71044709 -1.403732019
   [65,] 2.276017180 -0.0574715141 -0.879992572 0.75839216 -0.142720049
##
   [66,] 0.162950612 -0.1600290478 -0.017225214 0.41385806 0.761823558
   [67,] -0.540007445 0.3028011617 0.140886363 0.24565865 1.171043692
##
##
   [68,] -0.602121815 -0.7868412125 0.452628015 -0.20772959 0.653584028
   [69,] 0.085669899 0.4051919939 -0.504976274 2.24820049 -0.985272375
   [70,] -0.883315069  0.5646381789  0.584428453 -2.20950326  1.369883806
##
##
   [71,] 0.007571949
                     ##
   [73,] 1.507515487 0.3806656970 -0.125362035 1.06176849 0.033247113
##
   [74,] -0.598075736   0.2183370412   -0.977435536   -1.66743637   -1.177746027
##
   [75,]
          1.789246376 1.7555390186 -0.079773246 -0.41392108 1.349244011
##
         1.156436169 -0.6257746103 -0.112694236 -0.60413238 -1.096243188
   [76,]
   [77,] 0.373873376 0.7730341492 1.152566604 -1.23106339 -0.356753133
##
   [78,]
          0.453746705  0.4051457203  -0.552587380  1.56168488  -0.455045010
   [79,] 0.427076927 0.2810173765 0.007277129 -2.08747876 0.681410710
   [80,] 1.697406183 -1.6471162395 0.728039425 1.62787306 -1.224720109
##
   [81,] -0.803706471 0.3304010458 0.410543858 -0.88124769 0.880052559
   [82,] -0.787588572  0.6338710564  0.923196102  1.12030881 -0.911171451
##
##
   [83,] -0.315815041 1.6494725209 1.232697263 1.14074262 -0.142513512
   [84,] -0.286563907 0.2941981694 -1.716040085 0.35490801 0.737841357
##
   [85,] -1.358899139 -0.9582380859 -0.444605676 -1.12254184 0.398275531
   [86,] -0.463897751 0.8918981275 0.744655630 -0.37265371 0.835501548
##
##
   ##
   [88,] 0.406827199 0.4817265533 -1.460726388 -0.13560848 -0.516314532
##
   [89,] 0.901696305 -0.2336079451 -1.172511948 0.13054606 -0.314176915
   [90,] 0.991405156 0.0665601392 -0.718376002 -1.25034136 -0.655601705
```

```
[91,] -0.132532929 -0.0009203882 0.119774967 -0.89462996 -0.790352726
    [92,] 1.461366376 -0.3047664478 1.094435626 0.12729225 0.897034681
##
    [93,] -0.286200740 1.9220966947 0.149587568 1.29383636 1.240521272
   [94,] 0.859672112 -0.1755023023 0.433258232 0.81615481 -0.932994244
    [95,] -1.895335524 1.1653708652 1.679915251 -2.49430752 -0.075524150
    [96,] -0.294135805 -0.1015568385 0.516332450 -1.11093913 -0.893621819
##
    [97.] 0.571026111 2.2337862316 0.938633790 -0.37519024 0.244991485
          ##
    [98,]
    [99,] 0.421879198 -0.4233428516 -0.315286391 -0.58324249 -0.417024610
   [100,] 0.503674442 1.6604189809 -0.144705962 -0.57083932 -0.313400666
##
                                         [,28]
                [,26]
                             [,27]
                                                       [,29]
                                                                   [,30]
##
     [1,] -0.654419100 -0.050239212 -0.179593705 -0.5412642092 0.24313425
##
     [2,] -0.471243117 -0.958501916 1.249123094 -1.0980807044 -0.89419289
##
     [3,] 1.969782009 -0.791613872 0.028343562 0.4662856827 0.83411712
##
     [4,] 0.083618813 0.951340939 0.113144239 -0.0015331229 -0.56441588
##
     [5,] -0.020451523 1.193994975 0.363253088 -0.1765255897 -0.64426029
##
     [6,] -0.117166348 -0.010076488 -1.007636990 -1.6990216315 0.92389880
##
     [7,] -1.001736856 0.403841231 0.989514721 -0.2599974630 0.16751154
     [8,] 0.189795992 -1.469611924 -1.223902411 0.8468884040
##
                                                              0.73979986
     [9,] -0.411637359 -0.019054340 -0.059001927 1.9554078723
##
                                                              0.26230199
##
    [10,] -1.078617513 -0.768550924 1.624185343 0.7626828058
                                                             1.34983241
    [11,] 0.828510078 0.572855093 -0.068121610 -0.4517459930 1.89604377
    [12,] -0.752450914   0.237985090   0.351152355   0.3867726863 -0.51567001
##
    [13,] -0.399691195   0.886574450   0.947289323 -0.4911649280   0.88360619
##
##
    [14,] -0.239578620 -0.642266759 -2.184344329 -0.8656065674 -0.44268187
    [15,] -0.047282392 1.370366827 1.409804340 -1.3961015572 -0.81695768
##
    [16,] 0.850394250 -1.680586135 -0.013138661 0.3676432140 -0.52095896
    [17,] -2.519844637 -0.603086508 0.452823681 0.7118569192 1.85608775
    [18,] -0.707272634 0.495665446 -0.733852447 -0.7522104470 -1.36109690
    [19,] -0.634361798  0.720007381  0.092172503  0.3386334934  -0.27737199
    [20,] 2.099514277 -0.709309564 -0.389769314 -0.0761366897 1.83534911
##
##
    [21,] -1.247209583 -1.002681532 0.083475684 -1.1293019969 1.21726095
    [22,] 0.471040093 -0.129963877 -0.723504008 1.3493962443 1.70558035
   [23,] -2.503398492 0.216528403 0.375914569 0.3046603918 1.48458838
##
##
    [24,] -0.005331627 -0.681156205 -0.751502090 -0.6035117360
                                                              1.03595345
##
    [25,] 0.825707242 0.641463456 -1.634883609 0.3587803589 0.08239059
##
    [26,] 0.610067837 0.172888313 1.718887774 -0.8720858954 -0.03379019
##
    [27,] 0.033076984 -2.176387776 -1.333035605 -1.9827983528 0.48271798
    [28,] -1.110960580 -0.761667664 1.601120643 -1.0267524278 0.65378069
##
    [29,] -0.696524934 -1.134924084 0.056342810 -0.3180952137 -0.02173387
    [30,] 0.184089863 1.148876564 0.089127516 -1.0447622484 0.30963189
    [31,] 0.691555011 -0.186783200 -0.272032423 -0.0506149551 -1.22432393
##
    [32,] -0.120443080 -1.145623619 0.539087675 0.6423093072 -0.86690896
##
    [33,] -0.305478183  0.424099629  0.463736055 -0.9789828020 -0.97114009
    [34,] 1.738330798 -0.734831130 0.393861216 0.8920042913 -0.12605099
    [35,] 0.639251032 0.691962676 -1.926994999 0.2662684860 -1.85224646
##
##
    [36,] 0.297904051 0.868593113 0.254259977 -0.5730885735 1.18538584
##
    [37,] 0.016635138 -0.007347875 0.880490266 -1.1148193920 -0.43867884
    [38,] -1.233210767 1.668344847 0.512596190 0.3094258976 0.97228925
##
    [39,] -0.896641393 -1.806830192 -0.469473279 -0.9912486109 -1.21067294
##
    [40,] 0.604069726 -1.120427809 -1.020968261 -0.5134675498 -0.55478744
##
   [41,] 1.446087208 -0.002286627 0.287681222 0.2263194792 1.32107560
##
   [42,] -0.363209096  0.171892756 -1.117088789 -0.6857853905  0.71931680
    [43,] 1.163455107 -0.267609069 0.108020572 2.2772916306 -0.54606377
```

```
[44,] -0.337822418  0.428514296 -1.030308833 -1.5819252424  0.28364403
##
   [45,] 0.282255248 -1.737867314 0.009629276 -0.5382438023 -1.23938020
    [46,] 0.878194422 -1.076714740 1.377196628 -0.2437745629 -1.25184391
   [47,] -2.700746102 -0.436817549 1.327275690 0.3343793764 0.45563710
    [48,] 1.807166771 -1.093999365 -0.799642411 -0.0953824151
##
   [49,] -0.608927686 -2.027681396 0.648558175 0.6178819118 2.13963823
    [50,] -0.247256647  0.309075248 -0.965392374 -0.7690744333  1.32955943
          1.283959346  0.498476757  -1.587231239  -0.5162435856  -0.65741607
##
    ſ51.Ì
##
    [52,] 0.458992757 -2.531659475 1.825473211 -1.4871138266 -0.25250771
##
    [53,] 1.152402589 -0.516198892 0.147676802 0.3596958294 -0.98944528
    [54,] -0.459809076 -1.491445660 -1.166876061 0.4204631595 1.89152764
    [55,] 0.903751483 -0.265392045 -0.931269889 -0.5160932600 0.85121931
##
    [56,] -1.150452676 -0.020673286 0.758878691 0.9050543420 0.75720396
##
    [57,] 0.528167030 0.733947857 0.229197299 -1.2179974703 -0.43314318
##
    [58,] -1.611582610 -0.717924702 0.134021129 -0.8303427916 -0.63511239
    [59,] -1.111999361  0.876897597 -1.312649498 -0.5748482188  0.90457279
##
##
    [60,] 0.642575009 0.019844804 -0.743638323 1.5974921185 1.72484875
    [61,] 0.111807654 -1.550822025 -1.585409206 0.8817679193 -0.41356533
    ##
    [63,] 0.414740761 0.267370359 -0.710709850 0.2039794214 -0.92504661
##
    [64,] 0.101553679 0.451881144 -0.492480644 0.3194450259 -1.27667957
    [65,] -0.768771268  0.284486602  2.379495481 -1.0110507184 -1.44601402
##
    [66,] 0.851107672 -0.128792988 -0.939193296 -1.1931212388 -1.28755972
     [67,] \quad 0.153493406 \quad -0.089328524 \quad 1.302448833 \quad 1.1402100848 \quad 0.59880902 
    [68,] -0.098890111 0.874256060 0.646793509 -1.8724309030 -1.64329760
##
    [69,] 0.973597928 0.719849655 1.592943970 0.6668272254 -0.02667572
##
    [70,] -0.470207937 0.021073845 -2.257547292 0.6645949196 1.71833945
    [71,] -0.736355009 -0.456495779 -0.339939779 -1.9454126924 -0.04122943
   [72,] 1.416337610 0.801022108 1.048549428 -0.0105845146 -2.24715817
    [73,] 0.154363533 0.557056995 0.886114353 0.5500343814 0.54455131
##
    [74,] -0.292578314 -1.966044062 0.527513526 -0.8716298570 -0.07270149
##
    [75,] 1.463625071 0.247697743 0.245432017 -2.1233589915 -0.27973067
    [76,] 0.409714811 0.561401654 -2.466401134 -0.1813943658 -0.28767348
   [77,] 0.641279831 -0.332956445 -0.757004633 -0.2919641579 -0.35776806
##
    [78,] 0.147727891 -1.253583250 -0.661982844 -0.2962613738 1.25938354
##
##
    [79,] 0.609252539 0.391916602 1.107470515 -0.4504974728 -1.10986504
    [80,] -0.764559385 -0.325231764 -0.976565830 0.9133976699 -0.77213872
##
     [81,] \quad 0.379084529 \quad -0.120411524 \quad -1.776431876 \quad -0.4696798230 \quad 0.65013501 
    [82,] -0.817297139 -1.066004499 1.764473529 0.4227220120 -0.26095290
##
##
    [83,] -1.002702192 1.914957713 0.979426434 0.4139624290 0.02885099
    [84,] -0.692338804  0.329324859  1.553503158 -0.5067904521 -1.02913263
##
    [85,] -2.119434766 -1.126547727 -1.031741803 -0.5066789908 0.39860024
    [86,] -1.208946815 1.119828784 -0.349418990 -0.8729564173 -0.77602222
    [87,] -0.028720357 -2.129823414 -0.070263680 0.3442779247 -0.99421674
##
    [88,] -1.400331150 -0.587954920 0.149588783 -0.2740691550 -0.72642596
    [89,] 0.710797184 0.687366120 -0.663651815 -1.0065260838 0.32054892
##
    [90,] -0.756408468  0.920230361 -0.079856275  0.8989159747
                                                              0.70450417
    [91,] 0.293276211 1.668129786 -1.107315091 0.0005904796 0.93420073
   [92,] -0.400282690 -0.015456210 0.449214403 0.5599762846 0.25597019
    [93,] 0.824094750 -0.285388851 0.592773990 0.6113110833 -0.13094452
##
##
   [94,] -0.417231856  0.547440293 -0.401663946 -0.8298472491 -0.14142980
##
   [95,] -2.014346498 -0.391919121 -1.042955012 1.0778955472 0.50324056
##
   [96,] 0.943260482 0.887928790 1.068159148 1.6357067591 0.63004657
   [97,] -0.482522265  0.873410435 -0.888880461  0.1117118733 -0.12205776
```

```
[99,] -2.193372775 -0.211741903 0.981943005 0.8169442893 -0.27453286
  [100,] 0.105539308 0.379439099 0.253250966 -1.2462152102 0.73881234
##
                [,31]
                           [,32]
                                      [,33]
                                                   [,34]
                                                              [,35]
##
    ##
    [2,] -0.962368160 0.10113872 1.03105983 2.2768426102 -0.97110229
    [3.] 2.439034492 0.26715036 -0.31620821 -0.6886149614 0.34606862
##
    [4,] 1.617442451 -0.10598628 1.44530868 0.1657776688 -1.73505853
##
##
    [5,] -0.608181649 -0.17552940 -1.86210692 0.9414013888 0.91060793
    [6,] 1.335723024 0.97773542 -0.79667529 -0.1551671268 1.35449242
##
    [7,] -0.365250927 -0.68402084 -0.64426300 -0.3325038071 0.96339629
    [8,] 1.142577012 -0.57648575 -1.06740906 -0.8336436361 1.18013587
##
##
    [9,] 1.270516021 0.45603296 -1.33852817 -0.0872348839 -1.31892032
   [10,] -1.258225391 -2.69430837   0.60467128   1.2068314679 -0.56626856
##
   [11,] 0.617129802 0.76077872 -1.21422769 2.5642000733 1.07343374
##
##
   [12,] -0.321778756  0.31998613 -2.00149139  0.1895915639 -0.91427901
   [13,] 0.830563183 -0.76264805 0.14090364 -0.3923714090 0.17306503
##
   [14,] -0.166931807 -1.63874162 -0.04221757 2.1831766738 1.67389754
   [15,] -0.017210771 -1.57076859 0.59457687 -0.3902531533 0.36035063
   [16,] -0.057424265  0.28801105  1.52189216  0.3535962877  0.57511436
##
   [17,] 2.005474644 0.59128029 -1.03464804 0.2781717796 -0.10454075
   [18,] -1.626019848 -0.99707928 -0.73271264 0.1585835297 0.17869739
   [19,] -0.478985616   0.04535425   2.14845242   -2.0006774433   -0.29562202
##
   [20.] -0.574651770 0.09080426 0.27501070 0.1295298125 -1.22418035
##
   [21,] -1.515565810 1.05739451 0.15844439 -1.2892531141 -1.06565441
   [22,] 0.331581447 0.37812206 0.69381604 1.4208580340 1.12941408
##
   [23,] -0.497632520 -0.87761481 1.41734440 0.0382099218 -0.47937939
   [24,] 0.929781721 1.70124187 -0.17508395 -0.5429510424 0.34645820
##
   [25,] 1.260819911 -1.85678000 -2.75646428 0.5048220567 0.62960192
   [26,] 0.379313135 -0.18109458 -0.92204003 -0.1459931469 -1.44377423
##
   [27,] 0.086176053 -1.36923438 -0.28565503 -0.8531943835 -0.47127112
##
   [28,] 1.979244768 0.38607421 -0.28288799 0.7278041449 1.55235752
   [29,] -0.315277003 -0.16286423 -0.32883103 -1.2103919775 -0.01310944
   [30,] -0.309893325  0.04468715 -1.11420093  0.1586934618  0.13835402
##
##
   [31,] -1.298108743  0.33370307  0.06210234  0.9769266560  0.98349488
##
   [32,] -0.684598866 -1.13027529 -0.51369768 0.0728238931 0.06050880
##
   [33,] -0.879673895 1.72400259 -3.81050110 0.5450248664 0.04134137
##
   [34,] 1.120075577 -0.51657600 0.71870847 0.2344996811 -1.00754114
   [35,] -1.441066807 0.92630923 -1.91087820 0.8227203861 0.50319972
##
   [36,] -0.150264718  0.03684689 -1.18977685  1.5489010446  1.46516563
   [37,] 0.532866267 0.49791031 -0.13306511 0.0831806229 -2.50115630
   [38,] 0.176687636 -0.80700062 0.16290983 0.0747209516 0.74978328
##
   [39,] -0.522372260 1.85157801 -0.83339782 0.1593604724 2.78336175
##
   [40,] 0.277292583 -0.18455138 0.84289875 0.1875945098 0.19353380
   [41,] 0.396106432 0.96704589 0.22513138 -0.5346145923 0.64121733
   [42,] -1.071291749 0.26902470 0.14829254 0.4374551094 -2.01560412
##
   [43,] -1.567761170 -0.23773411 -0.22871413 1.3984397746 0.40684058
   [44,] -0.858156146 -1.59763083 1.12918831 1.2324160051 -0.88234275
   [45,] 0.177417967 -1.01610281 -0.88953574 -0.6749405786 0.01656230
##
   ##
   [47,] 0.002580789 0.63458158 1.56865161 -1.1772593518 -0.94949100
##
   [48,] 1.382920979 -0.55680065 1.78130458 0.2699998524 1.26812538
##
   [49,] -1.453238488 -2.45667553 0.86194746 0.0965096642 0.96515083
   [50,] 0.921161418 -1.66019091 -1.37404027 -0.1698614483 -0.39190610
```

