

# Tugas Besar IF3270 Pembelajaran Mesin Artificial Neural Network

## Bagian A: Implementasi Forward Propagation untuk Feed Forward Neural Network

Jaringan saraf tiruan pada bagian feed forward neural network (FFNN) menggunakan bahasa python.

### Kelompok 1

- 13520004 Gede Prasidha Bhawarnawa
- 13521076 Moh. Aghna Maysan Abyan
- 13521110 Yanuar Sano Nur Rasyid
- 13521152 Muhammad Naufal Nalendra

```
In [ ]: # Import necessary Libraries
import numpy as np
import networkx as nx
import matplotlib.pyplot as plt
import pandas as pd
import sys
import json
```

Fungsi aktivasi

```
In [ ]: # Softmax Activation Function Implementation
def softmax(arr):
    arr = np.array(arr)
    arr = np.exp(arr)
    sum_arr = np.sum(arr)
    return arr/sum_arr
```

```
In [ ]: # Sigmoid Activation Function Implementation
def sigmoid(arr):
    numerator = np.exp(arr)
    denominator = numerator + 1
    return numerator / denominator
```

```
In [ ]: # Linear Activation Function Implementation
def linear(arr):
    return arr
```

```
In [ ]: # Rectified Linear Unit (ReLU) Activation Function Implementation
def relu(val):
    if val < 0:
        return 0
    else:
        return val
```

```
In [ ]: def countSSError(results, expected_results):
    results = np.array(results)
```

```

expected_results = np.array(expected_results)
if results.shape != expected_results.shape:
    print("Error: array shape mismatch")
    sys.exit(1)
else:
    return np.sum(np.square(results - expected_results))

```

## Implementasi

```

In [ ]: # Node Class and Instances
class Node:
    def __init__(self, node_number, node_type, node_level, activation_function,
                 self.node_number = node_number
                 self.node_type = node_type
                 self.node_value = node_value # For non-input nodes, this value is 0
                 self.node_level = node_level
                 self.activation_function = activation_function
                 self.weight = weight
                 self.output = 0
                 self.error = 0

    def getNodeNumber(self):
        return self.node_number

    def getNodeType(self):
        return self.node_type

    def getNodeValue(self):
        return self.node_value

    def setNodeValue(self, node_value):
        self.node_value = node_value

    def getNodeLevel(self):
        return self.node_level

    def getActivationFunction(self):
        return self.activation_function

    def getActivationFunctionValue(self, value):
        if self.activation_function == "linear":
            return linear(value)
        elif self.activation_function == "sigmoid":
            return sigmoid(value)
        elif self.activation_function == "relu":
            return relu(value)
        else: # Uses softmax
            return softmax(value)

    def getWeight(self):
        return self.weight

    def getStrWeight(self):
        return str(self.weight)

    def getNextLayerNodeNumbers(self, nodes):
        next_layer_nodes = []
        for node in nodes:
            if node.getNodeLevel() == self.node_level + 1:

```

```
        next_layer_nodes.append(node.getNodeNumber())
    return next_layer_nodes
```

```
In [ ]: class Model:
    def __init__(self, number_of_layers:int, number_of_nodes:int, nodes:list, ex
    self.number_of_layers = number_of_layers
    self.number_of_nodes = number_of_nodes
    self.nodes = nodes # We assume that bias are also nodes of value 1
    self.expected_results = expected_results
    self.max_sse = max_sse

    def getNumberOfLayers(self):
        return self.number_of_layers

    def getNumberOfNodes(self):
        return self.number_of_nodes

    def getNodeList(self):
        return self.nodes

    def getNodeByIndex(self, index):
        return self.nodes[index]

    def setNodeValueByIndex(self, index, node_value):
        self.nodes[index].setNodeValue(node_value)

    def getNodeByLevel(self, layer):
        nodes = []
        for node in self.nodes:
            if node.getNodeLevel() == layer:
                nodes.append(node)
        return nodes

    def getExpectedResults(self):
        return self.expected_results

    def getMaxSSE(self):
        return self.max_sse

    def getModelInfo(self):
        print("Number of Layers: ", self.number_of_layers)
        print("Number of Nodes: ", self.number_of_nodes) # Bias is also counted
        print("Nodes: ")
        for node in self.nodes:
            node.getNodeInfo()

    def printModelSummary(self):
        print("Model Summary:")
        print("-----")
        print("{:^10} | {:^10} | {:^10} | {:^10} | {:^10}".format("Node Number",
        for level in range(0, self.number_of_layers+2):
            nodes = self.getNodeByLevel(level)
            for node in nodes:
                print("{:^10d} | {:^10s} | {:^10d} | {:^10s} | {:^10s}".format(
                    node.getNodeNumber(), node.getNodeType(), node.getNodeLevel()
        print("-----")
        print("Expected Results: ", str(self.expected_results))
        print("Max SSE: ", self.max_sse)

    def getInputNodeNumbers(self):
```

```

        input_nodes = []
        for node in self.nodes:
            if node.getNodeLevel() == 0 and node.getNodeType() == "input":
                input_nodes.append(node.getNodeNumber())
        return input_nodes

    def getOutputNodeValues(self):
        output_nodes = []
        for node in self.nodes:
            if node.getNodeLevel() == self.number_of_layers - 1:
                output_nodes.append(node.getNodeValue())
        return output_nodes

    def printModelVisualization(self):
        edge_list = []
        layer_dict = {}
        for node in self.nodes:
            next_layer_nodes = node.getNextLayerNodeNumbers(self.nodes)
            for next_layer_node in next_layer_nodes:
                if self.getNodeByIndex(next_layer_node).getNodeType() == "bias":
                    pass
                else:
                    edge_pair = (node.getNodeNumber(), next_layer_node)
                    if edge_pair not in edge_list:
                        edge_list.append(edge_pair)
            layer_dict[node.getNodeNumber()] = node.getNodeLevel()
        G = nx.Graph(edge_list)
        nx.set_node_attributes(G, layer_dict, "layer")
        pos = nx.multipartite_layout(G, subset_key="layer", align="vertical")
        nx.draw(G, pos=pos, with_labels=True, node_size=1000, node_color='skyblue')
        plt.title("Feed-forward Neural Network Model Representation")
        plt.show()

    def exportToJSON(self, pathname):
        data = {}
        data["model"] = []
        for node in self.nodes:
            node_data = {
                "node_number": node.getNodeNumber(),
                "node_type": node.getNodeType(),
                "node_value": node.getNodeValue(),
                "node_level": node.getNodeLevel(),
                "activation_function": node.getActivationFunction(),
                "weight": node.getWeight()
            }
            data["model"].append(node_data)
        data["expected_results"] = self.expected_results
        data["max_sse"] = self.max_sse
        with open(pathname, 'w') as outfile:
            json.dump(data, outfile)

    def loadJSON(self, pathname):
        with open(pathname) as json_file:
            data = json.load(json_file)
            number_of_layers = 0
            number_of_nodes = 0
            nodes = []
            for node in data["model"]:
                node_instance = Node(node["node_number"], node["node_type"], nod
                nodes.append(node_instance)

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        if node["node_level"] > number_of_layers:
            number_of_layers = node["node_level"]
            number_of_nodes += 1
    expected_results = data["expected_results"]
    max_sse = data["max_sse"]
    return Model(number_of_layers, number_of_nodes, nodes, expected_resu

