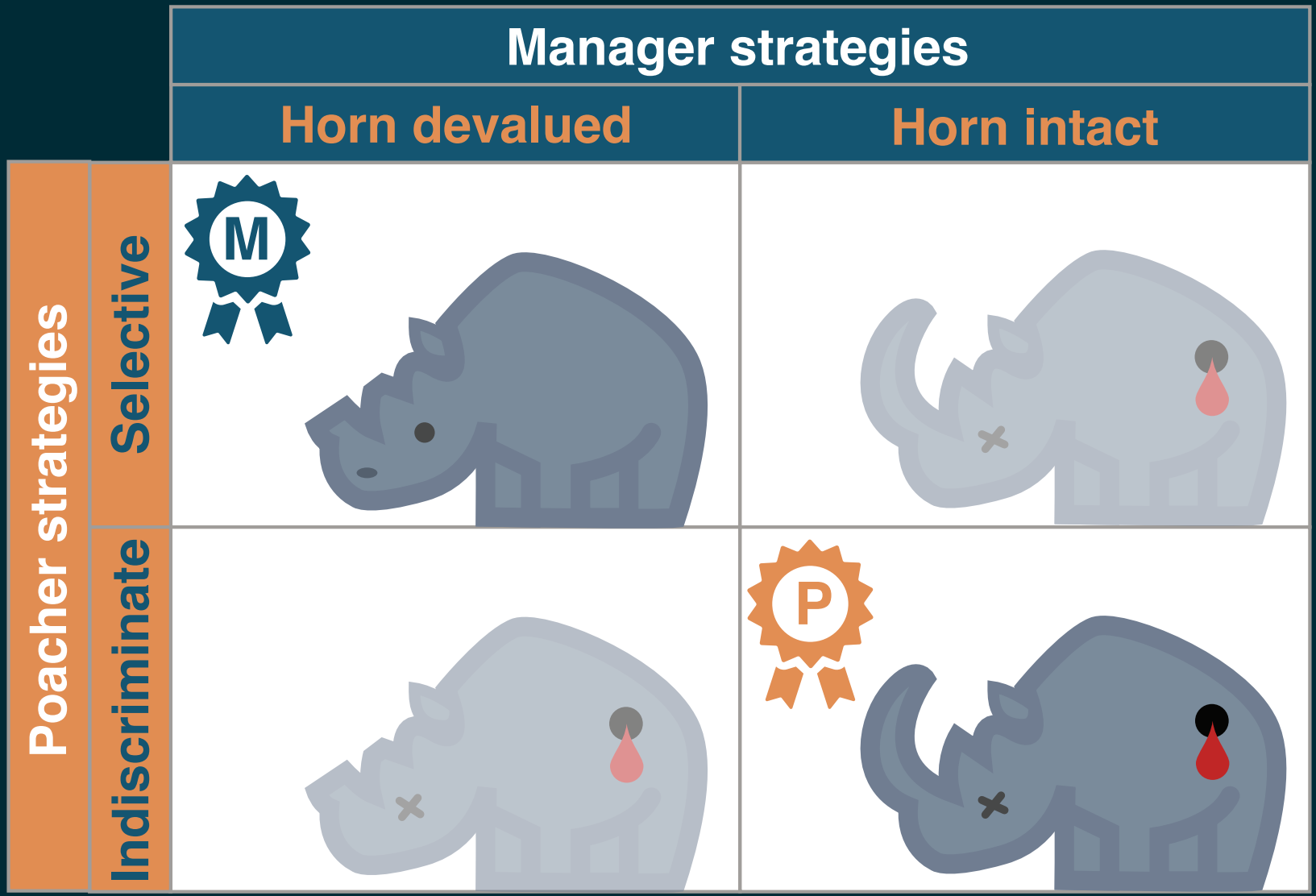
Rhinos with a bit of Python

@NikoletaGlyn

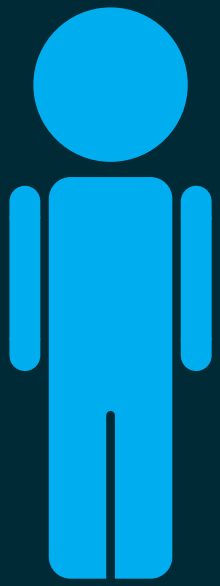
Tamsin E. Lee Vincent Knight

rhino-ceros

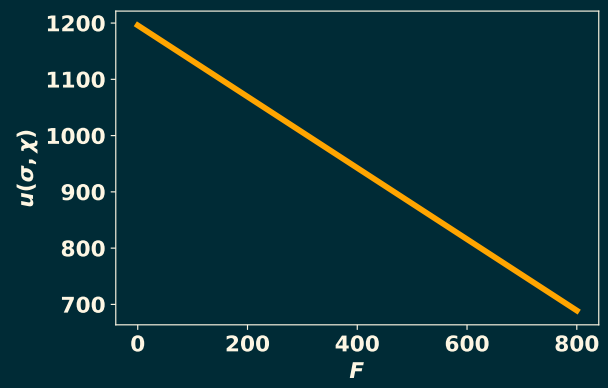


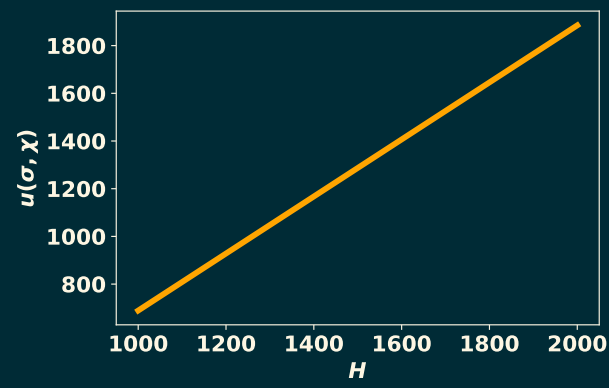
http://www.bbc.com/earth/story/20150518-the-epic-history-of-rhinos?ocid=twert

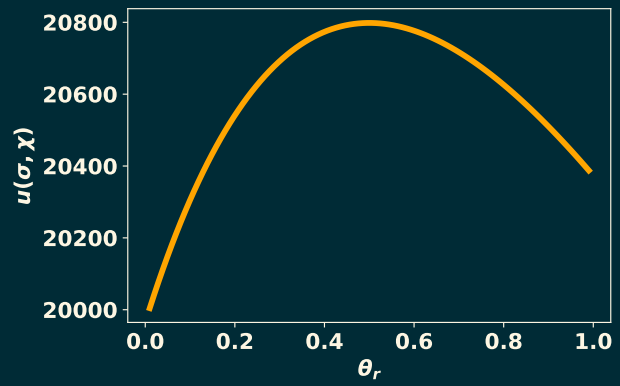
selective

