

ADM-HW4

3. Algorithmic question.

We can sort an integer array in time $O(n+R)$ using counting sort Algorithm, where n is the size of array and R is the range of array (min - max).

Proof:-

$A = [2, 1, 0, 5, 4, 8, 7, 9, 3]$

0 1 2 3 4 5 6 7 8

func CountSort(A)

$n = \text{size}(A)$, $\text{min} = +\infty$, $\text{max} = -\infty$, $\gamma = 0$

\therefore First find min and max from A

$\equiv s1$ for ($i=0$ $i < n$ $i++$) n times

if $A[i] < \text{min} \Rightarrow \text{min} = A[i]$

if $A[i] > \text{max} \Rightarrow \text{max} = A[i]$

\therefore $\text{min} = 0$ $\text{max} = 9 \approx \gamma = \text{max} - \text{min} = 9$

\therefore Initialize empty array Count of size $\gamma+1$ with zeros.

Count = Array($\gamma+1$)

Count =

0	0	0	0	0	0	0	0	0	0
0	1	2	3	4	5	6	7	8	9

$\equiv s2$ for ($i=0$ $i < n$ $i++$) n times

$++\text{Count}[A[i]]$

Count =

1	1	1	1	1	1	0	1	1	1
0	1	2	3	4	5	6	7	8	9

\therefore Update the Count Array with cumulative sum at each index

$\equiv s3$ for ($i=1$ $i \leq K$ $i++$) R times

$\text{Count}[i] = \text{Count}[i] + \text{Count}[i-1]$

Count =

1	2	3	4	5	6	6	7	8	9
0	1	2	3	4	5	6	7	8	9

∴ Now initialize an Output Array with the same size as A

Output = Array(size(n))

Output = [0|0|0|0|0|0|0|0|0|0]

∴ Now traverse the A in reverse and assign values in output array using below mechanism.

≡ S4 for (i = n-1 i ≥ 0 i--) n times
Output[--count[A[i]]] = A[i]

Output = [0|1|2|3|4|5|7|8|9]

∴ Output is the sorted Array.

COMPLEXITY ANALYSIS :-

In the above algorithm we have 4 looping statement

• S1, S2, S3, S4

S1 = n, S2 = n, S3 = R, S4 = n

Hence the time complexity can be defined as

~~XXXXXX~~

$$\boxed{O(n+n+R+n) = O(n+R)}$$

∴ The above algorithm is not valid for negative integers, but with some modifications (like normalizing the values) we can also make it work for negative integers.