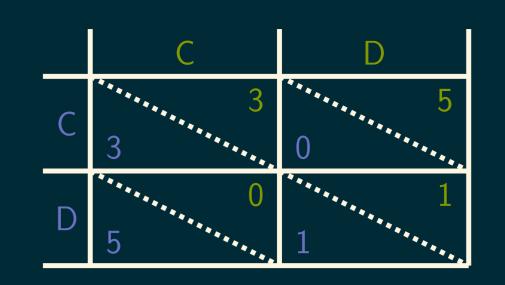
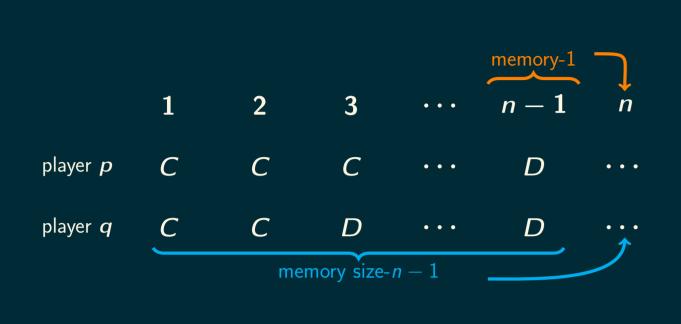
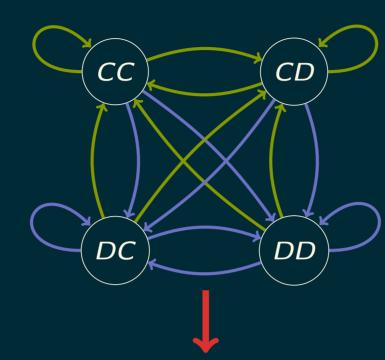
THE POWER OF MEMORY

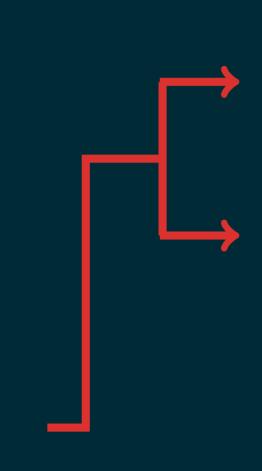
Is memory size advantageous in interactions (social, biological, ...)?







$$\begin{bmatrix} p_1q_1 & p_1\left(-q_1+1\right) & q_1\left(-p_1+1\right) & (-p_1+1)\left(-q_1+1\right) \\ p_2q_3 & p_2\left(-q_3+1\right) & q_3\left(-p_2+1\right) & (-p_2+1)\left(-q_3+1\right) \\ p_3q_2 & p_3\left(-q_2+1\right) & q_2\left(-p_3+1\right) & (-p_3+1)\left(-q_2+1\right) \\ p_4q_4 & p_4\left(-q_4+1\right) & q_4\left(-p_4+1\right) & (-p_4+1)\left(-q_4+1\right) \end{bmatrix}$$



W. H. Press and F. J. Dyson. Iterated Prisoner's Dilemma contains strategies that dominate any evolutionary opponent PNAS 2012.

$$p^*
ightarrow ext{manipulates}
ightarrow q$$

This work considers an optimisation approach to identify:

$$p^*
ightarrow ext{best response}
ightarrow q$$

$$u_q(p) = \frac{\frac{1}{2} pQp^T + c^Tp + a}{\frac{1}{2} p\bar{Q}p^T + \bar{c}^Tp + \bar{a}},$$

where
$$p \in \mathbb{R}^4_{[0,1]}$$

PURELY RANDOM STRATEGIES p = (p, p, p, p)

