

```
import matplotlib.pyplot as plt
import math
```

Constant

Energy to send a packet

```
EnergyTxRxCircuitry = 50      #nJ/bit
packet = 2000                #bit
k = 1                        #nJ/bit/m2

battery = 5                  #mJ

PacketEnergy = packet*EnergyTxRxCircuitry
print("Energy necessary to send a packet: ", PacketEnergy, "nJ")

Energy necessary to send a packet:  100000 nJ
```

Finding system's lifetime

Sensors positioning

```
sensors = [(1,2), (10,3), (4,8), (16,7), (6,1), (9,12), (14,4), (3,
10), (7,7), (12, 14)]
sink = (20,20)
x_coords = [sensor[0] for sensor in sensors]
y_coords = [sensor[1] for sensor in sensors]
```

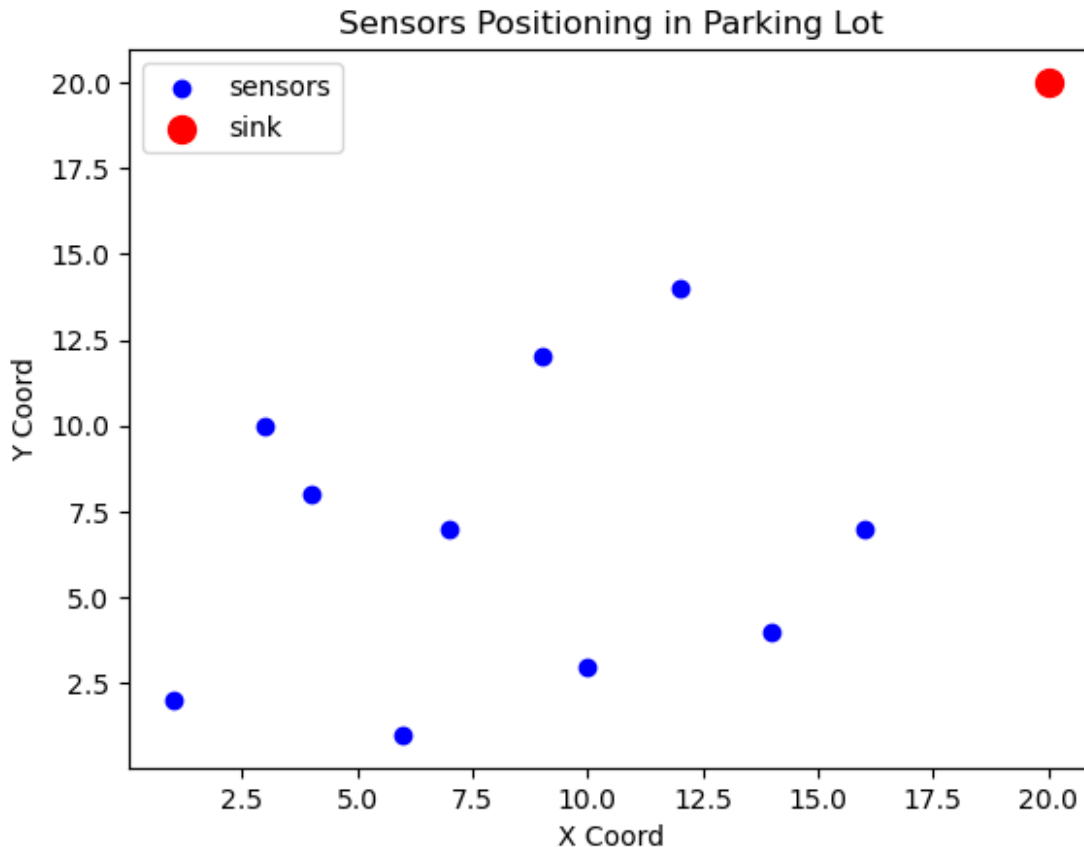
Plot of the sensors

```
plt.scatter(x_coords, y_coords, color='b', label='sensors')
plt.scatter(20, 20, color='r', marker='o', s=100, label='sink')

plt.xlabel('X Coord')
plt.ylabel('Y Coord')
plt.title('Sensors Positioning in Parking Lot')

plt.legend()

plt.show()
```