```
[51,] -0.448951203  0.07169230  0.75638492 -1.5141597470  0.06678323
##
   [52,] -1.353921650 -0.81092612 0.48734146 -1.6054677957
                                                          0.94340122
   [53,] -0.225628343 -1.22927976 -1.03284365 -0.9805346756
   [54,] 2.642563088 -0.46954316 -0.77529676 0.1182806759
                                                          1.78135539
   [55,] 0.678694610 0.98601568 0.33735549
                                            1.0181166389
                                                          0.30022397
##
   [56,] -0.029166320 -0.54934600 1.01932292 1.5145863928
                                                         0.28088413
   [57,] 1.258127319 -0.16184639 -0.06386392 -0.6704017420
                                                          1.95606050
   [58,] -0.592231527 1.74653446 -0.56231909 0.3622736907
##
                                                          1.00987851
    [59,] -0.615142157  0.33979108 -1.42915126 -1.2835758012
##
                                                          0.89724730
   [60,] 0.834189393 0.09329722 -0.26291493 -0.0050408594 0.12085075
##
   [61,] -0.649577998  0.93625188  0.04535950 -1.1521487761 -1.74129536
   [62,] 0.231775601 0.25282603 0.50991864 -0.3144022008 -0.41564235
##
   [63,] 0.146476319 0.15534353 -0.39473548 0.7164956840 1.61168557
   [64,] -0.107814067  0.80251925  0.76984259 -1.0097423891 -1.38224345
##
##
   [65,] -0.348574876  0.39067306  0.06676853  1.2512547460 -0.48871759
##
   [66,]
         1.321726779 -1.00600271 1.61213296 -1.9048212414 -0.37047751
    [67,] \quad 0.360024341 \quad -0.48008474 \quad 0.05939724 \quad -0.6675926477 \quad -0.27196231 
##
    [68,] -0.331298790 1.80225114 -0.17768728 -0.8198324017 -0.22983539
   [69,] 0.716552124 0.33513189 -1.06658156 -0.4447576659 -0.63861396
   [70,] -0.861910151 -0.36384938 -0.29936801 -0.5676592104 1.29365720
##
   [71,] 1.066044325 1.45623415 -0.10601684 -1.2453085198 -0.53889293
   [72,] 0.269873688 -0.06842974 0.34621917 0.3008715385 -1.10020316
   [73,] 1.389260828 0.33885628 -0.80014470 -0.7914570404 0.38870434
##
   [74,] -0.657188769 -0.81580735 -1.14148261 -0.0002869956 0.07622615
   [75,] -0.841335219 1.31907519 -0.35613771 -0.1302131340 2.23140713
##
   [76,] 0.782499239 1.30031603 1.92303403 1.6056672192 -0.25665453
##
   [77,] -0.574874069 0.16640858 2.45918504 1.4423659506 -0.74639815
   [78,] 0.788720942 -0.32293951 0.29969544 1.0494184532 0.51217601
##
   [79,] -0.139585145  0.63363022 -0.03689899  0.2147429968  1.17050184
   [80,]
          0.244085046 1.57310610 -0.54004841 1.9434000062 -0.17949837
##
   [81,]
##
   [82,]
          ##
   [83,]
          1.343578157 -0.95049220 -0.82734767 0.5120467677 -0.34146024
          0.334926133 -0.18411785 -0.24641328 -0.3898250104 1.75150108
##
   [84,]
##
   [85,]
          0.185692580 -1.00313452 0.16369610 1.4117973572 -1.69205372
##
          0.642708106 1.67817230 1.08335376 0.6817050720 -0.44440017
   [86,]
##
          1.225622005 -0.13733784 2.51355546 -0.6877775562 -1.93330046
##
   [88,]
          1.271143614 - 1.10727844  1.43097640  0.4347588520  0.55028065
   [89,]
         ##
         2.188556506 -0.86085245 0.01251993 1.9527722465 0.71407476
##
   [90,]
   [91,] -0.934087396 -1.06954147 0.98811340 0.3610535889 -0.10141971
   [92,] 0.156463384 0.01292533 -0.60619527 0.5758967700 1.38438170
##
   [93,] 1.164985574 -0.12977820 1.42550466
                                            1.5166958025 0.78774317
   [94,] 0.973055295 -0.88054549 1.13266969 0.6004179055 -0.65683933
##
   [95,] 0.586867373 -1.42940580 0.43630697 1.1932126304 1.68564422
   [96,] -1.622251182 -0.36750302 0.88160521 -0.5457185463 -0.69549520
##
   [97,] -0.730915755 -1.80703597 0.62004354 -0.4530841516 -0.47432417
   [98,] 0.139972042 -0.19215516 -0.72825643 1.4022960939 0.52348910
   [99,] -1.703524347 1.68055626 -1.48545593 -0.9657495394 1.53648443
##
   [100,] 0.014169810 0.47730208 -1.59925593 -0.7151518210 -2.48018983
##
                           [,37]
                                       [,38]
               [,36]
                                                   [,39]
                                                               [,40]
##
     [1,] 0.14320492 -0.400441746 0.81472437 0.185189569 -2.740020152
##
    [2,] -0.73812063 2.354198962 -1.06036648 0.167502602 0.083627419
    [3,] 0.67040380 0.392796424 0.48093828 -0.030910536 -0.708627632
##
```

```
##
    [4,] 1.67136032 -0.563437720 -0.27291881 -0.458465991 -0.938306488
##
    [5,] 0.12337542 -0.136785667 -0.03335821 -0.789000426 0.847839355
##
    [6,] -0.61346736 -0.432630687 -0.20813939 2.253229769 -0.203780272
##
    [7,] -0.22069209   0.352494094   -1.51820326   -0.848616346   -1.207554246
##
    [8,] 0.18172095 0.294682536 0.41869490 0.994266887 0.043313592
##
    [9,] -0.35524160 1.001565684 0.09480739 0.165720110 -2.311639876
   [10.] 0.65696003 -2.391047817 1.13157082 0.180814989 -0.725538734
##
   [11,] -0.85412069 -0.403247940 -0.24153343 0.590602585 -0.361933881
##
   [12.]
          0.43737409 -0.817693300 0.44964211 0.390897487 -0.204134177
   [13,] 0.24576140 1.621190808 -2.29344962 1.282933927 1.173807367
##
   [14,] 0.68892022 0.225821817 0.33138345 -0.095666785 -1.017211194
   [15,] 0.66561602 0.581117087 0.83947285 -1.570304116 0.130843118
##
   [16,] -1.19914285 -1.361397556 -2.32491017 -0.009753811 -0.724513652
   [17,] -1.00740154 -0.504935596 1.59253367 0.356074020 1.463416733
##
##
   [18,] 0.08435617 0.693101545 -0.43490682 1.198657523 0.356666049
##
   [19,]
         1.33057002 0.507029336 0.29909486 -0.454808224 -0.083282441
##
   [20,] -1.71025141 0.243915113 0.94625383 -0.272802782 0.582300779
##
   [21,] 1.03019529 -0.808675869 0.44799168 0.321435423 0.782533170
   [22,] 0.94443417 0.364380805 0.30231270 -0.253796563 0.218754165
##
##
   [23,] -0.28893881 -0.051061301 1.11843607 -0.458485728 -0.484485202
##
   [24,] 1.09866740 -1.559032645 0.54957890 0.186474259 0.047968425
   [25,] 1.02885888 -0.087901243 -1.37293158 0.330612365 -1.795648165
##
   [26,] 0.25401578 -1.969012845 -1.92423435 -1.463336760 1.823412623
   [27,] 0.38743445 0.401977576 -0.29714843 -0.501538463 -0.261574883
   [28,] -0.09626496 -1.037468546 -0.46174736 1.411587690 -0.519476575
##
   [29,] 1.46944497 2.459395748 0.50634576 -1.089252478 1.589545044
##
   [30,] -1.62352936 -0.280890993 -1.35654998 -0.259290692 0.184036000
   [31,] 0.30770687 -1.517718753 -0.91188444 0.520078466 1.063601609
##
   [32,] 0.83738642 0.625607373 -0.03180701 -2.299647623 -0.311229273
   [33,] -0.66169007 1.321614798 -0.80885606 -0.770736028 2.163321418
   [34,] -0.28727240  0.854383716  0.41323932  1.000062564 -1.030809827
##
##
   [35,] 1.57126902 0.004012215 -0.68428435 -0.179405500 0.605532809
##
   [36,] -0.24891714   0.021689424 -0.15637971   0.794989551   0.346580284
   [37,] 1.52149464 -0.555790338 0.95843451 0.808442506 -0.256257929
##
   [38,] -0.58448430 1.191803186 0.35420176 -0.538729603 -2.167291112
##
   [39,] 0.36654694 0.027467952 -0.03914752 0.319712457 1.969328424
##
   [40,] 1.02637111 -0.502772046 0.46866878 1.479549150 0.418161048
##
   [41,]
          1.20238594 -0.930060325 1.15977430 -0.138294863 0.689507984
##
   [42,]
##
   [43,] -0.54387615 -3.538447232 0.31520110 1.064874410 -2.307820776
   [44,] 0.57090897 0.933127018 0.40654064 0.079821862 -0.972606283
##
   [45,] 0.14502402 -0.738544615 -0.27425881 0.361549884 1.897705778
   [46,] -0.92665334 -0.109387809 -1.33442507 -2.520853883 -1.252181481
   ##
   [48,] -1.55012957  0.728858143 -0.29276869  0.174527619 -0.420470878
   [49,] 1.68423067 0.034492621 0.36186125 -2.677299974 0.636099495
##
   [50,] 0.23177696 -0.692315016 1.58468186 -1.652454817 1.736058838
   [52,] 0.95120275 -1.179793528 -1.36298028 -0.547894305 -0.170660932
##
   [53,] 0.07731257 0.756144033 -0.10101094 -1.125308166 -0.946236662
##
   [54,] 2.07641029 -1.075566948 1.98548078 0.419629111 -0.677164115
##
   [55,] -0.51596325  0.401085660  0.30252628  1.924245316  -0.359926084
##
   [56,] 0.44576646 -2.366415207 -0.16069696 0.053181186 0.534045508
   [57,] -1.28325242 -0.294160845 -0.93922249 -2.308369671 -0.349763909
```

```
[58,] -0.85331167 1.014415161 2.04697691 0.046901518 -0.519781053
##
   [60,] 0.13835671 -0.592990431 0.91618287 -0.162866042 -0.628074859
##
   [61,] 0.88023186 0.509211517 0.15279458 1.017571489 -1.269550400
   [62,] -0.39404565 1.235929266 -0.88402616 -0.867854596 1.067906500
##
   [63,] -0.58518965 -0.102918418 0.77321097 0.254074406 -0.862206091
   [64.] 0.90117752 1.160975098 1.97589267 -1.731784486 -0.460924950
   [65,] 0.51467409 -0.476399444 -1.20936771 -0.300324927 1.066889017
##
   [66,] 1.03925876 -0.530226967 -1.24422626 -0.090712041 -0.816232954
   [67,] -0.45024976 -0.761088428 0.06655033 -0.240384517 -1.966620037
##
   [68,] 1.23418441 -0.402096367 0.15221176 0.984529856 2.129210115
   [69,] -0.67064166 -0.387507007 -1.30075740 -0.431859323 -0.941423021
##
   [70,] -2.73433780 1.203443720 -0.91427739 0.219587887 0.512041458
##
   [71,] 0.19304188 -0.147111076 -0.52688090 0.890780728 -0.046326599
##
   [72,] 0.84877137 0.377932602 -1.48914844 0.642729155 -1.459201604
   [73,] 0.84090509 0.612498410 -0.39486488 1.001299643 0.457529409
##
##
   [74,] -1.60209440 -0.703125473 0.50043520 0.169353428 -0.945386723
   [75,] 0.58829104 -0.240613522 -0.71251340 -1.101479763 0.095463990
   [76,] -0.48668341 1.304584155 -0.38090163 0.413177200 1.324343076
##
   [77,] -1.90158570 -1.946690795 -0.04527455 -0.879478431 -0.194863104
   [78,] -0.10417117  0.731844064  0.24417740 -0.091938863 -1.171475626
##
   ##
   [80,] -0.28228700  0.801807575 -0.26125847  0.225070945  1.078140091
   [81,] -0.71447890 0.429740974 -0.91695583 -1.173302458 -0.262568945
   [82,] -2.10630007 -0.168677770 0.52498136 1.119539669 0.285490338
##
   [83,] -1.84955461 0.304209863 1.31178682 -0.044027330 1.384459765
##
   [84,] -0.49681393 1.446217437 0.20313568 0.381450334
                                                      0.760300204
   [85,] -0.87645171 -0.709555610 -0.07693168 0.524256343
                                                      0.471976445
   [86,] 0.62274653 1.036894974 0.08349875 -0.457824994 1.882027646
##
   [87,] 0.72015484 0.022371035 0.49181724 0.121002392 1.344160394
   [88,] -0.63549346 -0.851382710 0.75722169 0.295998925 -0.480144263
##
##
   [89,] -0.83516607 0.079357343 -0.32562599 -0.083620251 0.406460052
   [90,] -0.83886743 -0.486421033 -0.45732155 0.432432969 -0.327905934
   [91,] -1.31877026 -0.179337584 1.48314130 1.470338398 -0.004744144
##
##
   [92,] -0.32623394 -0.002692377 -0.49028371 0.596831166 0.064257541
##
   [93,] 0.16954399 0.126026483 0.04033577 -0.262250082 -0.256998302
   [94,] -0.09315430 -0.534438065 0.09812260 -0.382759412 -0.648203322
##
   [95,] 0.53392198 -1.135612742 -0.87762757 0.859389512 0.514001842
##
   [96,] -1.19884526 -0.549114572 -1.56752591 0.239325715 -1.303515062
   [97,] 2.04488234 0.004498460 0.13043188 0.113843457 0.297524061
##
   [98,] 1.53859083 -1.073112445 0.95528916 1.372440721 1.336885789
##
   [99.]
         0.32563649 0.097049639 0.59309685 1.572718137 -0.017593335
         0.69851180 - 0.643065216 - 0.99225559 - 1.391946743 - 0.721318841
##
  Γ100.l
##
              [,41]
                          [,42]
                                     [,43]
                                                [,44]
                                                           [,45]
         ##
    [1,]
         0.67130644 1.737528563 1.11148325 -0.999005740 1.94904862
##
    [2,]
##
    [3,]
         0.99467483 0.298205415 -1.20286481 -1.573859457 -0.28044474
         1.51385687 1.587901586 0.51636888 1.123847157 -0.98452119
##
    [4,]
##
    [5,] -0.55873290  0.321048076 -0.03039004  0.515496723  0.84178835
         0.08473509 -0.580245977 -0.33364271 0.790880080 -0.79019699
##
##
         [7,]
##
    [8,] 0.41975296 -0.818724518 -0.14934735 0.293741203 0.61477009
##
    [9.]
         [10,] 0.65857519 0.174246357 1.42022304 0.687006774 0.21802809
##
```

```
[11,] -0.95910466  0.647382632 -1.50964839  0.280406124 -0.71226174
   [12,] -0.57904067 -1.414536756  0.66398726 -1.259469296  0.67286886
##
   [13,] -1.71934653 -0.366557085 -0.45609749 -0.103500346 0.50316102
   [14,] 0.13800814 -1.940060597 0.94533395 -0.687613596 1.08755835
##
   [15,] -1.68891893 -0.414100766 1.89629602 1.130250163 -0.97038286
##
   [16,] -1.30513431 1.080423074 0.51202425 -1.742349813 0.08687690
   [17.] 0.79465338 0.167792445 0.59131220 0.362034705 -1.94912618
   [18,] -0.46823691 -0.986286802 0.53813342 -1.010038425 1.61663016
##
##
   [19,] 2.52006504 1.952398442 -1.05532485 1.048582068 -1.57868017
   ##
   [21,] -0.58464894 -0.144201833 -0.54562300 0.714916804 -0.84245898
   [22,] 0.36920252 -1.026789984 -1.32531124 0.944087356 -1.61216592
##
##
   [23,] 1.76511903 -2.062483100 2.30446956 0.000350976 -0.17572740
   ##
##
   [25,] -1.04534733 -0.306286094 -0.97635653 1.162389131 0.62447660
##
   [26,] 0.38859592 1.909150463 -0.13911654 -0.357255213 0.97841770
##
   [27,] -0.91533345 2.737760839 0.21276633 -0.396581185 -0.51472914
   [28,] -1.66256924 -0.090137250 0.07301886 -1.669205839 -0.22738043
   [29,] -0.44674917 -0.914044628 2.15215481 0.109106270 -0.86652067
##
##
   [30,] 0.80820277 -0.998730959 0.89060260 0.813374948 0.54860682
##
   [31,] 0.75659300 0.634069955 0.13827011 -0.924416020 0.03386926
   [32,] -1.62902739 -1.312776123 -0.08225089 -0.467372012 0.65632608
##
         0.76268048 \ -0.014134349 \quad 0.13030174 \ -0.669815292 \quad 0.14022959
   [33,]
         ##
   Γ34.]
   [35,] 0.84303105 0.867441451 -0.20753165 0.383064111 0.19440098
##
   [36,] 0.63694281 -1.172821028 -1.34779892 2.072182241 -1.28005763
##
   [37,] 0.52400474 1.012513721 0.19856653 0.173983582 -0.04360924
   [38,] -0.57848612 -2.027173345 0.85155099 0.344229006 1.11255754
##
   [39,] -0.67357263 -0.019338593 -0.50916976 -1.164474667 -0.34754729
   [40,] -1.49778411 -0.107543888 -0.32053619 0.984769675 -0.68126357
   [41,] 1.94665717 0.865167246 0.27404756 -1.853479409 -0.34822489
##
##
   [42,] 1.16760410 0.084604591 -0.36844915 0.797463324 0.93236829
   [43,] -0.62797889 1.915785129 -0.02438251 2.425950536 -0.52666848
   [44,] -0.72470762  0.614354691 -1.26141541 -0.379772586  0.34472708
##
##
   [45,] 0.63830077 -0.194662106 -0.88111657 1.142340351
                                                      0.16958871
##
   ##
   [47,] -0.46646183  0.028031771 -1.22982567  0.336509614 -1.69933133
##
   [48,] 0.63571219 0.346030157 -0.58236522 0.778085643 -0.02502248
   [49,] -1.21169512 -0.008717727 -1.66397029 0.133143151 2.21279728
##
##
   [50,] 0.01520945 0.380617968 -0.25821773 1.010358599 -0.45346367
   [51,] 1.29976985 0.557451043 -1.49459008 0.370720431 -0.42510979
   [52,] 0.59515972 0.356241471 -0.03569452 -0.407100689 -0.46043818
##
   [53,] -0.42671029 -1.287116686 -1.55481658 -1.569859494 0.10759310
   [54,] 0.48844020 0.248883173 -0.49299726 0.069602082 -0.99657155
##
   ##
   [56,]
##
   [57,] 0.06627046 -0.188936600 -0.52969708 -0.931355963 -0.28815084
   [58,] 1.71403156 -1.104780251 0.29832056 -1.235935840 -0.24904337
##
   [59,] -0.16752383 -0.202681113 -0.50278243  0.816856375 -1.15493468
##
   [60,] 0.54006490 -0.295579047 -0.30080871 0.947793849 -1.41787969
##
   [61,] -0.33345388 2.016821415 0.70450108 0.667643155 -0.23431676
##
   [62,] 0.79122392 0.599420584 0.68643110 -2.508643145 1.61428580
##
   [63,] 0.35327105 -0.270319555 -1.44888873 0.586569441 1.30401790
   [64,] -0.78107164 -1.020454481 -0.63770777 -1.089804196 -0.63926192
```

