

$$A3) \quad \mathbf{z} = \begin{bmatrix} x \\ \dot{x} \\ I \end{bmatrix} = \begin{bmatrix} z_1 \\ z_2 \\ z_3 \end{bmatrix} \quad \dot{\mathbf{z}} = \begin{bmatrix} z_2 \\ \frac{5m}{7} \left(mg \sin \phi + \frac{c z_3^2}{(\delta - z_1)^2} - k(z_1 - d) - b z_2 \right) \\ \frac{1}{L_0 + L_1 e^{-\kappa(\delta - z_1)}} (V - z_3 R) \end{bmatrix}$$

$$\begin{aligned} \dot{z}_1 &= z_2 \\ \dot{z}_2 &= \frac{5m}{7} \left(mg \sin \phi + \frac{c z_3^2}{(\delta - z_1)^2} - k(z_1 - d) - b z_2 \right) \\ \dot{z}_3 &= \frac{1}{L_0 + L_1 e^{-\kappa(\delta - z_1)}} (V - z_3 R) \end{aligned}$$

Characterising the equilibrium point : $f(z^e, v^e) = 0$

$$\begin{aligned} 0 &= z_2^e \\ 0 &= \frac{5m}{7} \left(mg \sin \phi + \frac{c (z_3^e)^2}{(\delta - z_1^e)^2} - k(z_1^e - d) - 0 \right) \quad \text{as } z_2^e = 0 \\ 0 &= \frac{1}{L_0 + L_1 e^{-\kappa(\delta - z_1^e)}} (V^e - z_3^e R) \quad \text{makes sense as vel of ball = 0} \end{aligned}$$

Subtracting:

$$\begin{aligned} \dot{z}_1 &= z_2 - z_2^e \\ \dot{z}_2 &= \frac{5m}{7} \left(mg \sin \phi + \frac{c z_3^2}{(\delta - z_1)^2} - k(z_1 - d) - b z_2 \right) - \frac{5m}{7} \left(mg \sin \phi + \frac{c (z_3^e)^2}{(\delta - z_1^e)^2} - k(z_1^e - d) \right) \\ \dot{z}_3 &= \frac{V - z_3 R}{L_0 + L_1 e^{-\kappa(\delta - z_1)}} - \frac{V^e - z_3^e R}{L_0 + L_1 e^{-\kappa(\delta - z_1^e)}} \end{aligned}$$