

This document was exported from Numbers. Each table was converted to an Excel worksheet. All other objects on each Numbers sheet were placed on separate worksheets. Please be aware that formula calculations may differ in Excel.

Numbers Sheet Name	Numbers Table Name	Excel Worksheet Name
Trim Validation		
	Table 1	Trim Validation
Linearization Validation		
	Table 1	Linearization Validation
Trim result		
	Table 1	Trim result
Trim error		
	Table 1	Trim error
Linearization Result		
	Table 1	Linearization Result

			Speed sweep, no disturbances								Inclination angle sweep @ 112 km/h				Wind sweep @ 112 km/h			Friction sweep @ 112 km/h									
	Trim speed	(km/h)	25	50	75	100	125	150	175	200	112	112	112	112	112	112	112	112	112	112							
Disturbances	Inclination angle	(deg)	0	0	0	0	0	0	0	0	-3	0	3	6	0	0	0	0	0	0							
	Wind velocity	(m/s)	0	0	0	0	0	0	0	0	0	0	0	0	-10	0	10	0	0	0							
	change in rolling friction	(-)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.05	0	0.05							
Controls	Throttle Setting	(-)	0.0553993	0.0969893	0.1654978	0.2581629	0.3832678	0.5492906	0.7649533	1.0392747	0.0578412	0.3136479	0.5759624	0.8443461	0.4043346	0.3136479	0.2485900	0.0697943	0.3136479	0.5611125							
	Brake Setting	(-)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0							
States	Distance	(m)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0							
	Speed	(m/s)	6.9444444	13.888888	20.833333	27.777777	34.722222	41.666666	48.611111	55.555555	31.111111	31.111111	31.111111	31.111111	31.111111	31.111111	31.111111	31.111111	31.111111	31.111111							
	Front wheel angular speed	(rad/s)	23.824081	47.648163	71.472245	95.296327	119.12040	142.94449	166.76857	190.59265	106.73188	106.73188	106.73188	106.73188	106.73188	106.73188	106.73188	107.41653	106.73188	106.04287							
	Rear wheel angular speed	(rad/s)	24.098828	48.244989	72.485229	96.865277	121.42969	146.22210	171.28593	196.66567	107.09646	108.63048	110.13536	111.67787	109.14649	108.63048	108.25307	107.84095	108.63048	109.43439							
	Total motor torque	(Nm)	249.29707	271.39740	308.23129	359.79873	426.09973	507.13428	602.90239	713.40406	72.911577	389.78446	705.99424	1020.6742	500.10932	389.78446	310.01110	87.371598	389.78446	692.19733							
Outputs	Distance	(km)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0							
	Speed	(km/h)	25	50	75	100	125	150	175	200	112	112	112	112	112	112	112	112	112	112							
	Front wheel RPM	(RPM)	227.50322	455.00644	682.50967	910.01289	1137.5161	1365.0193	1592.5225	1820.0257	1019.2144	1019.2144	1019.2144	1019.2144	1019.2144	1019.2144	1019.2144	1025.7523	1019.2144	1012.6349							
	Rear wheel RPM	(RPM)	230.12686	460.70571	692.18295	924.99526	1159.5681	1396.3182	1635.6602	1878.0188	1022.6959	1037.3447	1051.7152	1066.4451	1042.2722	1037.3447	1033.7407	1029.8052	1037.3447	1045.0215							
	Front wheel % slip	(%)	-0.510634	-0.510634	-0.510634	-0.510634	-0.510634	-0.510634	-0.510634	-0.510634	-0.510634	-0.510634	-0.510634	-0.510634	-0.510634	-0.510634	-0.510634	0.1275577	-0.510634	-1.1528876							
	Rear wheel % slip	(%)	0.6367080	0.7355377	0.8994397	1.1273501	1.4180795	1.7705852	2.1842953	2.6594825	-0.170790	1.2591315	2.6618915	4.0997380	1.7401291	1.2591315	0.9073349	0.5231789	1.2591315	2.0084915							