```

```

In [ ]: def readJSON(filename):
    nodes = []
    file = pd.read_json(filename)
    expect = file['expect']
    case = file['case']
    number_of_layers = len(case['model']['layers']) + 1 # Including input Layers
    node_counts = [case['model']['input_size']]
    for idx in range(0, number_of_layers - 1):
        layer = case['model']['layers'][idx]
        layer_node_count = layer['number_of_neurons']
        node_counts.append(layer_node_count)
    sum_per_layer = []
    for layer_idx in range(0, number_of_layers - 1):
        sum_per_layer.append(sum(node_counts[0:layer_idx+1]) + layer_idx)
    print("Node counts for all layers in the model: ", node_counts)
    # print("Node counts for all layers in the model: ", node_counts)
    # Set node_idx to start counting the nodes from index 0
    node_idx = 0
    # Set every first node value as bias
    set_node_to_bias = True
    # Retrieve input values
    # input_vals = case['input'][0]
    # print("Input values: ", input_vals)
    # Process input nodes
    for node_count in range(case['model']['input_size'] + 1):
        node_number = node_idx
        node_type = 'bias' if set_node_to_bias else 'input'
        node_level = 0
        node_value = 1 if set_node_to_bias else 0
        activation_function = ''
        # Weights info for the input Layer is located on the first array of the
        weights_info = case['weights'][0][node_count]
        weights = {}
        for next_layer_node_idx in range(node_counts[1]):
            weights_idx = -1
            if number_of_layers == 2:
                weights_idx = next_layer_node_idx + sum_per_layer[0] + 1
            elif number_of_layers > 2:
                weights_idx = next_layer_node_idx + sum_per_layer[0] + 2
            weights[weights_idx] = round(weights_info[next_layer_node_idx], 3)
        new_node = Node(node_number, node_type, node_level, activation_function,
        # Set next nodes as non-bias and add 1 to the node_idx
        set_node_to_bias = False
        node_idx += 1
        nodes.append(new_node)
    # Process hidden Layer nodes
    if len(node_counts) > 2: # If there are hidden Layers, more than just input
        # Reset set_node_to_bias to True for each hidden Layer
        set_node_to_bias = True
        for layer_idx in range(len(node_counts) - 1):
            if layer_idx == 0:
                continue # Input Layer has been processed
            for node_count in range(node_counts[layer_idx] + 1):

```

```

        node_number = node_idx
        node_type = 'bias' if set_node_to_bias else 'hidden'
        node_level = layer_idx
        node_value = 1 if set_node_to_bias else 0
        activation_function = case['model']['layers'][layer_idx-1]['activation']
        weights_info = case['weights'][layer_idx][node_count]
        weights = {}
        for next_layer_node_idx in range(node_counts[layer_idx + 1]):
            weight_idx = -1
            if layer_idx == number_of_layers - 2:
                weight_idx = next_layer_node_idx + sum_per_layer[layer_idx]
            else:
                weight_idx = next_layer_node_idx + sum_per_layer[layer_idx]
            weights[weight_idx] = round(weights_info[next_layer_node_idx])
            new_node = Node(node_number, node_type, node_level, activation_function,
                           set_node_to_bias = False)
            node_idx += 1
            nodes.append(new_node)
            set_node_to_bias = True
    # Process output layer nodes
    for node_count in range(node_counts[-1]):
        node_number = node_idx
        node_type = 'output'
        node_level = number_of_layers - 1
        node_value = 0
        activation_function = case['model']['layers'][-1]['activation_function']
        weights = {}
        new_node = Node(node_number, node_type, node_level, activation_function,
                       node_idx += 1
                       nodes.append(new_node)
    # Check nodes results:
    # for node in nodes:
    #     print("Node Info:")
    #     print("Node Number: ", node.getNodeNumber())
    #     print("Node Type: ", node.getNodeType())
    #     print("Node Level: ", node.getNodeLevel())
    #     print("Node Value: ", node.getNodeValue())
    #     print("Activation Function: ", node.getActivationFunction())
    #     print("Node weights: ", node.getWeight())
    #     print()
    expected_results = expect['output']
    max_sse = expect['max_sse']
    result = Model(number_of_layers, sum(node_counts), nodes, expected_results,
                   # print("Model Layers: ", number_of_layers)
                   # result.getModelInfo()
                   result.printModelSummary()
                   result.printModelVisualization()
    return result

```

In [ ]: `def inferenceData(model_src_name, return_model=False):`

```

model = readJSON(model_src_name)
# Fill all input nodes with values and then feed the values to the nodes of
input_nodes = model.getInputNodeNumbers()
file = pd.read_json(model_src_name)
expect = file['expect']
case = file['case']
data = case['input']

if np.array(data).ndim == 2:
    final_results = []

```

```

for arr in data:
    if len(arr) != len(input_nodes):
        print("Number of input nodes and number of features are not equal")
        sys.exit(1)

for idx in range(len(arr)):
    # print("Inserting value {} to input node {}".format(arr[idx], i
    model.setNodeValueByIndex(input_nodes[idx], arr[idx])

# Debug first Layer, whether the values are inserted correctly
# for node in model.getNodeByLevel(0):
#     print("Node {} has value {}".format(node.getNodeNumber(), node

for layer in range(0, model.getNumberOfLayers()+1):
    # Get all nodes in the Layer and then one by one feed the values
    # At first the values will be based purely on the node's values
    # Then it will be passed to the activation function to get the final
    nodes = model.getNodeByLevel(layer)
    next_node_values = {}
    for node in nodes:
        for next_node_key in node.getWeight().keys():
            if next_node_key not in next_node_values.keys():
                next_node_values[next_node_key] = node.getWeight()[n
            else:
                next_node_values[next_node_key] += node.getWeight()[n
    isSoftmax = False
    for next_node_key in next_node_values.keys():
        # print("Next node key: ", next_node_key)
        next_node = model.getNodeByIndex(next_node_key)
        next_node_value = next_node_values[next_node_key]
        if next_node.getActivationFunction() != "softmax" and not is
            isSoftmax = False
            next_node_value = next_node.getActivationFunctionValue(n
            next_node.setNodeValue(next_node_value)
            next_node_values[next_node_key] = next_node_value
        else:
            next_node.setNodeValue(next_node_value)
            next_node_values[next_node_key] = next_node_value
            isSoftmax = True
    if isSoftmax:
        # Process all nodes in the layer and then feed the values to the
        process_layer = layer + 1
        nodes = model.getNodeByLevel(process_layer)
        node_numbers_in_order = []
        node_values_in_order = []
        nodes_new_value_pair_key = {}
        for node in nodes:
            node_numbers_in_order.append(node.getNodeNumber())
            node_values_in_order.append(node.getNodeValue())
            nodes_new_value_pair_key[node.getNodeNumber()] = 0
        node_values_in_order = softmax(node_values_in_order)
        for idx in range(len(node_values_in_order)):
            nodes_new_value_pair_key[node_numbers_in_order[idx]] = n
        for node in nodes:
            if node.getNodeNumber() in nodes_new_value_pair_key.keys():
                node.setNodeValue(nodes_new_value_pair_key[node.getNodeN
# Debug the Layer, whether the values are inserted and calculate the
# for node in model.getNodeByLevel(layer+1):
#     print("Node {} has value {}".format(node.getNodeNumber(), node

```

```

        # print(model.getOutputNodeValues())
        final_results.append(model.getOutputNodeValues())
print("Raw final results: ", [x.tolist() for x in np.array(final_results)])
# Compare the results with the expected results
expected_results = model.getExpectedResults()
print("Expected results: ", expected_results)
print("Max SSE: ", model.getMaxSSE(), ", SSE: ", countSSError(final_results))
if countSSError(final_results, expected_results) <= model.getMaxSSE():
    print("The model is valid as the error is less than or the same as the maximum SS")
else:
    print("The model is invalid as the error is more than the maximum SS")

if return_model:
    return model

```

Test case sigmoid

```
In [ ]: # For Sigmoid model (sigmoid.json)
src_name = "testcase/ffnn/sigmoid.json"
inferenceData(src_name, False)
```

Node counts for all layers in the model: [3, 2, 4]