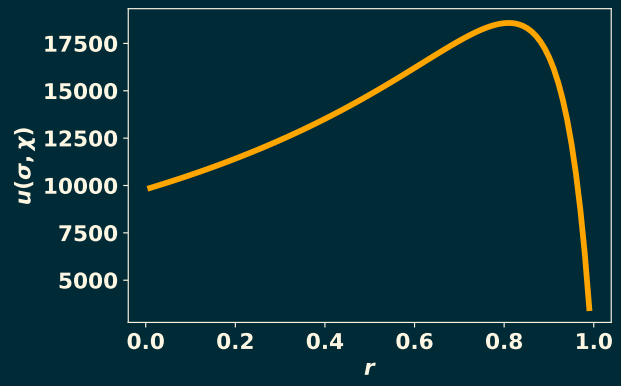


indiscriminate


1200
1100
1000
900
800
700
u(σ, χ)
0
200
400
600
800
F


1800
1600
1400
1200
1000
800
u(σ, χ)
1000
1200
1400
1600
1800
2000
H


20800
20600
20400
20200
20000
u(σ, χ)
0.0
0.2
0.4
0.6
0.8
1.0
θr


17500
15000
12500
10000
7500
5000
u(σ, χ)
0.0
0.2
0.4
0.6
0.8
1.0
r

Theorem (Selective)

A population of selective poachers is unstable.