	Torque utilization, T/Tmax, %	(%)	5.5399349	6.0310534	6.8495843	7.9955274	9.4688830	11.269650	13.397831	15.853423	1.6202572	8.6618770	15.688761	22.681648	11.113540	8.6618770	6.8891357	1.9415910	8.6618770	15.382163							
	Power utilization, P/Pmax, %	(%)	4.4501981	9.6989370	16.549789	25.816299	38.326785	54.929069	76.495334	103.92747	5.7841278	31.364797	57.596246	84.434615	40.433468	31.364797	24.859005	6.9794347	31.364797	56.111258							
State Derivatives	d/dt (Distance)	(m/s)	6.9444444	13.888888	20.833333	27.777777	34.722222	41.666666	48.611111	55.555555	31.111111	31.111111	31.111111	31.111111	31.111111	31.111111	31.111111	31.111111	31.111111	31.111111							
	d/dt (Speed)	(m/s/s)	-2.44E-14	-4.66E-15	-4.24E-15	5.67E-15	4.55E-15	-4.44E-15	-1.60E-15	1.07E-15	-6.95E-15	3.56E-15	-3.96E-15	-2.10E-14	-3.10E-15	3.56E-15	-3.25E-15	2.83E-15	3.56E-15	-4.49E-15							
	d/dt (Front wheel angular speed)	(rad/s/s)	4.75E-12	2.13E-13	-1.03E-13	-7.03E-13	-3.32E-13	-1.03E-13	6.32E-14	1.97E-13	6.87E-13	-1.26E-13	6.63E-13	2.16E-12	6.71E-13	-1.26E-13	6.87E-13	-5.05E-13	-1.26E-13	5.53E-13							
	d/dt (Rear wheel angular speed)	(rad/s/s)	-5.88E-13	5.84E-13	8.29E-13	-2.64E-13	-4.26E-13	8.68E-13	2.17E-13	-3.87E-13	4.86E-13	-4.86E-13	-1.18E-14	1.44E-12	-1.34E-13	-4.86E-13	-1.34E-13	1.58E-14	-4.86E-13	2.37E-13							
	d/dt (Total motor torque)	(Nm/s)	0.00E+00	2.27E-12	0	0	-4.55E-12	-2.27E-12	4.55E-12	-4.55E-12	5.68E-13	0	0	0	-2.27E-12	0	0	0	0	0							
Constants	Car mass	(kg)	2126	2126	2126	2126	2126	2126	2126	2126	2126	2126	2126	2126	2126	2126	2126	2126	2126	2126							
	Wheel inertia (each)	(kg.m2)	1.8	1.8	1.8	1.8	1.8	1.8	1.8	1.8	1.8	1.8	1.8	1.8	1.8	1.8	1.8	1.8	1.8	1.8							
	CG-to-front-axle	(m)	1.1	1.1	1.1	1.1	1.1	1.1	1.1	1.1	1.1	1.1	1.1	1.1	1.1	1.1	1.1	1.1	1.1	1.1							
	CG-to-rear-axle	(m)	1.3	1.3	1.3	1.3	1.3	1.3	1.3	1.3	1.3	1.3	1.3	1.3	1.3	1.3	1.3	1.3	1.3	1.3							
	CG-to-ground	(m)	0.58	0.58	0.58	0.58	0.58	0.58	0.58	0.58	0.58	0.58	0.58	0.58	0.58	0.58	0.58	0.58	0.58	0.58							
	CG-to-drag-axis	(m)	0.2	0.2	0.2	0.2	0.2	0.2	0.2	0.2	0.2	0.2	0.2	0.2	0.2	0.2	0.2	0.2	0.2	0.2							
	Static Friction (nominal)	(-)	0.8	0.8	0.8	0.8	0.8	0.8	0.8	0.8	0.8	0.8	0.8	0.8	0.8	0.8	0.8	0.8	0.8	0.8							
	Tire constant 1	(-)	7	7	7	7	7	7	7	7	7	7	7	7	7	7	7	7	7	7							
	Tire constant 2	(-)	1.4	1.4	1.4	1.4	1.4	1.4	1.4	1.4	1.4	1.4	1.4	1.4	1.4	1.4	1.4	1.4	1.4	1.4							
	Tire Radius	(m)	0.29	0.29	0.29	0.29	0.29	0.29	0.29	0.29	0.29	0.29	0.29	0.29	0.29	0.29	0.29	0.29	0.29	0.29							
	Rolling friction coefficient	(-)	0.04	0.04	0.04	0.04	0.04	0.04	0.04	0.04	0.04	0.04	0.04	0.04	0.04	0.04	0.04	0.04	0.04	0.04							
	Density	(kg/m3)	1.225	1.225	1.225	1.225	1.225	1.225	1.225	1.225	1.225	1.225	1.225	1.225	1.225	1.225	1.225	1.225	1.225	1.225							
	Drag area	(m2)	0.86	0.86	0.86	0.86	0.86	0.86	0.86	0.86	0.86	0.86	0.86	0.86	0.86	0.86	0.86	0.86	0.86	0.86							
	Acc. due to gravity	(m/s/s)	9.81	9.81	9.81	9.81	9.81	9.81	9.81	9.81	9.81	9.81	9.81	9.81	9.81	9.81	9.81	9.81	9.81	9.81							
	Maximum Power	(W)	135000	135000	135000	135000	135000	135000	135000	135000	135000	135000	135000	135000	135000	135000	135000	135000	135000	135000							
	Maximum Torque	(Nm)	4500	4500	4500	4500	4500	4500	4500	4500	4500	4500	4500	4500	4500	4500	4500	4500	4500	4500							
	Drivetrain time constant	(sec)	0.025	0.025	0.025	0.025	0.025	0.025	0.025	0.025	0.025	0.025	0.025	0.025	0.025	0.025	0.025	0.025	0.025	0.025							