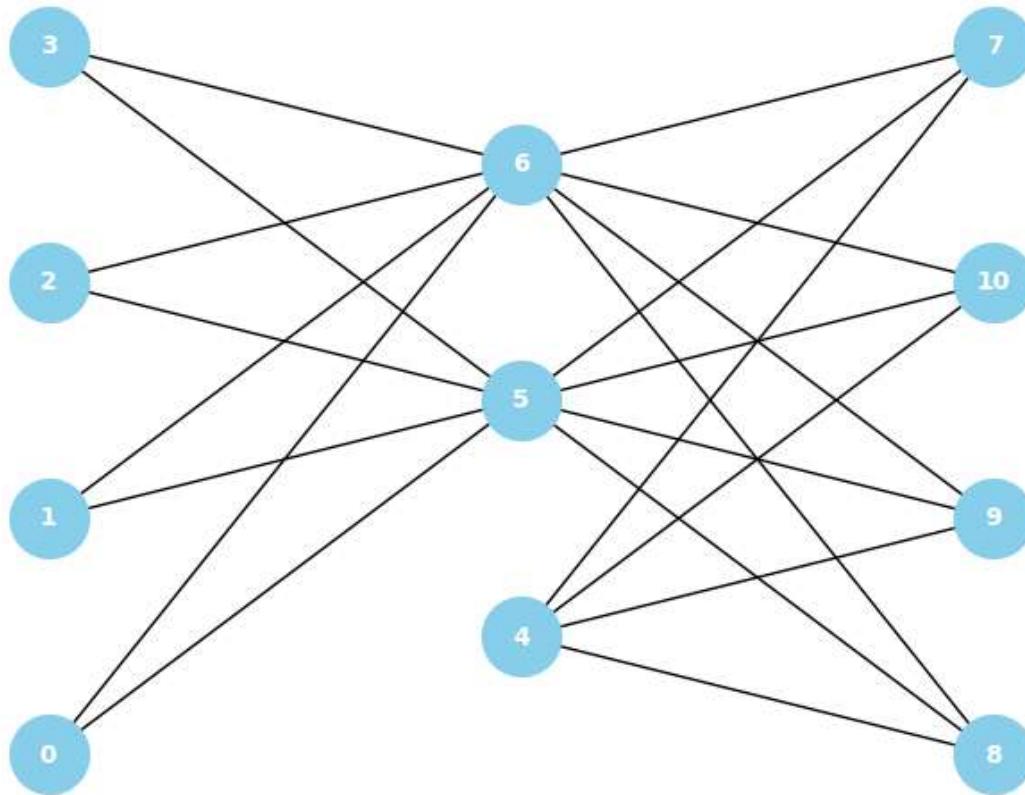
Model Summary:

Node Number	Node Type	Layer Depth	Activation Function	Weight
0	bias	0		{5: 0.6, 6: -1.2}
1	input	0		{5: -1.2, 6: -1.7}
2	input	0		{5: 1.4, 6: -1.6}
3	input	0		{5: -0.7, 6: 1.1}
4	bias	1	sigmoid	{7: -0.4, 8: 1.6, 9: 1.6, 10: -1.5}
5	hidden	1	sigmoid	{7: -0.0, 8: 0.0, 9: -1.5, 10: 0.7}
6	hidden	1	sigmoid	{7: 2.1, 8: -0.2, 9: 0.0, 10: 1.8}
7	output	2	sigmoid	{}
8	output	2	sigmoid	{}
9	output	2	sigmoid	{}
10	output	2	sigmoid	{}

Expected Results: [[0.41197346, 0.8314294, 0.53018536, 0.31607396], [0.78266141, 0.80843631, 0.55350518, 0.64278501], [0.58987524, 0.82160954, 0.75436518, 0.34919895], [0.6722003999999999, 0.8166043900000001, 0.59020258, 0.5087098800000001], [0.47322841, 0.82808466, 0.69105452, 0.2935832300000003]]

Max SSE: 1e-06

## Feed-forward Neural Network Model Representation



```
Raw final results: [[0.4119734556100492, 0.8314293993694081, 0.5301853632739774, 0.31607396490909706], [0.7826614091150282, 0.808436308319498, 0.5535051760955713, 0.6427850098146376], [0.5898752435296561, 0.8216095372737501, 0.7543651777362295, 0.3491989467036674], [0.6722003953978934, 0.8166043910016146, 0.5902025844263002, 0.5087098836277426], [0.4732284109743184, 0.8280846566130694, 0.6910545248579614, 0.2935832341653264]]
```

```
Expected results: [[0.41197346, 0.8314294, 0.53018536, 0.31607396], [0.78266141, 0.80843631, 0.55350518, 0.64278501], [0.58987524, 0.82160954, 0.75436518, 0.34919895], [0.6722003999999999, 0.8166043900000001, 0.59020258, 0.5087098800000001], [0.47322841, 0.82808466, 0.69105452, 0.2935832300000003]]
```

Max SSE: 1e-06 , SSE: 2.1756063057014992e-16

The model is valid as the error is less than or the same as the maximum SSE

Test case linear

```
In [ ]: # For linear.json testcase
src_name = "testcase/ffnn/linear.json"
inferenceData(src_name, False)
```

Node counts for all layers in the model: [1, 1]

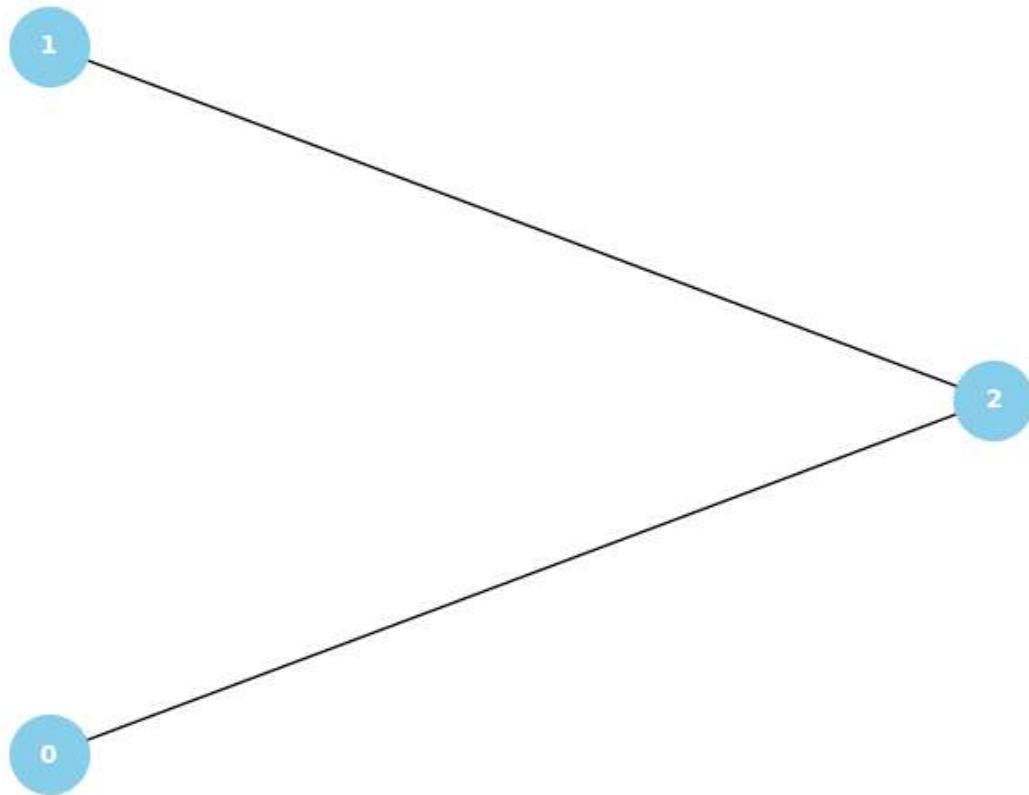
Model Summary:

Node Number	Node Type	Layer Depth	Activation Function	Weight
0	bias	0		{2: 1.0}
1	input	0		{2: 3.0}
2	output	1	linear	{}

Expected Results: [[-11], [-8], [-5], [-2], [1], [4], [7], [10], [13], [16]]

Max SSE: 1e-12

## Feed-forward Neural Network Model Representation



Raw final results: `[[ -11.0], [-8.0], [-5.0], [-2.0], [1.0], [4.0], [7.0], [10.0], [13.0], [16.0]]`  
 Expected results: `[[ -11], [-8], [-5], [-2], [1], [4], [7], [10], [13], [16]]`  
 Max SSE: `1e-12`, SSE: `0.0`  
 The model is valid as the error is less than or the same as the maximum SSE

Test case relu

```
In [ ]: # For ReLU model (relu.json)
src_name = "testcase/ffnn/relu.json"
inferenceData(src_name, False)
```

