

大学物理之《光学》

一. 质点运动学

$$\textcircled{1} |\int_a^b d\vec{r}| = |\vec{r}_b - \vec{r}_a| \text{ 位移模长} \quad \textcircled{2} \int_a^b |d\vec{r}| = s_{ab} \text{ 路程} \quad \textcircled{3} \int_a^b d\vec{r} = \vec{r}_b - \vec{r}_a$$

$$\text{切向加速度 } a_t = \frac{dv}{dt}, a_n = \frac{v^2}{\rho}; \text{极坐标 径向 } a_r = \frac{dr}{dt} - r\omega^2, \text{横向 } a_\theta = r \frac{d\theta}{dt} + 2 \frac{dr}{dt} \cdot \frac{d\theta}{dt}$$

二. 质点运动定律

三. 机械能和功

$$\text{保守力 } \oint \vec{F} \cdot d\vec{r} = 0 \quad \vec{F} = -\nabla E_p = -\left(\frac{\partial}{\partial x}\vec{i} + \frac{\partial}{\partial y}\vec{j} + \frac{\partial}{\partial z}\vec{k}\right) E_p$$

四. 动量和角动量

$$e = \frac{v_2' - v_1'}{v_1 - v_2} \quad \begin{cases} v_1' = v_1 - m_2 \frac{(1+e)(v_1 - v_2)}{m_1 + m_2} \\ v_2' = v_2 + m_1 \frac{(1+e)(v_1 - v_2)}{m_1 + m_2} \end{cases}$$

$$\text{变质量 } F = m \frac{dv}{dt} + u \frac{dm}{dt}$$

$$\text{角动量 } \vec{L} = \vec{r} \times \vec{p} \quad \vec{M} = \vec{r} \times \vec{F} = \frac{d\vec{L}}{dt}$$

五. 刚体力学基础

$$\vec{\alpha} = \frac{d\vec{\omega}}{dt}, \vec{a}_t = \vec{\alpha} \times \vec{r}, \vec{a}_n = \vec{\omega} \times (\vec{\omega} \times \vec{r})$$

$$J = \sum m_i r_i^2 = J_c + md^2$$

$$\vec{M} = J\vec{\alpha}, \vec{L} = J\vec{\omega}, M\alpha t = L - L_0$$

$$E_k = \frac{1}{2} J \omega^2, A = \int m d\theta = E_k - E_{k0}$$

$$\text{进动 } \vec{M} = \vec{\omega}_p \times \vec{L}, \omega_p = \frac{M}{J\omega} = \frac{mgr}{J\omega}$$

$$\text{电扇 } P = M\omega$$

六. 振动力学基础

$$x = A \cos(\omega t + \varphi), \omega = \sqrt{\frac{k}{m}}, T = 2\pi \sqrt{\frac{m}{k}}$$

$$E_p = \frac{1}{2} k x^2, E_k = \frac{1}{2} m v^2, E = \frac{1}{2} k A^2$$

$$\text{同向同频 } x = A \cos(\omega t + \varphi) \quad A = \sqrt{A_1^2 + A_2^2 + 2A_1 A_2 \cos(\varphi_2 - \varphi_1)}$$

$$\text{* 阻尼 } \tan \varphi = \frac{A_1 \sin \varphi_1 + A_2 \sin \varphi_2}{A_1 \cos \varphi_1 + A_2 \cos \varphi_2}$$

七. 狭义相对论基础

$$\Delta t = \frac{\Delta t_0}{\sqrt{1 - \frac{u^2}{c^2}}} \quad (L = L_0 \sqrt{1 - \frac{u^2}{c^2}}) \quad \begin{cases} x' = \frac{x - ut}{\sqrt{1 - \frac{u^2}{c^2}}}, t' = \frac{t - \frac{u}{c^2}x}{\sqrt{1 - \frac{u^2}{c^2}}} \\ x = \frac{x' + ut'}{\sqrt{1 - \frac{u^2}{c^2}}}, t = \frac{t' + \frac{u}{c^2}x'}{\sqrt{1 - \frac{u^2}{c^2}}} \end{cases}$$











八. 热力学平衡态

$$pV = \nu RT, R = 8.31$$

$$p = nkT, n \text{ 分子数密度 } k = \frac{R}{N_A} = 1.38 \times 10^{-23}$$

$$\text{理想压强 } p = \frac{1}{3} n m \bar{v}^2 = \frac{2}{3} n \bar{\epsilon}_t, \text{ 平均平动动能 } \bar{\epsilon}_t = \frac{3}{2} kT$$

$$\text{平均动能: } \frac{3}{2} kT, \frac{5}{2} kT, 3kT \quad \text{内能 } E = \nu \frac{i}{2} RT$$