```
[65,] -0.02412029  0.093812649  0.03856060  1.461346636  1.76312643
##
    [66,] \quad 0.30401684 \quad 1.002702337 \quad -1.26127914 \quad 0.019216570 \quad -0.75803737 
   [67,] 1.50819469 1.186347542 -1.21046539 -0.726037115 -1.33835262
   [68,] 0.21392458 -1.536256006 -0.62148634 -1.005815086 -0.29797016
##
   [69,] -1.00945560 -0.607841855 -1.35736211 0.516245483 0.28096052
##
   [70,] -0.48841857 -1.859337861 1.12264341 0.234661788 -0.99275627
   [71.] -0.15916131 -0.180956582 0.35234402 -1.002828251 0.54874891
   [72,] 1.29903957 0.387491058 1.72087981 -0.051290168 -0.28988928
##
   [73,] -0.86108936 1.017692348 0.13490023 -0.282474773 0.09690304
##
   [74,] 0.23961718 1.849294587 0.35320395 0.413013670 -0.47773276
##
   [75,] -0.40541064 -1.396525177 -0.35470619 -0.602285319 -1.55772534
   [76,] 0.91064441 0.157204900 0.98749806 0.745238330 0.38022402
##
   [77,] 0.72435843 -0.677398273 -0.19911238 0.964357216 -0.58667547
##
   [78,] 0.17936373 0.423494794 -0.25984655 0.940277680 -0.13681541
##
##
   [79,] 0.91707802 -1.168063533 0.22917649 0.594284018 -1.24317933
##
   [80,] 0.87417649 -0.475585021 -1.26582676 1.561602550 -0.24434669
##
   [81,] -0.81062770 -1.015410291 1.38831412 1.868497326 0.62882936
##
   [82,] 0.03754786 -0.440343273 -0.60577417 0.069883502 -0.32022877
   [83,] -0.82677325 -0.508411161 0.91594011 -1.383610039 -1.88411471
##
   [84,] -0.28612457  0.296198802 -0.12404305  0.398865770 -0.78933997
##
##
   [85,] 0.39432667 -0.443209072 -0.25893873 0.795897532 -0.65254849
##
   [86,] 0.54546579 -0.428825241 0.21167531 -0.952975796 0.23269429
   ##
   [88,] -0.07606592 -0.451440214 -0.10127334 -0.177052343 -0.26688009
   [89,] -1.62702732 -0.342354489 0.83318053 0.300380543 -0.80256980
##
   [90,] 1.11229297 -1.604112519 -0.16278131 -0.154208405 0.28506262
##
   [91,] 0.24187062 -1.328253208 -0.24799367 0.795414343 1.31015359
   [92,] -0.30538875  0.004627850  0.16817262  0.238233851
                                                        1.48739512
   [93,] 1.14727895 -0.690651735 0.57976239 0.638765904 1.25289105
##
                                                        0.26966463
   [94,] 0.41107381 -1.643806133 1.50945186 0.311459391
   [95,] 1.15249695 1.202418230 0.69600699 -0.893564370
##
                                                        2.45112730
##
   [96,] -0.04417171 -1.829867166 -0.87599532 0.240399439
                                                        0.20705325
   [97,] -2.90664545  0.800176073  1.39963427  0.042198110
##
                                                        1.27503432
   [98,] 0.59284028 0.792793791 -0.54593282 -0.819062178 1.58352737
##
         ##
   [99,]
##
  Γ100.
          ##
                            [,47]
                                         [,48]
                                                     [,49]
##
          [1,]
##
          2.366528822 -2.183436265 -0.0778726244 0.238040139 0.09840594
    [2,]
##
          0.070613390 \ -0.285622591 \ \ 2.4809687014 \ -0.511065483 \ \ 0.22695521
    [3,]
          0.851844989 -0.768101954 -0.2568782116 0.065828408 -1.73802270
##
    [4,]
##
    [5,]
          1.243866977 -0.346709167 -1.1641869523 -1.048615498 0.35155713
    [6,] 0.884429090 1.497954176 -0.6462414652 0.770909152 -0.05670992
##
    [7,] 0.552875818 -0.344291794 0.4089862842 -0.342673106 -0.41737632
##
    [8,] -0.747852605 -0.237114990 -0.1905044249 1.332878504 -0.45444696
##
    [9,] 0.236657382 -0.742030664 -0.2127643581 -0.168060064 -0.51543266
##
    [10,] -0.250187840 0.778452103 2.3032508801 2.294858767 0.35040369
##
   [11,] -0.115478771 0.779613998 -0.7036865267 0.403904485 1.24567966
##
   [12,] -0.306491416 -0.977003508 -0.8617318637 -1.230090064 -0.42109524
   [13,] -0.167557109 -0.984052390 0.9434537420 0.004948872 -0.02758531
##
##
   [14,] -0.236975114 -1.200961803 -0.9258932235 0.072259731 2.97862100
##
   [15,] 0.835882853 2.075910418 -1.0638663447 0.833311126 1.92645674
##
   [16,] 0.048871012 -1.152690910 1.2960777989 -0.982130667 -0.10367918
   [17,] -0.301566389 -0.023143877 0.2397514098 0.022690994 0.71089371
```

```
[18,] -1.028501816  0.847056981 -0.5341901183  0.881216710  0.15188141
##
   [19,] 0.769464609 0.294178482 -0.1045835537 0.463338615 -0.04209345
   [20,] 1.041307745 -0.533291966 -0.5926457824 0.835195434 0.89647058
   [21,] 0.314870090 0.005193754 -1.5772564893 -0.394307503
##
                                                           1.05052156
   [22,] -1.241337521 1.243469731 0.3186206176 -0.745004728
##
   [23,] -0.536441078 -0.562977351 2.4530230270 -0.735733946 0.35584862
   [24.] -0.967519173  0.903312593 -1.0694495419 -0.113126441 -0.65206887
   [25,] -0.119030564 0.273350471 0.6977384708 0.145608037 -1.27347627
##
##
   [26,] -0.506082011   0.884175577 -1.7915661976 -2.082817077 -3.18628158
   ##
   [28,] 0.023501657 -0.260667825 1.2889933925 0.305593054 0.07842694
##
   [29,]
          1.756860702  0.762492602  1.4468383402  -0.724404654
                                                            0.51053692
   [30,] 0.379465509 1.868183137 0.0150717149 1.548066645 1.15063408
   [31,] 1.662442224 0.058455429 -0.5056930546 -0.380178081 -0.08887505
##
##
   [32,]
          0.214848145 -0.108218187 0.0163380023 0.506556422 1.09920724
##
   [33,] 0.684830959 -0.664759673 -0.0518546653 -0.158417969 -0.53569673
##
   [34,] 0.058684180 -0.569615106 -0.8895235439 1.275255371 0.46547711
   [35,] -0.757822977   1.489537560 -0.1416589924 -0.044343893   0.33107192
   [36,] -1.605898393  0.025605843  0.1907113696 -0.927531307  1.21731919
##
   [37,] -1.120746318 -1.202986661 0.3138378429 0.010741054 -0.06134066
##
   [39,] -1.208373776 1.836338280 0.9858297895 -0.953047602 0.18998190
   [40,] -0.516552771 1.055449712 -2.3699037424 0.251130267
##
                                                           1.32503702
   [41,] 0.956483197 -1.628456736 0.1211119762 0.514375547
                                                            0.28761763
   [42,] -0.281040909 0.503728629 -1.9751898664 -0.421784350 0.37376794
##
   [43,] 0.415015272 0.845130383 -1.0436742031 0.160803378 0.89691377
##
   [44,] -0.131062346 2.107145875 -1.4357608500 -1.039877104 -2.52152841
   [45,] 2.056301042 -0.593908157 0.8842966897 0.763382473 1.04793700
   [46,] -0.093046324 1.533352652 -0.3099433416 -1.363946303 1.24738404
   [47,] 1.558459060 -0.283756616 -0.8637519715 1.009251997 -0.65326300
          1.388482977 -1.047772839 -0.4681344198 -0.297178532 1.62819547
##
   [48,]
##
   [49,] 0.987990195 0.274739622 0.6400129529 -1.908582913 -0.41260073
##
   [50,]
         1.171240210 0.744237040 -1.0120898220 -0.269249054 0.16220721
   [51,] 0.180848726 0.226732030 -1.6986480899 1.134523666 1.78337057
##
##
   [52,] -0.359804725 -0.203772195 -2.1650946276 -0.711258879 -0.46504432
##
   [53,] 0.332630161 0.541094333 -0.0996671451 0.261286018 -0.64811102
##
   [54,] -0.853933148  0.568937178 -0.6550409584  0.098838790  0.01570445
##
   [55,] 0.785582632 0.051553185 -0.6067434914 -0.937049313 -0.09981181
   [56,] 0.135492950 1.724991840 0.3784023825 -1.034936019 1.76830821
##
##
   [57,] -1.381721495 -0.800199397 -0.2642685195 1.379492156 2.14951791
   [58,] 0.775767865 -0.319530203 -1.8186768203 0.019931506 -1.01822075
##
   [59,] 0.666317674 -0.620905211 0.2964722548 -1.169117020 0.13054217
   [60,] -1.421465495 -0.950731808 1.4466948444 -0.478913042 0.01404745
##
   [61,] 0.451219895 1.112159030 0.3902103611 -1.099125775 -1.91524738
   [62,] 0.574439180 0.971240817 -0.0004197991 -0.404064029 0.57736897
##
   [63,] 0.678981294 -2.121620034 -0.7174449292 -0.711293600 -0.68456453
   [64,] -0.515181567 -0.021339896 -0.3647216322 -0.025358357 -0.26418308
   [65,] -0.339152036 1.627506558 -0.7366892650 1.306782652 1.40786757
   [66,] 0.967268812 1.062229416 0.1739818563 -1.405215631 0.39792615
##
   [67,]
         0.946691443 0.189351309 -1.0232724592 -0.470358091 1.19964162
   [68,] 0.128616081 -0.138332125 1.0411592284 -0.881795013 -0.14348428
##
##
   [69,] 1.887666971 0.414680006 0.3786647873 -0.192050674 0.84857893
##
   [70,] 0.294687296 -0.923090412 0.1612801020 1.095728552 -1.28109897
   [71,] -1.333677187  0.383704347  0.4267557785  -2.403652389  0.21424427
```

```
[72,] 0.300852378 0.379337289 0.0678474382 0.705337944 0.66430148
##
    [73,] 0.375606897 -0.946924745 -0.0423591011 -1.107302806 0.63724603
    [74,] -0.790283886 -0.887737707 1.5525767711 0.111051351 -0.02304846
     [75,] \quad 0.348869844 \quad -0.258908740 \quad 0.2774183814 \quad -0.470791147 \quad 0.04570067 
    [76,] 2.310154659 1.305007256 -1.3720298860 -0.440910551 -1.03960838
##
    [77,] -1.156190885 -0.574944515 0.7162865530 0.616704794 0.21149674
    [78.] 0.676121375 -1.363038544 0.4604977015 -0.641337673 0.67815822
    [79,] 0.358765870 -1.464494255 -1.2200836132 -0.233599182 0.77338020
##
##
    [80,] 0.608672140 -0.375101962 1.7462060886 -0.130948293
                                                               0.14690656
    [81,] -1.285378355 -1.198781626 0.7236657867 1.255156875 0.23076040
##
    [82,] -0.275692692 -0.245655958 2.3827872567 -0.083980528 -0.10372872
    [83,] 1.114567787 0.068641172 -0.4943093951 -0.418674869 1.97124141
##
    [84,] -0.201912042 -0.118038092 1.5618439479 -0.453500361 0.32538627
    [85,] 0.978668241 -0.234477556 -1.6816132159 -0.215659268 -0.24922975
##
##
    [86,] -1.944200140 2.001904740 0.2435402813 -0.380183140 -0.50497822
##
    [87,]
          0.087166342 -0.567805537 0.0113463247 -0.584388023 -1.58881492
##
    [88,] 2.136754507 -0.282463614 -0.5213030623 0.274929250 0.57080528
    [89,] 0.961580180 -0.152903199 0.4429544154 0.213983588 -0.96840648
    [90,] -1.001465438 -0.077864281 0.5060307586 -1.655198425 1.63480036
    [91,] -0.678946209  0.052654845  0.4931991590 -1.891165953 -0.39867591
##
    [92,] 0.251229201 0.991316353 -1.4354947503 0.055910271 0.96817648
    [93,] -0.003981987  0.544220324  0.0769913103 -1.423887222 -1.31611458
##
    [94,] 0.046890293 0.526014886 0.2557475002 -1.577084167 -0.23624960
    [95,] -0.059578199 -0.765785237 0.3020227412 -2.142167898 -0.64339771
    [96,] 0.792895276 -1.325325299 0.4463114307 -2.401616622 -0.98342396
##
    [97,] -0.536630738 -0.720519491 -0.9148885536 1.302882061 1.20845255
##
    [98,] -0.212497242 -0.304770886 -0.2283477971 -0.298277879 -0.22188836
    [99,] 0.020041741 -0.606367470 -0.5145741737 -1.518651101 0.07158057
   [100,] -0.053497783 -0.829589946 -0.6485415277 0.410241217 1.47840370
##
##
                 [,51]
                              [,52]
                                         [,53]
                                                       [,54]
                                                                   [,55]
##
     [1,] -0.186897778 -1.204103797 0.23870237 -0.139136874 0.76714552
##
     [2,] -0.541697958 -0.488088643 0.19187708 0.346691589 -0.34227445
##
     [3,] -0.969374090  0.363516263  0.23596381 -1.203131897 -0.21005314
     [4,] -1.509418340 1.283297759 0.11803988 0.744453043 0.50160855
##
##
     [5,] 0.764459473 0.993771793 -0.05141983 -2.486368239 0.84778821
##
     [6,] 0.022627070 -0.095485581 -0.13087880 -0.411055508 -1.84458694
##
     [7,] 0.340423337 1.033111129 -1.39226290 -1.568834021 -1.56537088
##
     [8,] 1.025502154 -0.988951201 0.18574049 1.708553312 -0.08020142
     [9,] -0.179746640 1.034728197 0.92264780 1.663539021 1.62102539
##
    [10,] -0.646966646 -0.428354976 -0.54460301 -0.714810205 2.13951609
##
    [11,] 0.847696149 -1.239021906 -1.16397664 -0.656633286 0.18169225
    [12,] -0.284854753 0.190994579 0.02603249 0.360727519 -0.33658784
##
    [13,] 1.671506866 -1.098956786 0.58911845 -1.069230710 0.82642495
##
    [14,] 1.533730463 -0.646063347 -1.24969547 0.318976360 0.35747428
    [15,] 0.583063069 0.010755220 -0.21715761 -0.739820729 -0.09006860
##
    [16,]
          0.567705682 - 0.197197886 - 1.38582844 - 0.468729996 - 0.07054641
##
    [17,] 0.289112192 1.280734043 -0.43538828 -2.576308926 -0.36618045
    [18,] -2.384167109 0.669922958 0.22429326 0.436112160 0.42225611
##
    [19,] 0.088619132 -1.872011393 1.79927730 -1.036311035 -1.40916379
##
    [20,] 1.523915315 -1.039951280 1.53327019 -0.836147688 0.72967805
    [21,] -1.932059469 -1.051652314 1.89871266 -0.725004235 -1.48242940
##
##
   [22,] 1.771747959 0.236561279 0.54530406 1.672814895 1.67769345
##
   [23,] -0.442652257  0.507387641  0.23634650 -1.066003812  0.60342729
    [24,] 0.846362977 0.941229674 -0.55792732 -0.691725183 0.53110667
```