Proof.

$$u(1,1) > u(0,1),$$

where

$$u(1,1) = H(1-r)^{1-\alpha} F(1-r)^{\beta+\gamma-1}$$

and

$$u(0,1) = H(\theta_r r + 1 - r)(1-r)^{-\alpha} - F(1-r)^{\beta+\gamma}.$$

This gives the condition,

$$H\theta_r < -F(1-r)^{\gamma+\beta+\alpha-1}$$

□

```
>>> import sympy as sym
```

```
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```

```
>>> (2 + 3) ** 2
25
```

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```
>>> a, b = sym.symbols('a, b')
>>> expr = (a + b) ** 2
>>> expr.expand()
a**2 + 2*a*b + b**2
```

```
>>> import imp
>>> tools = imp.load_source('tools', '../tools.py')

>>> tools.utility(1, 1)
-F*(-r + 1)**beta*(-r + 1)**gamma/(-r + 1) + H*(-r + 1)*(-r + 1)**(-alpha)

>>> tools.utility(0, 1)
-F*(-r + 1)**beta*(-r + 1)**gamma + H*(-r + 1)**(-alpha)*(r*(theta_r - 1) + 1)
```

Theorem (Mixed)

A mixed stable strategy ($s = s^\star$) *never exists for* $0 < r < 1$.

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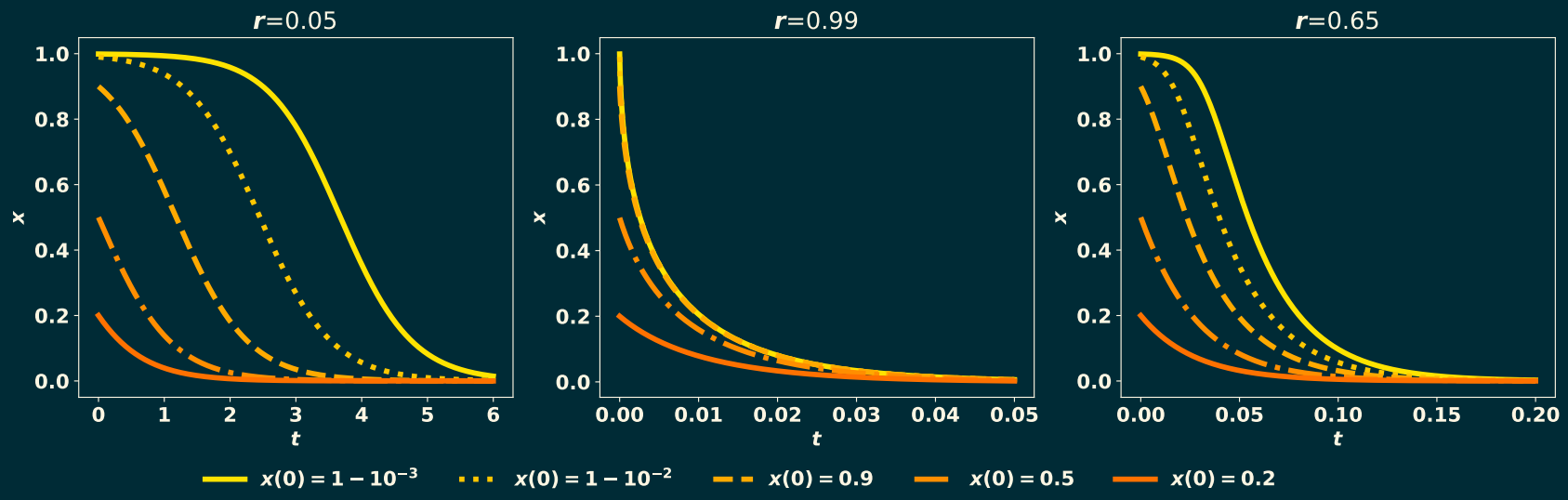
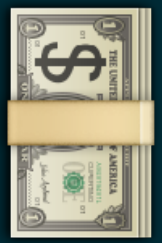
A mixed stable strategy ($s = s^\star$) *never exists for* $0 < r < 1$.

