

# Enunciados + CAPTURA PANTALLA

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## Capítulo 1: Física de partículas y relatividad especial

### 1. A quantum field

- (a) Is a field with quanta that are operators
- (b) Is a field parameterized by the position operator
- © Commutes with the Hamiltonian
- (d) Is an operator that can create or destroy particles

### 2. The particle generations

- (a) Are in some sense duplicates of each other, with each generation having increasing mass
- (b) Occur in pairs of three particles each
- © Have varying electrical charge but the same mass
- (d) Consists of three leptons and three quarks each

### 3. In relativistic situations

- (a) Particle number and type is not fixed
- (b) Particle number is fixed, but particle types are not
- © Particle number can vary, but new particle types cannot appear
- (d) Particle number and types are fixed

### 4. In quantum field theory

- (a) Time is promoted to an operator
- (b) Time and momentum satisfy a commutation relation
- © Position is demoted from being an operator
- (d) Position and momentum continue to satisfy the canonical commutation relation

### 5. Leptons experience

- (a) The strong force, but not the weak force
- (b) The weak force and electromagnetism
- © The weak force only
- (d) The weak force and the strong force

**6. The number of force-carrying particles is**

- (a) Equivalent to the number of generators for the fields gauge group
- (b) Random
- © Proportional to the number of fundamental matter particles involved in the interaction
- (d) Proportional to the number of generators minus one

**7. The gauge group of the strong force is:**

- (a) SU(2)
- (b) U(1)
- © SU(3)
- (d) SU(1)

**8. Antineutrinos**

- (a) Have charge -1 and lepton number 0
- (b) Have lepton number +1 and charge 0
- © Have lepton number -1 and charge 0
- (d) Are identical to neutrinos, since they carry no charge

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**Soluciones 1: Física de partículas y relatividad especial**

- 1. d
- 2. a
- 3. a
- 4. c
- 5. b
- 6. a
- 7. c
- 8. c
- 9. c
- 10. d

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**Capítulo 2: Teoría de campos lagrangiana**

# Quiz

1. Find the equation of motion for a forced harmonic oscillator with Lagrangian

$$L = \frac{1}{2} m \dot{x}^2 - \frac{1}{2} m \omega^2 x^2 + \alpha x$$

Here  $\alpha$  is a constant.



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## Quantum Field Theory Demystified

2. Consider a Lagrangian given by

$$\mathcal{L} = -\frac{1}{2} \partial_\mu \phi \partial^\mu \phi - \frac{1}{2} m^2 \phi^2 - V(\phi)$$

- (a) Write down the field equations for this system.
  - (b) Find the canonical momentum density  $\pi(x)$ .
  - (c) Write down the Hamiltonian.
3. Consider a free scalar field with Lagrangian  $\mathcal{L} = \partial_\mu \phi \partial^\mu \phi$  and suppose that the field varies according to  $\phi \rightarrow \phi + \alpha$ , where  $\alpha$  is a constant. Determine the conserved current.
  4. Refer to the Lagrangian for a complex scalar field Eq. (2.37). Determine

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## Soluciones 2: Teoría de campos lagrangiana

## Chapter 2

1.  $\frac{d^2x}{dt^2} + \omega^2x = -\frac{\alpha}{m}$
2. (a)  $\partial_\mu \partial^\mu \varphi - m^2 \varphi = \frac{\partial V}{\partial \varphi}$   
(b)  $\pi = \dot{\varphi}$   
(c)  $H = \int d^3x \left( \frac{1}{2} \pi^2 + \frac{1}{2} (\nabla \varphi)^2 + \frac{1}{2} m^2 \varphi^2 + V(\varphi) \right)$
3.  $J^\mu = \partial^\mu \varphi$
4. Each field separately satisfies a Klein-Gordon equation, that is,  $\partial_\mu \partial^\mu \varphi + m^2 \varphi = 0$ ,  $\partial_\mu \partial^\mu \varphi^\dagger + m^2 \varphi^\dagger = 0$ . To get this result apply Eq. (2.14) to the Lagrangian Eq. (2.37).
5.  $Q = i \int d^3x \left( \varphi^\dagger \frac{\partial \varphi}{\partial t} - \varphi \frac{\partial \varphi^\dagger}{\partial t} \right)$
6. The action is invariant under that transformation.

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## Capítulo 3: Una Introducción a la teoría de grupos

## Quiz

1. Consider an element of  $SU(2)$  given by  $U = e^{i\sigma_x \alpha/2}$ . By writing down the power series expansion, write  $U$  in terms of trigonometry functions.
2. Consider  $SU(3)$  and calculate  $\text{tr}(\lambda_i \lambda_j)$ .
3. How many casimir operators are there for  $SU(2)$ ?
4. Write down the casimir operators for  $SU(2)$ .