```
[25,] 0.894652788 -0.087655818 -1.17843850 -1.031938413 1.13609210
##
   [26,] -0.887474541 -0.222931510 -0.63230336  0.617294115 -0.37642320
   [27,] -1.056270920 1.191339462 1.06577833 1.950658462 -0.57607312
   [28,] -0.071654638 2.732181231 1.38296288 0.026598632 -0.09679105
##
   [29,] 0.989212610 -0.383148162 -0.74397514 -0.307026844 -0.74996242
##
   [30,] 0.826013055 1.217758973 -1.21946454 0.244709335 0.72301229
   [31.] -0.787768221 2.439716966 -0.28458628 -0.012687234 0.62548799
   [32,] 0.399286436 0.937264438 -0.81767065 1.254672122 -0.27463022
##
##
   [33,] -1.201591059 1.363256535 0.26610535 -0.772827451 -3.32922565
##
   [34,] 1.390348567 0.828678584 -0.71468419 -0.436636233 -0.69354587
   [35,] -0.385156398 1.137049779 0.82594935 0.932162630 -1.60497371
   [36,] -0.550848867 -2.066291945 -1.00569918 -0.947265467 0.94541234
##
   [37,] -1.812173563  0.769960820 -1.21820289  0.607356238 -1.38648714
   [38,] 1.554779986 -1.279073159 -0.83073859 -0.076889825 1.59219367
##
##
   [39,] 1.133515760 0.026429908 -1.26511510 -0.748374445 0.12408470
   [40,] 0.244515370 0.814811702 0.97536166 2.409808978 0.56772493
##
##
   [41,] 0.023291492 1.793625920 -1.32536487 0.682074237 -0.26152717
   [42,] -1.543544142 0.397464264 -1.28172400 0.552473409 2.19345948
   [43,] -1.518245178  0.391995957 -1.08352884  0.811347731 -0.62802611
##
   [44,] -0.543703418 -0.095592920 0.35109052 0.603175718 -0.17483631
##
   [45,] 0.883250246 0.193732469 -1.53922004 -0.246176105 -0.15421734
   [46,] -0.309106618 1.017437313 -0.68469534 0.560420158 1.62715818
##
   [47,] 0.690282640 1.250619950 -0.94584060 0.515807851 1.54412466
   [48,] 0.482339796 -1.876093142 1.66595604 1.050071545 -1.66075821
   [49,] -0.494275473  0.066995658 -0.54706302 -0.398866514  1.13341999
##
   [50,] 0.523658771 -0.021176998 -0.87201816 0.536581822 -0.75599700
##
   [51,] -0.252298665  0.544294134  1.00243206 -0.134105712 -1.49813086
   [52,] -0.094606027 -0.189182301 -0.94323925 -0.845167863 0.12501393
##
   [53,] 0.997416648 -0.942603926 -0.41581803 -0.926933399 -2.04998576
   [54,] -0.622841650 -0.207108171 1.65557459 1.056738022 0.02857959
##
   [55,] -1.248154388 -0.324892488 -1.00589731 -0.986001118 -0.65446632
##
   [56,] -0.313635847  0.539053586  0.07867825 -2.106323983 -0.12698228
   [57,] 1.506240317 -0.960451273 -0.23292347 -0.042272344 0.74936061
   [58,] -1.469525644 0.241119100 0.24536996 -0.272642577 0.20977487
##
##
   [59,] 0.732285696 1.461020442 -1.60079644 -0.206087272 0.41967393
##
   [60,] 0.828259976 0.206255232 -1.14595649 -0.565730336 -0.40868243
##
   [61,] 0.348113429 0.690837363 -0.03342395 0.894235741 0.24437916
##
   [62,] 1.144692134 0.735023733 0.39256413 1.136845563 -0.16866634
   [63,] -0.627429555 -0.457059325 -2.18751936 0.005988202 -0.09988610
##
##
   [64,] 1.670452364 0.773388432 -0.36826364 -1.579651843 -0.60693269
   [65,] -1.748395466 0.002841411 0.07056045 -0.419516524 -0.09724819
##
   [66,] 1.006002163 1.711799175 1.41617609 0.677646785 1.26571157
   [67,] -0.086657335  0.419068757 -1.59067149  1.420779153  1.02008244
##
   [68,] 0.634464206 -0.387549059 -0.68889667 1.538964686 2.03124908
   [69,] 0.302730044 -0.169110585 -0.82211648 -0.124306139 -0.22228496
          ##
   [70,]
##
   [71,]
          1.444887539 -0.909602024 1.28002870 -0.637316542 -0.19655121
   [72,]
          ##
   [73,]
          1.477713042 -0.265815287 -0.54054571 -0.995176847 0.26219854
          0.003248571 \quad 0.800230488 \quad 0.04345621 \quad -0.114215334 \quad -1.22344319
##
   [74,]
##
   [75,] 0.775751106 2.349911982 -0.41519855 0.742491500 -0.52241241
##
   [76,] 1.750207622 1.162005615 -0.17272414 0.988234144 0.71450039
   [77,] -2.431392512 -0.047987498 2.28451648 -0.559223426 -0.21725259
##
   [78,] 0.564663414 0.929664688 0.64356377 2.015269212 -0.71940037
```

```
[79,] 0.382862745 1.338131704 -1.20791276 0.898088821 -1.84875036
##
    [80,] 0.866708209 -1.292711955 -0.08554302 -0.935498723 -0.05396838
    [81,] -0.375720935  0.596707056  0.77893438  0.116213258  2.25241605
    [82,] -1.351035602 -0.478579463 1.05671406 2.636120190 0.05004569
##
##
    [83,] -1.351129681 2.387861555
                                  2.70410105 0.849049868 -0.60599148
##
    [84,] 0.166297951 -1.678598649 0.66678655
                                              1.041889785 0.99226178
    [85.] -0.522134060 1.469595551 -1.13347559 0.618619008 0.24012061
    [86,] -0.765351861 0.909047859 2.00637579 0.033690913 -0.25570053
##
##
    [87,] -0.017272500 -1.146985236 -0.03379273 -1.371609630 1.42391977
##
    [88,] -0.355971171 -0.391564715 -0.26833069 -0.684093661 -1.03944201
    [89,] -0.938118524  0.737221484 -2.16284166 -0.572682929  0.04157491
    [90,] -0.655093657  0.046386631  0.83386689  1.778794158 -0.75676783
##
    [91,] 1.047129413 -0.442757051 -2.30979170 0.161519911 -0.10066507
    [92,] -0.591554523 -0.542198785 0.80964170 0.258766913 -0.09529449
##
##
    [93,] -1.147293376 -0.485258044 -1.09320565 -1.731180284 0.53942962
##
    [94,] -0.066891974 -0.304337280 -0.26542089 -0.276910258 -1.42206293
##
    [95,] -0.451222058  0.652604703  2.29044465 -0.522914858  0.98797174
##
    [96,] 0.705394542 -0.583233674 -0.30072583 0.082796986 1.36220887
    [97,] -1.032701078 0.279368542 0.47301590 1.436471756 -0.38340382
##
##
    [98,] -1.999713264 0.559469877 0.02918362 0.723680160 -0.13519824
    [99,] 0.325369649 -2.646687843 1.33723884 -0.761484521 -0.49219847
##
   [100,] 1.726856198 -1.065326157 0.01948443 0.518410814 -1.61853827
##
               [,56]
                            [,57]
                                        [,58]
                                                    [,59]
                                                                [,60]
     [1,] -0.36014095 0.554038710 0.71712980 0.374305210 -1.38215574
##
         1.48185471 0.479861770 1.86157266 -0.266192208 1.09508662
##
     [2,]
##
     [3,] 2.01791810 -0.604706895 0.37782393 -0.669588989 -1.23987472
##
     [4,] 0.03813605 0.101368854 0.12969715 -0.135244294 -1.07606417
     [5,] -1.36089204   0.113473695   1.00744932   0.027275827   -0.51556495
##
##
     [6,] -0.18609791 -0.183109103 -1.85536042 -0.159212869 0.80426763
     [7,] 0.09036231 -1.743291626 -0.69833920 -0.894453339 0.51123890
##
     [8,] -0.04027612 1.074168311 1.92354419 0.578561307 0.93320881
##
##
     [9,] 0.01170944 -1.014751709 1.52185013 -2.042348421 -1.67849378
    [10,] 0.83364385 0.407424465 2.09336966 0.875052740 0.92425337
    [11,] -0.71689152 0.697778872 2.00318698 0.583490970 0.24562878
##
##
    [12,] -1.71901219 0.008204151 0.07397013 -0.087663472
                                                           0.07646699
##
    [13,] -0.17305848 -0.903594671 1.05579985 -1.087217204 1.27233069
##
    [14,] -0.28672955 2.690161929 -0.56532925 0.675105579 0.37054521
##
    [15,] 1.08574846 0.817961527 -1.33991125 0.395909137 -0.61556325
    [16,] -1.56791957  0.697200925  -0.04319269  -1.029899613  -0.44553943
##
##
    [18,] 1.26808386 -0.729457176 0.67753912 -0.915620486 -0.43313223
##
    [19,] 0.22504810 0.378824793 0.76340840 -0.454104935 2.38887343
##
    [20,] 1.62393275 -0.368319486 0.10067515 -0.318512795 -1.39672215
##
    [21,] -1.11484549 1.697303535 -0.43474324 0.697462538 0.45876947
    [22,] 0.71804679 0.120820492 0.71309510 1.864076758 0.17107774
##
    [23,] -0.58022061 -2.354705849 -1.26109929 -0.579718668 -0.45192569
##
    [24,] -0.29959382  0.977568567 -1.12033372  0.501684770 -0.58674673
    [25,] 1.43824709 -0.760677516 -0.49011088 1.913336123 -0.51989299
##
    [26,] -0.34634358  0.707636078 -0.35990439  0.648112584 -1.49218567
    [27,] 0.76280559 0.821874203 -0.03596826 1.548743476 0.97799142
##
##
   [28,] 1.91872370 0.360165471 0.10036951 -0.805721970 -0.81292490
##
   [29,] -0.15552641  0.382511123  1.42376334  -0.622105144  0.89035374
##
   [30,] 0.40287491 -1.226601233 -2.02830971 0.816331583 1.43815661
    [31,] -1.72901207 -0.261950362 1.09606604 0.268182826 -0.20923691
```

```
[32,] -1.10552564 1.565451649 0.21664865 0.110232242 -0.40742437
##
   [33,] -0.58818543 0.201048522 1.45551591 -0.578517575 0.46773048
   [34,] -0.26842910  0.253614066 -0.35517761 -0.686162302 -1.43020709
##
   [35,] 0.34597224 0.276012519 0.24114579 -1.104424314 1.53575969
##
   [36,] 1.30617892 -0.053495482 -0.21018348 0.796029591 -0.49919068
##
   [37,] -0.58011576 -0.658180242 -1.58081685 -0.459761547 0.53420298
   [38,] -0.86301677 -0.200030201 1.76390393 0.716485161 1.52809730
          ##
   [39.]
##
   [40,] 1.10689317 0.578322295 -0.91541170 -1.209381404 -0.55392159
   [41,] 1.35576649 -0.164289538 -0.36971641 0.459850205 -0.47647337
##
   [42,] -1.36294432 -0.836249907 1.01545781 0.999633597 0.01258759
         1.32506673 -0.569433575 -1.83926249 -0.339728448 -1.11553139
##
   [43,]
   [44,] -0.26841398   0.065663585   0.76802308   0.328761237 -0.92239355
   [45,] 1.59480752 -0.346010461 -0.78962538 0.031493035 0.72956448
##
##
          1.16688747 0.523155198 1.80756497 1.197389552 -0.66112242
   [46,]
##
   [47,] 0.83262690 -1.804118893 -0.26185572 -1.065655982 -2.15173002
   [48,] 1.19781368 0.494242435 1.03144785 -0.909978732 -1.22064365
##
   [49,] -0.75884214  0.403646010  1.60729664  1.058494708  0.82680248
   [50,] 1.18370742 0.686402512 -1.04534214 0.953573797 0.03069773
##
##
   [51,] -1.59789118 2.377903647 0.45838577 1.819095875 -1.70462668
   [52,] 0.44284008 -0.715141419 -0.53893002 0.851436130 0.78782001
##
   [53,] -0.71348413 -0.848956133 -0.43327479 0.768874165 0.45745207
##
   [54,] 1.63589515 -0.293764442 -1.26464126 0.030432366 -0.37296345
   [55,] -0.92568755 -0.252777379 -1.32858642 0.103070211 -0.41307593
   [56,] -0.96238389 -0.807404242 -2.32542931 -0.822931780 -0.59727186
##
   [57,] 0.68977697 0.374382942 0.04748559 0.366899550 -0.15251179
##
   [58,] 0.27405096 -2.136929114 0.85482028 0.188503749 -0.78314723
   [59,] 0.18039584 0.444670871 -0.14461991 -0.858371907 -0.25573941
   [60,] 0.98665819 -0.307200270 -0.27313286 0.457289718 3.10715207
##
   [61,] 1.61233098 0.367799146 0.29115007 0.001548294 -0.94431131
   [62,] -0.13845651  0.770686651 -1.16023464  0.990603002 -1.20241121
##
##
   [63,] 1.23994326 1.289926434 -0.88212006 -0.348159754 -0.10833661
##
   [64,] -1.57407958 -1.748607627 1.58609205 1.625894352 -0.63895317
   [65,] -1.55881150  0.565723720  2.07434921  0.118986288  -0.32120601
##
##
   [66,] -0.03872956 -0.308936747 -1.43452262 0.092303343 -1.93241214
##
   ##
   [68,] -0.30112487 1.530216330 -0.80138130 0.374154721 -0.50765524
##
   [69,] -0.20281344 -0.847248483 -1.00047345 -0.077284799 -1.24784484
   [70,] -1.40417017 -0.598230541 0.13482824 -1.186395970 0.36940453
##
##
   [71,] 0.15057838 0.570160134 -1.14494017 1.147538367 0.39807515
   [72,] -0.71010506 1.238762256 -0.57164052 -0.281422367 -0.98083038
   [73,] 2.08157773 -0.504173321 -0.85627216 -0.560616459 -1.60252815
##
##
   [74,] -2.06742693  0.018949045  0.47759808 -0.357646816  1.33309181
##
   [75,] -0.07224454 1.155110055 0.71335823 -0.401367014 -0.04468779
   [76,] -0.28111238   0.232578413   1.52239204   0.580818970   -0.68772212
   [77,] -0.17477540 0.522981868 -0.58773919 -1.377584934 1.94723044
##
##
   [78,] -1.14230919 -2.454835031 0.75582694 0.470801173 0.27801347
   [79,] -0.25339812 -0.564027550 -0.66810365 1.440653561 -0.25151604
##
   [80,] 0.51288710 1.979118848 -0.57564604 -0.624777854 0.02946549
##
   [81,] 3.19278586 1.150308364 -0.50898911 -0.274566864 0.88842431
   [82,] 1.53995145 0.394560989 -0.52638861 -1.336213600 -0.28152958
##
##
   [83,] -0.93047517  0.371778562  1.19944855 -2.245247826 -1.52780298
##
   [84,] -0.73054038 -0.765764530 -1.18572083 -1.306838574 1.55755197
   [85,] -1.19445876  0.084546236 -0.15628796  1.463279954  1.79136935
```

```
0.46467949 0.329740730 -0.73178533 -0.338383713 1.70787852
##
    [87,] 1.65747027 -1.085159289 0.84066304 0.340478578 0.46986468
    [88,] 1.12382652 0.917159455 0.28837484 1.537348284 0.84390429
    [89,] -0.76205114 -2.190142392   0.80024098 -0.167399586 -0.19767940
    [90,] -0.81317344  0.677780997 -0.59483787  0.158647256  1.14756571
    [91,] 0.93113542 -0.037221548 0.37537376 -0.230107793 1.05130579
##
    [92.] 0.12375030 0.018033974 -1.46340074 -0.680654435 -0.50539702
    [93,] 0.19336089 0.672972805 -1.21905453 -1.125127203 -1.20129871
##
##
    [94,] -2.79800898 -1.556393386 -0.32068827 -0.920057675 0.52251681
    [95,] -0.76946920 0.104416807 -0.29453724 -0.514610379 -1.55706895
##
    [96,] 0.65100673 0.112138386 -0.70732286 0.250927883 -0.78536765
    [97,] -1.29921712 -0.747041208 0.69183180 0.653699692 -0.18671348
##
    [98,] 0.14836770 0.302563634 0.33655638 -1.901230016 0.25972058
    [99,] 0.73632483 -0.510924316 0.68088627 -0.442728840 0.51765301
##
##
   [100,]
          0.54042805 \quad 0.559679997 \quad -0.30641934 \quad -0.115468875 \quad 0.37517171
##
                [,61]
                            [,62]
                                         [,63]
                                                      [,64]
                                                                  [,65]
##
          0.78051115 -1.523077273 -0.245983986 -0.005092181 0.225212954
     [1,]
##
          0.43361489 - 0.168683458 \ 0.162934858 - 0.183553608 - 0.051299607
##
     [3,] 0.53103276 0.010221709 2.927557337 1.585266314 -0.664393751
##
     [4,] 0.39331389 -0.944389023 -1.673116945 0.312650749 -0.199495375
     [5,] -1.65914949 -0.582022721 -1.167269940 0.803230879 -0.028174979
##
##
     [6,] -1.24630422 0.954510226 -0.038351143 0.275564006 -1.475577840
     [7,] 1.19899252 0.283271958 0.080168236 -1.776896345 0.963219483
##
     [8,] 0.79938503 1.057962917 1.095196294 -1.224624785 0.319201955
##
     [9,] -0.09894661 -0.828120583 0.041899009 2.046690143 0.570615264
##
    [11,] -0.29514180 1.005151593 -0.811706369 -1.002622828 -0.029972363
##
    [12,] 1.45320619 0.062409983 0.650318818 -0.413263057 0.574901764
##
    [13,] -0.18484122  0.053804371 -1.120421078 -1.010054835 -1.342690782
    [14,] 0.65258754 1.065792026 1.056815799 -0.374244700 0.398332696
    [15,] -0.19691544 -0.170293311 0.002790209 0.360945873 -0.456045339
##
##
    [16,] 0.08600931 0.810004925 -0.788036650 -0.177408891 0.780385582
    [17,] 0.44414040 -0.416631875 -0.272396593 -0.736980677 -0.847779404
    [18,] -0.49138780 -0.007882879 0.087094828 0.444505751 -0.296518947
##
    [19,] -1.55793566 -0.097348122 0.172121674 0.412213970 -0.107002328
##
    [20,] 0.05762833 0.071807336 0.030170238 -0.212737937 -0.255230921
##
    [21,] 1.17586040 -0.901822736 -1.465025886 -1.270534149 0.690110872
##
    [22,] 1.06815905 1.080656415 -0.856793784 0.227286045 1.334418371
    [23,] -0.86929083 -1.053141271 -0.753504076 -0.969800162 1.618687600
##
##
    [24,] -0.38958682 -0.648824840 -0.444639036 -0.862796901 2.015722363
    [25,] -0.01575242 -0.518134626 -1.058870699 0.114484563 -1.062441249
##
    [26,] -1.47789280    1.575656465   -0.408042718   -0.820908903    0.307336169
    [27,] 0.75738614 -0.959574491 -0.448953162 0.388865572 -0.872348853
##
    [28,] 0.19036982 0.991741863 -1.229631657 -0.783614445 0.514090761
    [29,] 0.05162114 -0.642972767 -0.394506515 -1.430069455 -0.184745349
    [30,] -0.71707886 1.277975300 -0.280079805 -0.488038938 -0.282003017
##
##
    [31,] -1.91225751 -0.308072614 0.475003017 0.061790726 0.805645444
    [32,] -1.51549343 1.046690180 -2.084441878 2.982561097 -0.594755708
##
    [33,] 0.84547605 -1.034634163 1.524198735 0.653434170 1.524436195
##
    [34,] -0.87749288 -1.136779441 -1.078403453 -1.546934542 0.241919255
##
    [35,] 0.35862006 0.479822818 -0.698452479 -1.298696021 0.669711580
##
    [36,] 0.60674046 0.266186019 -0.246170015 -1.233268802 -0.370581285
##
    [37,] 0.54070683 0.128998064 0.520155505 -0.680377689 -1.152727049
    [38,] -0.07400891 -1.103040947 -1.065859813 0.479681443 1.248688589
```