AGAINST A SINGLE OPPONENT





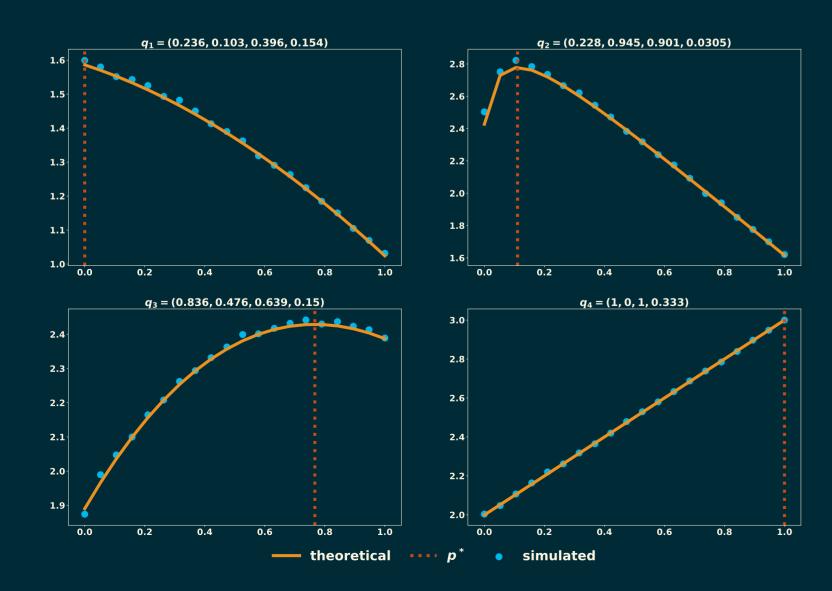
$$p^* = \operatorname{argmax}(u_q(p)), \ p \in S_q,$$

where the set S_q is defined as:

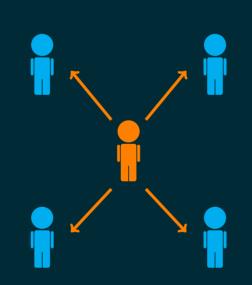




$$\mathcal{S}_q = \left\{ oldsymbol{0}, oldsymbol{p}_\pm, oldsymbol{1} igg| oldsymbol{0} < oldsymbol{p}_\pm < oldsymbol{1}, \ oldsymbol{p}_\pm
eq rac{-d_0}{d_1} \end{array}
ight\}$$



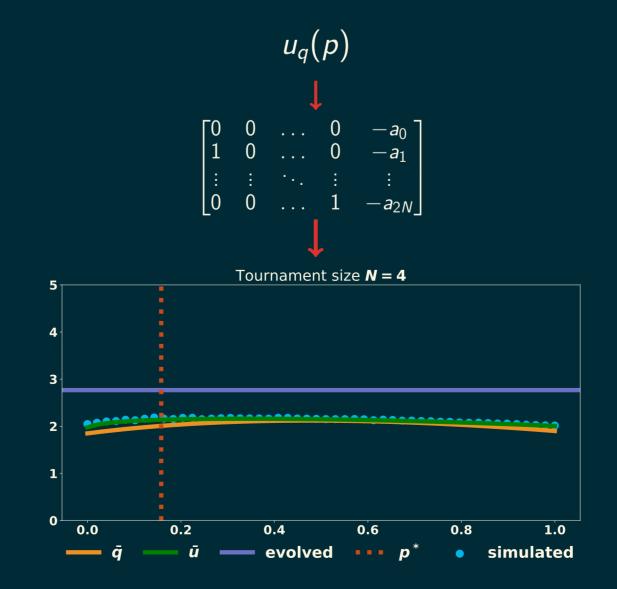
AGAINST MULTIPLE OPPONENTS



$$p^* = \operatorname{argmax}(\sum_{i=1}^N u_q^{(i)}(p)), \ p \in S_{q(i)},$$

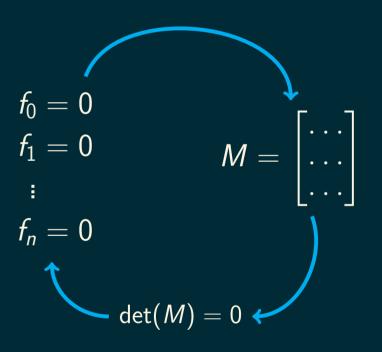
where the set $S_{q(i)}$ is defined as:

$$S_{q(i)} = egin{array}{l} 2N \ u \ i=1 \ \lambda_i
eq rac{do_i}{dt} \end{array}$$



FUTURE WORK

 $p=(p_1,p_2,p_3,p_4)
ightarrow ext{RESULTANT THEORY}$



SUMMARY

- 1. The utility of a given player p against a given opponent q can be written in a compact way.
- 2. Obtaining the optimal random behaviour p^* reduces to a search over a small finite set.
- 3. Optimising against the mean utility can not be captured by optimising against the mean opponent.