

B1) Due to the forces present on the System, the ball is only able to equilibrate within a defined space along the plane; Utilizing the characterised EQ points defined in Section [I], this space can be defined

$$0 = \frac{v^e - z_3^e R}{L_0 + L_1 e^{-k(\delta - z_1^e)}} \Rightarrow v^e = z_3^e R$$

$$0 = \frac{5}{7m} \left[ mg \sin \phi + \frac{c(z_3^e)^2}{(\delta - z_1^e)^2} - k(z_1^e - d) \right]$$

$$0 = mg \sin \phi (\delta - z_1^e)^2 + c(z_3^e)^2 - k(z_1^e - d)(\delta - z_1^e)^2$$

$$c(z_3^e)^2 = (\delta - z_1^e)^2 [k(z_1^e - d) - mg \sin \phi]$$

$$z_3^e = \frac{(\delta - z_1^e) (k(z_1^e - d) - mg \sin \phi)^{1/2}}{\sqrt{c}}$$

$$\therefore v^e = \frac{R(\delta - z_1^e) (k(z_1^e - d) - mg \sin \phi)^{1/2}}{\sqrt{c}}$$

Evidently from these equations, inputting a value of  $z_1^e(x^e) \leq \left( \frac{mg \sin \phi}{k} + d \right)$  would result in the voltage and current becoming undefined, i.e.: resulting in a zero or imaginary value. Furthermore, a value of  $z_1^e(x^e) \geq \delta$  would create a zero or negative result for the equilibrium values which indicate that <sup>the electromagnet</sup> polarity has <sup>switched</sup> ~~changed~~, thus the ball ~~would~~ <sup>would</sup> not achieve equilibrium. These derivations enable the space to be defined:

$$x_{\min} < x^e < x_{\max}$$

$$\text{where } x_{\min} = d + \frac{mg \sin \phi}{k} \quad x_{\max} = \delta$$

Furthermore, using equation ( $v^e = \dots$ ) the ball's equilibrium position at which the equilibrium voltage attains a maximum can be determined.

[...]

As presented in the figure the maximum voltage is app. equal to 0.2 volts where the equilibrium position is equal to 0.467m.