```
[39,] 0.49396027 -0.705802360 1.171337871 -0.792756789 0.120098825
##
   [40,] 0.10796732 2.051615002 0.066546996 1.551314273 0.006335366
   [41,] 0.26269666 0.618389995 -1.087025373 1.124295772 -0.256043241
   [42,] -0.30830153 -0.782586987 -1.011631684 -0.195136299 -0.369775381
   [43,] -0.46950748 -0.504477783 -0.585581688 -1.031396820 -0.314897509
   [44,] 0.46287727 -0.684140402 -0.844272454 0.828480987 -0.221449467
##
   [45.] -0.30974695 -0.178026983 -0.005740142 -0.615587781 -0.836747070
   [46,] 0.76924984 2.030840625 -0.267694889 -1.481335508 -0.836494749
##
   [47,] 0.28300739 -0.308693237 -0.074046516 0.516964697 -1.262026890
   [48,] -1.63041674 1.656542061 -0.348685165 -0.077343260 0.759666032
   [49,] 0.26148274 0.854758249 0.681133976 1.091828068 0.169802760
   ##
   [51,] 1.35842430 -1.566781702 0.010864989 0.506330754 -1.569631695
   [52,] 0.94635459 -0.616443609 -0.029889857 0.156228944 0.104525459
##
##
   [53,] -1.24654632 1.628305836 0.831006673 -0.317233500 -1.621194088
   [54,] -1.24154486 -1.366009356 0.455986778 1.158744861 -0.315735472
##
##
   [55,] 1.40272612 1.014596540 -0.146959760 -0.687770602 0.471187356
##
   [56,] -0.24788252  0.500987989  0.189832217  1.647072163  0.818214018
   [57,] 0.63694168 -0.891507067 0.566627226 0.067011580 -1.330251670
##
   [58,] 0.29518803 -0.991860490 -0.338361678 -0.326535933 1.075887587
##
   [59,] 0.36541539 1.609245620 0.958730111 0.174445597 -0.886349695
   [60,] 1.15404449 0.566578156 0.888968633 0.339551270 -0.129026777
   [61,] -0.33313040 1.001627846 -0.083749413 0.103617138 -1.080731561
##
         1.38319627 1.033058990 1.457013484 0.672751195 1.218858777
   [62.]
   [63,] -0.35328068 -2.664402061 -0.399264243 -0.626588368 -0.714341168
##
   [64,] 0.11444864 -0.532386405 0.917520451 0.198266243 0.522214184
##
   [65,] 0.80823451 0.537288078 0.503856472 -0.118422429 -0.669150809
   [66,] 0.39418196 -1.009286963 0.378095259 0.958600745 -1.009194680
##
   [67,] -0.70701230 -0.904812390 -1.822456915 0.667661273 1.033639522
   [68,] -1.26922782 0.420241912 0.751265059 -0.601592146 0.557173868
##
   [69,] 1.08306305 0.452264440 -1.261606223 -0.959439802 2.468386802
##
   [70,] -0.57895484 1.408507773 0.615182502 1.493454732 0.051867374
   [71,] -0.34412039 -0.815729155 -0.310801538 -1.769186589
                                                          0.946628799
   [72,] -0.56894361  0.383311441  1.366093142  0.643916706  0.525684381
##
##
   [73,] -0.30202481 1.328410029 1.401798853 -1.324365323 -1.636076788
##
   ##
   [75,] 0.60668434 -0.625350373 0.727972198 -1.132793088 -1.099643875
##
   [76,] -0.95406260 -0.944345527 -0.785803082 -1.088488087 1.006853935
   [77,] -0.20327444 -1.566185280 -0.326443156 -0.815577563 -0.403679009
##
##
   [78,] 0.26729369 0.307768733 0.646524255 -1.103126446 -0.647687966
   [79,] -0.86881715 -2.502999574 -2.392563093 2.130895045 -0.618995457
##
   [80,] -1.62363848 1.489096854 -0.536121112 -1.217709340 -0.039666882
   [81,] -0.34020201  0.580736819  0.887467787  0.439692565 -2.343772940
##
   [82,] -1.27586222 -0.125184689 -0.782460028 -0.939217718 0.698755244
   [83,] -0.24467099 -1.471449677 -0.651184313 -0.927866638 2.143276067
   [84,] 0.95927513 -0.890929897 -0.003024634 -0.666296809 -0.309508192
##
   [85,] -0.11205192  0.794334567 -1.452024664 -1.059578299  0.911844282
   [86,] 0.15951087 -1.330337797 -0.200741927 -0.990600285 -1.119256829
##
   [87,] 0.92237311 -0.728581851 -1.331064004 1.612901829 2.027664775
##
   [88,] 0.90667433 -0.267551649 -1.432162823 0.072599879 1.186390165
##
   [89,] -0.64155211   0.649211679 -0.250746344 -0.472787656 -0.066850421
##
   [90,] -0.60859222 -0.140688241 -0.887624895 -0.328510175 -2.059623960
   [91,] 0.03098931 -0.195623765 0.117509049 0.179411702 -0.672568667
##
   [92,] -1.02902035  0.168683140 -0.323740082  0.167632455  1.775202656
```

```
[93,] -0.90372991 -0.670550491 -0.907175712 0.198256288 0.991700722
##
    [94,] 0.68722570 0.536167113 -1.282219852 1.797810522 0.242318029
    [95,] -1.49898417 -0.481621683 -0.174874648 -0.127516495 -1.536042279
   [96,] 0.12607592 1.086255318 -2.030941485 0.253145026 1.035458209
    [97,] -0.01345626 -0.335793044 -0.650388385 0.161183175 -0.061340157
##
    [98,] 0.25328625 -1.830869294 0.688969928 1.877003045 0.952560335
    [99,] -0.74122343 -0.995811664 0.491520543 -0.034713376 -0.626705876
   [100,] 0.55468091 2.844251135 -2.126206307 -1.758080195 -0.837877922
##
##
               [.66]
                            [,67]
                                          [,68]
                                                     [,69]
                                                                  Γ.701
##
     [1,] -1.63157713 0.051677912 -0.6191986641 0.75524096 0.267018653
     [3,] -0.80105412 1.714240117 -1.4805378573 -1.18869904 1.251590247
##
##
     [4,] -0.44416891 -0.311446294 0.0128612072 0.10643940 0.619296102
     [5,] 0.80279507 1.706077495 -0.0581826673 0.49869683 0.319749126
##
##
     [6,] -1.20710544   0.072262668 -0.8743881815 -0.88252006 -0.484232415
##
     [7,] 1.30826215 -0.199100742 -0.1570617141 -0.95460929 -0.075930655
##
     [8,] 0.34782022 -1.048260330 0.0210955408 -0.34346445 -1.483343244
##
     [9,] -1.68301722 -1.404891774 -0.0509637418 0.97641807 0.147592601
    [10,] 0.22328668 1.118834090 -0.6493068803 1.33566500 -0.047453720
##
    [11,] 0.67538686 0.911228612 0.4869571337 -0.96393737 0.096082640
##
    [12,] -1.02672928 -0.313575594 0.3589201485 -0.46002266 0.272655979
##
    [13,] 0.13436178 -1.513364341 0.3870056075 -0.89968754 -0.569761182
    [14,] -1.43672044 -1.542101833 -0.0009481861 -0.87879870 -1.396028948
##
    [15,] 0.38019767 -0.505725703 1.7629280908 0.97487391 0.416048390
    [16,] -0.16176443  0.564198122 -0.1159856063 -0.26838948  0.421160904
##
    [17,] -0.20916744  0.036894298 -1.4340065612  2.20513303  0.080523563
##
    [18,] 1.04644118 0.589915776 -0.4513244573 -0.71495713 1.166022392
    [19,] 0.18690815 0.859077795 0.4489309729 -0.94551558 1.593995455
    [20,] -1.11475044   0.419555770   -0.6037224408   0.07052174   -1.475115482
    [21,] -1.37144207 1.992150461 -0.5812089832 -0.35975060 -0.414611035
    [22,] 0.41254565 -0.239818270 0.4322409579 0.88051379 0.591923446
##
##
    [23,] -0.52485672 -0.890400719 1.2903272681 0.45933634 0.082785668
    [24,] 0.73170615 -0.344899518 -0.0544657784 -1.92154471 1.284910477
   [25,] -0.55636835 -0.535006915 1.0017798472 -0.24637861 -0.574235189
##
    [26,] -1.48505230    1.982067618   1.1089051323    0.17102256 -2.130003477
##
##
    [27,] 0.51876632 0.422250362 -0.1456099451 -0.69992765 -0.628849136
##
    [28,] 0.30306557 -1.758123325 -1.1254667174 -0.12265974 0.119048500
##
    [29,] -0.61516790 0.935311653 0.1479471697 -1.79855962 -0.112197228
    [30,] -0.49505911   0.380344147   0.2519646920   1.36289351 -0.392046768
##
##
    [31,] -0.26901159 1.221583623 -0.8465143017 0.22777409 0.977032560
    [32,] 0.51027648 -0.586673033 -1.1414484268 -0.49269212 0.758471966
##
    [33,] 0.45324549 -0.037795975 0.9452655506 -0.54057080 0.262685110
    [34,] 0.11953503 0.046668841 -0.4493883697 -1.10854491 -0.944838087
    [35,] -1.07139135 0.767555883 0.6341708815 -0.13208357 2.249276941
##
    [36,] 0.59619119 1.229675886 -0.5861189006 -0.70748635 -1.064447959
    [37,] 0.60667074 1.329455536 2.1095508602 -2.42614461 1.285810664
##
    [38,] -0.71829877 2.016714834 -0.7825875567 -0.71537839 -0.349525368
    [39,] 0.89793143 -0.093910107 0.2415055710 0.89148001 -1.395545472
   [40,] 0.61529612 -1.137766766 0.3480491873 -1.89289058 -1.405010464
    [41,] -1.90746329 -1.126434150 0.0800180426 -0.12788508 -0.340795437
##
   [42,] 1.11941206 -0.757588978 0.3220231545 0.14103879 -0.647817548
##
##
   [43,] -0.71058730 -0.004435064 1.3857009976 0.71142869 0.853840260
   [44,] -2.26359338 1.435757221 0.7812596480 0.24299575 -1.057524187
   [45,] 1.22592625 0.798096607 0.2360038525 0.56533740 -1.625492791
```

```
1.26880933 - 1.741167792 0.4708342219 - 0.50714320 0.513071928
##
   [47,] 1.42815301 2.273145842 0.3104774831 -0.27481688 -0.775666640
   [48,] 1.66823462 0.671637222 0.9592980888 1.05863511 0.616245512
   [49,] -2.51301680 -0.199754037 0.5260017919 0.76957022 -0.427460126
   [50,] -1.55668668 0.275406821 0.8564065835 -0.28432390 1.306072444
##
   [51,] 0.43655395 0.728910746 -0.5632741348 0.03067787 0.021930408
   [52.] 0.64576071 1.289111496 -0.5846086600 -0.64943992 -0.758271676
   [53,] -0.62739815  0.301421750 -0.5562803289  0.35661551  0.609815031
##
   [54,] -1.58451426 -0.282522017 -0.1556517226 0.60516198 1.540023105
   [55,] -1.30530596 -0.037334598 -2.3524285855 1.44682341 -0.022210322
##
   [56,] 0.43077829 0.701536299 0.2624964456 -0.28873710 1.770360989
   [57,] -0.36914916  0.616634775  0.6239018739  0.64005923 -0.199943814
##
   [58,] 0.25110060 -1.268110928 0.0453874387 -0.80635404 0.853234960
##
   [59,] 0.66109077 0.775893110 1.0058094622 -0.04424215 0.717757597
##
   [60,] -0.83002764 -0.121761721 1.0227206463 0.46538246 -0.142490218
##
   [61,]
          0.29601464 - 0.371575849 - 2.0418275077 - 0.78355323 2.327257956
##
   [62,] 0.51386079 -0.211824071 -0.4747707302 -1.52909860 -0.333134298
##
   [63,] 0.74542739 0.582725271 -0.1010804390 1.70963107 0.091928594
   [64,] 0.60604170 -0.727868665 -0.3508424271 -0.23742572 1.195989917
   [65,] -1.08019123 1.550057150 -1.5364788232 0.93981135 -1.822612528
##
   [66,] -0.44537900 1.049166688 -1.5607519036 -0.15582401 -1.761709904
   [67,] 1.38872662 -0.289495477 0.7369498088 1.37663278 -0.912258695
   [68,] 0.31077957 -1.953474959 0.4218209312 -0.55875493 0.855185104
##
   [69,] -1.89502066 0.420800000 0.0871173014 1.19924960 1.914659398
   [70,] 0.96794288 -1.389286707 -2.4268877839 0.45809298 -0.828251126
##
   ##
   [73,] 0.73538815 0.309850615 0.9805328710 -0.44304205 0.877319319
   [74,] -2.33052433 -1.885484830 -0.2968481575 -0.81190635 -0.735553320
##
   [75,] -1.03377626 -1.156464546 -0.0430709809 -1.34685804 1.806573675
   [76,] -0.66172342 1.797464432 1.3092111621 1.36805516 -0.775143732
##
##
   [77,] -1.08254051 -0.304516553 -0.0192200991 -0.17978637 -0.665814128
   [78,] -1.15894839  0.338402517  0.2033569319 -1.04910167  0.006329724
   ##
##
   [80,] 0.49389860 0.299191469 1.0057468404 -0.30340552 1.051334655
##
    [81,] \quad 0.12596446 \quad -0.505863490 \quad -1.4528006857 \quad -2.93411321 \quad -1.741749736 
##
   [82,] 0.35553857 0.364619249 0.3225747113 -0.43125518 -0.728408392
##
   [83,]
         0.90298632 -0.524588013 -0.3360696499 -0.76364019 1.563923869
   [84,] 0.21510591 -0.275745972 1.1708192060 -0.34686187 1.430172015
##
##
   [85,] -1.15389950 0.057911971 -2.4432476720 -0.05254338 -0.371709647
   [86,] 0.33168823 -0.822834084 0.6507095696 0.39518248 -1.731221356
##
   [88,] 0.71249247 2.118958911 -0.9400163159 -1.50897138 0.659606654
   [89,] 0.63177147 0.367009810 0.5148355823 1.03001535 -0.456629135
##
   [90,] -0.86409550 -0.306970046 1.2852771515 0.05607073 0.312061931
   [91,] -0.74680666   0.071522461 -0.7231332305 -1.16277082 -0.228006409
##
   [92,] -0.97864252 -0.593496126 1.5666930422 0.48963235 -0.737848175
   [93,] -0.12165956  0.122960744 -0.4111440230  0.76080094 -0.666359230
   [94,] 0.91058660 0.558476393 -1.0156935294 0.96244926 0.700166550
##
   [95,] 2.39504625 1.047387553 -1.7590283600 -0.73618191
                                                        0.220640522
##
   [96,] -0.57464055 1.331485105 -0.7815549202 1.29182983 1.060224079
##
   [97,] 0.35403983 1.523945517 0.6495121956 -1.16005149 0.189918129
   [98,] -1.82132386 2.881965115 1.3883037704 -0.32166541 0.310387464
##
   [99,] -0.16574618  0.021185787  0.3766054675 -0.64894280  1.029258081
```