	圆环 转轴通过中心 与环面垂直		圆环 转轴沿直径
$J = mr^2$		$J = \frac{mr^2}{2}$	
	薄圆盘 转轴通过中心 与盘面垂直		圆筒 转轴沿几何轴
$J = \frac{mr^2}{2}$		$J = \frac{m}{2}(r_1^2 + r_2^2)$	
	圆柱体 转轴沿几何轴		圆柱体 转轴通过中心 与几何轴垂直
$J = \frac{mr^2}{2}$		$J = \frac{mr^2}{4} + \frac{ml^2}{12}$	
	细棒 转轴通过中心 与棒垂直		细棒 转轴通过端点 与棒垂直
$J = \frac{ml^2}{12}$		$J = \frac{ml^2}{3}$	
	球体 转轴沿直径		球壳 转轴沿直径
$J = \frac{2mr^2}{5}$		$J = \frac{2mr^2}{3}$	

九. 热力学定律

十七. 机械波

软绳 $u = \sqrt{\frac{F}{\rho}}$

固体 $u = \sqrt{\frac{G}{\rho}} = \sqrt{\frac{Y}{\rho}}$

气体 $u = \sqrt{\frac{\gamma RT}{M}}$

波动方程 $\frac{d^2 y}{dx^2} = u^2 \frac{d^2 y}{dt^2}$

能量密度 $\epsilon_k = \frac{d\epsilon_k}{dV}$

$= \frac{1}{2} \rho \omega^2 A^2 \sin^2(\omega t - \frac{x}{u})$

$\epsilon_p = \frac{d\epsilon_p}{dV} = \frac{1}{2} \rho \omega^2 A^2 \sin^2(\omega t - \frac{x}{u} + \varphi)$

$\epsilon = \rho \omega^2 A^2 \sin^2(\omega t - \frac{x}{u}) \quad \bar{\epsilon} = \frac{1}{2} \rho \omega^2 A^2$

能流密度 $J = \epsilon u \quad I = \bar{\epsilon} u = \frac{1}{2} \rho \omega^2 A^2 u$ (强度)

多普勒 $V = \frac{u \pm v_r \cos \alpha}{u \mp v_s \cos \beta} \quad v_s$

相对论多普勒

红移 $1+z = (1+\frac{v}{c})\gamma = \frac{1-\cos\theta/c}{\sqrt{1-\frac{v^2}{c^2}}}$

$z = \frac{\lambda_o - \lambda_e}{\lambda_e}$

引力红移 $1+z = \frac{1}{\sqrt{1-\frac{2GM}{rc^2}}}$

观超光速

$AB = v\delta t$
 $AC = v\delta t \cos \theta$
 $BC = v\delta t \sin \theta$
 $t_2 - t_1 = \delta t$
 $t'_1 = t_1 + \frac{D_L + v\delta t \cos \theta}{c}$
 $t'_2 = t_2 + \frac{D_L}{c}$

$\delta t' = t'_2 - t'_1 = t_2 - t_1 - \frac{v\delta t \cos \theta}{c} = \delta t - \frac{v\delta t \cos \theta}{c} = \delta t(1 - \beta \cos \theta)$, where $\beta = \frac{v}{c}$

$\delta t = \frac{\delta t'}{1 - \beta \cos \theta}$

$BC = D_L \sin \phi \approx \phi D_L = v\delta t \sin \theta \Rightarrow \phi D_L = v \sin \theta \frac{\delta t'}{1 - \beta \cos \theta}$

沿路径 CB 的观测横向速度为 $v_T = \frac{\phi D_L}{\delta t'} = \frac{v \sin \theta}{1 - \beta \cos \theta}$

$\beta_T = \frac{v_T}{c} = \frac{\beta \sin \theta}{1 - \beta \cos \theta}$

$\frac{\partial \beta_T}{\partial \theta} = \frac{\partial}{\partial \theta} \left[\frac{\beta \sin \theta}{1 - \beta \cos \theta} \right] = \frac{\beta \cos \theta}{1 - \beta \cos \theta} - \frac{(\beta \sin \theta)^2}{(1 - \beta \cos \theta)^2} = 0$

$\Rightarrow \beta \cos \theta (1 - \beta \cos \theta)^2 = (\beta \sin \theta)^2$