Node counts for all layers in the model: `[2, 3]`

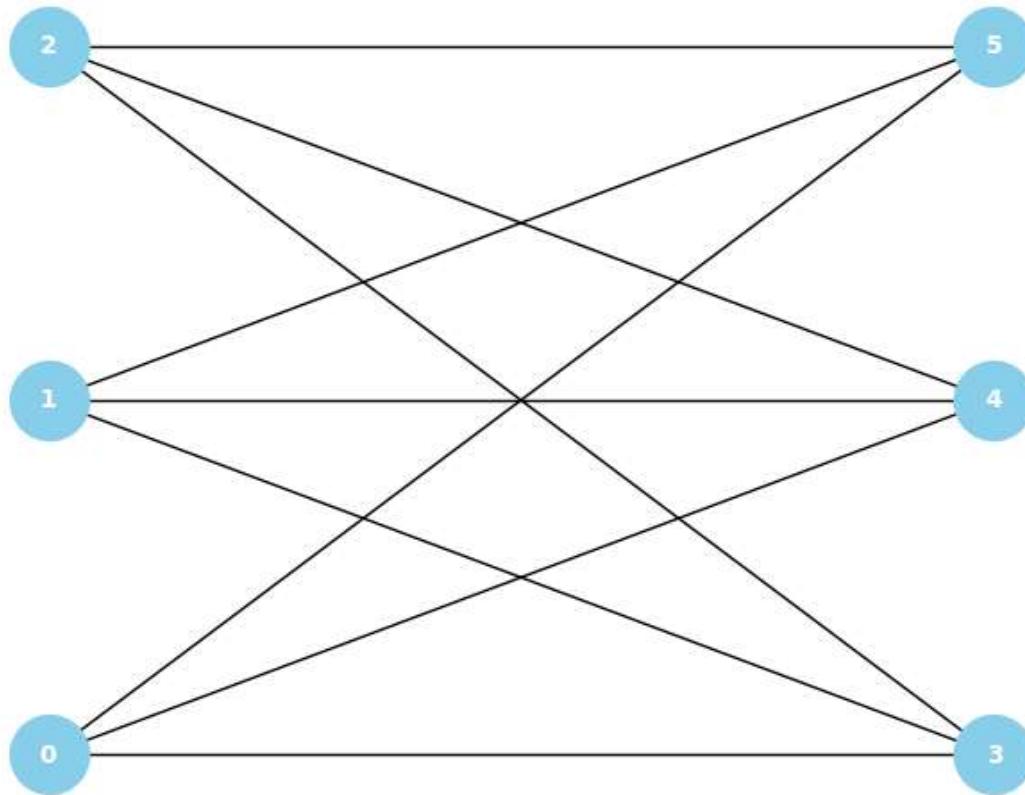
Model Summary:

Node Number	Node Type	Layer Depth	Activation Function	Weight
0	bias	0		{3: 0.1, 4: 0.2, 5: 0.3}
1	input	0		{3: 0.47, 4: -0.6, 5: 0.2}
2	input	0		{3: 1.1, 4: -1.3, 5: 0.5}
3	output	1	relu	{}
4	output	1	relu	{}
5	output	1	relu	{}

Expected Results: `[[0.31, 0, 0.375]]`

Max SSE: `1e-06`

## Feed-forward Neural Network Model Representation



Raw final results: [[0.3099999999999999, 0.0, 0.3750000000000001]]

Expected results: [[0.31, 0, 0.375]]

Max SSE: 1e-06 , SSE: 2.465190328815662e-32

The model is valid as the error is less than or the same as the maximum SSE

Test case relu di docs

```
In [ ]: # For ReLU model (reludocs.json)
src_name = "testcase/ffnn/reludocs.json"
inferenceData(src_name, False)
```

Node counts for all layers in the model: [2, 3]

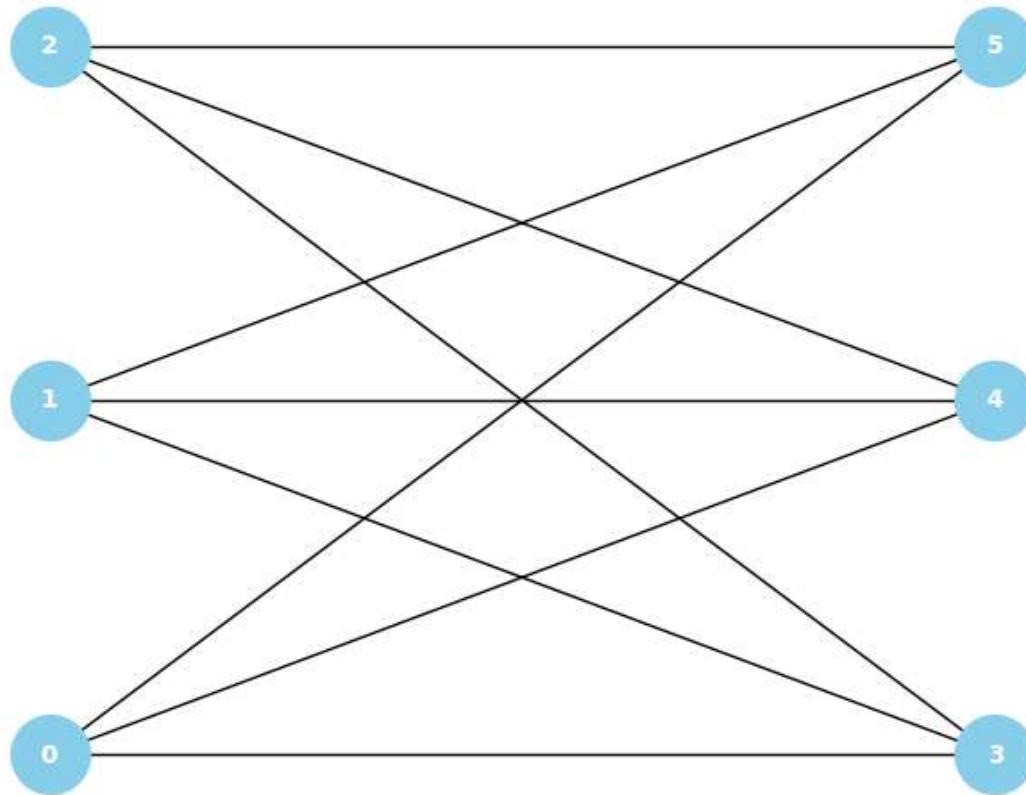
Model Summary:

Node Number	Node Type	Layer Depth	Activation Function	Weight
0	bias	0		{3: 0.1, 4: 0.2, 5: 0.3}
1	input	0		{3: 0.4, 4: -0.5, 5: 0.6}
2	input	0		{3: 0.7, 4: 0.8, 5: -0.9}
3	output	1	relu	{}
4	output	1	relu	{}
5	output	1	relu	{}

Expected Results: [[0.05, 1.1, 0.0]]

Max SSE: 1e-06

## Feed-forward Neural Network Model Representation



Raw final results: [[0.04999999999999993, 1.1, 0.0]]

Expected results: [[0.05, 1.1, 0.0]]

Max SSE: 1e-06 , SSE: 4.8148248609680896e-33

The model is valid as the error is less than or the same as the maximum SSE

Test case softmax

```
In [ ]: # For Softmax model (softmax.json)
src_name = " testcase/ffnn/softmax.json"
inferenceData(src_name, False)
```

Node counts for all layers in the model: [8, 3]

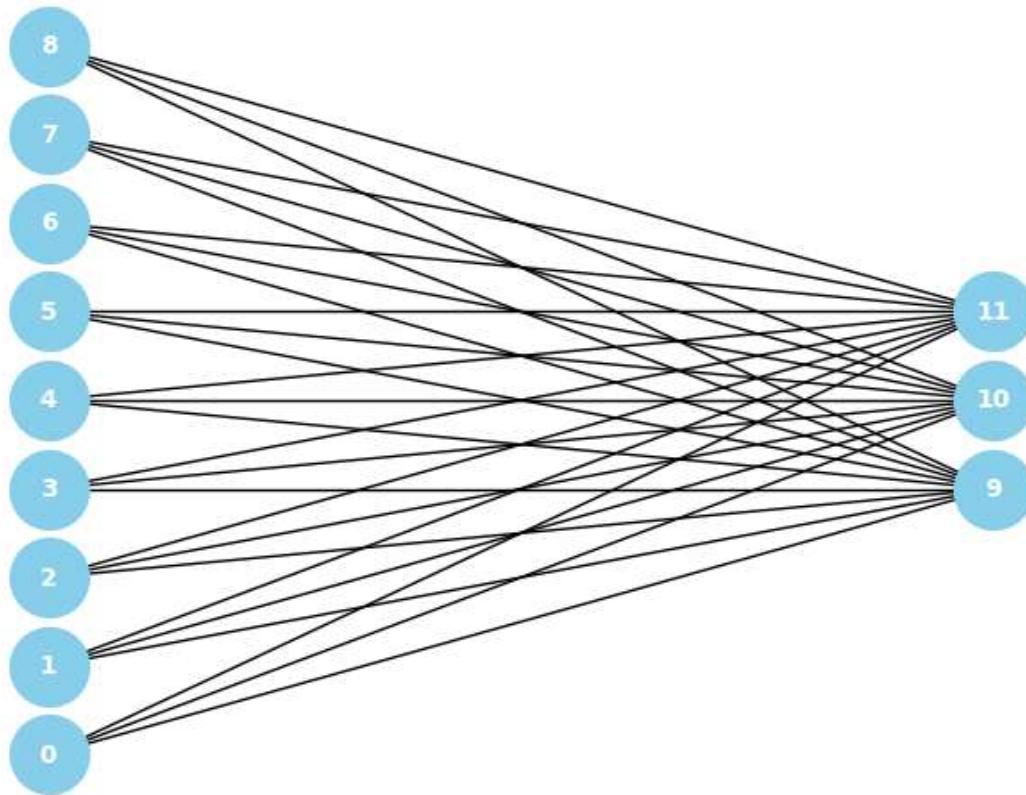
Model Summary:

Node Number	Node Type	Layer Depth	Activation Function	Weight
0	bias	0		{9: 0.1, 10: 0.9, 11: -0.1}
1	input	0		{9: -0.2, 10: 0.8, 11: 0.2}
2	input	0		{9: 0.3, 10: -0.7, 11: 0.3}
3	input	0		{9: 0.4, 10: 0.6, 11: -0.4}
4	input	0		{9: 0.5, 10: 0.5, 11: 0.5}
5	input	0		{9: -0.6, 10: 0.4, 11: 0.6}
6	input	0		{9: -0.7, 10: -0.3, 11: 0.7}
7	input	0		{9: 0.8, 10: 0.2, 11: -0.8}
8	input	0		{9: 0.9, 10: -0.1, 11: 0.0}
9	output	1	softmax	{}
10	output	1	softmax	{}
11	output	1	softmax	{}

Expected Results: [[0.76439061, 0.21168068, 0.02392871]]

Max SSE: 1e-05

## Feed-forward Neural Network Model Representation



Raw final results: [[0.7643906087005896, 0.21168068289764497, 0.023928708401765485]]

Expected results: [[0.76439061, 0.21168068, 0.02392871]]

Max SSE: 1e-05 , SSE: 1.263916713483999e-17

The model is valid as the error is less than or the same as the maximum SSE

Test case multilayer

```
In [ ]: # For Multilayer model (multilayer.json)
src_name = " testcase/ffnn/multilayer.json"
inferenceData(src_name, False)
```

Node counts for all layers in the model: [3, 4, 3, 2, 1]

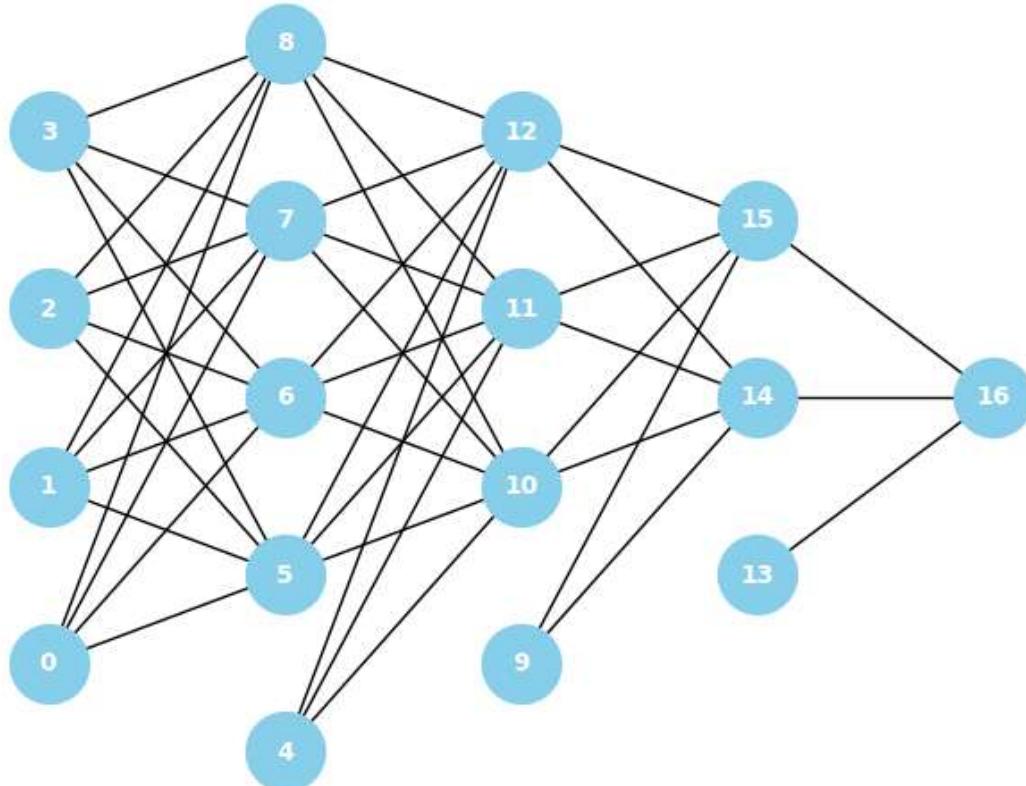
Model Summary:

Node Number	Node Type	Layer Depth	Activation Function	Weight
0	bias	0		{5: 0.1, 6: 0.2, 7: 0.3, 8: -1.2}
1	input	0		{5: -0.5, 6: 0.6, 7: 0.7, 8: 0.5}
2	input	0		{5: 0.9, 6: 1.0, 7: -1.1, 8: -1.0}
3	input	0		{5: 1.3, 6: 1.4, 7: 1.5, 8: 0.1}
4	bias	1	relu	{10: 0.1, 11: 0.1, 12: 0.3}
5	hidden	1	relu	{10: -0.4, 11: 0.5, 12: 0.6}
6	hidden	1	relu	{10: 0.7, 11: 0.4, 12: -0.9}
7	hidden	1	relu	{10: 0.2, 11: 0.3, 12: 0.4}
8	hidden	1	relu	{10: -0.1, 11: 0.2, 12: 0.1}
9	bias	2	relu	{14: 0.1, 15: 0.2}
10	hidden	2	relu	{14: -0.3, 15: 0.4}
11	hidden	2	relu	{14: 0.6, 15: 0.1}
12	hidden	2	relu	{14: 0.1, 15: -0.4}
13	bias	3	relu	{16: 0.1}
14	hidden	3	relu	{16: -0.2}
15	hidden	3	relu	{16: 0.3}
16	output	4	sigmoid	{}

Expected Results: [[0.48467479999999996]]

Max SSE: 1e-06

### Feed-forward Neural Network Model Representation



Raw final results: [[0.4846748017763878]]

Expected results: [[0.4846747999999996]]

Max SSE: 1e-06 , SSE: 3.15555366793979e-18

The model is valid as the error is less than or the same as the maximum SSE

## Test case multilayer softmax

```
In [ ]: # For Multilayer model (multilayer.json)
src_name = " testcase/ffnn/multilayer_softmax.json"
inferenceData(src_name, False)
```

Node counts for all layers in the model: [4, 4, 4, 4, 2]