```
[100,] -0.10372980 -0.605288941 0.1843205586 1.68989512 0.513186635
##
                            [,72]
                [,71]
                                        [,73]
                                                     [,74]
                                                                [.75]
##
     [1,] -0.64696372 1.171442815 -0.19583796 0.094827721 -0.43245196
##
     [2,] -1.32475359  0.100325551  0.13841285 -1.489422922  1.97319655
##
     [3,] -1.77703243 -1.269036403 1.26992220 0.451102811 -0.82326058
##
     [4,] -0.64183564  0.930529603 -1.05814924 -0.277477341  0.40808545
     [5.] 0.67532460 -0.917339157 0.67697213 0.597586334 -1.57554025
##
          0.19036670 \quad 2.333090232 \quad -0.14748721 \quad 0.768308451 \quad -0.77492374
##
     [6.]
##
     [7.]
         0.12564589 -1.448452213 -0.36731804 -0.453297837 -0.68386978
##
     [8,] 2.74646202 -0.163707599 -1.51278189 1.051054297 -0.30817845
     [9,] -1.54956179  0.719703420 -0.87000386 -0.366011533 -0.78958980
    [10,] 0.10970418 -0.020436866 1.62694600 1.126159493 0.74989565
##
##
    [11,] 0.72383777 1.490184420 1.06807818 -0.486034118 1.43211306
##
    [12,] -2.19805809 -1.866825753 -0.43551167 0.112541777
                                                           2.14632539
##
    [13,] 0.66433371 -2.497368918 0.99414955 -1.856938766
                                                           0.63197595
##
    [14,] -0.28618567  0.041326725  1.74061028  0.032505766
                                                           0.61468096
##
    [15,] 0.65302231 0.223087413 -2.26252581 0.143914455
                                                           0.54933322
##
    [16,] 1.05006054 -2.113174228 0.13664307 -0.938265153
                                                           0.53490687
    [17,] 2.81433936 -1.442427266 0.17275606 -0.377680053 0.01701982
##
##
    [18,] -0.50209460 -1.025918786 0.69168281 1.420859436 -0.78840071
##
    [19,] 0.58906913 0.979325916 -0.45271185 1.131392203 0.31213955
    [20,] 0.34207373 -0.745562023 0.25529002 -1.733415876 -1.85436396
##
          0.92930550 -1.108618778 0.52305392 2.435288359 -0.43290012
##
    [21,]
          0.50416411 -0.540481624 -0.12761434 -0.807623084
##
    [22,]
                                                           0.70642611
##
    [23,]
          0.57128921 1.338634318 0.06898147 -0.190000147 0.89971493
    [24,]
         ##
         0.43222569 1.120351308 0.71624869 0.303633633 -1.45298579
    [25,]
    [26,] -0.94257436 -0.006261495 -0.99644319 -0.110260271 1.62821076
##
    [27,] 1.41091052 -0.716503895 0.58453805 0.160505046 0.02062289
    [28,] -1.86267340 -0.053104044 0.96352215 0.533835821
                                                           0.25313644
    [29,] 0.08804076 2.035168375 -0.93336988 -0.104462421
##
                                                           0.50763283
##
    [30,] -0.13029654 -0.936573708  0.66649445  0.616894505 -1.18176982
##
    [31,] 0.29959946 -2.929056698 2.00794654 -0.593465163 1.02724767
    [32,] -0.15608415 -0.311039393 0.08590772 1.906365923 0.87339175
##
##
    [33,] 0.85060740 -0.673726897 0.25491511 0.789136467 -0.74064155
    [34,] 1.44165728 1.385186890 -0.40779873 0.219178270 0.90683746
##
##
    [35,] 2.07448808 0.871299563 -0.53697332 0.967188248 -0.17142303
##
    [36,] -0.07138182 -1.750204066 0.24657886 0.970139264 1.11902741
##
    [37,] 1.07826096 0.227826057 -0.05265018 0.316803707 -0.76868821
##
    [38,] -1.36653533 1.703086332 0.74960273 -0.021935746 -1.18975098
    [39,] 1.29680894 0.640851782 -0.15228239 0.683413369 0.92579555
##
    [40,] -0.84948497 -0.316954861 -1.27987155 1.870418386 0.90462392
##
    [41,] -0.15450792  0.479522684  2.28446739  -0.138962307
                                                           0.94088542
##
    [42,] -0.59394168  0.460662232  1.06226975  0.558077394  1.78317202
    [43,] 1.11422597 -0.049580157 -0.24562654 -0.385259416 0.33152922
    [44,] -0.51842480 -0.968780409 1.83412747 -0.577113300 -0.29792594
##
##
    [45,] 0.36676582 -0.391789730 2.54486075 1.011004156 -1.56308211
##
    [46,] -1.02447405 0.463694695 0.06489210 -0.659965484 -0.51053405
   [47,] -0.48919147 -1.613466139 -0.31464504 1.029530682 -0.88580217
##
    [48,] 0.60939545 0.537028335 -1.34874187 0.183516253 1.27347014
##
    [49,] 0.21022290 -1.528222918 0.04121335 1.219534877 1.55195035
##
   [50,] -1.02465192 -1.221489770 -0.28397307 -0.604066002 -1.30817361
##
   [51,] -0.50742346   0.814855485   0.11775741   2.048232179 -0.46603652
    [52,] 2.02300149 1.060394702 0.10081280 1.860840305 -0.11789843
```

```
[53,] 0.31655060 0.092389745 2.12846209 0.263576802 -1.69484702
##
   [54,] 0.22848189 0.365141479 1.21848211 0.900540634 0.04186885
   [55,] -0.43953915  0.272573022 -0.28803335  0.230303112 -0.39291055
   [56,] -0.94062470 -1.197574169 0.03669827 -0.237508673 0.02186656
##
   [57,] 0.31184961 -1.949951816 -0.83924038 -0.348308527
                                                         0.35050292
##
   [58,] -0.36555719 -0.406962496 1.23178533 0.985722195 0.83906068
   [59,] -1.50735665 -0.345726210 -1.26221315 -0.388799882 -0.08522911
   [60,] -0.29746798  0.112814028 -0.43882293  0.761490949  1.25356917
##
##
   [61,] -0.34522113  0.339575579 -0.91005246 -0.836648747
                                                         0.31840758
##
   [62,] 1.96830947 -1.184859934 1.88956398 -0.320926565 0.34944714
   [63,] -1.42761365 0.038827988 0.34692992 0.794390577 0.48492072
   [64,] 1.65345931 2.381559312 -0.92824628 0.425118171 -0.51392070
##
   [65,] -1.76201190 -1.562034843 -1.16787597 -0.597108291 0.20584216
   [66,] 0.45914145 0.784212249 1.81115118 -1.029477690 -1.60698066
##
##
   [67,] 0.31803793 0.322056366 -1.37083258 0.185953241 0.48331174
##
   [68,] 0.11351793 0.190402476 -0.30658586 -0.498269729 -2.12848309
   [69,] -0.40078932 1.194921408 -0.04883917 -0.412595990 -0.46503191
##
   [70,] 0.72275784 0.955081398 -1.13347565 -0.919284420 -0.53165270
   [71,] 1.41011588 -0.930668630 -1.09990469 0.006529262 1.34849621
##
##
   [72,] -1.20544292 -0.153349835 0.10570720 -0.289788451 -0.19383434
##
   [74,] -0.26728618  0.258173498  0.45981911 -0.307426731 -0.18389576
   [75,] -0.13540282   0.597754340   0.67874951 -1.308022589   0.04143923
##
   [76,] -0.31373409  0.266012377 -0.71749122 -0.378658380 -1.32548144
   [77,] -0.30141061 -1.352167768 -0.90205661 0.352546259 -1.07112834
##
   [78,] 1.03961591 -0.007148701 0.64312474 0.484168808 2.02546585
##
   [79,] -1.94115130 -1.977225425 -1.24060404 0.943915352 -0.07951236
   [80,] -0.54539650 -0.064708294 0.37347637 1.534800427 -0.17952009
##
   [81,] 0.84549992 -0.098887470 -2.12655547 1.181088050 0.52835733
   [82,] -0.06732172 -1.721761603 -0.46805418 -0.660338837 -0.21978884
   [83,] -1.17079629 -0.504882445 -0.71535944 0.222253128 0.65246027
##
##
   [84,] -1.34666232 -2.653649186 -2.29682181 1.034482525 1.94956347
   [85,] -0.13394916  0.186444778 -0.38486689  0.987871201 -0.40547407
   [86,] -0.79356063 -0.855463441 -1.04282969 -0.663058290 -1.85534547
##
##
   [87,] -0.83776706  0.102647594 -0.81916083 -0.025969951  1.03637131
##
   [88,] -0.74479454 0.675731673 -0.68851792 -1.767897387 -0.29524400
##
   [89,] 0.36749655 -0.266928270 1.71946840 0.473528588 0.21196692
##
   1.14315110 0.200404603 0.38151401 1.642870544 0.69480832
   [91,]
##
##
   [92,] 1.51557909 -0.413419314 1.08207243 0.035085238 -0.82205375
   [93,] 1.34957285 0.853038122 0.30361675 0.470302851 0.06810019
   [94,] 0.14661190 -0.215523760 -0.58084436 -0.182989588 1.04102753
##
   [95,] -1.24861145 1.265799557 0.07186357 -0.310089923 -1.14997175
   [96,] -1.01985579 -0.169590603 1.07596869 -0.840053289 0.50935470
##
   [98,] 2.29264915 -0.529391858 1.10136187 -0.667749479 0.50941202
##
##
   [99,] -0.27752313 1.606022848 0.80346348 0.171900417 0.22972547
   [100,] 0.86087309 0.910898075 0.21025830 1.602067102 -0.03816801
##
##
                 [,76]
                             [,77]
                                        [,78]
                                                    [,79]
                                                                 [,80]
##
    [1,] -1.1414608535  0.305011645  0.58315129  1.678032731  0.1871331076
##
    [2,] 0.8928141566 0.073480498 -0.34698476 0.008190577 -0.5544174301
##
    [3,] -0.6111845514 1.209707452 -0.59925860 1.126581636 -0.1465095501
##
    [4,] 0.2348793614 1.072905446 -1.14585897 -0.211962837 -0.8256566830
    [5,] 0.0361952817 0.789863437 0.67828777 0.321743092 -0.8311938297
##
```

```
1.8098667597 -1.568602482 0.14943473 0.600249940 -0.2004590130
##
         2.2652365761 -0.282031289 -1.48611099 2.403182220 -1.3545591019
##
    [7,]
         1.5444409610 0.530161825 2.24238199 -0.164841848 0.8042103009
##
##
    [9,] 0.8729119250 -0.440866536 0.21299903 0.419300477 -1.2434548350
##
   [10,] -0.4409062951 0.304604603 0.55887767 -0.873809976 -1.9533896746
   ##
   [12.] -0.7887436337 0.909199196 0.54067417 0.428935168 1.3976135904
   [13,] -0.4059150430 -1.461911950 -0.12481099 0.374967847 1.0543661014
##
   [15,] 0.9889038046 -1.252547276 0.49972104 -1.230501602 -0.5801970267
   [16,] -0.3204660685 -0.587737249 -0.79901583 0.579413213 -0.0724923848
   [17,] 0.7384726876 -0.283220624 -1.93702865 -0.760410335 -1.4676558251
##
   [18,] -1.4179190158 -1.331745429 -0.95844239 -1.259784402 -0.9037330432
   [19,] 0.1258379537 -0.410339330 -1.42319056 0.492758366 1.8331774887
##
   [20,] -1.5648629608 1.177482732 -0.26874895 0.447530064 0.2302124146
##
   [21,] -0.9086677528 -1.064660462 -0.86392659 0.090827052 0.1663430245
##
   [22,] -0.0919618316 1.329877695 0.15293360 -0.010300191 0.3026152549
   [23,] 1.3997383966 -1.026732721 0.33914071 -2.263962404 -0.0585733659
   [24,] -1.1732904230    0.686564095    1.20422219    2.491757869    -1.8908554689
##
   [25,] 0.7921405212 0.837121136 0.22428669 1.247527234 0.1638948194
##
   [26,] -0.5155621213 -2.037780015 0.07607765 -0.099581363 -0.3031808580
   [27,] -1.0944488057 -0.337012481 0.17470872 -0.185571977 1.5678966311
##
   [28,] -1.1355931609 -2.117914180 0.54243246 0.857058124 0.2529264705
   [29,] 0.9949208202 0.450853164 -0.31942089 0.590082153 -0.1144015271
##
   [30,] 0.7359708317 -1.074772779 -1.48039190 -0.570886493 0.9960340036
   [31,] 0.6570765679 0.939838530 -0.07550756 -1.036792740 0.4537864560
##
   [33,] 0.7787361434 -0.395913307 -0.29532346 0.860554330 0.1434015037
   [35,] -0.6418277588 -0.269727931 0.16912610 1.324329202 0.5557382040
   [36,] 1.7075005450 -0.271597043 -1.28312662 1.476756519 1.1091305887
##
   [37,] -0.4153775596 -0.063874341 -1.41443021 0.848844003 0.5388297060
   [38,] -0.6302898876 -0.739383822 1.13740703 -0.001177174 -1.5916243667
   [39,] 1.1064143721 1.308264398 0.36753421 0.892753704 -0.7159918970
##
   [40,] 0.5405177095 -0.746203711 0.38297794 -0.976604973 0.4846423012
##
##
   [41,] 1.4508558990 0.703290360 -0.21717049 -0.186971572 -0.3505723700
   [42,] 0.7941375441 0.194078399 -0.54417774 -1.395438498 -1.5572900365
##
   [43,] 0.8140293065 -0.163090075 -0.51741934 -0.785901966 -0.3563118341
   [44,] -0.1849183847 0.204255143 -0.55228714 -0.621115476 0.7081931291
##
   [45,] 0.1552513120 0.189905820 -0.71640963 0.480828638 0.2960841567
   [46,] -0.0005673964   0.262765016   -2.62759981   -0.358201817   -0.2140329360
##
   [47,] -0.6126338782 0.550045460 0.70174014 1.060764814 -0.4242583912
   [48,] -1.4135975104 -0.496492823 0.68985801 0.568348707 0.7786587368
##
   [49,] -0.0335023863 1.522133529 -0.88797878 0.254763284 1.4938972516
   [50,] -1.3131193935 -1.774561316 -1.67914564 -0.284849927 0.1404409495
   [51,] 1.2127949028 -1.633679731 1.15579110 0.148841470 -0.5675287313
##
   [52,] 0.6289538466 -1.670491199 0.84598538 0.274188974 1.8735770584
   [53,] -0.3490107113 1.481097326 -0.16045976 1.426822428 -0.0006525727
   [54,] 1.7530758950 0.589743591 1.10139670 -0.733959045 0.7894625527
##
   [55,]
         ##
         1.9063214367  0.554435531  0.91962463  -1.193530385  0.2398023483
   [56,]
##
   [57,] 0.3478542264 -0.904605142 -0.30256516 0.207096729 0.7041973483
##
   [58,] -1.6167109140 0.701259208 -0.11628822 -1.535234900 0.1279879671
   [59,] 0.1407790201 0.540616792 -0.39070190 -0.432590475 -0.5022542224
```

```
[60,] 0.5276388443 -0.006467768 -1.13184708 -1.037563687 -0.3943684645
##
   [61,] -0.7112950315 -0.410681453 0.90026249 -1.881215978 0.0677326093
   [62,] 1.8477692857 1.379112224 1.97334369 -1.097727840 0.4781473499
   [63,] 1.4334734197 -0.235317290 -0.52865128 0.271710665 -0.2686849459
##
   [64,] 0.0322055351 0.661079198 2.11815565 2.179553328 -0.4467323509
##
   [65,] 0.3845580664 0.693551858 -1.56616248 0.861733545 0.4016338291
   [66,] -0.3752095097 -0.507609336 -1.28661133 -0.058102341 0.2191598432
   [67,] -0.5238996935 1.343144122 -1.07144429 -1.170411268 -0.4323137263
##
##
   [68,] -2.2897814308 1.259089813 0.16536719 1.723198146 0.6891189702
   [69,] -0.2922268949 -1.179775123 -0.27784862 0.130423739 0.0278793308
##
   [70,] -1.1711574794 1.203717377 -2.12106758 0.213688393 -0.6716659668
   [71,] -0.7990157917 1.415584646 0.51638552 -0.127006341 0.5777949010
##
   [72,] 0.8675685081 1.328624249 0.40162591 0.447451464 -0.7298876066
   [73,] 0.6190665638 -0.571006396 -1.50676429 -0.454143125 -0.5497464601
##
##
   [74,] -0.5357870330 0.751077596 0.10985869 -0.370183567 -0.8866783336
   ##
##
   [76,] 1.4706127595 -0.638811282 0.04200290 0.284627017 -0.6241287568
   [77,] -1.0662979277 -0.541417006 1.67024759 0.896084860 -0.5289344240
   ##
   [79,] -2.2194051229 1.776170990 0.91686398 -0.156480444 0.7161318219
   [80,] 0.4939808392 -2.424698731 -0.07266249 0.678051521 -1.6215086760
##
   [81,] -1.3135250976   0.245650569   0.11298776   0.745692618 -0.8544789969
   ##
   [83,] 1.7390844040 0.341238118 0.30071664 -2.451872315 0.1504138570
##
   [84,] -2.2052544514 -0.265018144 0.49987998 0.823514136 2.1875434324
   [85,] 0.9034317365 -0.603097086 -2.00795472 1.419032714 0.8199597959
##
   [86,] -2.4020758679 -0.009135280 0.15996292 -1.012748987 -1.0663867556
   [87,] 0.5886095189 -0.008882872 0.33077466 -1.093529274 0.2700596061
   [88,] 2.0906063024 0.682227760 -0.04972848 -0.673518990 -0.7649046319
##
   [89,] 0.1079713923 1.774412672 1.04961148 -0.169069312 -0.0234724094
         1.0518800082 -0.377026135 0.13287803 -2.056237230 0.2818794417
##
   [90,]
##
   [91,] 0.1232144234 0.235153560 0.01725499 0.602100203 -2.8219595869
   [92,] -0.2183743530 -2.024199837 0.66795215 -0.036691345 -0.1511943467
   [93,] 0.6153209488 -0.893246407 0.31509953 -0.830069972 -2.0060867048
##
##
   [94,] 0.7885863722 -0.188578951 -0.54854113 0.480312649 0.1352759730
##
   [96,] -0.1823444078 -0.083611914 -1.83425921 0.769362783 -0.2050849305
##
   [97,] -1.6369477486 1.409680474 0.04162469 -0.097915401 -0.8268959038
   [98,] -0.1241344407 1.116707239 1.26680488 -0.591466825 -0.2192598129
##
   [99,] 0.1738358550 2.158538876 0.31225246 0.204317303 0.5105027223
##
  [100,] -2.9736297362 1.020958096 0.96167276 0.220254952 -1.6262367315
##
                          [,82]
                                     [,83]
                                                 [,84]
                                                            [,85]
              [,81]
    [1,] 1.04557456 -1.707663770 -0.348563056 0.946591649 -0.46617694
##
##
    [2,] 0.34079678 -0.227307455 0.701538332 0.815869846 -0.95459019
##
    [3,] 0.06613566 -1.532587915 1.771204164 0.564946232 1.51167005
    [4,] -0.23102495 -0.842605142 -0.889921387 -0.459939493 0.77925000
##
    [5,] -0.22227681 0.376463990 0.803455788 2.001683499 0.27416505
##
    [6,] 0.85765720 -0.385128198 -1.546160437 -2.685360397 0.76938792
##
##
    [7,] 0.70428034 0.633996935 1.341798984 -0.972399271 -0.46865023
    [8,] -1.12995860 1.580014938 1.895740971 0.192981509 -0.97069793
##
##
    [9,] 0.92079613 1.029498629 0.663909664 -0.161346422 0.56291211
##
   [10,] -0.41103883 -2.169792088 0.535379159 0.210811972 -1.33114446
##
   [11,] -0.37775757 -0.284175613 0.499258669 -1.883039807 0.41529560
```

