

Tutorial 2 - 10B - 51725018 - Group 8

Problem 1 ① "ID and Name of customers who own an account in a branch in their city"

$$\{x, y \mid \exists z \text{ customer}(x, y, z) \wedge \exists x', y' \text{ Account}(x', z, x, y')\}$$

② "ID and name of customers who do not own any account"

$$\{x, y \mid \exists z \text{ customer}(x, y, z) \wedge (\forall x', y', z', w' \text{ Account}(x', y', z', w') \rightarrow \neg (\exists z'' \text{ Account}(x'', z, x, w'')))\}$$

③ "ID and name of customer who own an account with a balance which is no less than the balance of any other account"

$$\{x, y \mid \exists z \text{ Customer}(x, y, z) \wedge (\exists a, b \text{ Account}(a, b, x', b, a) \wedge x = x') \wedge \forall c, d \text{ Account}(c, d, x', d, c) \wedge b \leq d)\}$$

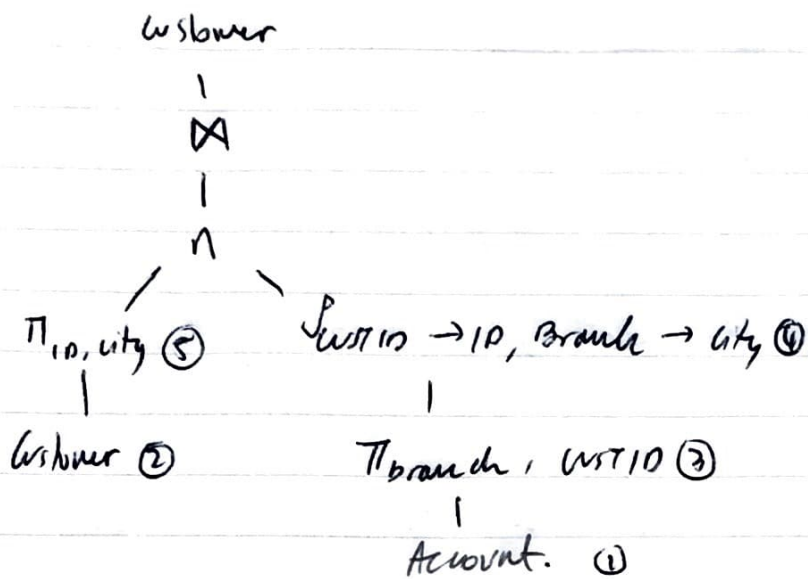
Problem 2 : could not solve it. since it has not been covered yet.

Problem 3 :

$$\text{CUSTOMER} \bowtie (\pi_{ID, \text{city}}(\text{Customer}) \cap \rho_{\text{CustID} \rightarrow ID, \text{Branch} \rightarrow \text{CITY}}(\pi_{\text{branch}, \text{CUSTID}}(\text{Account})))$$

let $\eta =$

$$\left. \begin{array}{l} ID \mapsto x, \\ \text{Name} \mapsto y, \\ \text{City} \mapsto z, \\ \text{Number} \mapsto a, \\ \text{branch} \mapsto b, \\ \text{CustID} \mapsto c, \\ \text{balance} \mapsto d, \end{array} \right\}$$



① $Account \rightarrow Account(a, b, c, d)$

② $Customer \rightarrow Customer(x, y, z)$

③ $\exists a, d \text{ } Account(a, b, c, d)$

④ $\exists a, d \text{ } Account(a, z, z, d)$

⑤ $\exists y \text{ } Customer(x, y, z)$

⑥ $\cap \Rightarrow R \cap S = R - (R - S) = \rho_R \cap (\rho_R \cap \neg \rho_S)$
 $= \rho_R \cap (\neg \rho_R \vee \rho_S)$

where $R = \text{⑤}$ $S = \text{④}$

$\therefore \cap \Rightarrow \exists y \text{ } Customer(x, y, z) \cap \neg (\exists y \text{ } Customer(y, y, z) \cap \neg (\exists a, d \text{ } Account(a, z, z, d)))$

$= \exists y \text{ } Customer(x, y, z) \cap (\forall y \text{ } Customer \vee \exists a, d \text{ } Account(a, z, z, d))$

We are left with $Customer \bowtie \text{⑥}$

$A \bowtie B = \pi_{xuy} (\sigma_{ID=ID'} (A \times \rho_{WSTID=ID'} B))$

$$\textcircled{1} \rho_{\text{WITIO}=\text{IO}'} B \quad \text{where } B = \textcircled{6}$$

Add $\{10' = x'\}$ to η

$$B = \exists y \text{ Worker}(x', y, z) \wedge (\forall y \text{ Worker}(x', y, z) \vee \exists a, d \text{ Account}(a, z, x, d))$$

$$\textcircled{2} A \times B = A \bowtie B$$

$$\textcircled{3} \sigma_{10=10'} (A \cap B) = A \cap B \cap x=x'$$

$$\textcircled{4} \pi_{u \vee v} (A \cap B \cap (x=x'))$$

$$\exists x' A \cap B \cap x=x'$$

$$\therefore \{x, y, z, a, b, c, d \mid \exists x' A \cap B \cap x=x'\}$$

where $A = \text{Customer}(x, y, z)$

$B = \exists y \text{ Worker}(x', y, z) \wedge (\forall y \text{ Worker}(x', y, z) \vee \exists a, d \text{ Account}(a, z, x, d))$

Problem 4:

$$\{x, z \mid R(x) \wedge \neg \exists y S(y, z)\}$$

R over A S over A, B

$$R(x) \quad \rho_{A \rightarrow A_x}(R)$$

$$S(y, z) \quad \rho_{A \rightarrow A_y, B \rightarrow B_z}(S)$$

$$\exists y (\rho_{A \rightarrow A_y, B \rightarrow B_z}(S)) \rightarrow \pi_{A_z}(\rho_{A \rightarrow A_y, B \rightarrow B_z}(S))$$

$$\neg (\exists y S(y, z)) \rightarrow \text{Adom}_{A_x} \times \text{Adom}_{A_y} - \pi_{A_z}(\rho_{A, B}(S))$$

∴ we have:

$$\rho_{A \rightarrow A_2}(R) \times (\text{Adom}_{A_1} \times \text{Adom}_{A_2}) - \pi_{A_2} \left(\int_{A, B} (s) \right)$$

↓
NOT SURE HOW TO CALCULATE THIS.