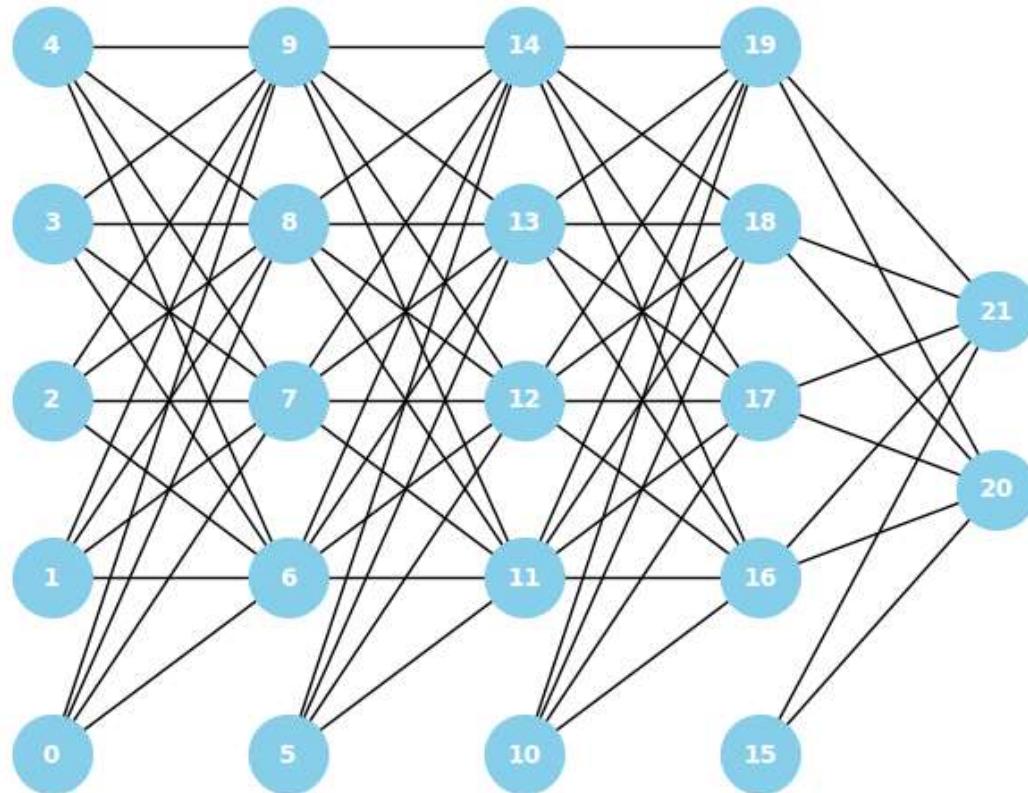
Model Summary:

Node Number	Node Type	Layer Depth	Activation Function	Weight
0	bias	0		{6: -0.9, 7: 1.2, 8: -0.6, 9: 0.3}
1	input	0		{6: 0.8, 7: -0.7, 8: 1.1, 9: -1.2}
2	input	0		{6: 0.3, 7: -1.4, 8: 0.7, 9: 1.2}
3	input	0		{6: 1.1, 7: -1.3, 8: 0.9, 9: 0.4}
4	input	0		{6: 0.5, 7: -0.8, 8: 1.4, 9: -0.9}
5	bias	1	relu	{11: 0.7, 12: -1.1, 13: 0.2, 14: -1.4}
6	hidden	1	relu	{11: 1.3, 12: -0.6, 13: 0.5, 14: -1.3}
7	hidden	1	relu	{11: -1.2, 12: 0.9, 13: 1.4, 14: -0.7}
8	hidden	1	relu	{11: 0.6, 12: -0.5, 13: 1.2, 14: -1.1}
9	hidden	1	relu	{11: 1.0, 12: -0.4, 13: 0.8, 14: -1.0}
10	bias	2	relu	{16: -1.3, 17: 0.7, 18: -0.8, 19: 1.3}
11	hidden	2	relu	{16: 0.2, 17: -1.0, 18: 1.1, 19: -0.6}
12	hidden	2	relu	{16: 1.4, 17: -0.9, 18: 0.3, 19: -1.4}
13	hidden	2	relu	{16: -0.7, 17: 1.2, 18: -1.1, 19: 0.5}
14	hidden	2	relu	{16: 0.9, 17: -0.7, 18: 1.3, 19: -0.8}
15	bias	3	relu	{20: 0.4, 21: -1.1}
16	hidden	3	relu	{20: -1.4, 21: 0.3}
17	hidden	3	relu	{20: 0.8, 21: 1.2}
18	hidden	3	relu	{20: 0.1, 21: -1.2}
19	hidden	3	relu	{20: 1.2, 21: 1.4}
20	output	4	softmax	{}
21	output	4	softmax	{}

Expected Results: [[0.7042294, 0.2957706]]

Max SSE: 1e-06

## Feed-forward Neural Network Model Representation



Raw final results: [[0.7042293996883686, 0.2957706003116313]]

Expected results: [[0.7042294, 0.2957706]]

Max SSE: 1e-06 , SSE: 1.942282085801731e-19

The model is valid as the error is less than or the same as the maximum SSE

Test case export and load from and to JSON file (multilayer model)

```
In [ ]: multilayer_model = inferenceData("testcase/ffnn/multilayer.json", True)
multilayer_model.exportToJson("exports/multilayer_model.json")
```

Node counts for all layers in the model: [3, 4, 3, 2, 1]

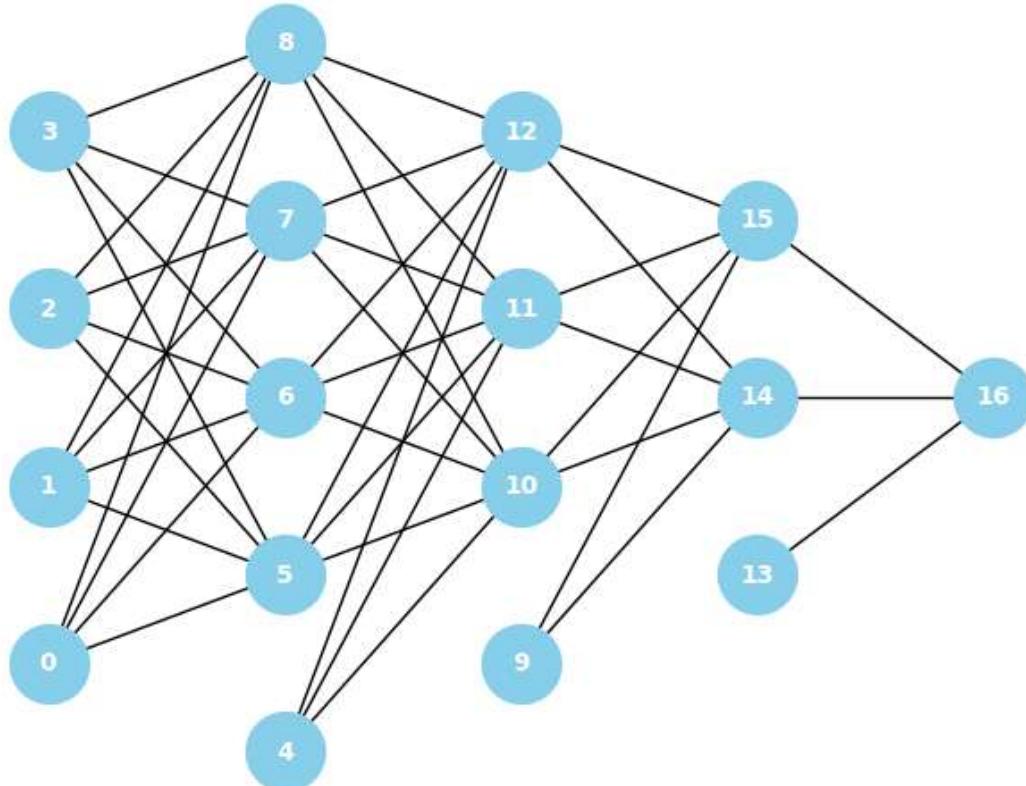
Model Summary:

Node Number	Node Type	Layer Depth	Activation Function	Weight
0	bias	0		{5: 0.1, 6: 0.2, 7: 0.3, 8: -1.2}
1	input	0		{5: -0.5, 6: 0.6, 7: 0.7, 8: 0.5}
2	input	0		{5: 0.9, 6: 1.0, 7: -1.1, 8: -1.0}
3	input	0		{5: 1.3, 6: 1.4, 7: 1.5, 8: 0.1}
4	bias	1	relu	{10: 0.1, 11: 0.1, 12: 0.3}
5	hidden	1	relu	{10: -0.4, 11: 0.5, 12: 0.6}
6	hidden	1	relu	{10: 0.7, 11: 0.4, 12: -0.9}
7	hidden	1	relu	{10: 0.2, 11: 0.3, 12: 0.4}
8	hidden	1	relu	{10: -0.1, 11: 0.2, 12: 0.1}
9	bias	2	relu	{14: 0.1, 15: 0.2}
10	hidden	2	relu	{14: -0.3, 15: 0.4}
11	hidden	2	relu	{14: 0.6, 15: 0.1}
12	hidden	2	relu	{14: 0.1, 15: -0.4}
13	bias	3	relu	{16: 0.1}
14	hidden	3	relu	{16: -0.2}
15	hidden	3	relu	{16: 0.3}
16	output	4	sigmoid	{}