```
[13,] 0.64661074 -1.961351750 1.017847345 0.252785223 0.25729741
##
   [14,] 2.76772787 0.294845284 0.055557338 -0.358699261 1.01356786
   [15,] -1.06274149 1.380965168 1.395582841 -0.379058843 0.87769626
   [16,] -0.42727307 -1.774735006 1.213751287 0.807688897
                                                         0.53875321
   [17,] -0.42861167 1.046301094 -0.743038310 -1.484605000
                                                         1.18290365
##
   [18,] 0.42415082 -0.434846019 1.320770024 2.120635822 -1.43570967
   [19.] -1.52014727 -0.207151615 -0.466718893 -1.116204991 -0.47897732
   [20,] 0.46203035 -0.570827112 0.319637279 0.757877171 -1.44531147
##
##
   [21,] 0.08873503 0.225520598 1.114933029 -1.125729687
                                                         0.07637302
   ##
   [23,] -1.12612066 -0.164867222 0.001703985 1.338952365
                                                         1.38091996
   [24,] -0.01713436 -0.942143720 -1.896702596 -0.765019487
##
                                                         0.09167359
   [25,] 0.50136063 -1.045404948 0.492632461 1.131784884 0.22913131
   [26,] 0.30131153 -0.293017449 -0.052977696 -0.401206041 0.35572748
##
##
   [27,]
          ##
   [28,]
         0.75361586  0.383857672  -0.948692445  -0.175086911  0.37812176
##
   [29,] 0.36057010 -0.121247034 -1.457845430 0.934126830 0.76437700
   [30,] -0.08716097  0.817929282 -1.000473711 -0.758930043 -0.82520518
   [31,] 1.25708095 -0.092811230 -0.644660322 1.432305087 -0.22721447
##
   [32,] -0.35167217 -0.486305735 0.028420511 0.334578037 0.97244862
##
##
   [33,] 0.69783886 -0.701845978 1.040301689 -0.851886895 -0.50246470
   [34,] 0.30279451 -0.059686816 -0.420797047 -0.472185327 0.89889047
          0.59235711 \ -0.454916711 \ \ 0.746354116 \ -0.506747485 \ -0.60899729
##
   [35,]
         0.02689754  0.320262761  0.080660290  0.007353696  1.51345275
##
   [36.]
   [37,] -0.69091839 -1.147112487 0.389611965 0.243096481 -0.04577217
##
   [38,]
         1.27695742 1.380982694 -0.825112448 0.018942943 0.81218866
##
   [39,] -0.70650791 -1.575422021 0.387822506 -1.076578335 -0.23721675
   [40,] 0.16124945 -1.244666828 -0.237529461 0.426974173 -0.05611000
##
   [41,] 1.06065845 -0.741735756 -0.003316561 -1.334938627 0.85121467
   [42,] 1.20782286 0.405977679 0.579766426 -0.221325429 1.38361027
   [43,] 0.11191176 -0.888053440 -0.619160140 -0.048951146 -0.40605760
##
##
   [44,] -0.04540095  0.605269160  0.527604382  1.140061505  1.12986220
   [45,] 0.08402064 -0.216919654 0.500475292 1.326913753 0.84156830
   [46,] -1.43902033  0.466689374 -0.752597919 -0.181984889  0.33079383
##
##
   [47,]
         1.13839092 0.118571231 0.353525156 -1.216418816 0.85833770
##
   ##
   [49,] 0.34658766 1.838906957 -0.339898817 1.329080818 -0.13694866
##
   [50,] 0.12144728 -0.469021732 1.419566432 0.168654113 -1.64025175
   [51,] -0.11146226 -1.266441134 -1.277194464 1.546248774 0.31581863
##
##
   [52,] -0.91362986 2.264751588 -0.493817419 -0.864068259 0.43938920
   [53,] 1.42903659 1.605837099 0.595397189 1.250447298 -0.41648695
##
   [54,] 0.87646508 -1.090829815 -2.187950549 -0.398812897 -0.40135023
   [55,] 0.46611437 -1.257404807 1.366727553 -0.621777052 -0.22550976
   [56,] 0.42954547 0.645586459 -0.875959796 0.416045756 1.46264878
##
          1.28772239 1.133534826 1.324385246 -2.734499390 -0.96353559
         1.20091113 -0.661363287 0.232991393 0.102511440 -0.63650131
##
   [58,]
##
   [59,] -0.11863093   0.104462665   0.585834648 -1.178550864 -1.76598938
   [60,] 0.37588350 -0.735782513 -0.297198793 1.009379943 -1.84522994
##
   [61,] 1.46036418 -0.058492279 -2.133679347 -0.210741150 0.70540564
         1.19571094 -0.876951753 1.222215454 0.278558549 -1.03925226
##
   [62,]
##
   [63,] -2.65429074 -0.290219311 0.639527440 -1.820058157 0.53604159
##
   [64,] -0.24718226 -1.371375518 -0.921475234 -0.463270409 0.58562436
##
   [65,] 1.31561626 -0.050000694 2.241645597 -0.713597983 0.49909607
   [66,] -1.07981059 -0.965933431 -1.521555086 3.216171096 0.23326399
```

```
[67,] -0.29188517 -1.065250766 1.532470299 -0.800369753 2.10703514
##
   [69,] -0.49558986 -1.436931631 0.655990753 -0.824811646 -0.12044791
   ##
##
   [71,] 0.19955107 -1.237645433 0.427012438 0.222259041 -1.48645123
   [72,] 0.57652319 1.079380622 0.510448884 -0.562292571 -0.10282532
##
   [73,] -0.08456486 1.046020730 -1.827357389 -0.766936030 -0.14792380
   [74,] -1.13409611 0.002354793 -0.421833171 -1.705541483 -1.75393855
##
##
   [75,] -0.16657933 -0.287462079 -0.641318663 0.088083510 0.21160201
##
   [76,] -1.13611132 -0.244606961 1.835870030 0.672956232 -1.09993696
   [77,] 0.33728457 -0.415474648 0.019338319 -0.445786866 1.06975915
   [78,] -0.20529937 -0.476821059 -0.400111074 -0.064232318 -0.38384578
##
   [79,] -2.62870545 1.541987388 -0.921290776 0.330822858 0.22572955
##
   [80,] 1.50760759 0.466480832 -1.571958157 0.516092015
                                                       2.89924480
##
   [81,] -0.09594560 -0.038483917 1.893957495 1.068214945 0.81119254
##
   [82,] 0.30841395 -0.775904613 -0.996422320 -1.301781979 -2.02409965
##
   [83,] 0.33449874 0.184857224 -1.145273913 1.799878929 0.19319899
   [84,] -0.68555260 0.402765520 -1.359654845 2.279975616 -0.09245809
   [85,] 1.77137391 0.737978527 -1.895771255 1.966552522 0.20511694
##
##
   [86,] -1.90856665 -0.004226220 0.595845124 1.234372938 -0.93439424
##
   [87,] -1.39492785 -0.258255466 0.710229197 -0.076927499 0.12710094
   [88,] -0.89651976 1.507452214 0.254948830 0.130670566
##
   [89,] -0.86438715 -2.078108317 1.327208782 -0.796677838 0.31748904
   [90,] 0.11886392 -0.909643860 0.437171337 -0.589727450 -0.84582040
##
   [91,] 1.20050536 -0.568478588 0.566902438 1.170490547 0.41944781
   [92,] -0.96288976 0.972215438 -0.964903046 0.657350024 0.74189548
##
   [93,] 1.01188782 -0.007287691 -2.021104762 1.163789372
                                                       0.25058939
   [94,] -0.30581730 1.854256714 1.430200350 0.696297713
                                                       0.42808756
   [95,] 0.39369981 -1.520465958 -1.098587696 -2.655743592 0.45692007
   [96,] -0.43468083  0.307909704  0.557277581 -0.383984194 -0.45410134
   [97,] 1.15490812 -0.884043792 0.147695632 0.123742340 0.64812957
##
##
   [98,] 0.21556960 -0.121852084 0.518675357 0.947782137 0.34942030
   [99,] 0.14578966 -0.559707876 -0.964527638 1.011918839 -0.52852871
  [100,] -0.78644863 -0.715447532 0.751197992 -0.981860369 0.03545725
##
##
              [,86]
                         [,87]
                                    [,88]
                                               [,89]
                                                          [,90]
##
    [1,] -0.91388221 -0.70163852 -0.98410671 -1.13944449 0.41168475
##
    [2,] -1.50539338 -1.05509871 -0.19429053 -0.45885718 0.18164103
##
    [3,] -1.59230529  0.65504625 -1.43382413 -2.25911292 -2.22133087
##
    [4,] 0.18664478 -0.80188691 -0.39857340 0.86213070 -1.58371322
##
    [5,] -1.98674152 -0.23571525 -0.43134141 0.90144541 -1.43112091
    [6,] 1.38342666 1.11531339 -0.54503870 -0.49526441 2.35214576
##
##
    ##
    [8,] 2.22989015 -0.55757959 0.88874268 1.25391397 -0.52902864
##
    [9,] 1.51092512 -0.80374872 -0.07051533 0.53111054 -1.16161206
   [10,] 0.24633456 1.67256318 0.20660295 0.38558063 -0.10478330
         [11,]
##
##
   [12,]
         0.33760671 -2.70680265 1.74457310 -0.07710834 0.08153367
##
   [13,]
         1.25630973 1.52408279 0.62095282 -0.43622419 0.79223799
   [14,] 0.13108514 0.83294760 0.04257191 0.96975475 -1.28429322
##
   [15,] -0.35523752 -1.76984974 0.36164434 0.37997417 2.36271723
   [16,] -0.06412923 2.31783575 0.16290301 0.11046713 1.06775141
##
##
   [17,] 0.58164801 -0.76156871 0.30632498 -1.42672418 -0.12319774
##
   [18,] 1.71261170 0.57983243 -1.68534374 -0.21189483 -0.31059579
   [19,] 0.61269872 -1.63157885 0.98522650 0.16751506 -0.04751218
```

```
[20,] 0.01092701 0.08577768 -1.83301626 -0.68151153 -0.65678850
##
    [21,] 0.23402359 1.62585549 -0.21047469 -0.50659513 -0.16251438
    [22,] -0.74127105  0.46822158 -0.03462979  0.02522993  0.17365229
          2.49375609 -0.01392664 0.06596791 -0.06679375
##
    [23,]
                                                         0.86128995
    [24,] 0.71440896 -1.30775360 -1.18235487 0.38059811
                                                         3.50058456
##
    [25,] 1.50871982 -1.15354606 1.40986707 -1.42746836 0.70176253
    [26.] -0.19209984 -0.14847838 -1.42876547 -0.56284080 -0.53623866
    [27,] -1.13362711 0.13425203 -0.68386285 0.88827422 0.19846111
##
    [28,] -1.03798699 -0.34838154 -1.56405225 -0.43589329 -1.26689548
##
##
    [29,] -0.45415740 1.00021149 -0.21467352 0.28524786 0.23865664
    [30,] 0.44900506 -0.29717917 0.16088290 0.76534658 -1.72558723
    [31,] 0.12464454 -0.71465314 0.86135861 1.28378343 0.26116487
##
    [32,] -0.12214260 -0.22577772 1.25215150 0.34850639 -0.76907430
    [33,] 0.76530007 -0.57434519 0.16951937 -0.81563030 -1.38396482
##
##
    [34,] 0.02055042 1.30808053 0.74137124 -0.56882885 0.32048795
##
    [35,] 0.84023403 0.05942897 0.43326570 1.03703781 0.75013724
##
                                 1.53797625 -0.84281959 0.27563771
    [36,] -0.74231469 0.28913905
    [37,] 1.99716442 -2.15303988 0.07186623 2.93620301 0.78478423
   [38,] -0.67429466 0.07456080 1.08859320 -0.98638654 0.11029216
##
    [39,] 1.69399750 0.12976291 -0.39555985 -0.61498803 -1.46004604
##
    [40,] -1.61299568 -1.71776324 -0.15296103 -1.40969604 -0.28109584
    [41,] 0.59939388 -1.37581604 -0.60379126 0.12253232 0.03553948
    [42,] -0.97944596 -0.53217327 0.51339889 -0.55945320 -1.11356032
##
          0.95530682 -0.46523888 -0.41224443 -0.05427725 0.59125116
    ſ43.l
##
    Γ44.]
         0.18434592 -1.51408471 -0.32543527 0.24509090 -0.31206900
    [45,] 0.52195821 0.74675370 -0.52766030 -0.38792878 -0.31340630
##
    [46,] -1.61551715 -0.17167859 -0.01208556 1.33965476 0.15789047
    [47,] 0.56178368 -1.53984020 1.00081743 0.93003825 -1.61089435
##
   [48,]
          1.10500932 -0.67187981 -1.33623539 0.83346270 -0.06560354
    [49,]
          0.72098830 0.11629689 -0.35474753 -1.34384357 -0.08397503
          0.40331906 3.30419791 0.70805068 0.58984791 -1.00934244
##
    [50,]
##
    [51,]
          1.53574339 -0.07022911 0.12461848 -0.59434968 0.29721918
##
    [52,]
          0.94298882 - 0.14436360 \ 0.99219684 \ 0.50314534 \ 0.73430319
          0.21492528 -1.50146225 -1.22349638 -1.18121765 0.14212934
##
    [53,]
##
    [54,]
          0.69563859 -1.78214329 -0.31658100 -1.51511158 0.11088286
##
    [55,] 1.27118700 0.58124938 -0.22015401 -0.47975341 -1.51868587
##
    [56,] -0.48307258  0.05108228 -0.30770154  0.25837618  0.55296655
##
    [57,] 1.31352541 -0.09165002 -0.28564638 0.88600717 -0.79678461
    [58,] 1.57142262 -0.58085238 -0.33726070 1.62189198 -0.18753446
##
##
    [59,] -0.79263997  0.36810846 -0.43718182  2.13326717 -0.96291298
    [60,] -0.38697077 -0.61402163 2.25661264 -0.41098524 0.80530347
    [61,] -0.37382040 0.15523129 0.61100183 -0.09267711 -0.06614084
##
    [62,] -0.41400178 -0.67484293 0.54827024 -0.08809678 1.01726070
##
    [63,] 0.28712207 -0.55812372 0.79294978 0.81008025 0.41668965
    [64,] 0.87790650 0.87046157 -0.28482776 0.19933632 -1.54573621
    [65,] 0.36331930 0.90225513 0.32997070 -0.33949716 -1.17476970
##
##
    [66,] -0.87194968 -0.34673254 -0.05925068 0.20472789 -1.01948643
    [67,] -0.98434007  0.45824288  0.28271813  0.41599423  2.21246533
    [68,] -0.73929767 1.39784688 -1.24996414 0.94149933 -0.10689455
##
    [69,] -0.77072453 1.45043307 -0.41553183 -1.25903656 0.20252289
##
    [70,] 0.10949852 0.13369390 0.17628220 0.93722763 0.18619289
##
    [71,] 0.32639459 0.89241163 -0.82081430 -0.83408721 0.18632098
##
    [72,] -1.03824112 -0.69314600 -0.01609058 0.86756888 0.71378023
    [73,] 0.43866791 -3.21787319 0.10165188 0.32418457 -1.05818742
```

```
[74,] -0.77252123 1.74337380 -1.68029013 0.72651835 0.01429265
##
   [75,] -0.93763206 -0.74254210 -0.60048294 -1.20861026 0.99247141
   [76,] 0.06966605 -0.28182398 -2.26071976 1.08207130 0.36417867
   [77,] -1.00613292 -0.41836643 -1.61881244 0.19287654 -0.50087370
##
   [78,] 1.37089106 -1.32755883 0.08158756 -0.16686040 -0.53787630
##
   [79,] -2.30097052 0.93481075 1.41600321 -0.44928139 -0.39245577
##
   [81,] -0.89102485  0.61132479 -0.09093114 -1.10081348  0.71459256
##
##
    [82,] 0.07099588 -0.27855895 0.07502606 -0.58775811 2.18795470
##
   [83,] -0.21307194 -1.21603301 -0.21708593 -0.31718357 -0.67155840
   [84,] -0.61246093 1.88296788 -0.01916635 0.89828813 0.25809667
   [85,] 0.06107556 1.13221706 -1.57864997 1.29355648 -1.21983732
##
##
   [86,] 0.10273886 0.05139273 0.74839097 0.83969627 -1.12736979
   [87,] -0.01697305 2.34351419 -0.58878140 0.46979661 0.41610006
##
##
          0.40135080 1.31308107 0.52912163 -0.14488386 -0.72887367
   [88,]
          1.46573563 -0.80783417 0.58839395 0.75572870 0.52876125
##
   [89,]
   [90,] 1.66425578 -0.55806246 -0.74596756 -0.52910549 1.42838246
##
   [91,] 0.35335464 -0.16956024 0.83083953 0.93123985 -0.35199995
   [92,] -0.36430159  0.65255214 -0.49300981 -0.12025997 -0.19251642
##
##
   [93,] -1.35362904 1.05017032 -0.63566350 1.84999609 -0.23612588
##
   [94,] 0.04457645 1.14895278 0.90220719 0.81588340 1.45806030
   [95,] -0.31244824 -0.45745910 0.57338345 1.66376707 -0.35724157
   [96,] 0.06863892 0.03573686 -1.50765520 0.21369612 -0.11330123
##
   [97,] -0.89051010 1.03420280 -0.47111711 0.58918873 -1.15544482
##
##
   [98,] -0.82623407 2.06464094 1.68489521 -0.52995801 0.26534910
   [99,] -1.04525087 -1.54530421 0.34679914 0.30086960 0.94590689
##
   [100,] 0.87437197 -0.67966529 -1.49264546 0.53671381 -0.03848747
##
                [,91]
                             [,92]
                                         [,93]
                                                      [,94]
                                                                  [,95]
##
    ##
    [2,] -1.168969160 0.0367025775 1.513759558 -0.0006826256 -0.206133734
    [3,] 1.531333354 1.1825136951 -0.161295253 2.7209365821 0.763464690
##
##
    [4,] -0.740267516 -0.3321966063 -0.136236566 -2.0195362661 -0.051801535
##
    [5,] 0.392131072 0.2538873820 -1.638365308 1.3421014300 0.655453863
    [6,] -0.821805532 -2.3567886271 0.560991884 -0.5997847300 -0.217788172
##
##
    [7,] -0.468702452 -0.9004700310 -1.658915025 0.1290708385 0.791390398
##
    [8,] 0.431090969 0.9763573382 0.384437030 0.9257023060 -0.961012270
##
    [9,] 0.392364427 0.3976294288 1.121326548 0.0785079662 -1.375198641
##
   [11,] 0.081173852 -0.6478720882 0.099536126 -0.6091949774 -0.379102416
   [12,] -0.997948582 -0.0577563670 -1.500680131 -0.9657802226 0.617426093
##
   [13,] 1.852940549 -0.2875376144 0.849230530 -1.0786352623 -0.735152555
   [14,] -0.433002214 -1.4129668001 -0.088946746 -1.3628264405 1.075370180
##
   [15,] 0.990503935 -0.7672041610 -0.186851029 1.0409248712 -0.831675885
##
   [16,] 0.171569049 0.1884742265 0.566105071 0.0174965304 -1.795436172
   [17,] 0.123672562 -0.7316512098 0.822496809 0.1688983735 0.552768367
   [18,] -1.336336620 0.9171681187 -0.881304484 -0.6338377507
##
                                                            1.206265126
##
   [19,] 0.230031470 -0.6252005407 0.001746887 -0.1143921213
                                                            0.568407594
   [20,] -1.190552212 -0.0008618322 -1.527681460 0.3889512323 -0.447177580
##
   [21,] 0.465228108 -0.8026254803 -1.239112147 1.0874259736 2.169965405
   [22,] 0.306766051 -0.5489624522 0.717011416 0.3151969862 -0.131701535
##
   [23,] -0.100338253  0.7906608648 -0.862400364  0.2424985029
##
                                                            0.445324473
##
   [24,] -0.036459714 -0.1669801266 -1.594692184 -0.2336842357
                                                            0.320347933
##
   [25,] 1.642613160 -0.7882444934 0.044178470 -0.7028271510 0.363644917
   [26,] -1.088148127  0.3556284900  0.008577016 -1.6490601373  1.446834582
```

