Lean 4 Cheatsheet

If a tactic is not recognized, write ${\tt import\ Mathlib.Tactic}$ at the top of your file.

| Logical symbol | Appears in goal | Appears in hypothesis |
|------------------------------------|-----------------|--|
| \forall (for all) | intro x | apply h or specialize h x |
| \rightarrow (implies) | intro h | apply h or specialize h1 h2 |
| $\neg \text{ (not)}$ | intro h | apply h or contradiction |
| \leftrightarrow (if and only if) | constructor | rw [h] or rw [← h] or apply h.1 or apply h.2 |
| \wedge (and) | constructor | obtain $\langle h1, h2 \rangle := h$ |
| \exists (there exists) | use x | obtain $\langle x, hx \rangle := h$ |
| \vee (or) | left or right | obtain h1 h2 := h |
| a = b (equality) | rfl or ext | rw [h] or rw [+ h] or subst h (if b is a variable) |

| Tactic | Effect |
|--|--|
| exact expr | prove the current goal exactly by expr. |
| $apply \ expr$ | prove the current goal by applying $expr$ to some arguments. |
| $\texttt{refine}\ expr$ | like exact, but $expr$ can contain sub-expressions ?_ that will be turned into new goals. |
| ${\tt convert}\ expr$ | prove the goal by showing that it is equal to the type of $expr$. |
| $\mathtt{have}\ \mathtt{h}\ :\ proposition\ :=\ expr$ | add a new hypothesis h of type proposition. |
| have h : proposition | also creates <i>proposition</i> as a new goal. |
| by_cases h : proposition | create two goals, one where h is the hypothesis that <i>proposition</i> is true and one where h is the hypothesis where it is false. |
| exfalso | replace the current goal by False. |
| by_contra h | proof by contradiction; adds the negation of the goal as hypothesis h. |
| <pre>push_neg or push_neg at h</pre> | push negations into quantifiers and connectives in the goal (or in h). |
| symm | swap a symmetric relation. |
| ${\sf trans}\ expr$ | split a transitive relation into two parts with $expr$ in the middle. |
| congr | prove an equality using congruence rules. |
| gcongr | prove an inequality using congruence rules. |
| rw [expr] | in the goal, replace (all occurrences of) the left-hand side of $expr$ by its right-hand side. $expr$ must be an equality or if and only if statement. |
| rw [$\leftarrow expr$] | \dots rewrites using $expr$ from right-to-left. |
| ${\tt rw}\ [{\it expr}]$ at h | rewrite in hypothesis h. |
| simp | simplify the goal using all lemmas tagged $@[simp]$ and basic reductions. |
| simp at h | simplify in hypothesis h. |
| simp [*, expr] | \dots also simplify with all hypotheses and $expr$. |
| simp only [expr] | \dots only simplify with $expr$ and basic reductions (not with simp-lemmas). |
| simp? | \dots generate a simp only [\dots] tactic that applies the same simplifications. |
| simp_rw [expr1, expr2] | like rw, but uses simp only at each step. |
| exact? | search for a single lemma that closes the goal using the current hypotheses. |
| apply? | gives a list of lemmas that can apply to the current goal. |
| rw? | gives a list of lemmas that can be used to rewrite the current goal. |
| linarith | prove linear (in)equalities from the hypotheses. |
| <pre>ring / noncomm_ring field_simp / abel / group</pre> | prove the goal by using the axioms of a commutative ring $/$ ring $/$ field $/$ abelian group $/$ group. |
| aesop | simplify the goal, and use various techniques to prove the goal. |
| tauto | prove logical tautologies. |