A Lorentz transformation can be described by boost matrices with rapidity defined by  $\tanh \phi = v/c$ . A boost in the  $x$  direction is represented by the matrix

$$\begin{pmatrix} \cosh \phi & \sinh \phi & 0 & 0 \\ \sinh \phi & \cosh \phi & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

5. Find the generator  $K_x$ .



## Chapter 3

1.  $U = \cos \alpha + i\sigma_x \sin \alpha$

2.  $2\delta_{ij}$

3. 1

4. Try  $\vec{\sigma}^2 = \sigma_x^2 + \sigma_y^2 + \sigma_z^2$

5.  $K_x = -i \begin{pmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$

6.  $K_y = -i \begin{pmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$

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### Solutions to Quizzes and Final Exam

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7. No, because the algebra among the generators requires the introduction of the angular momentum operators. Therefore, Lorentz transformations together with rotations form a group.

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## Capítulo 4: Simetrías discretas y números cuánticos

# Quiz

1. Angular momentum states transform under the parity operator as
  - (a)  $P|L, m_z\rangle = -|L, m_z\rangle$
  - (b)  $P|L, m_z\rangle = L|L, m_z\rangle$
  - (c)  $P|L, m_z\rangle = (-1)^L|L, m_z\rangle$
  - (d)  $P|L, m_z\rangle = |L, m_z\rangle$
2. The interaction Lagrangian of electromagnetism is invariant under charge conjugation if
  - (a)  $CA^\mu C^{-1} = -A^\mu$
  - (b) It is not invariant under charge conjugation
  - (c)  $CJ^\mu C^{-1} = J^\mu$
  - (d)  $CA^\mu C^{-1} = A^\mu$
3. Parity is
  - (a) Conserved in weak and electromagnetic interactions, but is violated in the strong interaction
  - (b) Conserved in strong interactions, but is violated in weak and electromagnetic interactions
  - (c) Not conserved
  - (d) Conserved in the strong and electromagnetic interactions, but is violated in the weak interaction

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## Soluciones 4: Simetrías discretas y números cuánticos

- 1. c
- 2. a
- 3. d

- 4. a
- 5. c

## Capitulo 5: La ecuación de Dirac

### Quiz

1. Given the Lagrangian

$$\mathcal{L} = \bar{\psi}(x)[i\gamma^\mu\partial_\mu - m]\psi$$

vary  $\psi(x)$  to find the equation of motion obeyed by  $\bar{\psi}(x)$ .

2. Calculate  $\{\gamma_5, \gamma^\mu\}$ .
3. Consider the solution of the Dirac equation with  $E = \omega_k > 0$ . Find a relationship between the  $u$  and  $v$  components of the Dirac field.
4. Find the normalization of the free space solutions of the Dirac equation using the density  $\bar{\psi}\gamma^0\psi$ .
5. Find  $S^{01}$ , the generator of a boost in the  $x$  direction.
6. We can introduce an electromagnetic field with a vector potential  $A_\mu$ . Let the source charge be  $q$ . Using the substitution  $p_\mu \rightarrow p_\mu - qA_\mu$ , determine the form of the Dirac equation in the presence of an electromagnetic field.

## Soluciones 5: La ecuación de Dirac



## Chapter 5

1.  $i \frac{\partial \bar{\psi}}{\partial x^\mu} \gamma^\mu + m \bar{\psi}$
2. 0
3.  $v = \frac{\vec{k} \cdot \vec{\sigma}}{\omega_k + m} u$
4.  $\psi(0) = \sqrt{2m} \begin{pmatrix} u \\ v \end{pmatrix}$
5.  $-\frac{i}{2} \begin{pmatrix} \sigma_1 & 0 \\ 0 & -\sigma_1 \end{pmatrix}$
6.  $\gamma^\mu (i\partial_\mu - qA_\mu)\psi - m\psi = 0$

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## Capitulo 6: Campos escalares

### Quiz

1. Given the Lagrangian

$$\mathcal{L} = \bar{\psi}(x)[i\gamma^\mu \partial_\mu - m]\psi$$

vary  $\psi(x)$  to find the equation of motion obeyed by  $\bar{\psi}(x)$ .

2. Calculate  $\{\gamma_5, \gamma^\mu\}$ .
3. Consider the solution of the Dirac equation with  $E = \omega_k > 0$ . Find a relationship between the  $u$  and  $v$  components of the Dirac field.
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5. Find  $S^{01}$ , the generator of a boost in the  $x$  direction.
6. We can introduce an electromagnetic field with a vector potential  $A_\mu$ . Let the source charge be  $q$ . Using the substitution  $p_\mu \rightarrow p_\mu - qA_\mu$ , determine the form of the Dirac equation in the presence of an electromagnetic field.