```
[27,] -1.566137072 0.0966561622 0.778804623 -0.0665753297 1.300893407
##
   [28,] -1.376382620 0.2269700048 -0.686304966 0.3733823407 -0.569471044
   [29,] -0.280583444 1.1973340438 -0.350632070 0.4094725158 0.625888604
##
   [31,] 0.909988286 0.9641192345 0.862249216 2.6305530894 0.360836799
##
   [32,] -0.137396126 -1.0585634166  0.910423486  0.4662802226 -1.879006175
   [33,] -0.348087172   0.8193515805   0.057542881 -0.8259661582   0.880151554
##
   [34,] -0.533332729  0.7531089234  0.979950078 -0.6446935100 -1.426115809
##
   [35,] 0.556625426 0.4301710591 0.351436585 -1.1618527814
                                                           0.146991288
##
   [36,] 1.040700640 -1.8063461043 -1.083112999 -2.5423034859 1.186750411
   [37,] -1.061318756 -0.7559952852 -0.106333729 -1.9122182199 -1.642859450
   [38,] 1.034938803 0.1040306509 0.832883815 0.2168505002 0.322808058
##
   [39,] -0.578298996  0.0266069130  0.633664143 -1.0793936111 -0.638065082
   [40,] 0.005033962 1.1934358905 0.178792717 0.0359313660 0.628693402
##
##
   [41,]
          0.209507949 1.9537708112 -0.460802308 -1.1375099189
                                                          0.482424684
##
   [42,]
          1.390784372  0.5115839823  -1.692555154  -0.1652679889
                                                          1.357785339
##
         0.238539017 -0.3641441356 1.315120496 0.4433140378 -0.002905162
   [43,]
         1.827863368
        1.455301774 1.2136672211 0.370605727 -1.1086892353 0.237999195
##
   [45,]
##
   [46,] -0.724153539  0.0868508703 -0.417224226 -1.5262864925 -1.522532027
##
   [47,] -0.815883494 -0.9849524024 0.382070698 -0.0619848260 0.612637110
   [48,] -0.285815213 -0.7597699033 -0.704331909 1.4358286107 0.083367878
   [49,] 0.537684392 -0.7305917618 1.363837473 -1.1154748390 0.961023877
##
   [50.] 0.340066605 1.2526040880 -0.368040250 -1.3704418533 1.570190301
   [51,] -0.875484265 -0.4924730508 2.907474651 -0.1280031760 -0.599619095
##
   [52,] 0.070101522 -1.1024417073 -1.337610171 0.2964759078 -0.148095867
##
   [53,] -1.396734042 -0.1880222972 -0.447923657 2.1084391256 -1.793990028
   [54,] 0.216382371 0.8630065864 -1.301472776 -2.5507841773 0.344850059
##
   [55,] -1.003462091 1.4651605681 0.440996467 -1.2906689021 0.915376172
   [56,] -0.227462823  0.2295207928  1.115728531  0.5436320020 -0.527860609
##
   ##
   [58,] -0.976761049 0.6053693493 -0.734805305 -1.2051693256 -0.985516298
   [59,] -0.949940445 0.1495397831 -0.218401659 1.3912127777 -0.601993099
   [60,] -1.431040641 -0.2215859784 -0.538422138 -0.1775856392 1.594072922
##
   [61,] 0.032480162 -0.1127065811 1.704289206 0.1142125076 -0.505221635
##
##
   [62,] 0.261930875 0.3733803629 -0.707130816 1.0723708505 -1.896178547
   [63,] -1.681999530 -0.1490833868 0.113823481 1.4419772612 -0.492044000
##
   [64,] 1.230704703 -2.0035693277 1.337248772 -0.4019339470 -0.076338969
   [65,] 0.144939931 1.7723609355 1.556711976 -0.5314738991 1.557625470
##
##
   [67,] -0.849210096 1.3196833628 -0.065171952 -0.5081005724 1.416423171
##
   [68,] 0.381236409 -0.3937056373 -0.300669422 0.2790556642 -1.077231456
   [69,] -0.869595346  0.8347980013 -0.168261724 -0.4715951227 -0.725483144
##
   [70,] -0.357967479 -0.3539550009 -1.041849904 0.6313191459 -1.642233254
   [71,] -0.798525107 -0.2126366773 -0.507454149 -0.6222838840 0.465854540
   [72,] -0.278217644 0.1601968911 -0.560622910 -2.6267827873 -0.737386667
##
   [73,] 0.725526276 1.2797617949 -0.207593974 0.4270890481 0.354033566
   [74,] -2.365705172 1.6906717365 -0.036961005 -1.4525113254 -0.739815933
##
   [75,] 0.023071469 -1.3603289715 -2.511469292 0.7054773516 -0.425478417
##
   [76,] 1.265183444 0.0893089753 -0.234773067 -0.0374874229 0.297314181
##
   [77,] -1.166020659 0.5544079532 1.872695083 0.8266490537 -1.174579734
##
   [78,] -0.898864159  0.9413605618  0.531505172 -0.5677788890  2.064969154
##
   [79,] -1.163914313 -0.3146801402 0.667960369 0.4695261577 1.440369042
   [80,] -0.132390462 -0.7937129538 1.678458455 -0.2225191495 -0.888678996
```

```
[81,] -1.891472077  0.0495057200 -0.747356753  0.4323718897  0.580978486
##
   [82,] 0.205245497 0.5990185211 0.447480820 0.1560528140 0.735242946
   [83,] 0.913215887 -0.5789655571 -0.757523624 0.7753745712 -1.419302540
   [84,] 1.599904312 -1.7005501431 1.156263572 -1.5346434838 0.950939459
##
   [85,] -0.352407934 2.0586798800 -1.106936185 0.2855454047
                                                             0.087599531
##
   [86,] 1.304411657 -1.1383469673 0.168046160 -0.4256381346 -0.112460073
   [87.] -1.200788396  0.6129079749  0.452907931  1.2786691970  0.553137117
##
   [88,] 1.122635843 -0.6380048660 -0.112904388 -0.1968059139 0.116860979
   [89,] 1.131027190 1.5086101886 2.187012613 0.7160799868 -0.424672763
   [90,] -1.396487481 0.0180388639 -0.241008724 -1.3885104032 -1.582012605
##
   [91,] 0.514843897 -0.5843672655 0.671689436 0.5918764454 1.103343598
   [92,] -0.696079924  0.3100340806  1.013604013  0.7210312150 -1.484652312
##
   [93,] -0.297402227 -2.2323264911 0.275920921 0.8859283167 -1.088214818
   [94,] 1.231444469 1.7867607013 -0.351214686 1.3853955228 1.165926065
##
##
   [95,] 2.184157749 1.0774213116 -0.643024840 -0.1050989116 1.608015756
   [96,] 0.195192209 0.5825135438 2.098245316 -1.3523084373 -0.243488125
##
##
   [97,] -1.988293964   0.0106302176   -0.959797920   0.0159231296   -0.082601334
   [98,] 1.573004340 1.0756724735 0.849599425 0.2340532891 0.061573939
   [99,] 0.386802709 -0.8878524664 0.974589269 -0.5338664885 -0.680747080
##
   [100,] -2.228219935 0.2113296476 0.513294508 -0.5401887264 -3.521906016
##
               [,96]
                           [,97]
                                         [,98]
                                                     [,99]
                                                               [,100]
##
    [1,] -1.27474780 1.354520268 1.4692032339 -0.159614198 0.74111071
##
    [2,] 0.49177291 0.077883720 0.4306430292 -1.032363279 -0.36547125
    \lceil 3. \rceil -0.43954918 0.244412341 -0.8949059387 -0.230051884 -0.85865950
##
    [4,] 0.31717254 0.933773388 -0.5978560120 0.210534815 -0.12599130
##
##
    [5,] -1.83297314 -0.221846495 -1.8335337168 0.825162201 -0.61881586
##
    [6,] 0.04514524 2.039850468 0.2010155666 0.617906033 -1.07703227
##
    [7,] -0.87673591 -0.474865939 0.2383421942 1.149685348 0.15642189
##
    [8,] 2.42475254 0.034561173 -0.8698769071 1.155717284 0.92485985
##
    [9,] 0.06001700 0.122759685 -4.3082098105 -0.413746431 -1.20589880
    [10,] -0.37152855    1.369925619    1.3089691007    0.003113223    0.72720265
##
##
   [11,] 1.80282882 -0.259288187 1.3297536662 -0.440323145 0.93083395
   [13,] 0.65675769 0.604213739 0.1811195904 -0.751692452 -1.03548648
##
##
   [14,] -0.91522197  0.404515743  -0.2619895325  -0.084091839  0.63755359
##
   [15,] 0.25721442 1.049274762 0.4074925186 -0.263939480 0.74143848
   [16,] 0.89977884 -0.741001017 -1.1044983686 -0.738388648 -0.37806462
##
   [17,] -1.40579897 -0.285028364 0.4677338293 -1.361074976 1.03493790
          ##
   [18,]
##
   [19,] 0.55931132 1.066071711 -0.0117882346 -0.025714429 -1.74328968
   [20,] 1.28575495 -0.624957216 1.2761930892 1.445500194 0.05603083
##
   [21,] -0.44082158  0.374399741  0.9452749692  0.182811250  0.19572165
   [22,] 2.28265954 -0.131204854 0.3066724290 -0.038169638 0.68017447
##
   [23,] -0.55075464 0.421835387 0.5227693584 -0.356236401 0.35375807
   [24,] 0.54108139 -0.438298584 1.8541366741 -1.082174846 -1.07566854
   [25,] -1.02421694   0.710766785   -0.3451345818   2.068897529   0.08328506
##
   [26,] -0.72641638 -1.078275969 -0.3164931300 -1.163798879 -1.66190366
   [27,] 1.34825769 0.427155934 0.5214338496 -0.591291562 -1.23590963
##
   [28,] 0.19855672 1.163302928 0.3647977779 0.460394783 1.03730501
##
   [29,]
         1.40859615
##
   [30,] -1.08759079 -0.050412281 1.6268835256 -0.101309669 0.17609950
##
   [31,] 0.86904270 1.079971434 0.0600666963 -2.906113165 -1.73400868
##
   [32,] 0.30384749 0.443758177 -1.0813335450 -0.333928540 -0.85514522
   [33,] 0.60177834 0.867080233 -0.7949093893 -0.102066372 -0.45057976
```

```
[34,] 0.35955696 -0.913503622 0.5714201761 0.091904805 0.40126274
##
    [35,] -1.04585650 -0.159240122 -0.1050282423 0.789432137 -1.16025688
    [36,] -0.28941172   0.152897165 -0.6689342762   1.277863478 -1.13956401
   [37,] 0.08145676 -1.218352796 -1.3212691553 0.487392122 -0.71017237
##
    [38,] 0.86059488 -0.334314275 1.8570489390 -0.328139394 1.05490148
##
    [39,] 0.62615373 -0.503945517 -2.0242906371 -1.168480474 -2.14725406
    [40.] -0.13677090 0.419784053 1.1916694325 0.126996379 -1.57604797
##
    [41,] -1.05457100 0.133947139 -0.7572357266 -0.151663930 -0.57080307
    ##
    [43,] 0.05265519 0.935229287 -1.7620845697 -0.271277971 -0.48849735
   [44,] 0.59870625 -0.945140668 -0.9866477283 0.962584116 0.07632585
    [45,] 0.13184891 0.811742006 -0.0004803698 -1.030416818 -0.21585093
##
    [46,] 1.00131296 1.619607593 -0.6034435287 0.506128055 -0.75163732
   [47,] -1.78165489 1.252346934 -0.2188794077 0.099864443 0.16178929
##
   [48,] -0.58278888 -0.648519923 -2.3793641253 -1.283404911 0.47705240
    [49,] 0.86961540 -1.397067007 0.6783220086 0.870090212 -0.87593725
##
##
    [50,] 0.68315567 0.798923706 -2.1755084612 0.643409210 0.57474624
    [51,] -1.42417359 -1.830480541 -1.3658631338 1.859811733 0.31709678
   [52,] 0.85276657 0.879548463 -0.4507743638 0.687557395 2.63119854
##
    [53,] 0.22345971 1.861294319 -0.5741821963 -0.806708109 -0.11334671
##
    [54,] 0.30390556 1.434601928 0.1145522063 1.458830749 -0.29478233
    [55,] -0.40890778 -1.115530400 0.0476201818 -0.123470648 1.52884692
    [56,] 2.14511108 0.014736352 1.0132638700 1.035703064 1.74249792
##
    [57.] -0.88658188    0.065124350    1.1586246924    0.081604197    1.15652473
    [58,] 0.97307541 -0.096546206 0.4879378659 -1.079126927 -1.88107050
##
    [59,] -0.45410970 -1.398912799 0.1313384881 1.081613607 -0.10664763
##
    [60,] 0.35571248 -2.084101908 -0.4738213169 -0.386309207 -0.76798762
    [61,] -0.86395112 -0.451180368 -0.7931195669 -1.581312355 -0.56258008
##
    [62,] 1.06745534 -0.840751913 1.2012363210 0.206441718 0.86101886
    [63,] -1.96491651 -0.564894295 -0.0380104018 -0.429032117 0.60546820
    [64,] -0.72049734 -0.071550838 -0.1520262653 0.064592610 -0.34118273
##
##
    [65,] 0.10147793 0.554382179 -0.0250895718 -0.531225598 0.93490341
    [66,] 1.62660812 0.348008487 -1.7324240503 -0.224896116 0.09434743
##
    [67,] 0.04031332 -0.572613310 -0.6599212768 -1.390633369 -1.37920487
##
         1.37016205 -1.387639950 2.2328548752 -0.712486078 -1.42168524
##
##
    [69,] -1.66849114 0.108751536 0.1621686908 -0.172621030 1.31023399
    [70,] -1.96849255 -1.736703571 -2.0074911155 -1.653881090 -0.34830082
##
    [71,] 0.34494744 1.740010437 0.1126619655 -0.324647973 -0.34967712
    [72,] -2.02899395 1.385538226 0.2586384737 0.183604505 0.01926513
##
##
    [73,] -1.06648621 -0.716728737 2.4839033927 0.424892290 0.22354400
    [74,] 0.48481189 -0.664024684 -0.8146073742 1.606804245 0.55447976
##
    [75,] -0.54574742 1.235060173 0.1057362394 0.119715997 -0.15041048
    [76,] 1.43551565 -0.271105955 0.4598511198 -0.562058301 -1.81611624
##
    [77,] -0.27176955 0.492685802 0.6892355066 0.634034887 1.06211388
   [78,] -1.73297539 -0.007374464 -0.9833502122 1.107004340 0.39323089
    [79,] -1.39505608 -2.035919186 -0.1137071197 0.681151719 0.53521123
##
##
    [80,] 0.87578434 -0.874433398 -0.0424988677 -1.125182844 0.47031088
    [81,] 1.59526085 0.754686326 -1.4608064116 -0.612963208 -0.57475399
##
    [82,] -0.28537569 -2.427736947 0.7162375500 -0.698366628 -0.06774922
    [83,] -1.83818607 -0.836870266 -1.2905184398 1.097222062 0.23077943
##
##
    [84,] 1.14176188 1.130860577 1.3448048414 -0.314873546 1.32602030
   [85,] -2.64601138 -1.197931497 -0.8098191347 1.080091453 -0.04229422
##
##
    [86,] -1.43135669 1.008502317 2.1574172265 -1.582808123 0.16782728
    [87,] 0.26221938 2.335627589 0.5356576054 -0.549740883 -0.90821971
```

```
[88,] -1.40526588 1.023265904 -0.0775722754 0.285286316 -0.66904876
##
    [89,] 1.10897323 -1.318148820 0.5915361334 1.392066956 -0.98964566
##
    [90,] 1.13373175 -0.664001561 1.5900760695 0.315036033 0.38566163
   [91,] -2.05849828 -0.076989489 -2.5159642043 -0.039834359 -0.29151646
##
##
    [92,] 0.62062036
                     1.454758540 -0.2608585313
                                                 0.497478506 -0.58136822
   [93,] -0.65507395  0.060491452  1.4418516230  0.584495974  -0.96039256
##
   [94,] -1.63226365 -1.541458225 1.4625694389 -0.773305693 0.00346609
##
   [95,] -0.21083074 -0.145429075 0.9698467867 -0.403440427
##
                                                              1.76274983
   [96,] -0.19347371 1.436344320 0.0012068720 1.171671960 -2.35213558
##
   [97,] 0.18116949 0.093033591 -0.0672609628 -0.642139589 0.82409963
##
   [98,] -0.01579832 -0.713378611 -1.7994201106 -1.396698564 0.26329688
   [99,] -0.24720640 -2.038072999 1.6437262501 -0.233832947 1.53763250
## [100,] 0.45436225 -0.633041854 -1.8553622294 -0.471281062 -0.55962005
#for each time you make a for loop run save evry chind you into a df
\#run an ols y against x
#do another cbind
#print r^2 for each you do
```

Add one final column to X to bring the number of columns to 101. Then try to compute \mathbb{R}^2 . What happens and why?

```
#X <- as.matrix(cbind(X, rnorm(100))</pre>
```