Expected Results: [[0.48467479999999996]]

Max SSE: 1e-06

### Feed-forward Neural Network Model Representation



Raw final results: [[0.4846748017763878]]

Expected results: [[0.4846747999999996]]

Max SSE: 1e-06 , SSE: 3.15555366793979e-18

The model is valid as the error is less than or the same as the maximum SSE

```
In [ ]: # Load a model from JSON
new_multilayer_model = Model(0, 0, [], [], 0)
new_multilayer_model = new_multilayer_model.loadJSON("exports/multilayer_model.json")
new_multilayer_model.printModelSummary()
new_multilayer_model.printModelVisualization()
```

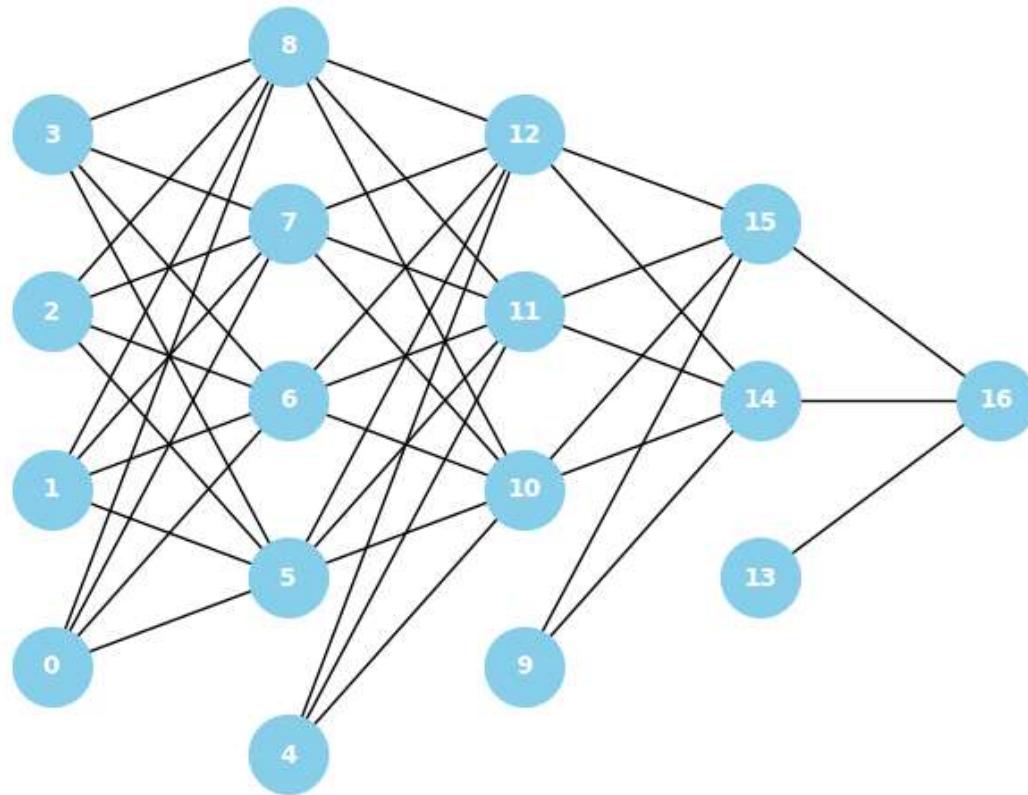
Model Summary:

Node Number	Node Type	Layer Depth	Activation Function	Weight
0	bias	0		{'5': 0.1, '6': 0.2, '7': 0.}
3, '8': -1.2}				
1	input	0		{'5': -0.5, '6': 0.6, '7': 0.}
7, '8': 0.5}				
2	input	0		{'5': 0.9, '6': 1.0, '7': -1.}
1, '8': -1.0}				
3	input	0		{'5': 1.3, '6': 1.4, '7': 1.}
5, '8': 0.1}				
4	bias	1	relu	{'10': 0.1, '11': 0.1, '12': 0.3}
0.3}				
5	hidden	1	relu	{'10': -0.4, '11': 0.5, '12': 0.6}
0.6}				
6	hidden	1	relu	{'10': 0.7, '11': 0.4, '12': -0.9}
-0.9}				
7	hidden	1	relu	{'10': 0.2, '11': 0.3, '12': 0.4}
0.4}				
8	hidden	1	relu	{'10': -0.1, '11': 0.2, '12': 0.1}
0.1}				
9	bias	2	relu	{'14': 0.1, '15': 0.2}
10	hidden	2	relu	{'14': -0.3, '15': 0.4}
11	hidden	2	relu	{'14': 0.6, '15': 0.1}
12	hidden	2	relu	{'14': 0.1, '15': -0.4}
13	bias	3	relu	{'16': 0.1}
14	hidden	3	relu	{'16': -0.2}
15	hidden	3	relu	{'16': 0.3}
16	output	4	sigmoid	{}

Expected Results: [[0.48467479999999996]]

Max SSE: 1e-06

## Feed-forward Neural Network Model Representation



Bagian B

```
In [ ]: from matplotlib import pyplot as plt
import numpy as np
import os

import json
import os
```

```
In [ ]: def parse_json_file(file_path: str):
    with open(file_path, 'r') as json_file:
        data = json.load(json_file)

    case = data['case']
    expect = data['expect']

    return case, expect

def parse_case(data: dict):
    model = data['model']
    input_data = data['input']
    initial_weights = data['initial_weights']
    target = data['target']
    learning_parameters = data['learning_parameters']

    return model, input_data, initial_weights, target, learning_parameters

def parse_model(data: dict):
    input_size = data['input_size']
    layers = data['layers']
```

```

    return input_size, layers

def parse_layers(data: dict):
    number_of_neurons = data['number_of_neurons']
    activation_function = data['activation_function']

    return number_of_neurons, activation_function

def parse_learning_parameters(data: dict):
    learning_rate = data['learning_rate']
    batch_size = data['batch_size']
    max_iteration = data['max_iteration']
    error_threshold = data['error_threshold']

    return learning_rate, batch_size, max_iteration, error_threshold

def parse_expect(data: dict):
    stopped_by = data['stopped_by']
    final_weights = data['final_weights']

    return stopped_by, final_weights

def save_json_file(file_path: str, data: dict):
    with open(file_path, 'w') as json_file:
        json.dump(data, json_file)

```

In [ ]:

```

class ActivationFunctions:
    @staticmethod
    def linear(x, derivative=False):
        if derivative:
            return 1
        return x

    @staticmethod
    def relu(x, derivative=False):
        if derivative:
            return np.where(x <= 0, 0, 1)
        return np.maximum(0, x)

    @staticmethod
    def sigmoid(x, derivative=False):
        if derivative:
            return x * (1 - x)
        return 1 / (1 + np.exp(-x))

    @staticmethod
    def softmax(x, derivative=False):
        if derivative:
            return x * (1 - x)
        return np.exp(x) / np.sum(np.exp(x), axis=0, keepdims=True)

```

In [ ]:

```

class NN:
    def __init__(self, model_config, initial_weights):
        self.input_size, self.layers = parse_model(model_config)
        self.weights = np.array(initial_weights)
        self.bias = 1
        self.learning_rate = None
        self.batch_size = None
        self.max_iteration = None