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## Soluciones 6: Campos escalares

## Chapter 6

1. 0
2.  $[n(\vec{k}) + 1] \hat{a}^\dagger(\vec{k}) |n(\vec{k})\rangle$
3. 0
4.  $[H, Q] = 0$

## Capítulo 7: Las reglas de Feynman

### Quiz

1. What is the amplitude for the process shown in Fig. 7.16?

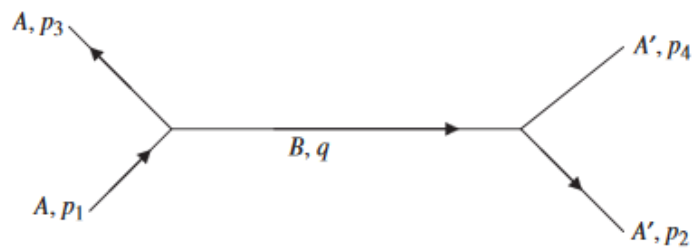


Figure 7.16 Feynman diagram for Question 1.

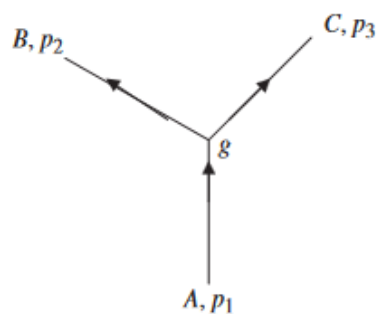


Figure 7.17 Feynman diagram for Question 1.

**Figure 7.17** Feynman diagram for Question 1.

2. Find the lifetime for the decay as shown in Fig. 7.17.
3. An internal line corresponds to a spin-0 boson of mass  $m$ . The propagator is
  - (a)  $i \frac{q + m}{q^2 - m^2}$
  - (b)  $\frac{i}{q^2 - m^2}$
  - (c)  $\frac{i}{q - m}$
  - (d)  $\delta(q^2 - m^2)$
4. In the interaction picture,
  - (a) The time evolution of states is governed by the free Hamiltonian
  - (b) States are stationary, operators evolve according to the interaction part of the Lagrangian
  - (c) States evolve according to the interaction part of the Hamiltonian, fields evolve according to the free part of the Hamiltonian
  - (d) States obey the Heisenberg equation of motion
5. Each vertex in a Feynman diagram requires the addition of
  - (a) One factor of the coupling constant  $-ig$
  - (b) One factor of the coupling constant  $-g$

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## Capítulo 8: Electrodinámica cuántica

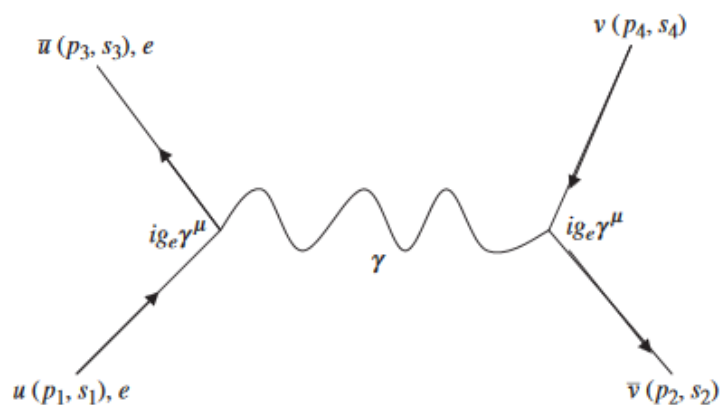
# Quiz

1. Compute  $[D_\mu, D_\nu]$ .
2. The Lagrangian of quantum electrodynamics can be best described as
  - (a) Admitting a local  $U(1)$  symmetry
  - (b) Admitting a global  $U(1)$  symmetry
  - (c) Admitting a local  $SU(2)$  symmetry
  - (d) Admitting a local  $SU(1)$  symmetry
3. Write down the amplitude for electron-positron scattering as shown in Fig. 8.11.



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## Quantum Field Theory Demystified



**Figure 8.11** Electron-muon scattering to lowest order.

4. The minimal coupling prescription for the QED Lagrangian is
  - (a)  $D_\mu \rightarrow \partial_\mu + ieA_\mu$

4. The minimal coupling prescription for the QED Lagrangian is

- (a)  $D_\mu = \partial_\mu + ig_e A_\mu$
- (b)  $D_\mu = \partial_\mu - ig_e A_\mu$
- (c)  $D_\mu = \partial_\mu + iq A_\mu$
- (d)  $D_\mu = \partial_\mu + iq \gamma^\mu A_\mu$

5. In a QED process an incoming antiparticle state is written as

- (a)  $\bar{v}(p, s)$
- (b)  $\bar{u}(p, s)$
- (c)  $u(p, s)$
- (d)  $v(p, s)$

## Soluciones 7 y 8

### Chapter 7

- 1.  $-i \frac{g^2}{(p_2 - p_4)^2 - m_B^2}$
- 2.  $\frac{1}{g^2}$
- 3. b
- 4. c
- 5. a
- 6.  $\alpha = 1/137$

### Chapter 8

- 1.  $iqF_{\mu\nu}$
- 2. a
- 3.  $-g_e^2 [v(k') \gamma^\mu \bar{v}(k)] \frac{g_{\mu\nu}}{(p - p')^2} \bar{u}(p') \gamma^\nu u(p)$
- 4. c
- 5. a