

## EQ1

A LoRaWAN network in Europe (carrier frequency 868 MHz, bandwidth 125 kHz) is composed by one gateway and 50 sensor nodes. The sensor nodes transmit packet with payload size of L byte according to a Poisson process with intensity  $\lambda = 1$  packet / minute. Find the biggest LoRa SF for having a success rate of at least 70%. Hint: use <https://www.thethingsnetwork.org/airtime-calculator> to compute the airtime of a packet.

- Goal of the first exercise is to find the **biggest LoRa SF** for having a **success rate** of at least 70%

### Libraries

```
import math
from google.colab import files
from IPython.display import Image
```

### Variables of the system

```
frequency = 868 #MHz
bandwidth = 125 #kHz

sensorNodes = 50
payload = 3 + 53 #Byte
Lambda = 1 #packet/minute
Lambda_s = Lambda * 60 #packet/s

LambdaSystem = sensorNodes / Lambda_s #packet/s
```

We'll implement ALOHA to handle the communication of our system

In this case the calculus are done with the hypothesis of SF7. The air time of the packet is calculated with the suggested site on the description.

```
Image("/content/SP7.png")
```

Input Bytes ?	Spreading Factor ?	Region ?	Bandwidth ?
56	SF7	EU868	125 kHz

---

Result

128.3 ms

Time on air

```
airtime_PacketS7 = 128.3 / 1000 #s
traffic = airtime_PacketS7 * LambdaSystem

Probability_Packet_retrasm = math.exp(-2 * traffic)

print("In this ways is possible to notice that the probability of
retrasmit a packet with a Spreading Factor 7 is: ",
Probability_Packet_retrasm)

In this ways is possible to notice that the probability of retrasm a
packet with a Spreading Factor 7 is:  0.8074829543006469
```

Now we'll try to implement it with SF8

```
Image("/content/SP8.png")
```

Input Bytes ?	Spreading Factor ?	Region ?	Bandwidth ?
56	SF8	EU868	125 kHz

**Result**

**225.8 ms**

Time on air

```
airtime_PacketS8 = 225.8 / 1000 #s  
traffic = airtime_PacketS8 * LambdaSystem
```

```
Probability_Packet_retransmS8 = math.exp(-2 * traffic)  
print("In this ways is possible to notice that the probability of  
retransmit a packet with a Spreading Factor 8 is: ",  
Probability_Packet_retransmS8)
```

```
In this ways is possible to notice that the probability of retransmit a  
packet with a Spreading Factor 8 is: 0.6863735037382898
```

We can notice that the probability is below the threshold, so the optimal spreading factor is equal to 7.