```

```

        self.error_threshold = None

    def forward_propagation(self, x):
        input_data = np.array(x)

        for layer, weight in zip(self.layers, self.weights):
            input_data = np.append(self.bias, input_data)
            activation_function = getattr(ActivationFunctions, layer['activation'])
            output = activation_function(np.dot(input_data, weight))

        input_data = output

    return output

    def train(self, input_data, target, learning_rate, batch_size, max_iteration):
        self.learning_rate = learning_rate
        self.batch_size = batch_size
        self.max_iteration = max_iteration
        self.error_threshold = error_threshold

        for epoch in range(max_iteration):
            total_error = 0.0

            for i in range(0, len(input_data), batch_size):
                batch_input = input_data[i:i+batch_size]
                batch_target = target[i:i+batch_size]

                batch_error = 0.0

                deltas = [None] * len(self.layers)

                for x, t in zip(batch_input, batch_target):
                    delta = 0
                    output = self.forward_propagation(x)

                    # Compute error
                    error = t - output
                    batch_error += np.sum(error ** 2 / 2)

                    # Backpropagation
                    delta = -error

                    for idx, layer in enumerate(self.layers[::-1]):
                        activation = getattr(ActivationFunctions, layer['activation'])
                        error = -1 * np.log(output) if activation == "softmax" else output - target
                        delta_output = delta * activation(output, derivative=True)
                        dw = np.append(self.bias, x)
                        delta_output = learning_rate * np.outer(delta_output, dw)

                        if idx > 0 and deltas[-idx] is not None:
                            delta_output = np.dot(self.weights[-idx][1:], delta_output)

                        if deltas[-idx-1] is None:
                            deltas[-idx-1] = delta_output
                        else:
                            deltas[-idx-1] += delta_output

                total_error += batch_error

```

```

# Update weights
for idx, delta in enumerate(deltas):
    self.weights[idx] -= delta.T

avg_error = total_error / len(input_data)

print(f"Epoch {epoch + 1}/{max_iteration}, Average Error: {avg_error}")

if avg_error < error_threshold:
    print("Training stopped: Error threshold reached.")
    break

print("Training complete.")

```

```

In [ ]: file_path = os.path.join('testcase', 'linear.json')

case, expect = parse_json_file(file_path)
model, input_data, initial_weights, target, learning_parameters = parse_case(case)
stopped_by, final_weights = parse_expect(expect)

nn = NN(model, initial_weights)
learning_rate, batch_size, max_iteration, error_threshold = parse_learning_params(learning_parameters)
nn.train(input_data, target, learning_rate, batch_size, max_iteration, error_threshold)

print(nn.weights)

```

Epoch 1/1, Average Error: 0.3325  
 Training complete.  
 $\begin{bmatrix} \begin{bmatrix} 0.22 & 0.36 & 0.11 \\ 0.64 & 0.3 & -0.89 \\ 0.28 & -0.7 & 0.37 \end{bmatrix} \end{bmatrix}$

```

In [ ]: file_path = os.path.join('testcase', 'linear_small_lr.json')

case, expect = parse_json_file(file_path)
model, input_data, initial_weights, target, learning_parameters = parse_case(case)
stopped_by, final_weights = parse_expect(expect)

nn = NN(model, initial_weights)
learning_rate, batch_size, max_iteration, error_threshold = parse_learning_params(learning_parameters)
nn.train(input_data, target, learning_rate, batch_size, max_iteration, error_threshold)

print(nn.weights)

```

Epoch 1/1, Average Error: 0.3325  
 Training complete.  
 $\begin{bmatrix} \begin{bmatrix} 0.1012 & 0.3006 & 0.1991 \\ 0.4024 & 0.201 & -0.7019 \\ 0.1018 & -0.799 & 0.4987 \end{bmatrix} \end{bmatrix}$

```

In [ ]: file_path = os.path.join('testcase', 'linear_two_iteration.json')

case, expect = parse_json_file(file_path)
model, input_data, initial_weights, target, learning_parameters = parse_case(case)
stopped_by, final_weights = parse_expect(expect)

```

```

nn = NN(model, initial_weights)
learning_rate, batch_size, max_iteration, error_threshold = parse_learning_params
nn.train(input_data, target, learning_rate, batch_size, max_iteration, error_threshold)

print(nn.weights)

```

Epoch 1/2, Average Error: 0.3325  
 Epoch 2/2, Average Error: 0.09092499999999996  
 Training complete.  
 [[[ 0.166 0.338 0.153]  
 [ 0.502 0.226 -0.789]  
 [ 0.214 -0.718 0.427]]]

```

In [ ]: file_path = os.path.join('testcase', 'relu_b.json')

case, expect = parse_json_file(file_path)
model, input_data, initial_weights, target, learning_parameters = parse_case(case)
stopped_by, final_weights = parse_expect(expect)

nn = NN(model, initial_weights)
learning_rate, batch_size, max_iteration, error_threshold = parse_learning_params
nn.train(input_data, target, learning_rate, batch_size, max_iteration, error_threshold)

print(nn.weights)

```

Epoch 1/1, Average Error: 1.396774999999999  
 Training complete.  
 [[[ -0.211 0.105 0.885 ]
 [ 0.3033 0.5285 0.3005]
 [ -0.489 -0.905 0.291 ]]]

```

In [ ]: file_path = os.path.join('testcase', 'sigmoid.json')

case, expect = parse_json_file(file_path)
model, input_data, initial_weights, target, learning_parameters = parse_case(case)
stopped_by, final_weights = parse_expect(expect)

nn = NN(model, initial_weights)
learning_rate, batch_size, max_iteration, error_threshold = parse_learning_params
nn.train(input_data, target, learning_rate, batch_size, max_iteration, error_threshold)

print(nn.weights)

```

Epoch 1/10, Average Error: 0.23640507030096655  
 Epoch 2/10, Average Error: 0.23539036744879444  
 Epoch 3/10, Average Error: 0.23438378905993162  
 Epoch 4/10, Average Error: 0.2333853294417322  
 Epoch 5/10, Average Error: 0.2323949777800034  
 Epoch 6/10, Average Error: 0.2314127183172226  
 Epoch 7/10, Average Error: 0.23043853053433763  
 Epoch 8/10, Average Error: 0.22947238933549008  
 Epoch 9/10, Average Error: 0.22851426523501334  
 Epoch 10/10, Average Error: 0.2275641245460821  
 Training complete.  
 [[[0.23291176 0.06015346]
 [0.12884088 0.64849474]
 [0.837615 0.23158199]]]

```
In [ ]: file_path = os.path.join('testcase', 'mlp.json')

case, expect = parse_json_file(file_path)
model, input_data, initial_weights, target, learning_parameters = parse_case(case)
stopped_by, final_weights = parse_expect(expect)

nn = NN(model, initial_weights)
learning_rate, batch_size, max_iteration, error_threshold = parse_learning_params(learning_parameters)
nn.train(input_data, target, learning_rate, batch_size, max_iteration, error_threshold)

print(nn.weights)
```

Epoch 1/1, Average Error: 0.338476

Training complete.

```
[[[ 0.22144  0.1956  ]
 [-0.34752  0.58888 ]
 [ 0.350368 0.41464 ]]
```

```
[[ 0.2748   0.188   ]
 [ 0.3252   -0.4824  ]
 [ 0.71496  0.712   ]]]
```

```
In [ ]: file_path = os.path.join('testcase', 'softmax.json')

case, expect = parse_json_file(file_path)
model, input_data, initial_weights, target, learning_parameters = parse_case(case)
stopped_by, final_weights = parse_expect(expect)

nn = NN(model, initial_weights)
learning_rate, batch_size, max_iteration, error_threshold = parse_learning_params(learning_parameters)
nn.train(input_data, target, learning_rate, batch_size, max_iteration, error_threshold)

print(nn.weights)
```

Epoch 1/10, Average Error: 0.6626829218214885

Epoch 2/10, Average Error: 0.6497532419843801

Epoch 3/10, Average Error: 0.6363579868724346

Epoch 4/10, Average Error: 0.622602255574003

Epoch 5/10, Average Error: 0.6086185574566528

Epoch 6/10, Average Error: 0.5945610927498114

Epoch 7/10, Average Error: 0.5805961840120056

Epoch 8/10, Average Error: 0.5668899957351127

Epoch 9/10, Average Error: 0.5535956018123217

Epoch 10/10, Average Error: 0.5408418171596573

Training complete.

```
[[[ 0.0755546  0.9088089 -0.08597513]
 [-0.18370219  0.75633116  0.2249669 ]
 [ 0.31604839 -0.75296816  0.33318705]
 [ 0.40542907  0.58987544 -0.39566149]
 [ 0.46957724  0.49230158  0.5346057 ]
 [-0.6407751   0.43246096  0.60751439]
 [-0.70024868 -0.32084212  0.71881792]
 [ 0.74063868  0.22981958 -0.77298742]
 [ 0.85639344 -0.06579594  0.00836027]]]
```