Theorem (Indiscriminate)

A population of indiscriminate poachers is evolutionarily stable.


r=0.05
r=0.99
r=0.65
x
t
1.0
0.8
0.6
0.4
0.2
0.0
0
1
2
3
4
5
6
0.00
0.01
0.02
0.03
0.04
0.05
0.00
0.05
0.10
0.15
0.20
x(0) = 1 − 10^−3
x(0) = 1 − 10^−2
x(0) = 0.9
x(0) = 0.5
x(0) = 0.2



Dear Kate,

Here's to the crazy ones. The [illegible]. The rebels. The troublemakers. The round pegs in the square holes. The ones who see things differently. They're not fond of rules. And they have no respect for the status quo. You can quote them, disagree with them, glorify or vilify them. About the only thing you can't do is ignore them. Because they change things. They push the human race forward. And while some may see them as the crazy ones, we see genius. Because the people who are crazy enough to think they can change the world, are the ones who do.

Take care,
John Appleseed

Theorem (Disincentive)

Using the modified utility model, a population of selective poachers is stable if and only if:

$$\theta_r H - F(1-r)^{\gamma+\beta+\alpha-1} < \frac{\Gamma(1-r)^{\alpha}}{r}$$

Theorem (Disincentive)

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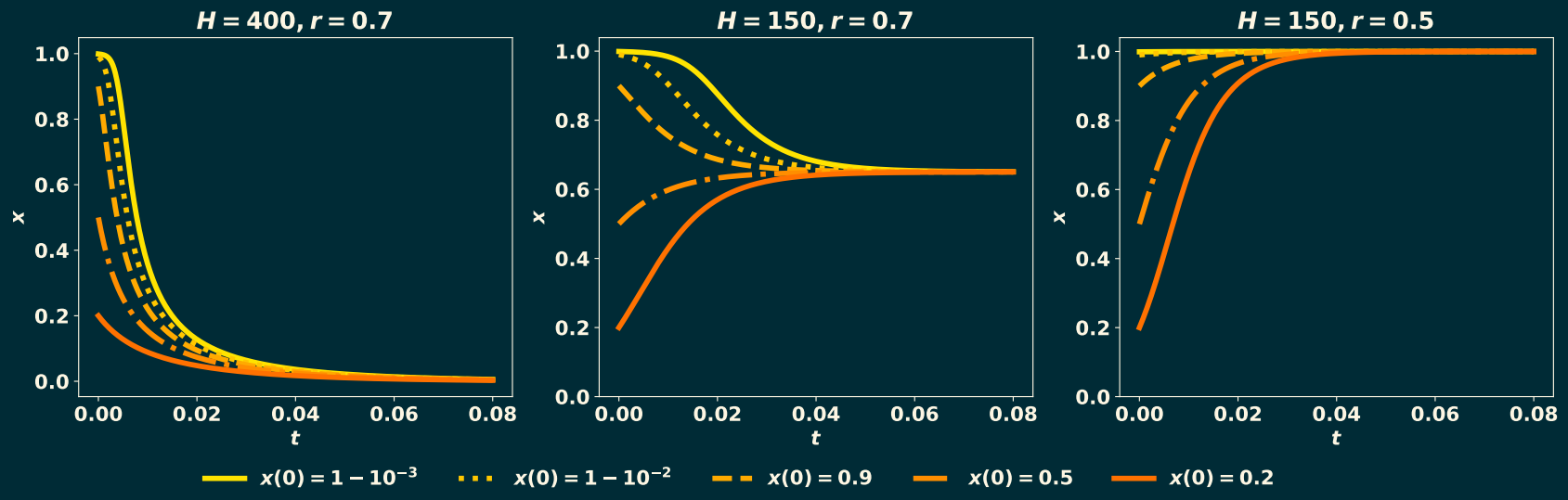
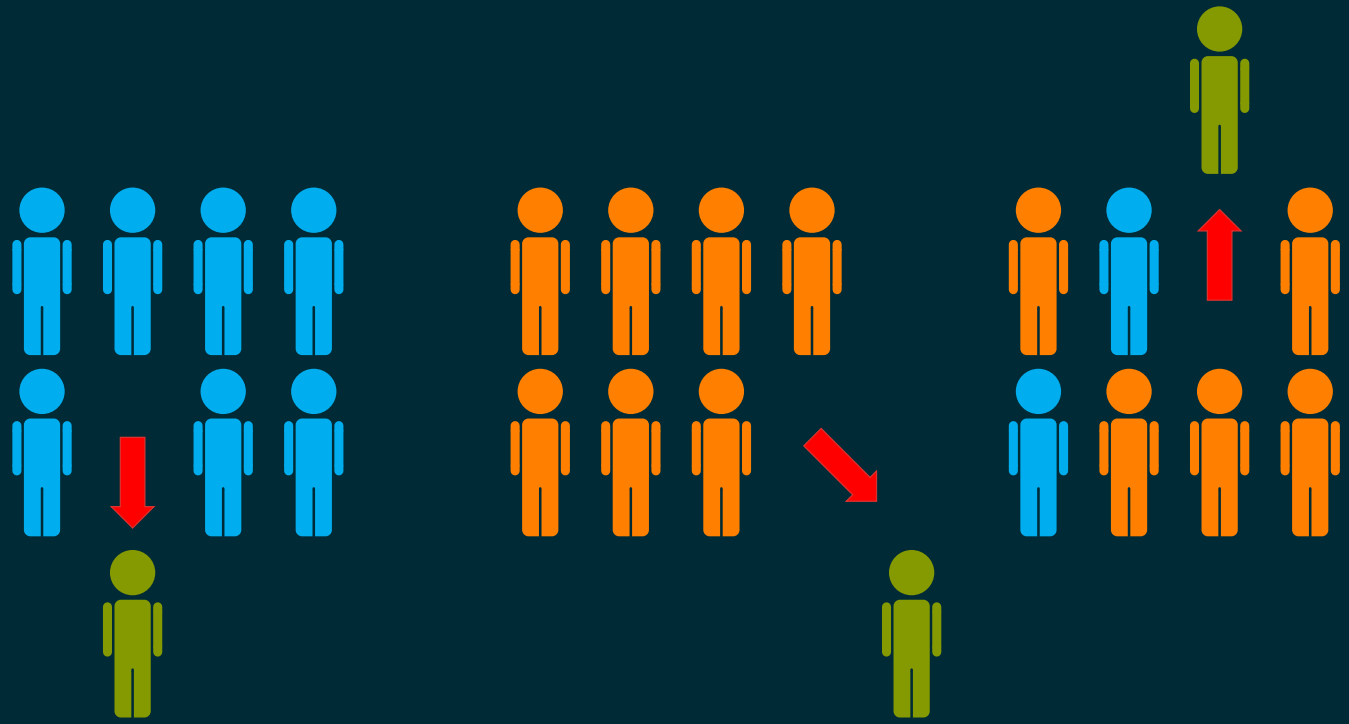


```
>>> import numpy as np
>>> from scipy.optimize import brentq
```

	r	θ_r	H	F	γ	α	β	indiscriminate	selective	mixed	indiscriminate ESS	selective ESS	mixed ESS
0	0.556	0.0	0.000	0.667	0.0	0.667	0.000	True	False	NaN	True	False	False
1	0.242	0.0	0.500	0.000	1.0	0.500	0.000	True	False	NaN	True	False	False
2	0.879	0.0	1.000	1.000	0.0	0.333	0.333	True	False	NaN	True	False	False
3	0.758	0.0	0.667	1.000	0.0	0.333	1.000	True	False	NaN	True	False	False
4	0.788	0.0	0.250	0.000	1.0	0.250	1.000	True	False	NaN	True	False	False



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https://github.com/Nikoleta-v3

https://arxiv.org/abs/1712.07640