Computing the distances from each node to the sink

```
distances = [math.sqrt((x - sink[0])**2 + (y - sink[1])**2) for x, y
in sensors]
max = -1
for i, dist in enumerate(distances):
    print(f"Distance from the the node {sensors[i]} to the sink is:
{dist:.2f} meters")
    if(dist > max):
        max = dist
```

```
Distance from the the node (1, 2) to the sink is: 26.17 meters
Distance from the the node (10, 3) to the sink is: 19.72 meters
Distance from the the node (4, 8) to the sink is: 20.00 meters
Distance from the the node (16, 7) to the sink is: 13.60 meters
Distance from the the node (6, 1) to the sink is: 23.60 meters
Distance from the the node (9, 12) to the sink is: 13.60 meters
Distance from the the node (14, 4) to the sink is: 17.09 meters
Distance from the the node (3, 10) to the sink is: 19.72 meters
Distance from the the node (7, 7) to the sink is: 18.38 meters
Distance from the the node (12, 14) to the sink is: 10.00 meters
```

All the nodes will consume the same amount of energy to power the transmission circuitry, so the node which is furthest from the sink will consume more energy to transmit the payload, so it will finish the battery earlier

```
MaxTransmissionEnergy = k*max**2 #nJ/bit
print("Max transmission energy: ", MaxTransmissionEnergy, " nJ/bit")

Max transmission energy: 685.0 nJ/bit
```

Total energy consumption of the furthest node

```
TotEnergy= EnergyTxRxCircuitry + MaxTransmissionEnergy
print("Total consumed energy:", TotEnergy, " nJ")

Total consumed energy: 735.0 nJ
```

Number of **cycles** needed to consume the battery:

```
cycles = battery / (TotEnergy/10e2)
print("Power cycles: ", cycles)
print(f"Lifetime: {cycles * 10:.2f} minutes")

Power cycles: 6.802721088435375
Lifetime: 68.03 minutes
```

Optimal sink position

To determine the optimal position of the sink while minimizing the total distance to all sensors, the sink should be positioned at the average x and y position of the nodes. This can be demonstrated to be true using mathematical analysis: define the cost function as the sum of all transmission costs, derive in x and y parameters and find the value of each parameter where the derivatives are null.

$$S = \sum_{i=1}^{10} E_{tx}(d) = \sum_{i=1}^{10} k \cdot d^2 = \sum_{i=1}^{10} k \cdot \left(\sqrt{(x_i - x)^2 + (y_i - y)^2} \right)^2$$

$$S = \sum_{i=1}^{10} E_{tx}(d) = \sum_{i=1}^{10} k \cdot d^2 = \sum_{i=1}^{10} k \cdot \left((x_i - x)^2 + (y_i - y)^2 \right)$$

Partial Derivative with respect to x

To find the minimum, differentiate S with respect to x :

$$\frac{\partial S}{\partial x} = \sum_{i=1}^{10} k \cdot 2(x - x_i)$$

Setting this derivative equal to zero:

$$\sum_{i=1}^{10} k \cdot 2(x - x_i) = 0$$

$$\sum_{i=1}^{10} (x_s - x_i) = 0$$

$$x_s = \frac{1}{10} \sum_{i=1}^{10} x_i$$

x_s is the **arithmetic mean** of the values x_i .

Similarly can be done with the partial derivative wrt y , so it's possible to affirm that the point that minimizes the transmission cost is simply the **arithmetic mean of the points**:

$$(x_s, y_s) = \left(\frac{1}{10} \sum_{i=1}^{10} x_i, \frac{1}{10} \sum_{i=1}^{10} y_i \right)$$

This means that the optimal transmission position is at the **average** location of all points

```
meanX = sum(x_coords) / len(x_coords)
meanY = sum(y_coords) / len(y_coords)

optimal_sink = (meanX, meanY)
optimal_sink_x = optimal_sink[0]
optimal_sink_y = optimal_sink[1]

print("Optimal coordinates for the sink: ", optimal_sink)

Optimal coordinates for the sink: (8.2, 6.8)

plt.scatter(x_coords, y_coords, color='b', label='Sensors')

plt.scatter(optimal_sink[0], optimal_sink[1], color='r', marker='x',
s=150, label='optimal Sink')

plt.xlabel('X Coordinate')
plt.ylabel('Y Coordinate')
plt.title('Sensors Positioning in Parking Lot with optimal Sink')

plt.legend()
plt.show()
```