$\bar{x} = \begin{Bmatrix} x \\ V \\ \omega_f \\ \omega_r \\ T \end{Bmatrix}$

State vector

$\bar{u} = \begin{Bmatrix} u_{acc} \\ u_{brk} \end{Bmatrix}$

Control vector

$\bar{v} = \begin{Bmatrix} \theta \\ V_{wind} \\ \Delta\mu_{rr} \end{Bmatrix}$

Disturbance vector

All model constants

Car dynamics model
(which you will set up)

- Create a MATLAB function with this input/output setup

- You will use this function for trimming & linearization

- You will also "embed" this function into your Simulink model

State derivatives

$\dot{\bar{x}} = \begin{Bmatrix} \dot{x} \\ \dot{V} \\ \dot{\omega}_f \\ \dot{\omega}_r \\ \dot{T} \end{Bmatrix}$

Output vector

$\bar{y} = \begin{Bmatrix} x_{km} = x/1000 \\ V_{kmph} = 3.6 V \\ RPM_f = \frac{30}{\pi} \omega_f \\ RPM_r = \frac{30}{\pi} \omega_r \\ \%s_f = 100 s_f \\ \%s_r = 100 s_r \\ \%T = 100 T/T_{max} \\ \%P = 100 P/P_{max} \end{Bmatrix}$

Linearization Result

A	0	342.222222222222	0	0	0	
	0	0.552688811870530	-39.1914100603803	-33.5978647227604	0	
	0	-122.260430556933	6806.38943306892	-111.244147772068	0	
	0	-875.946947926341	-94.4250001170157	5865.25179115281	1191.00809923182	
	0	0	0	816691.268044679	-171505.166289383	
Bu	0	0				
	0	0				
	0	0				
	0	0				
	260384.679581968	0				
Bw	0	0	0			
	-97.9365817305384	0.155883607204269	0			
	0	-0.170327673509263	0			
	0	-0.123941236103065	0			
	0	0	0			
C	0.001000000000000000	0	0	0	0	
	0	1232	0	0	0	
	0	0	11211.3588502583	0	0	
	0	0	0	11410.7920177614	0	
	0	-5211.34773174072	-1094.38302366555	0	0	
	0	-5304.049749309	0	-1113.85044735489	0	
	0	0	0	0	95.2806479385459	
	0	-252.911493206708	-27.263258159838	1693.46966964775	829.04234224885	
Du	0	0				
	0	0				
	0	0				
	0	0				
	0	0				
	0	0				
	0	0				
Dw	0	0	0			
	0	0	0			
	0	0	0			
	0	0	0			
	0	0	0			
	0	0	0			
	0	0	0			
	0	-0.0357854584308370	0			